

Machine learning:

Arthur Samuel → "The field of study that gives computers the ability to learn without being explicitly programmed."

Tom Mitchell → "A computer program said to learn from experience E with respect to some class of Tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E."

Supervised learning: "right answer"

correct output ← dataset → Actual

- Regression: Predict continuous valued output
- Classification: Discrete valued output (0 or 1)  
(0, 1, 2, 3)

# Unsupervised Learning : clustering

in dataset evry points are leveled same.

→ Social network analysis

→ Astronomical data analysis

→ Market segmentation

→ organized computing clusters

→ Gene grouping

Cocktail party problem:

→ We can derive structure by clustering the data based on relationships among the variables in the data.

two microphones in a room with two speakers. The recording of that two microphone can be distinguish two different output by this algo.

$[W, S, V] = \text{svd} (\text{repmat} (\text{sum} (x * x, 1), \text{size}(x, 1), 1) * x) * x'$ );

Non-Clustering: The 'CPA' allows us to find structure in a chaotic environment (ie. identifying individual voices and music from a mesh of sounds)

## Model Presentation:

$(x^{(i)}, y^{(i)}) \rightarrow$  i<sup>th</sup> dataset

Training Set

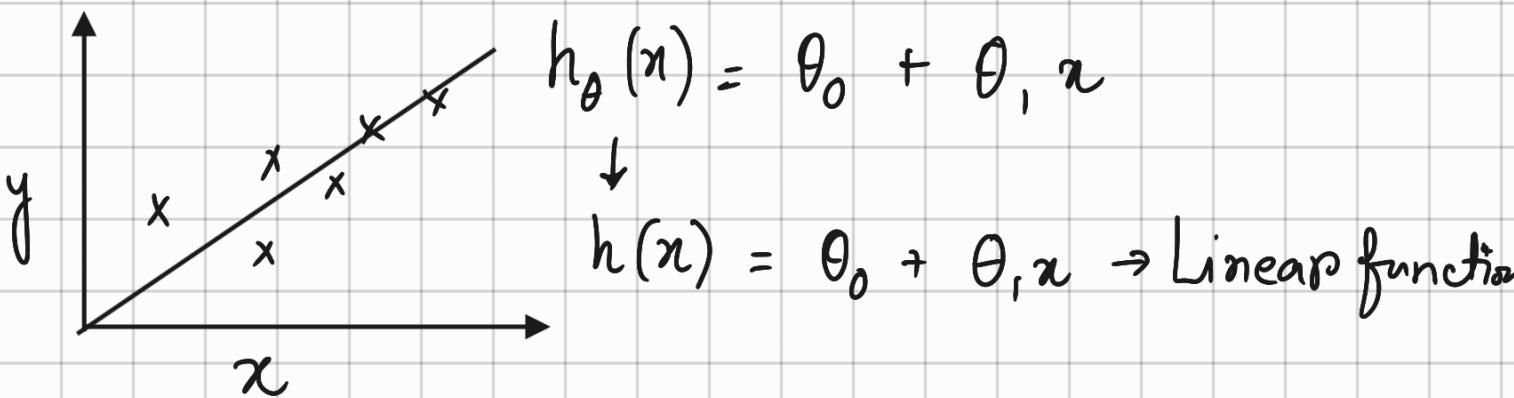


Learning Algorithm



Size of house  $\rightarrow h$   $\rightarrow$  Estimated price

$(x)$  hypothesis (estimated value of  $y$ )



Linear regression with one variable  
→ Univariate linear regression

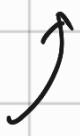
# Cost Function:

$m = \# \text{ training example}$

$$\boxed{\begin{matrix} \text{minimize} \\ \theta_0, \theta_1 \end{matrix}} \quad \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

find such

$\theta_0, \theta_1$  so that



to be minimized.

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

Cost function

Squared error function

$$\hookrightarrow J(\theta) = \frac{\text{sum}((x \times \theta - y) \cdot \text{r2})}{2m}$$

Vect.

$$\text{If } \theta_0 = 0 \quad J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (\theta_1 x^{(i)} - y^{(i)})^2$$

In our model  $\rightarrow$

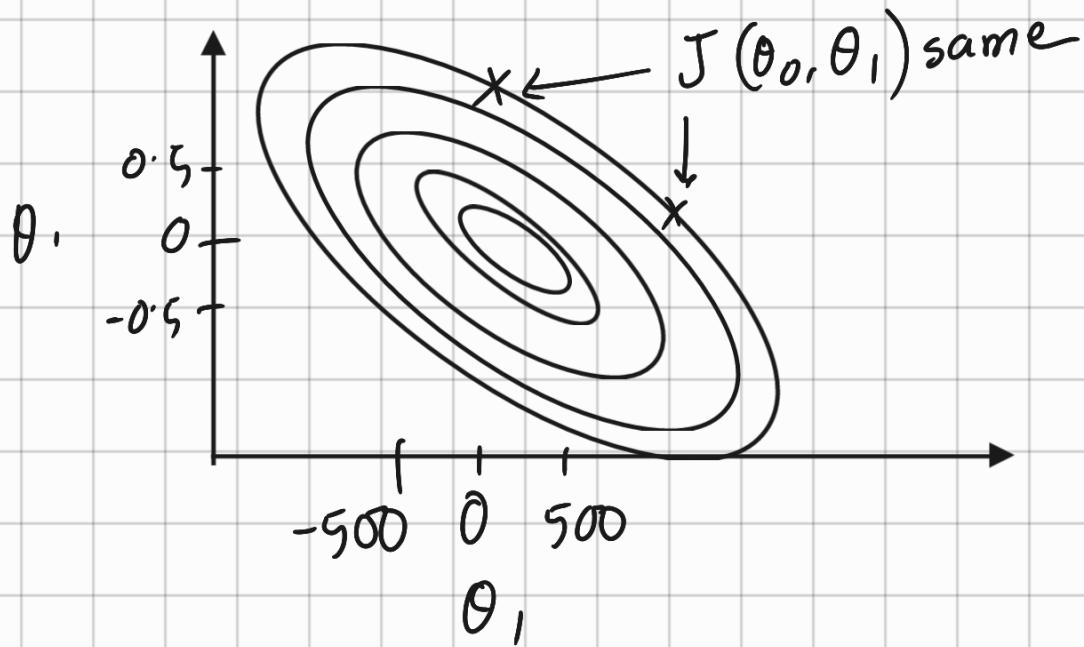
$$\text{hypothesis : } h_\theta(x) = \theta_0 + \theta_1 x$$

Parameters :  $\theta_0, \theta_1$

$$\text{Cost Function : } J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

Goal : minimize  $J(\theta_0, \theta_1)$   
 $\theta_0, \theta_1$

Contour plot or figure instead of 3d graph



Gradient descent :

Have some function:  $J(\theta_0 \dots \theta_n)$

Want:  $\min_{\theta_0 \dots \theta_n} J(\theta_0 \dots \theta_n)$

Outline:

→ Start with some  $\theta_0, \theta_1$

→ Keep changing  $\theta_0, \theta_1$  to reduce  $J(\theta_0, \theta_1)$

→ Until we hopefully end up with a minimum

$\therefore$  assignment

Algo:

repeat until convergence {

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) \text{ for } j=0 \& j=1$$

} 
 ↑ learning rate/step length  $\alpha \uparrow$  aggressive step  
 ↳ Simultaneously update  $\alpha \downarrow$  baby step  
 $\theta_0 \& \theta_1$

$$\left\{
 \begin{array}{l}
 \text{temp0} := \theta_0 - \alpha \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) \\
 \text{temp1} := \theta_1 - \alpha \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1) \\
 \theta_0 := \text{temp0} \\
 \theta_1 := \text{temp1}
 \end{array}
 \right.$$

$$\frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) = \frac{\partial}{\partial \theta_j} \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

$$= \frac{\partial}{\partial \theta_j} \frac{1}{2m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)})^2$$

$$\theta_0, j=0: \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\theta_1, j=1: \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) \cdot x^{(i)}$$

repeat until convergence {

$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})$$

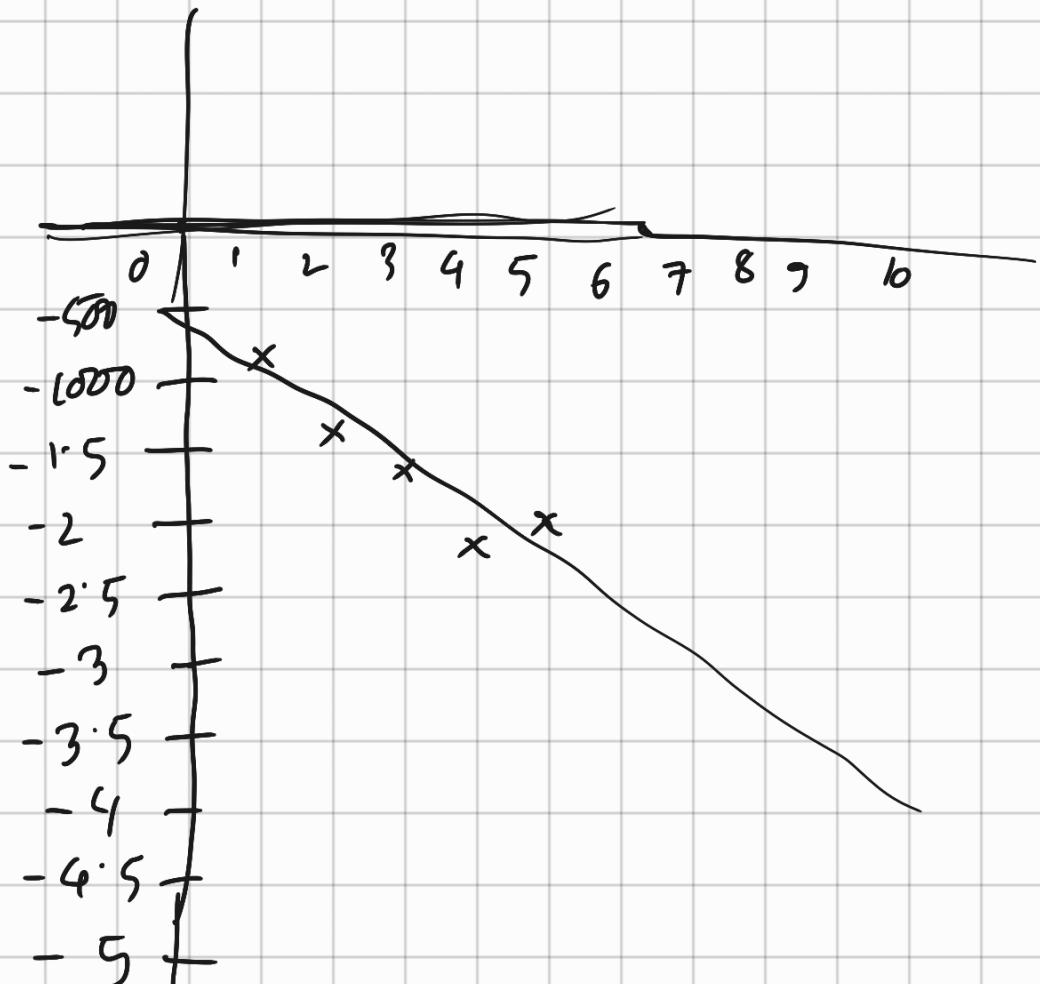
$$\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}). x^{(i)}$$

} update  $\theta_0$  &  $\theta_1$  simultaneously.

$J(\theta_0, \theta_1)$  is always a convex / Bowl-shape func.

Hence has only one global / local optimum.

x	y	h
3	2	3
1	2	1
0	1	0
4	3	4



# Linear Algebra Revision

prediction = datamatrix  $\times$  parameters

House Sizes:

2104

1416

1534

852

$$h_{\theta}(x) = -40 + 0.25n$$

$$\text{data matrix} = \begin{bmatrix} 1 & 2104 \\ 1 & 1416 \\ 1 & 1534 \\ 1 & 852 \end{bmatrix}$$

$$\text{parameters} = \begin{bmatrix} -40 \\ 0.25 \end{bmatrix}$$

$$\text{prediction} = \begin{bmatrix} h(2104) \\ h(1416) \\ h(1534) \\ h(852) \end{bmatrix}$$

$$\begin{bmatrix} 3 \\ -5 \\ 4 \end{bmatrix}^T \times \begin{bmatrix} 1 \\ 2 \\ 5 \end{bmatrix} = \begin{bmatrix} 3 & -5 & 4 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 5 \end{bmatrix}$$