

Stack → data structure which works on the principle of LIFO (Last In First Out)

Eg → stack of books



Eg → stack of plates / CD's / chairs.

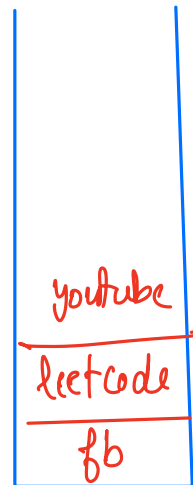
Eg → stack of functions.

Eg → Browser history

Forward and Backward Tabs



backward



forward

Operations in Stack

- ① $\text{push}(x) \rightarrow$ insert x at the top of the stack.
 - ② $\text{pop}() \rightarrow$ remove the top-most element of the stack.
 - ② $\text{top}() / \text{peek}() \rightarrow$ get the top-most element of the stack.
 - ④ $\text{isEmpty}() \rightarrow$ check if stack is empty or not.
- $\Rightarrow \underline{\underline{O(1)}}$

Implement Stack using Arrays -

$\text{push}(2) \checkmark$

$\text{push}(3) \checkmark$

$\text{push}(18) \checkmark$

$\text{push}(5) \checkmark$

$\text{pop}() \checkmark$

$\text{top}() / \text{peek}() \checkmark$

$\text{push}(10) \checkmark$

$\text{isEmpty}() \checkmark$

$\text{pop}() \checkmark$

$\text{pop}() \checkmark$

$\text{isEmpty}() \checkmark$

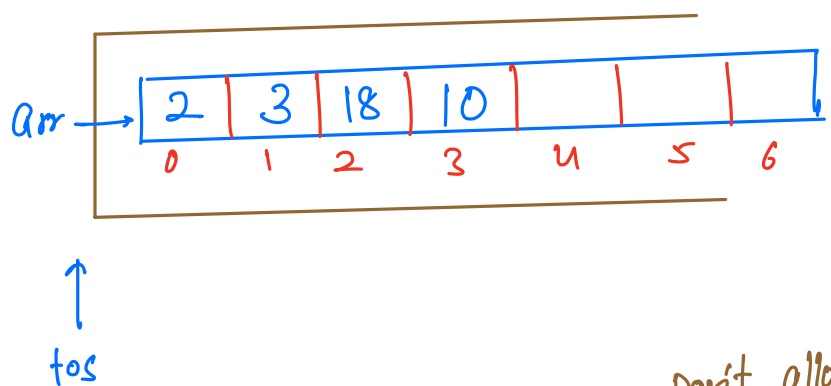
$\text{pop}() \checkmark$

$\text{pop}() \checkmark$

$\text{isEmpty}() \checkmark$



$\text{tos} \rightarrow$ index of the topmost element.



void $\text{push}(\text{int } x) \{$ \rightarrow **overflow** \rightarrow Don't allow the insertion
 $\text{tos}++;$
 $\text{arr}[\text{tos}] = x;$
}

\hookrightarrow Vector / ArrayLists

```
int top () {  
    if (tos == -1) { "stack is empty" }, return -1  
    return arr[tos];  
}
```

T.C $\rightarrow O(1)$

```
boolean isEmpty () {  
    if (tos == -1) { return true }  
    else { return false }  
}
```

```
void pop () {  
    if (tos == -1) { "stack is empty" }, return  
    tos--;  
}
```

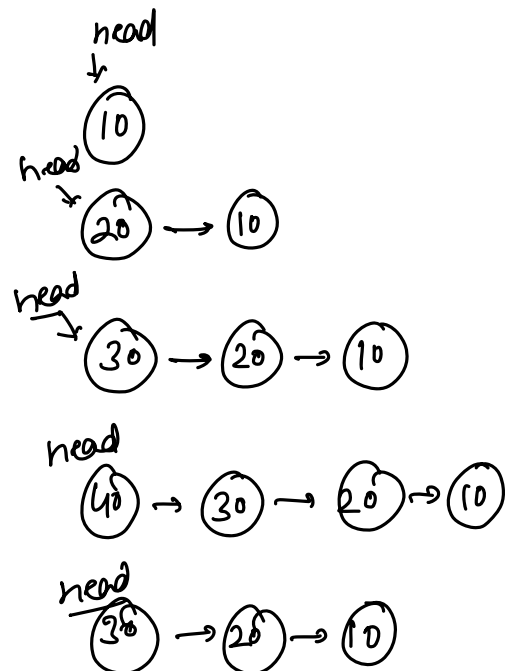
Implement Stack using Linked-list

→ push(), pop(), top()/peek(), isEmpty()



- ① push at head and pop from tail X [Lifo discipline is not maintained]
- ② push at tail and pop from head X [Lifo discipline is not maintained]
- ③ ✓ push at head and pop from head
- ④ push at tail and pop from tail X $O(N)$

push(10) → addAtHead(10)
push(20) → addAtHead(20)
push(30) → addAtHead(30)
push(40) → addAtHead(40)
pop() → removeAtHead()



Q.1 Check whether the given sequence of parentheses is valid or not?

[], { }, ()

Eg → () [{ } ()] → true.

() [] → true

({ }) → true.

({) } → false

([]) → false.

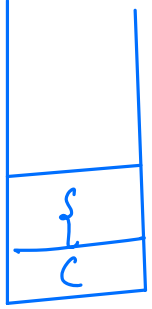
([{ } []] ()) → true.

Eg → ({ [{ } ()] } ()) → true.



stack.

Ex - $\overset{\checkmark}{(}\overset{\checkmark}{\{}}\rangle\}$ \rightarrow false.



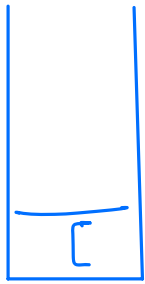
mis-match

Ex - $\overset{\checkmark}{(}\overset{\checkmark}{\{}}\overset{\downarrow}{\{}}\overset{\downarrow}{\{}}\overset{\downarrow}{\{}}\rangle\}$ \rightarrow false.



(more closing parenthesis)

Ex - $\overset{\checkmark}{[}\overset{\checkmark}{(}\overset{\downarrow}{)]}$ \rightarrow false.



(more -opening parenthesis)

code →

```
Stack < character > st;
```

```
for (i = 0; i < N; i++) {
```

```
    char ch = str[i];
```

```
    if (ch == '(' || ch == '{' || ch == '[') {
```

```
    {
        st.push(ch);
```

```
    }
    else {
```

```
        if (st.isEmpty() == true) { // more closing parenthesis
```

```
        {
            return false;
```

```
        else if (st.top() is not the counterpart of ch) { // mismatch
```

```
        {
            return false;
```

```
        }
        else {
```

```
        {
            st.pop();
```

```
        }
```

```
    }
```

```
}
```

$T.C \rightarrow O(N)$
 $S.C \rightarrow O(N)$

```
if (st.isEmpty() == true) {
```

```
{
    return true;
```

```
}
else {
```

```
    // more opening parenthesis
```

```
    return false;
```

```
}
```

Double Character Trouble

Given a string str. Remove equal adjacent characters.

Return the string without adjacent duplicates.

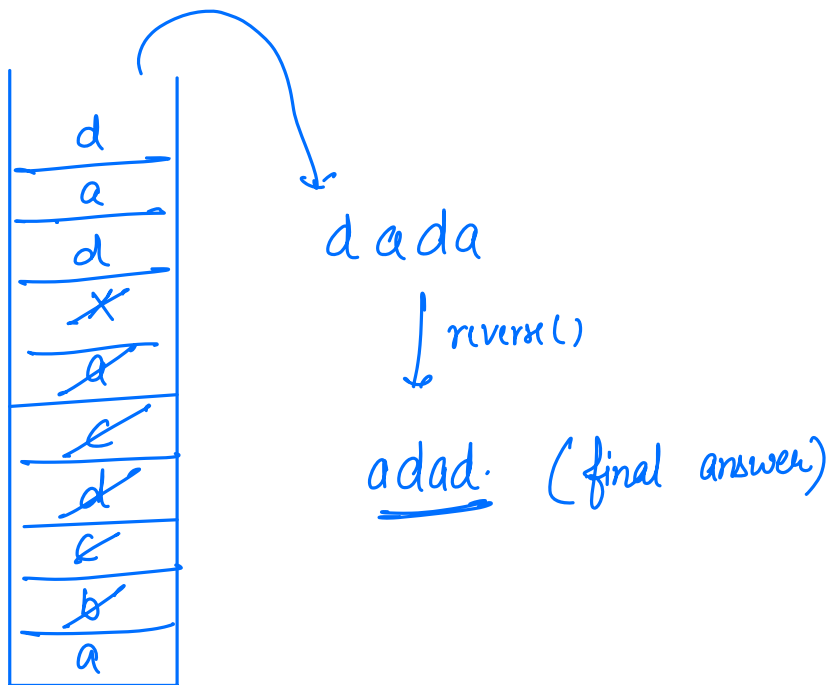
① ~~a~~~~b~~d → ad

② ab~~c~~bde → ab~~b~~de → ade

③ ab~~b~~bd → abd

④ ab~~b~~c~~b~~ca~~c~~x → ~~a~~~~c~~~~c~~~~a~~x → cx

⑤ a~~b~~c~~d~~d~~c~~c~~a~~a~~b~~~~x~~~~x~~dad → adad.



#code→

```
Stack<character> st;
```

```
st.push(str[0]);
```

```
for (i = 1; i < N; i++) {
```

```
    char ch = str[i];  
    if (st.isEmpty() == false && st.top() == ch) {  
        {  
            st.pop();  
        }  
    }  
    else {  
        {  
            st.push(ch);  
        }  
    }  
}
```

```
if (st.isEmpty() == true) { return "" };
```

```
String ans = "";
```

```
while (st.isEmpty() == false) {  
    {  
        ans += st.top();  
        st.pop();  
    }  
}
```

T.C → $O(N)$
S.C → $O(N)$

→ Reverse the ans string and return it;

infix

2 + 3

2 + (5 * 3)

op1 operator op2

postfix

2 3 +

2 5 3 * +

op1 op2 operator

Q: Evaluate given valid postfix expression.

① $\boxed{10 \mid 6 \mid \div}$ ans = 4.

② $\underbrace{2, 5, *}_{10}, 3, -$ ans = 7.

③ $\underbrace{2}_{2}, \underbrace{5, 3, *}_{15}, -$ ans = -13

④ $\underbrace{3, 5, +}_{8}, 2, -, \underbrace{2, 5, *}_{10}, -$ ans = -4

$\underbrace{\quad\quad\quad}_{6} \quad \underbrace{2, 5, *}_{10} -$

$\quad\quad\quad 6 \quad \quad -$

idea... \forall operators, we need to have two latest operands.

\Downarrow
Stack.

arr \rightarrow $\left[\overset{\checkmark}{3}, \overset{\checkmark}{5}, \overset{\downarrow}{+}, \overset{\checkmark}{2}, \overset{\downarrow}{-}, \overset{\checkmark}{2}, \overset{\checkmark}{5}, \overset{\downarrow}{*}, \overset{\downarrow}{-} \right]$

ans.

-4
10
8
2
6
2
8
8
3

op2 \rightarrow st.pop \rightarrow 10

op1 \rightarrow st.pop \rightarrow 6

op1 operator op2

#code.

```
int solution ( String [] arr , int N) {  
    Stack<Integer> st;  
    for( i = 0; i < N; i++) {  
        str = arr[i];  
        if( str is an operator) {  
            int op2 = st.pop();  
            int op1 = st.pop();  
            res = evaluate( op1, op2, operator);  
            st.push( res);  
        }  
        else {  
            st.push( Integer( str ));  
        }  
    }  
    return st.top();  
}
```

$T.C \rightarrow O(N)$
 $S.C \rightarrow O(N)$

```
int evaluate( int op1, int op2 , string operator){
```

```
    if( operator.equals( "+" ) ) {
```

```
        {
            return op1 + op2;
```

```
        }
        else if ( operator.equals( "-" ) ) {
```

```
            {
                return op1 - op2;
```

```
            }
            else if ( operator.equals( "*" ) ) {
```

```
                {
                    return op1 * op2;
```

```
                }
            else {
                return (op1 / op2);
```

```
        }
    }
```

-
- X
- ① Searching → Revise B.S problem painter partition
 - ② Hashing → Assignment + additional problems
 - ③ Strings → observation based problems.

Syllabus → Searching, 2P, Hashing, Strings.