

Searching

target \rightarrow what to search?

search-space \rightarrow where to search/ find it?

Word:

Newspaper

dictionary

contact

Phone diary

Directory / Phone contacts

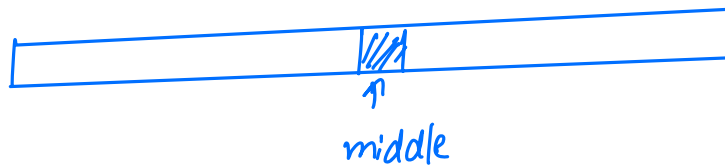
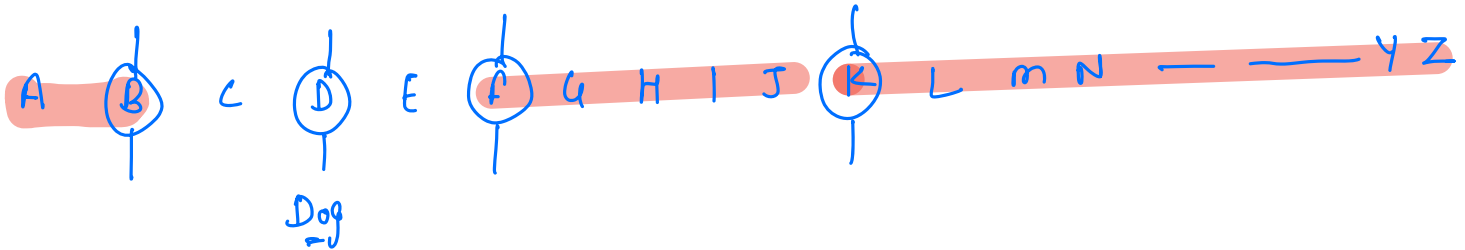
Book:

Book shelf

library.

Arranged/ organized in a particular order.

Dog.



Binary Search \rightarrow reducing the search space by half in every single iteration based on some condition.

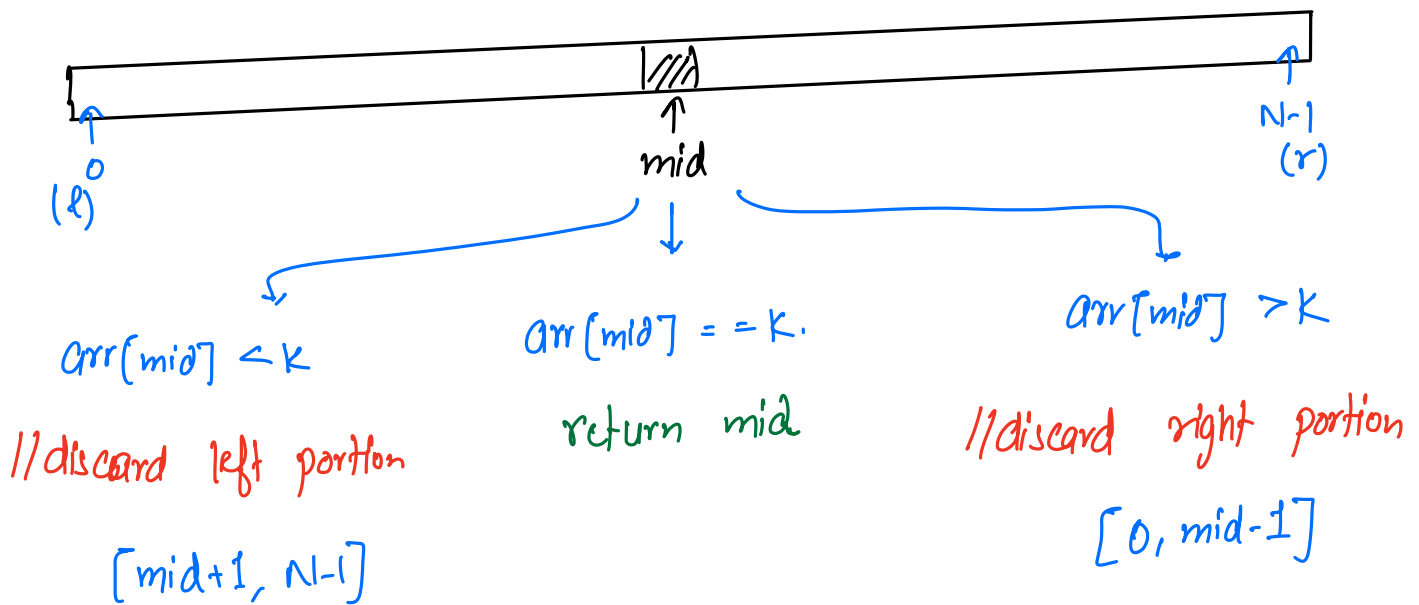
Qs Given a sorted array (ascending). Find the idx of the element K . Return -1 if element K doesn't exist.

arr \rightarrow [3 6 9 12 14 19 20 23 25 27] , $K = 20$
 0 1 2 3 4 5 6 7 8 9 ans = 6.

idea-1. Linear Search (iterating on all elements) T.C $\rightarrow O(N)$

idea-2 target $\rightarrow K$

search-space \rightarrow whole Array $[0, N-1]$



Arr \rightarrow [3 6 9 12 14 19 20 23 25 27], $x = 20$

0 1 2 3 4 5 6 7 8 9

l r mid

l	r	mid		
0	9	$\frac{0+9}{2} = 4$	// Discard left portion	$l = mid + 1$
5	9	$\frac{5+9}{2} = 7$	// Discard right portion	$r = mid - 1;$
5	6	$\frac{5+6}{2} = 5$	// Discard left portion	$l = mid + 1$
6	6	$\frac{6+6}{2} = 6$	return <u>mid</u>	

#code.

```

l = 0, r = N-1
while( l <= r ){
    mid = (l+r)/2;
    if( arr[mid] == x ){
        return mid;
    }
    else if( arr[mid] < x ){
        l = mid + 1;
    }
    else {
        r = mid - 1;
    }
}
return -1;

```

N
 \downarrow
 $N/2$
 \downarrow
 $N/4$
 \downarrow
 $N/8$
 \downarrow
 1

$T.C \rightarrow O(\log_2 N)$
 $S.C \rightarrow O(1)$

$\Rightarrow O(\log_2(\text{search-space}))$

Q.1 Given a sorted array containing duplicates as well.
find freq of an element k .

$k=5$

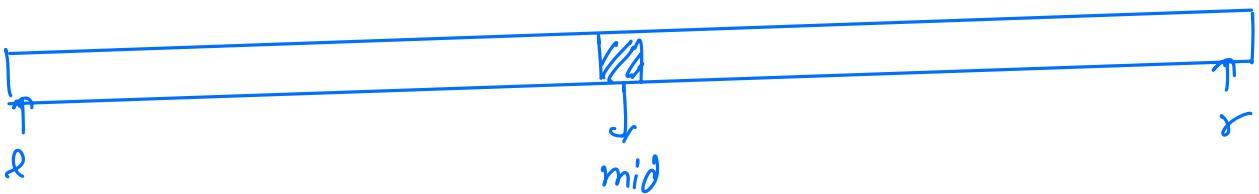
arr[] → $\begin{bmatrix} -5 & -5 & -3 & 0 & 0 & 1 & 1 & 1 & 5 & 5 & 5 & 5 & 5 & 5 & 8 & 10 & 15 & 15 \end{bmatrix}$
 $\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 & 16 & 17 \end{matrix}$
ans=7

idea-1. Linear search and update count if
 $arr[i] == k$.
 [T.C → $O(N)$, S.C → $O(1)$]

idea-2. $[freq = last\ occ - first\ occ + 1]$

target → first occurrence of k .

search space → $[0, N-1]$



first occurrence

$arr[mid] < k$	$arr[mid] == k$	$arr[mid] > k$
$l = mid + 1$	$ans = mid$	$r = mid - 1$
	$r = mid - 1$	

last occurrence

$arr[mid] < k$	$arr[mid] == k$	$arr[mid] > k$
$l = mid + 1$	$ans = mid$	$r = mid - 1$
	<u>$l = mid + 1$</u>	

arr[] → [-5 -5 -3 0 0 1 5 5 5 5 5 5 5 7 7 8 10 15 15]

Indices: 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18

Annotations: Blue circles around arr[4]=0, arr[5]=1, arr[6]=5, arr[9]=5. Blue arrows point to arr[5] from 'l' and to arr[6] from 'r'. A box contains 'k=5'.

l	r	mid	
0	18	$\frac{0+18}{2} = 9$	arr[mid] == k, ans = 9, r = mid - 1
0	8	$\frac{0+8}{2} = 4$	arr[mid] < k, l = mid + 1
5	8	$\frac{5+8}{2} = 6$	arr[mid] == k, ans = 6, r = mid - 1
5	5	$\frac{5+5}{2} = 5$	arr[mid] < k, l = mid + 1
6	5		<u>return ans.</u>

#code → #first occurrence

```

l = 0, r = N-1, fo = -1
while (l ≤ r) {
    mid = (l+r)/2;
    if (arr[mid] == k) {
        fo = mid;
        r = mid - 1;
    }
    else if (arr[mid] < k) {
        l = mid + 1;
    }
    else {
        r = mid - 1;
    }
}

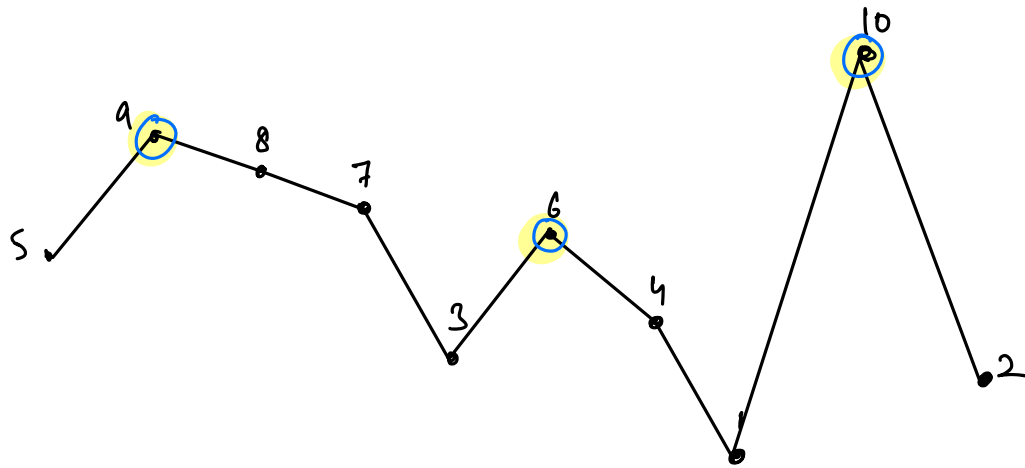
```

T.C → $O(\log_2 N)$
S.C → $O(1)$

Q1 Given an unsorted array of n distinct elements.
Find any one local maxima.

↓
[element which is not smaller than its adjacent elements]

arr[] → [5 9 8 7 3 6 4 1 10 2]



arr[] → [7 7 7 7]



idea.1 → Find the max element. ⇒ Linear Search T.C → $O(N)$

→ Iterate on all the elements & check

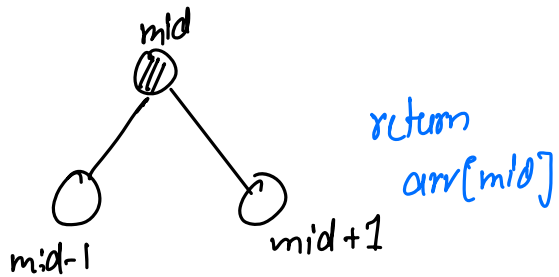
if $arr[i-1] \leq arr[i]$ & $arr[i+1] \leq arr[i]$

T.C → $O(N)$

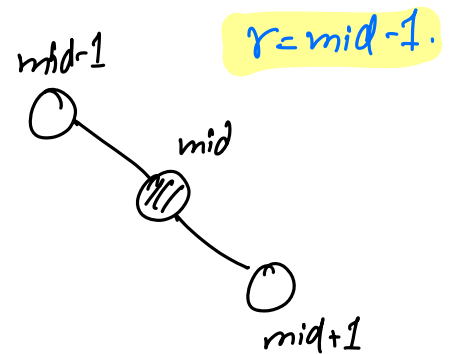
target \rightarrow any local maxima

search space $\rightarrow [0, N-1]$

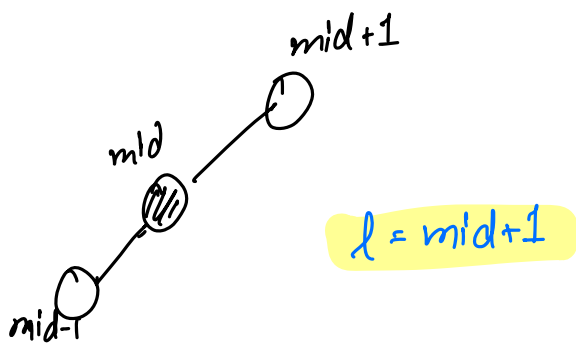
①



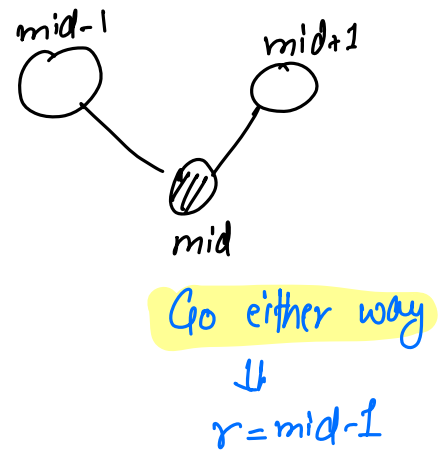
②



③



④



#code →

if (N == 1) { return arr[0] }

if (arr[0] ≥ arr[1]) { return arr[0] }

if (arr[N-1] ≥ arr[N-2]) { return arr[N-1] }

l = 1, r = N-2

while (l ≤ r) {

mid = (l+r)/2;

if (arr[mid] ≥ arr[mid-1] && arr[mid] ≥ arr[mid+1]) {

{ return arr[mid]; // Case-1

else if (arr[mid] ≥ arr[mid-1]) {

{ l = mid+1 // Case-3

else {

{ r = mid-1 // Case-2 & 4

}

return -1;

T.C → $O(\log_2 N)$
S.C → $O(1)$

Q. Every element occurs twice except for one.
Find unique element.



Note → Duplicates are adjacent to each other

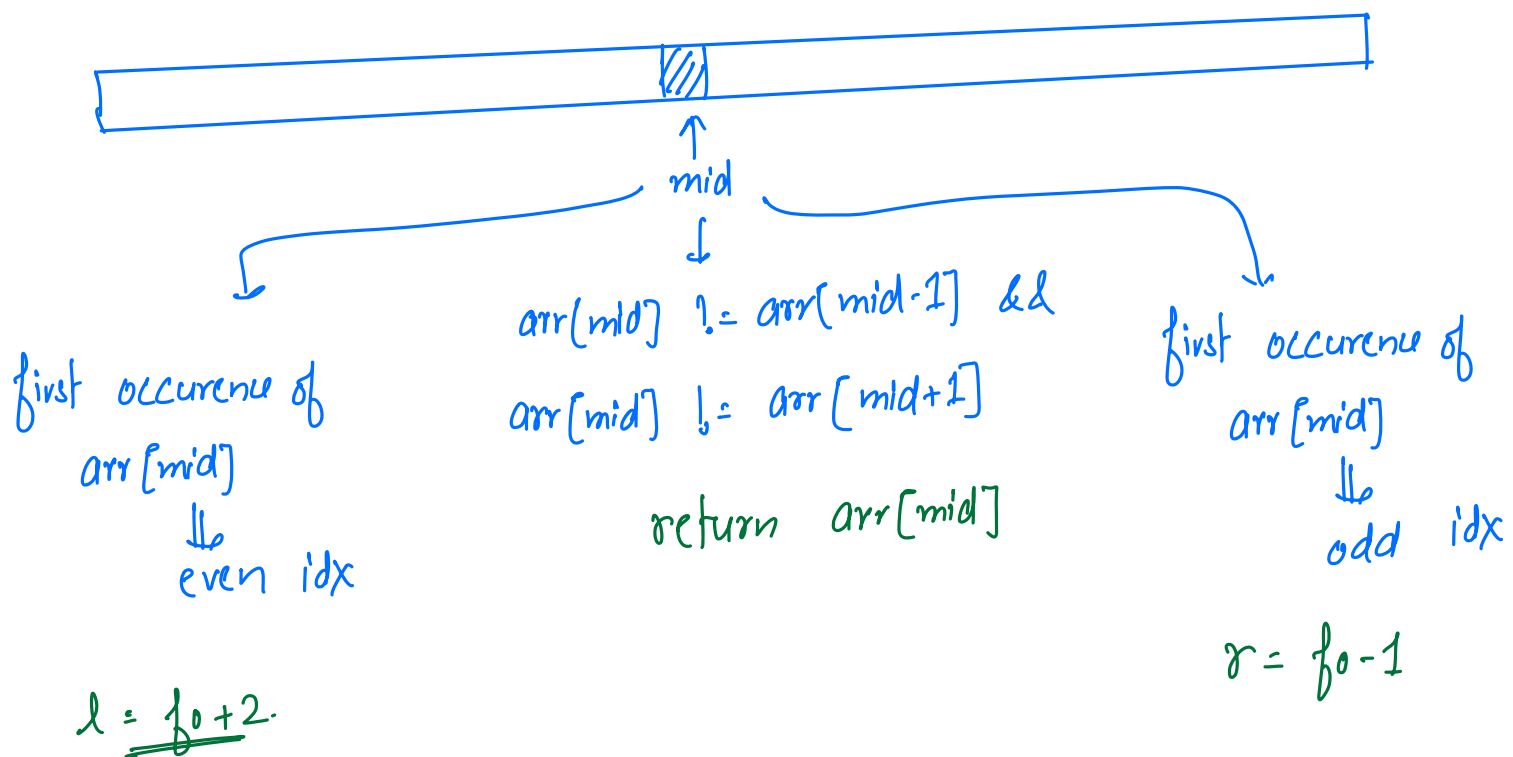
ans = 9.

arr[] →

3	3	1	1	8	8	10	10	9	6	6	2	2	4	4
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

target → unique element

Search-space → $[0, N-1]$



arr[] → [3 3 1 1 8 8 10 10 9 6 6 2 2 4 4]
 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 ↑ ↑
 l r

l	r	mid
0	14	$\frac{0+14}{2} = 7$
8	14	$\frac{8+14}{2} = 11$
8	10	$\frac{8+10}{2} = 9$
8	8	$\frac{8+8}{2} = 8$

f.o of 10 is present at 6 (even) idx.
 $l = f_o + 2$

f.o of 2 is present at 11 (odd) idx.
 $r = f_o - 1$

f.o. of 6 is present at 9 (odd) idx.
 $r = f_o - 1$

(arr[mid] is unique element)
 return arr[mid]

#code:->

if (N == 1) { return arr[0] }

if (arr[0] != arr[1]) { return arr[0] }

if (arr[N-1] != arr[N-2]) { return arr[N-1] }

l = 2, r = N-3

while (l <= r) {

mid = (l+r)/2;

if (arr[mid] != arr[mid-1] && arr[mid] != arr[mid+1]) {

{
return arr[mid];

fo = mid;

if (arr[mid-1] == arr[mid]) {

{
fo = mid-1;

if (fo % 2 == 0) {

{
l = fo+2;

else {

{
r = fo-1;

}

T.C $\rightarrow O(\log_2 N)$
S.C $\rightarrow O(1)$

✓ { target →
✓ { search-space →
✓ { condition on the basis of which search space
reduced by half.

⇓

Binary Search