

Q.1) Given $\text{arr}[N]$ where all the elements are lying in the range 1-5. Sort the array.

Corr \rightarrow $[\underline{5} \quad \underline{1} \quad \underline{2} \quad \underline{1} \quad \underline{4} \quad \underline{2} \quad \underline{2} \quad \underline{3} \quad \underline{3} \quad \underline{4} \quad \underline{3} \quad \underline{2} \quad \underline{2} \quad \underline{1} \quad \underline{1}]$

$$[1 \ 1 \ 1 \ 1 \ 2 \ 2 \ 2 \ 2 \ 2 \ 3 \ 3 \ 3 \ 4 \ 4 \ 5]$$

① freq HashMap.

② freq arr

0	4	5	3	2	1
0	1	2	3	4	5

element freq
 5 \rightarrow 1
 1 \rightarrow ~~x~~ 2 3 4
 2 \rightarrow ~~x~~ 2 3 4 5
 4 \rightarrow 1 2
 3 \rightarrow ~~x~~ 2 3

code. →

```
int freq[K+1];
```

```
for( i = 0; i < N; i++) {  
    freq[arr[i]]++;  
}
```

```
int idx = 0;
```

```
for( i = 1; i ≤ K; i++) {  
    for( j = 1; j ≤ freq[i]; j++) {  
        arr[idx] = i;  
        idx++;  
    }  
}
```

T.C → $O(N+K)$
S.C → $O(K)$

Count sort

i	j	no. of iterations
1	[1,a]	a
2	[1,b]	b
3	0	1
4	0	1
5	0	1
6	[1,c]	c
⋮	⋮	⋮
K	[1,x]	x

→ What if $1 ≤ arr[i] ≤ 10^9$, $1 ≤ N ≤ 10^5$

freq[10^9+1]

X

freq Hashmap? ✓

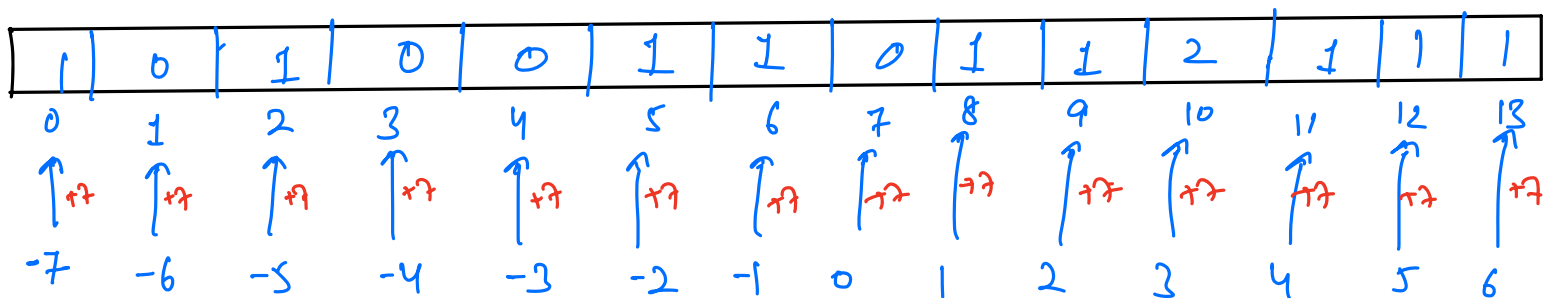
[∵ no. of keys in worst-case = 10^5]

• → -ve elements

$$\underline{\underline{-7}} \leq \text{arr}[i] \leq \underline{\underline{6}}, \quad 1 \leq N \leq 10^5$$

min max

arr → [2, 1, 3, -5, -2, -7, -1, 5, 3, 6, 4]



code →

// iterate and get min and the max element.

freq[max - min + 1]; // $\forall i, \text{freq}[i] = 0$

```
for( i = 0; i < N; i++) {  
    freq[ arr[i] - min ] ++ ;  
}
```

```
for( i = min; i <= max; i++) {  
    for( j = 1; j <= freq[ i - min ]; j++) {  
        print( i );  
    }  
}
```

T.C → $O(N + \text{max} - \text{min})$
S.C → $O(\text{max} - \text{min})$

Q1 int \rightarrow 3 4 5 7 6 8
5 4 3 2 1 0

$$345768 / 1000 \Rightarrow 345 \% 10 \rightarrow \underline{5}$$

N \rightarrow 368 , 10's digit

$$368 / 10 \Rightarrow 36 \% 10 \Rightarrow \underline{6}$$

$$j^{\text{th}} \text{ - digit of a number} \Rightarrow \left(\frac{N}{10^i} \right) \% 10$$

Q2 \rightarrow Given +ve integers. Sort these integers on the basis of tens place. \Rightarrow [stable]

arr \rightarrow [361, 432, 12, 78, 500, 112, 2]

\nearrow [500, 2, 12, 112, 432, 361, 78]

digit \rightarrow [0, 9] count?

arr \rightarrow [361, 432, 12, 78, 500, 112, 2]

0	\rightarrow	{ 500, 2 }
1	\rightarrow	{ 12, 112 }
2	\rightarrow	{ - }
3	\rightarrow	{ 432 }
4	\rightarrow	{ - }
5	\rightarrow	{ - }
6	\rightarrow	{ 361 }
7	\rightarrow	{ 78 }
8	\rightarrow	{ - }
9	\rightarrow	{ - }

o/p \rightarrow [500, 2, 12, 112, 432, 361, 78]

code \rightarrow

```
list < integer > [10] freq;
```

```
for( i=0; i < N; i++) {
```

```
    tens = (arr[i]/10)%10;
```

```
    freq[tens].insert(arr[i]);
```

```
}
```

```
for( i=0; i < 10; i++) {
```

```
    for( j=0; j < freq[i].size(); j++) {
```

```
        {
```

```
            print( freq[i].get(j));
```

```
        }
```

[T.C \rightarrow $O(N)$
S.C \rightarrow $O(N)$]

Radix Sort \rightarrow sort the elements from least significant digit to most significant digit.

3 6 1		5 0 0		5 0 0		2
4 3 2		3 6 1		0 0 2		1 2
1 2	$\xrightarrow{\text{0th place}}$	4 3 2		0 1 2		7 8
7 8		0 1 2	$\xrightarrow{\text{1st place}}$	1 1 2	$\xrightarrow{\text{2nd place}}$	1 1 2
5 0 0		1 1 2		4 3 2		3 6 1
1 1 2		0 0 2		2 6 1		4 3 2
2		0 7 8		0 7 8		5 0 0

$d \rightarrow$ no. of digits in the maximum number.

$\left[\begin{array}{l} \text{T.C} \rightarrow O(N \cdot d) \\ \text{S.C} \rightarrow O(N) \end{array} \right]$

$d \rightarrow ?$

```

max = 0
for (i = 0; i < N; i++) {
    max = Max(max, arr[i])
}

int m = max; digits = 0
while (m != 0) {
    m /= 10;
    digits++;
}
    
```

Break \rightarrow 10:31 \rightarrow 10:38

Q1 Given $arr[N]$ and all elements are distinct. Find sum of $(\max - \min)$ of all subsets.

$arr \rightarrow [3, 1, -4]$

	max	min	max-min
$[]$	-	-	0
$[3]$	3	3	0 +
$[1]$	1	1	0 +
$[-4]$	-4	-4	0 +
$[3, 1]$	3	1	2 +
$[3, -4]$	3	-4	7 +
$[1, -4]$	1	-4	5 +
$[3, 1, -4]$	3	-4	7
$\Sigma \max_s - \Sigma \min_s$			<u>21</u>

subsets \rightarrow set of elements attained by deleting 0 or more elements.

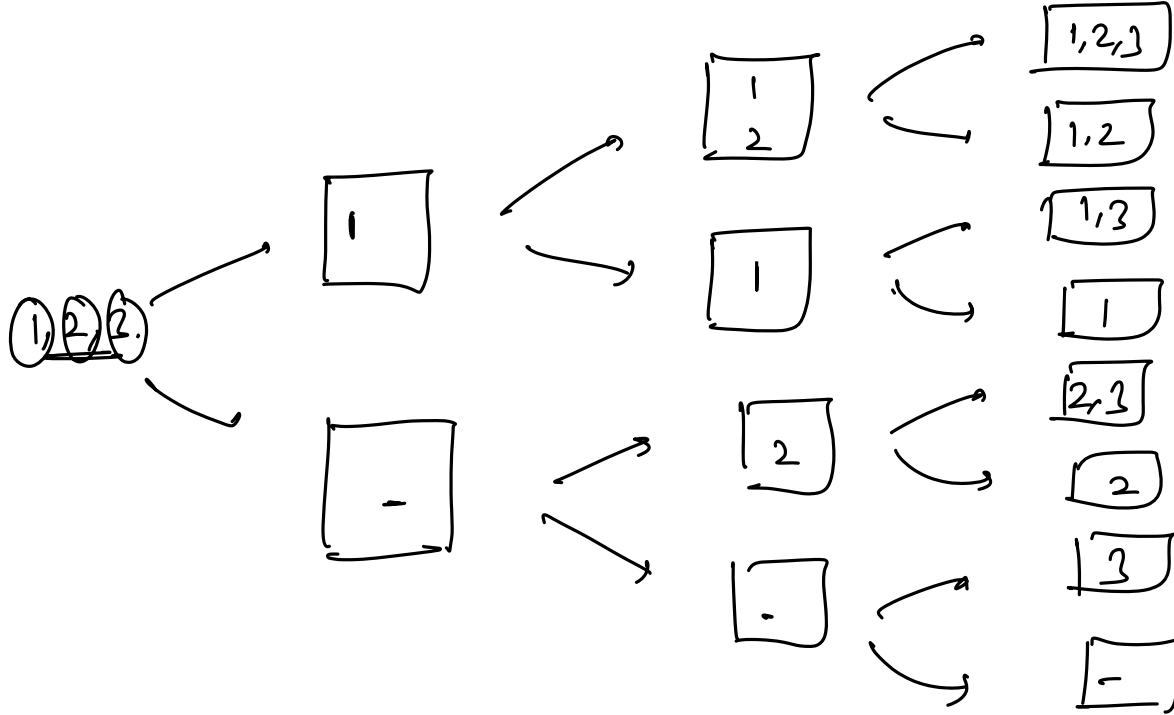
$arr \rightarrow [1, 7, 9, 3, 4]$

$[7, 3, 4]$ ✓

$[7, 34]$ X

$[1, 3]$ ✓

$[-]$ ✓



B.f idea → Generate all subsets, and for every subset find the minimum & maximum element & take their difference.

T.C → $O(2^N * N)$ ⇒ exponential T.C

Contribution?

$$\sum (\max - \min)_S = \sum \max_S - \sum \min_S$$

$$\left\{ \begin{array}{l} \text{Contribution} = \text{arr}[i] * \text{no. of subsets in which} \\ \text{arr}[i] \text{ will be the maximum} \\ \text{element} \end{array} \right\}$$

arr \rightarrow [3, 2, 8, 7, 4, 6]

① In how many subsets, 6 is the maximum element.

[6]

$\Rightarrow 2^{\text{no. of smaller elements than 6.}}$

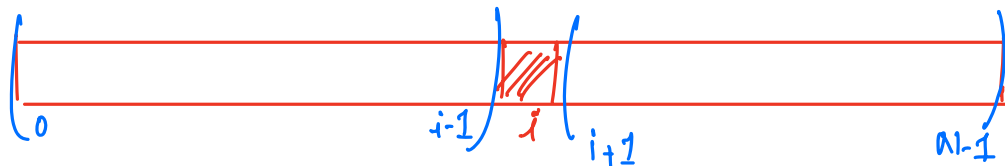
$$\Rightarrow 2^3 = \underline{8.}$$

② In how many subsets, 6 is the minimum element.

$\Rightarrow 2^{\text{no. of greater elements than 6}}$

$$\Rightarrow 2^2 = \underline{4.}$$

Sorting



count of smaller elements than arr[i] $\rightarrow i$

count of greater elements than arr[i] $\rightarrow n - i - 1$

$$[a, b] \Rightarrow b - a + 1$$

$$[i+1, n-1] \Rightarrow n-1 - (i+1) + 1$$

$$\Rightarrow n-1 - i - 1 + 1$$

\therefore Contribution of $\text{arr}[i]$ in $\Sigma_{\max_s} = \text{arr}[i] * 2^i$
 Contribution of $\text{arr}[i]$ in $\Sigma_{\min_s} = \text{arr}[i] * 2^{N-i-1}$

1 code:-

sort(arr), long max_s = 0, long min_s = 0, mod = $10^9 + 7$

```
for( i = 0; i < N; i++) {
    max_s = max_s + arr[i] * fastpower(2, i, mod);
    min_s = min_s + arr[i] * fastpower(2, N-i-1, mod);
}
```

return (int) ((max_s - min_s) % mod)

$$\left[\begin{array}{l} T.C \rightarrow O(N \log N) \\ S.C \rightarrow O(\log N) \end{array} \right]$$

$$1 \leq N \leq 10^4$$

$$1 \leq \text{arv}(i) \leq 10^3$$

take modulo with 10^9+7 .

{Doubt Session → 11:00 A.m → 1:30 P.m} → Inversion Count
Doubts on Sorting