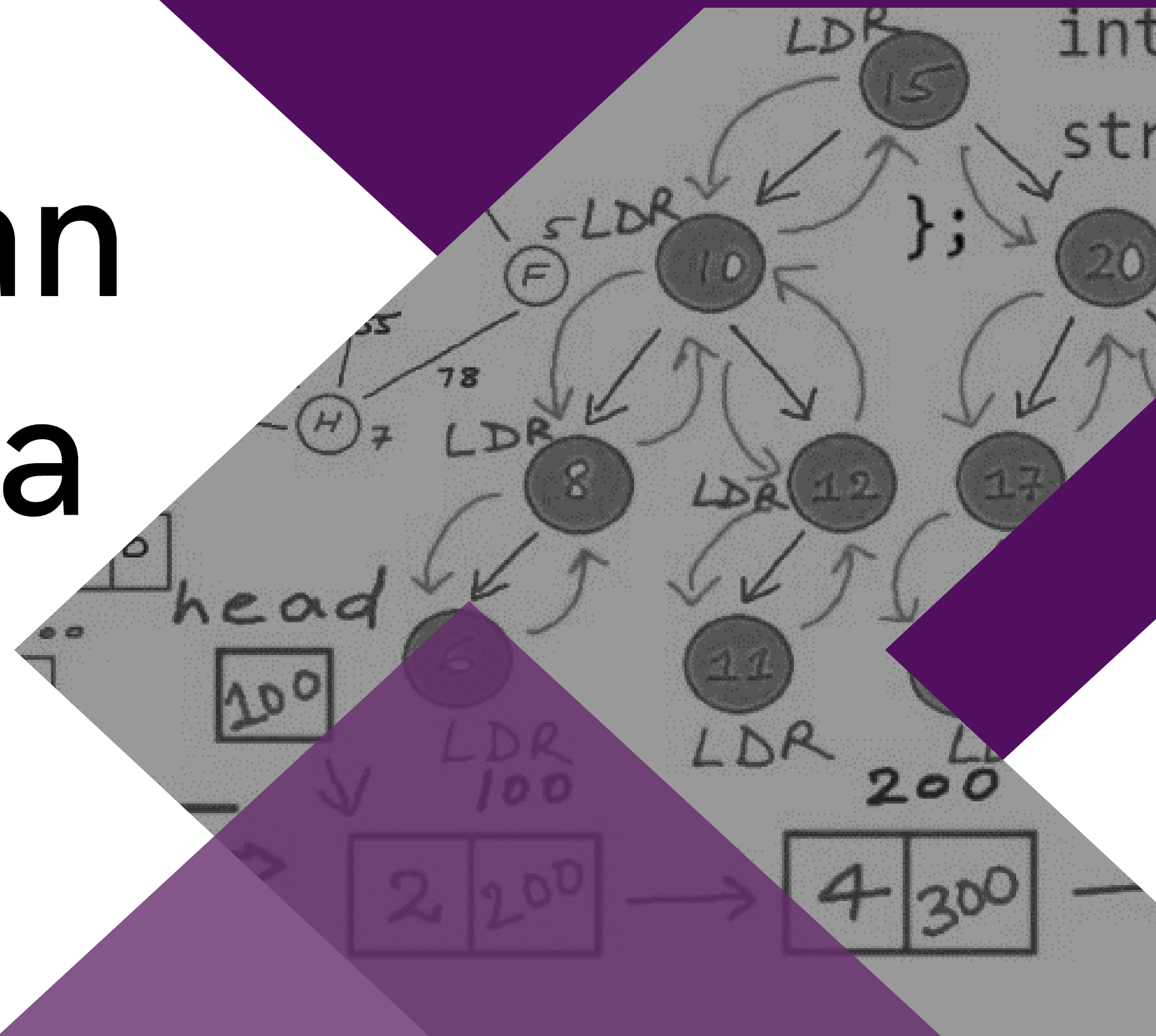
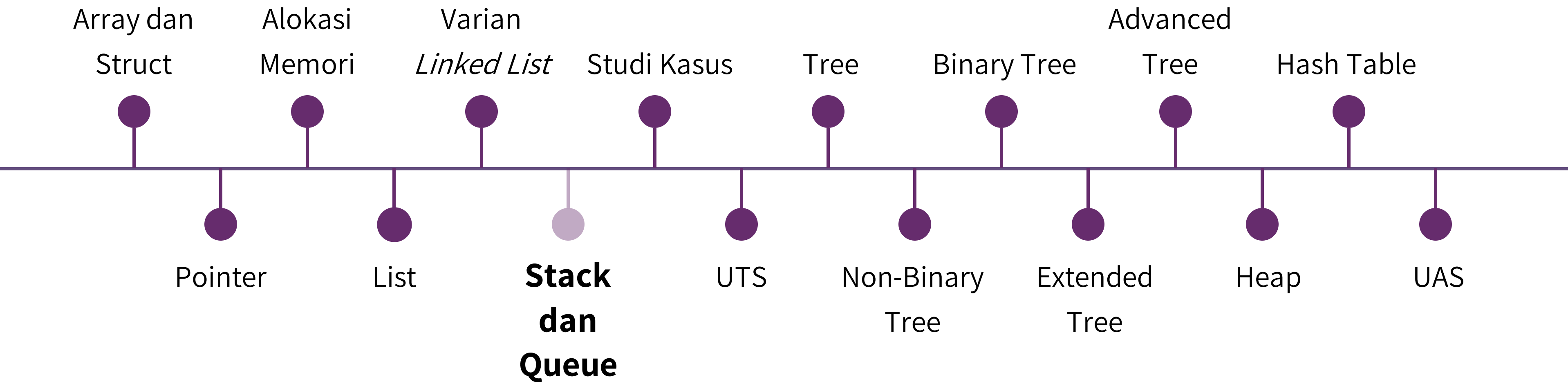


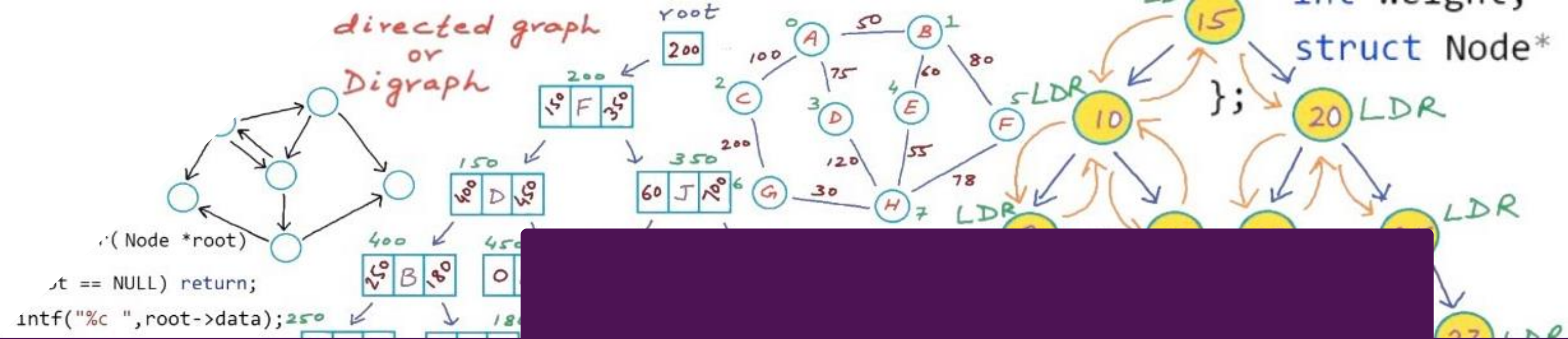
Algoritma dan Struktur Data



Pekan 6



Tujuan



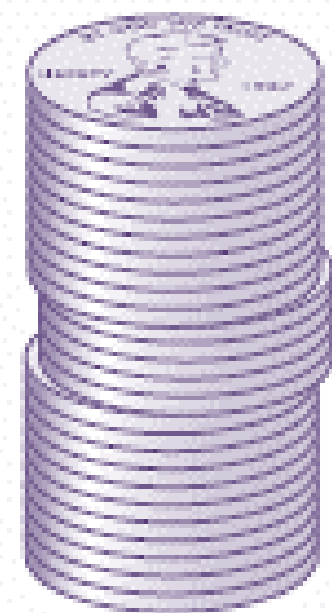
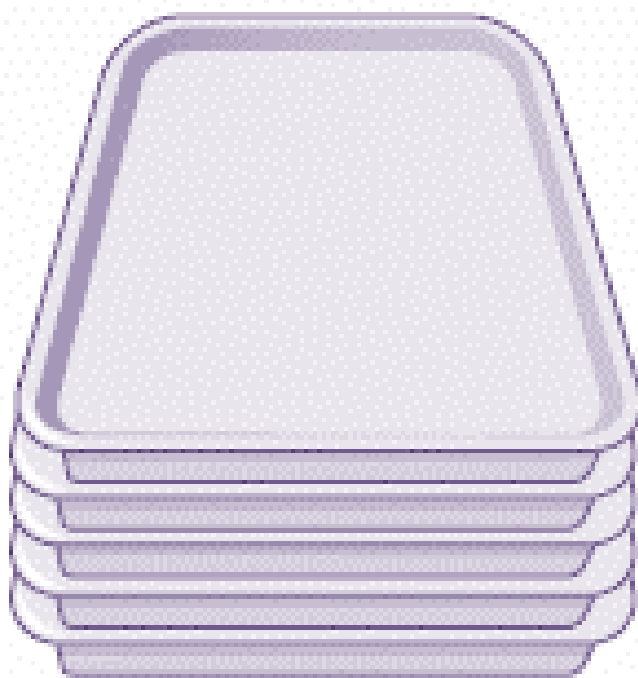
1	Mahasiswa memahami konsep stack dan operasinya
2	Mahasiswa memahami konsep queue dan operasinya
3	Mahasiswa mampu mengimplementasikan ADT stack dan queue dalam bentuk array
4	Mahasiswa mampu mengimplementasikan ADT stack dan queue dalam bentuk linked list.

ADT - Stack



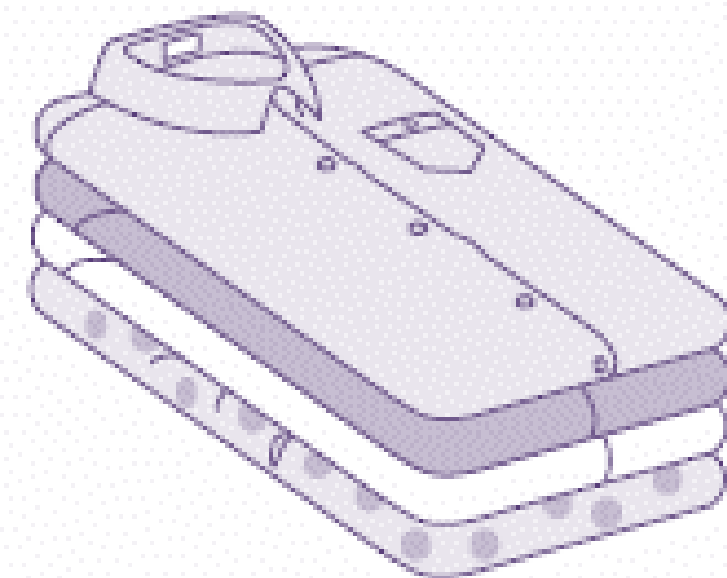
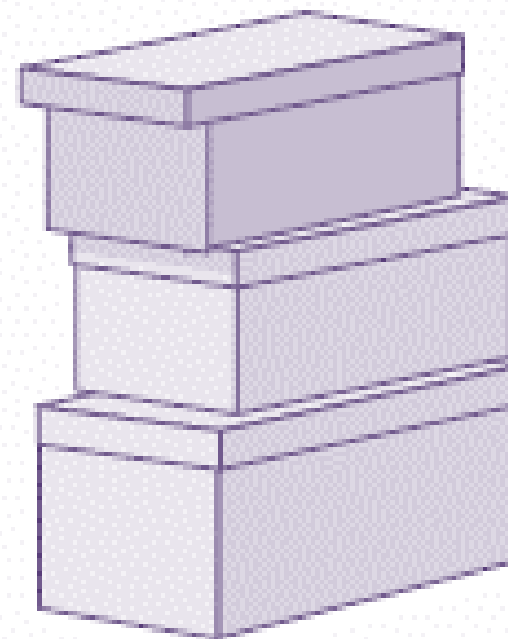
Stack

A stack of
cafeteria trays



A stack
of pennies

A stack of
shoe boxes



A stack of
neatly folded shirts

Stack

An abstract data type in which elements are added and removed from only one end; a “last in, first out” (LIFO) structure.

A last-in, first-out (LIFO) data structure that operates much like a pile of papers: we add new elements to the top of the stack and remove elements starting with the top of the stack.

A list data structure in which elements are inserted in and removed from the same end, the top of the stack

Stack Operations

Push(key) Add a new element to the top of the stack.

Pop() Remove the element from the top of the stack and return it.

Top() Return most recently added key

IsEmpty() Check whether there are any elements

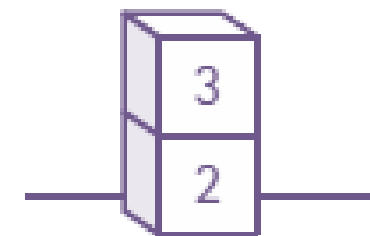
StackType stack;

(Empty)

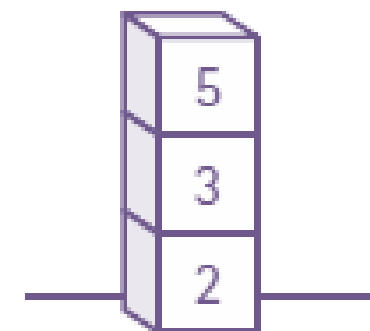
stack.Push(block2);



stack.Push(block3);

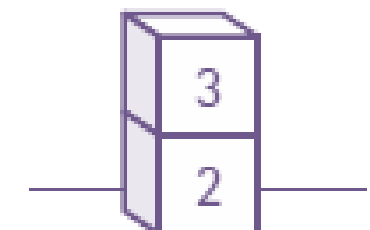


stack.Push(block5);



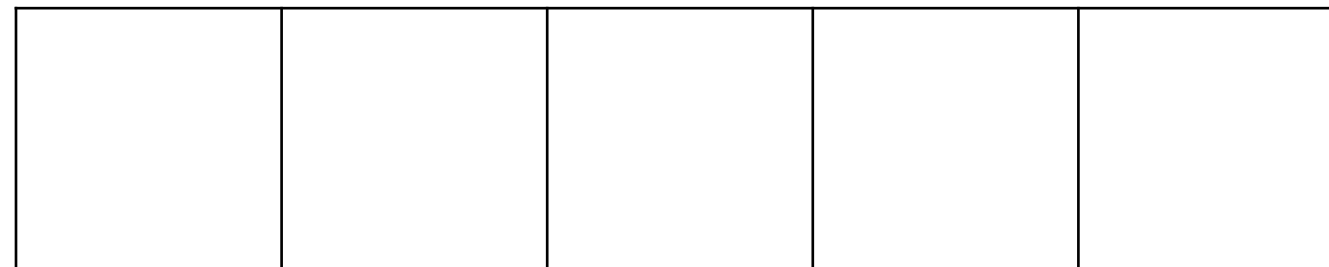
5 = stack.Top();

stack.Pop();



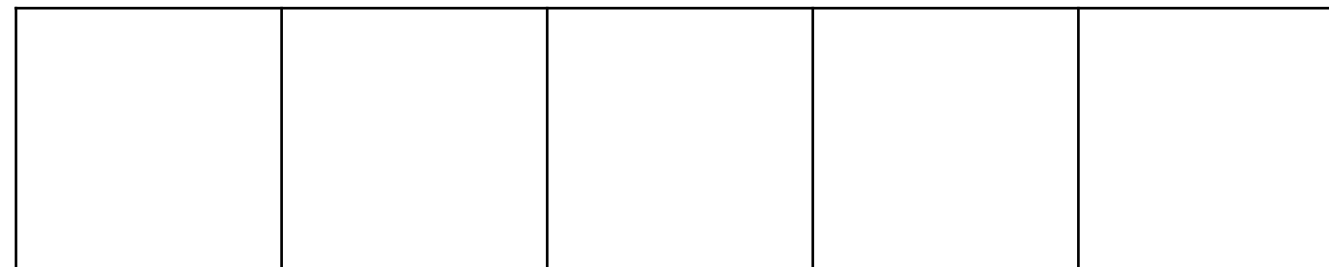
Stack Implementation with Arrays

numElements:0



Stack Implementation with Arrays

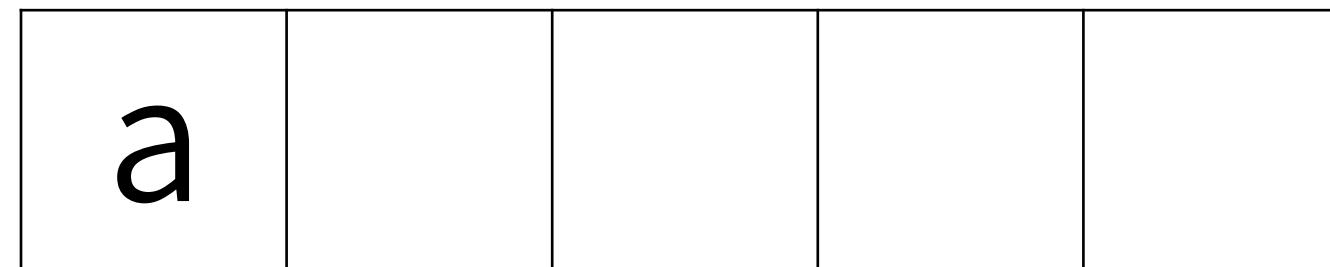
numElements:0



Push (a)

Stack Implementation with Arrays

numElements:1



Push (a)

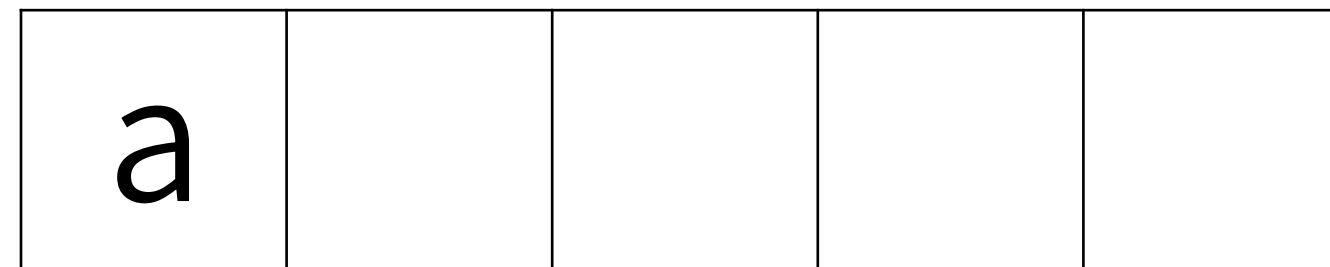
Stack Implementation with Arrays

numElements:1

a				
---	--	--	--	--

Stack Implementation with Arrays

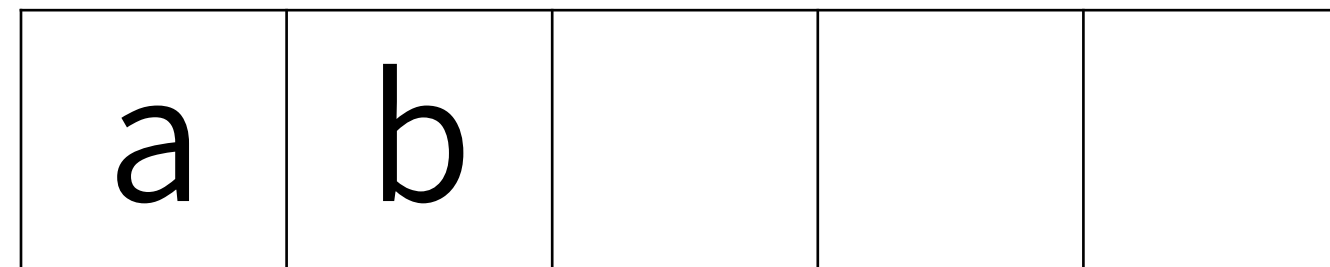
numElements:1



Push (b)

Stack Implementation with Arrays

numElements:2



Push (b)

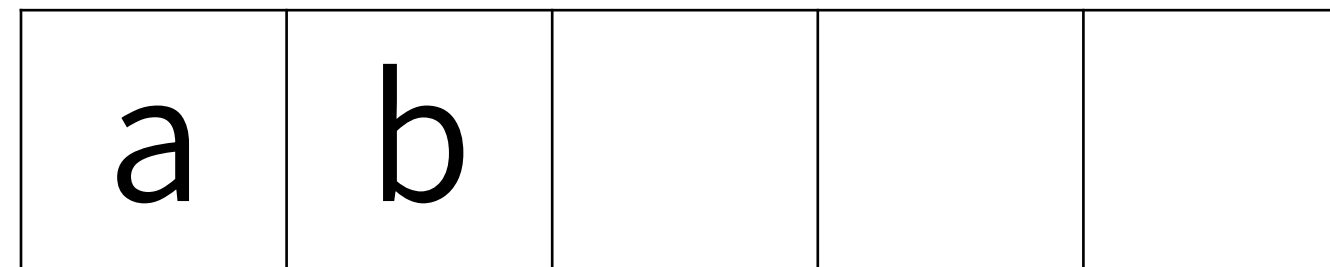
Stack Implementation with Arrays

numElements:2

a	b			
---	---	--	--	--

Stack Implementation with Arrays

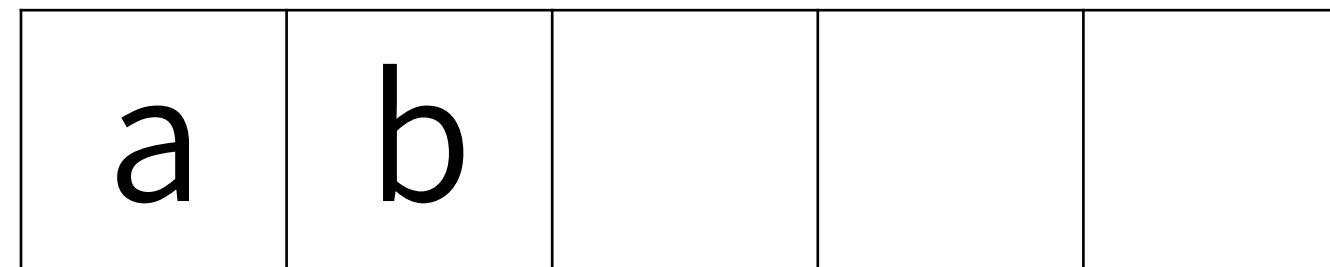
numElements:2



Top ()

Stack Implementation with Arrays

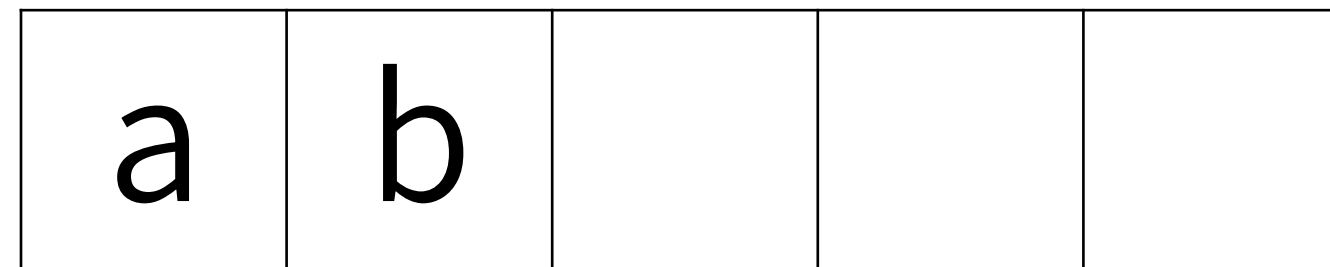
numElements:2



Top () → 5

Stack Implementation with Arrays

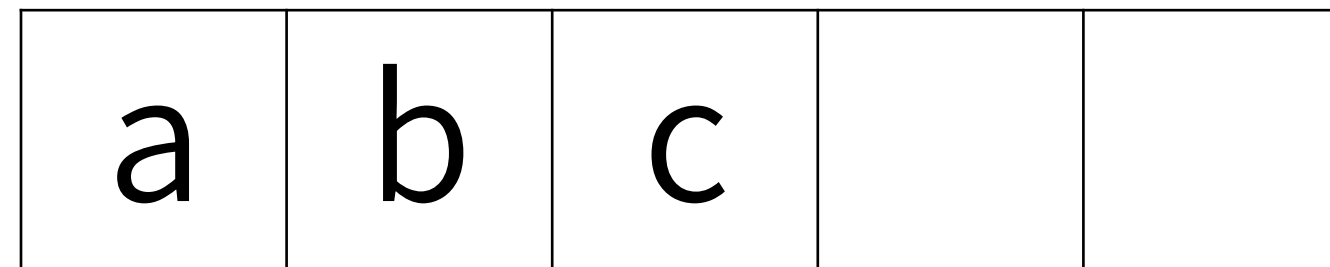
numElements:2



Push (c)

Stack Implementation with Arrays

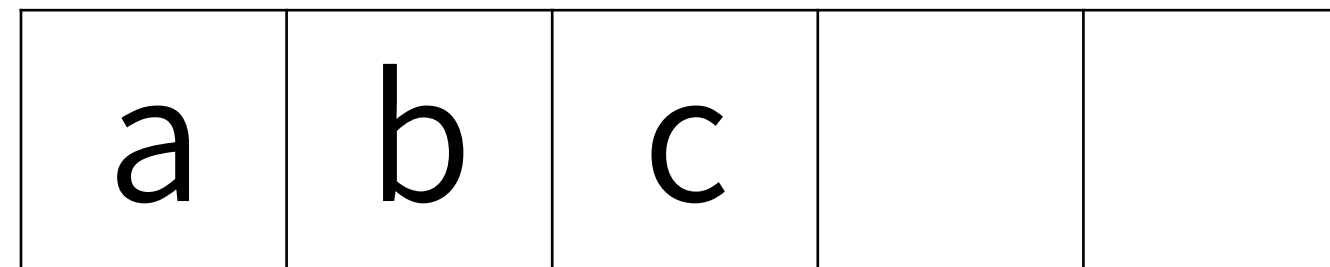
numElements:3



Push (c)

Stack Implementation with Arrays

numElements:3



Push (c)

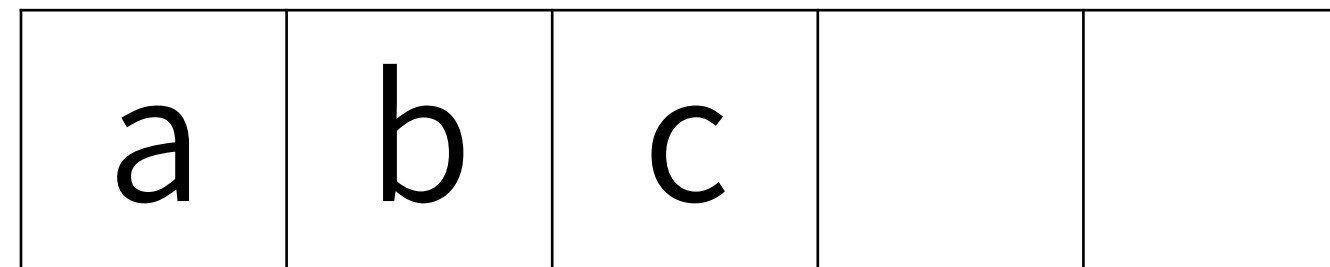
Stack Implementation with Arrays

numElements:3

a	b	c		
---	---	---	--	--

Stack Implementation with Arrays

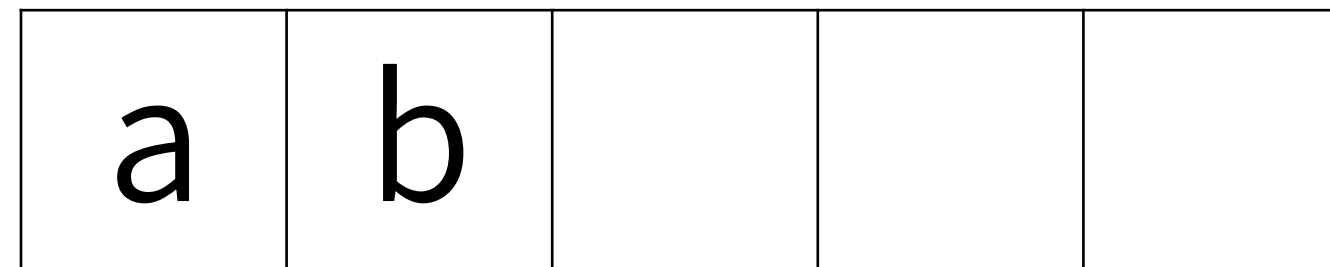
numElements:3



Pop ()

Stack Implementation with Arrays

numElements:2



Pop () → c

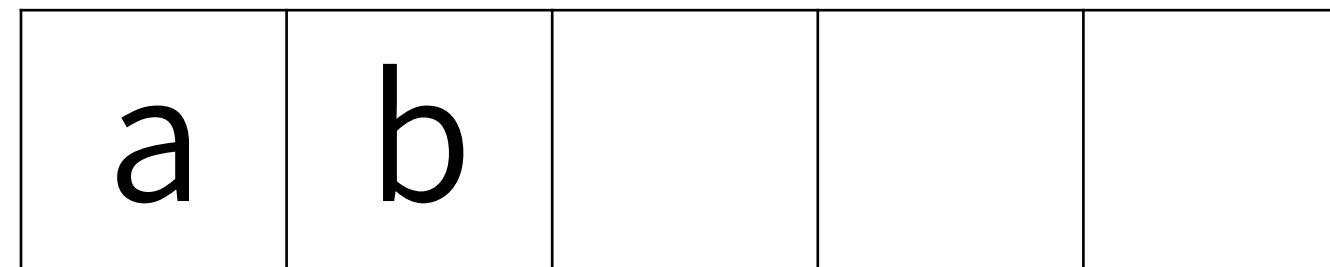
Stack Implementation with Arrays

numElements:2

a	b			
---	---	--	--	--

Stack Implementation with Arrays

numElements:2



Push (d)

Stack Implementation with Arrays

numElements:3

a	b	d		
---	---	---	--	--

Push (d)

Stack Implementation with Arrays

numElements:3

a	b	d		
---	---	---	--	--

Stack Implementation with Arrays

numElements:3

a	b	d		
---	---	---	--	--

Push (e)

Stack Implementation with Arrays

numElements:4

a	b	d	e	
---	---	---	---	--

Push (e)

Stack Implementation with Arrays

numElements:4

a	b	d	e	
---	---	---	---	--

Stack Implementation with Arrays

numElements:4

a	b	d	e	
---	---	---	---	--

Push (f)

Stack Implementation with Arrays

numElements:5

a	b	d	e	f
---	---	---	---	---

Push (f)

Stack Implementation with Arrays

numElements:5

a	b	d	e	f
---	---	---	---	---

Stack Implementation with Arrays

numElements:5

a	b	d	e	f
---	---	---	---	---

Push (g)

Stack Implementation with Arrays

numElements:5

a	b	d	e	f
---	---	---	---	---

Push (g) → ERROR

Stack Implementation with Arrays

numElements:5

a	b	d	e	f
---	---	---	---	---

Empty()

Stack Implementation with Arrays

numElements:5

a	b	d	e	f
---	---	---	---	---

Empty() → False

Stack Implementation with Arrays

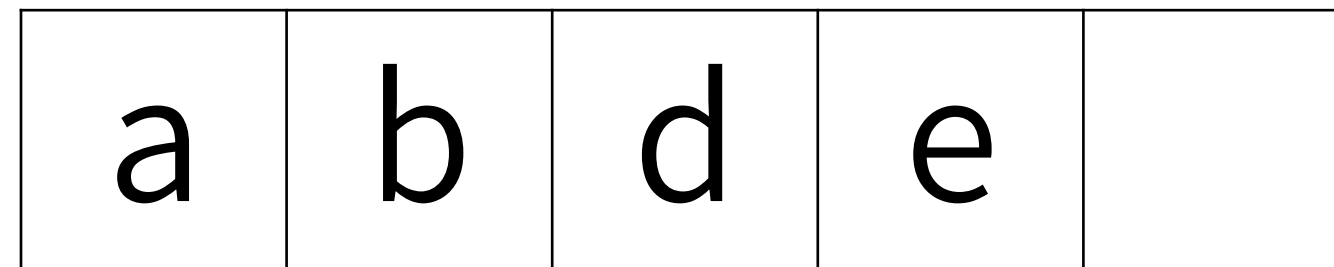
numElements:5

a	b	d	e	f
---	---	---	---	---

Pop ()

Stack Implementation with Arrays

numElements:4



Pop () → f

Stack Implementation with Arrays

numElements:4

a	b	d	e	
---	---	---	---	--

Stack Implementation with Arrays

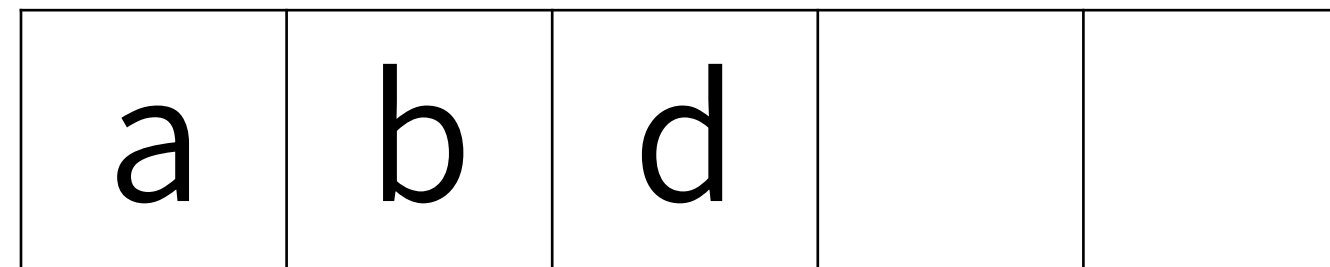
numElements:4

a	b	d	e	
---	---	---	---	--

Pop ()

Stack Implementation with Arrays

numElements:3



Pop () → e

Stack Implementation with Arrays

numElements:3

a	b	d		
---	---	---	--	--

Stack Implementation with Arrays

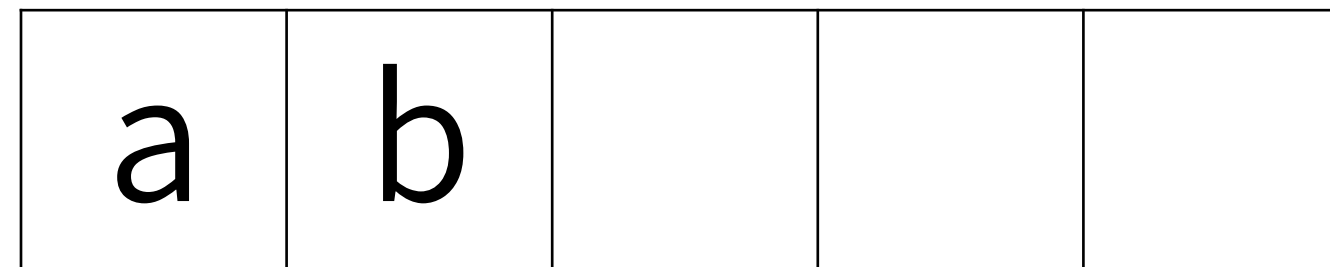
numElements:3

a	b	d		
---	---	---	--	--

Pop ()

Stack Implementation with Arrays

numElements:2



Pop () → d

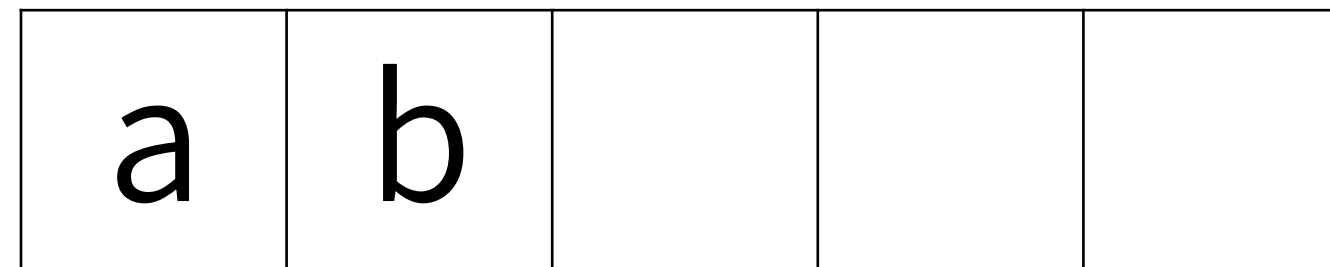
Stack Implementation with Arrays

numElements:2

a	b			
---	---	--	--	--

Stack Implementation with Arrays

numElements:2



Pop ()

Stack Implementation with Arrays

numElements:1



Pop () → b

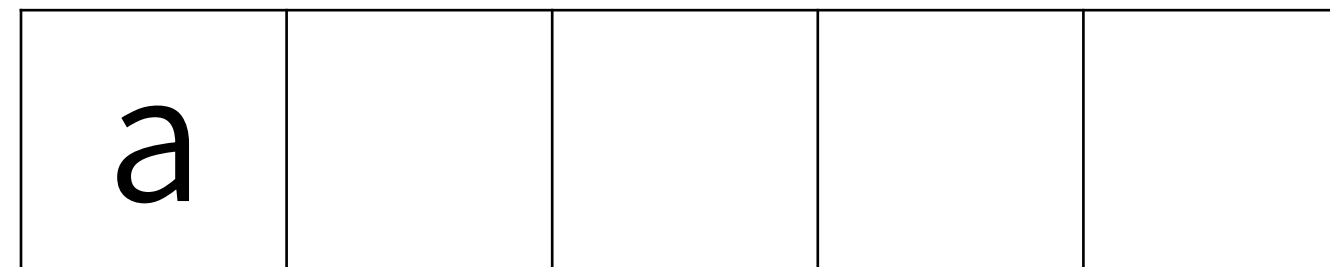
Stack Implementation with Arrays

numElements:1

a				
---	--	--	--	--

Stack Implementation with Arrays

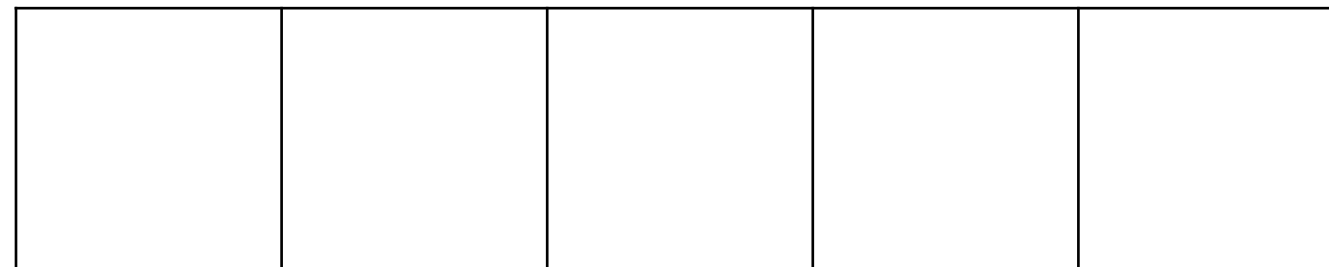
numElements:1



Pop ()

Stack Implementation with Arrays

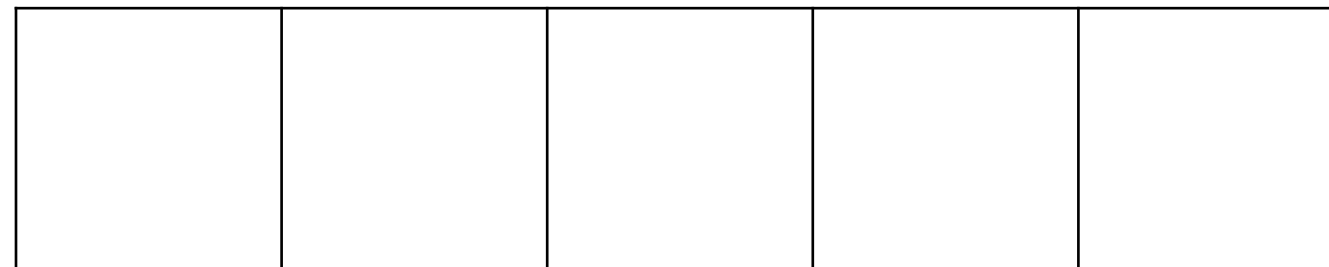
numElements:0



Pop () → a

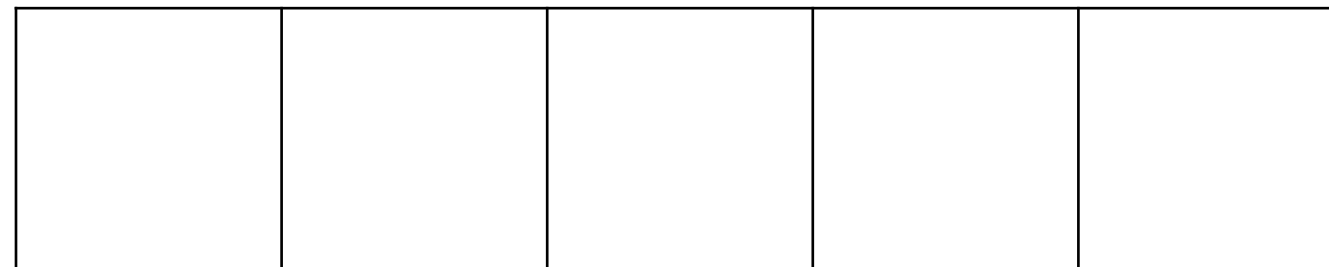
Stack Implementation with Arrays

numElements:0



Stack Implementation with Arrays

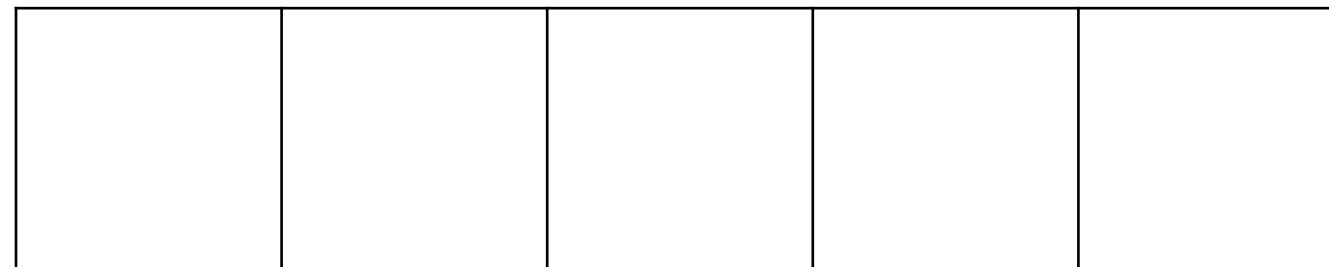
numElements:0



Empty()

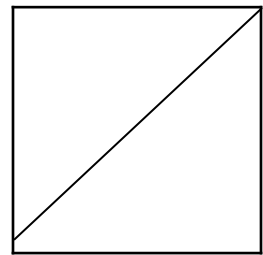
Stack Implementation with Arrays

numElements:0



`Empty() → True`

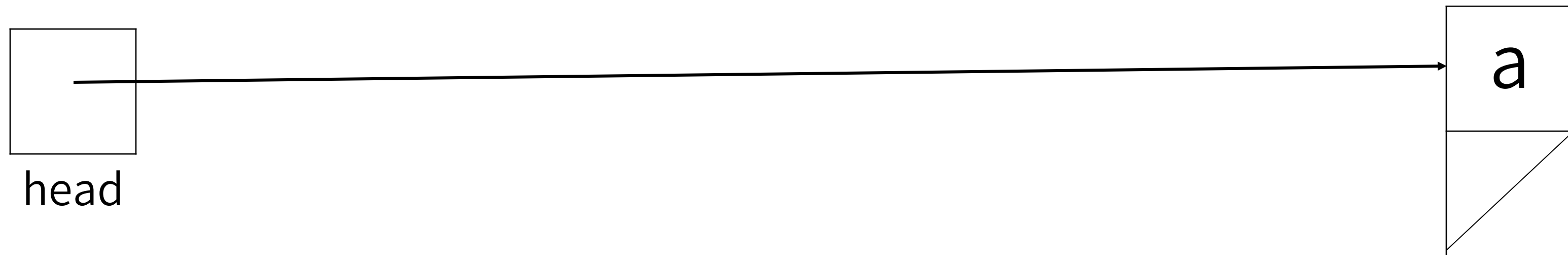
Stack Implementation with Linked List



head

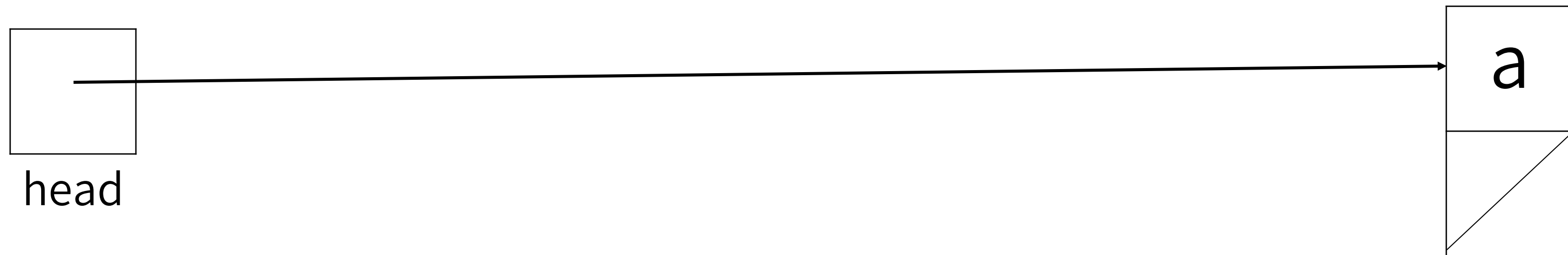
Push (a)

Stack Implementation with Linked List

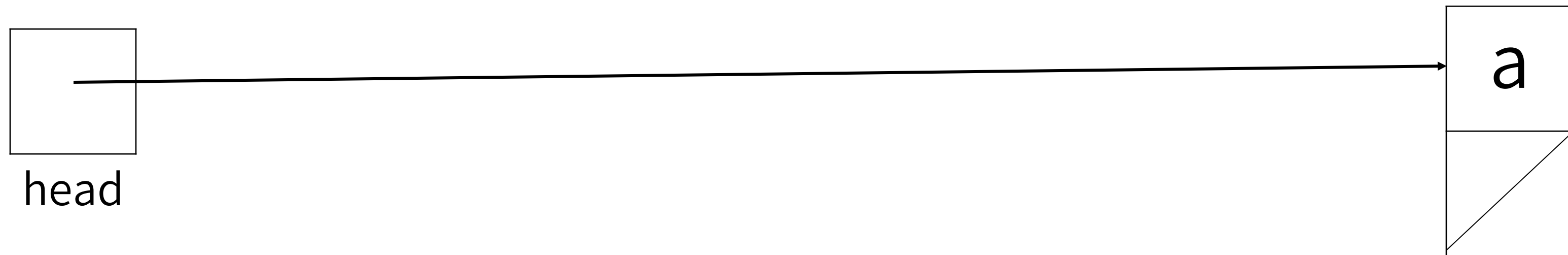


Push (a)

Stack Implementation with Linked List



Stack Implementation with Linked List



Push (b)

Stack Implementation with Linked List

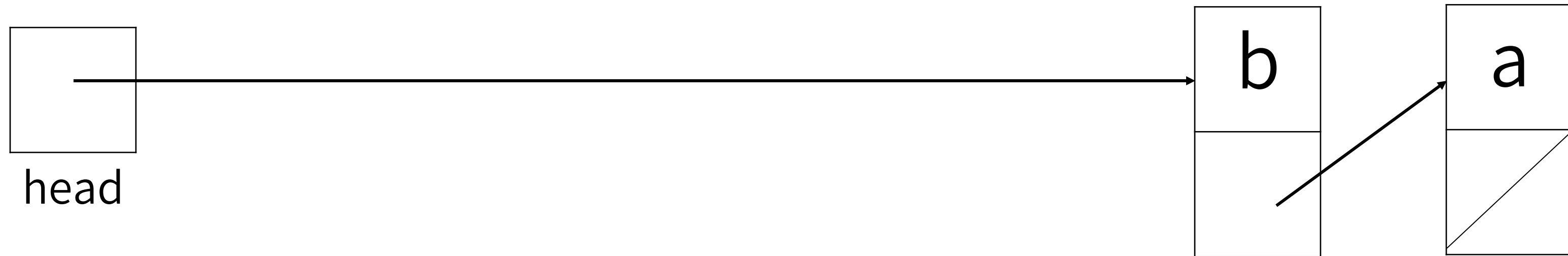


Push (b)

Stack Implementation with Linked List



Stack Implementation with Linked List



Top ()

Stack Implementation with Linked List



`Top () → b`

Stack Implementation with Linked List



Stack Implementation with Linked List



Push (c)

Stack Implementation with Linked List



Push (c)

Stack Implementation with Linked List



Stack Implementation with Linked List



Pop ()

Stack Implementation with Linked List



Pop ()

Stack Implementation with Linked List



Pop () → c

Stack Implementation with Linked List



Stack Implementation with Linked List



Push (d)

Stack Implementation with Linked List



Push (d)

Stack Implementation with Linked List

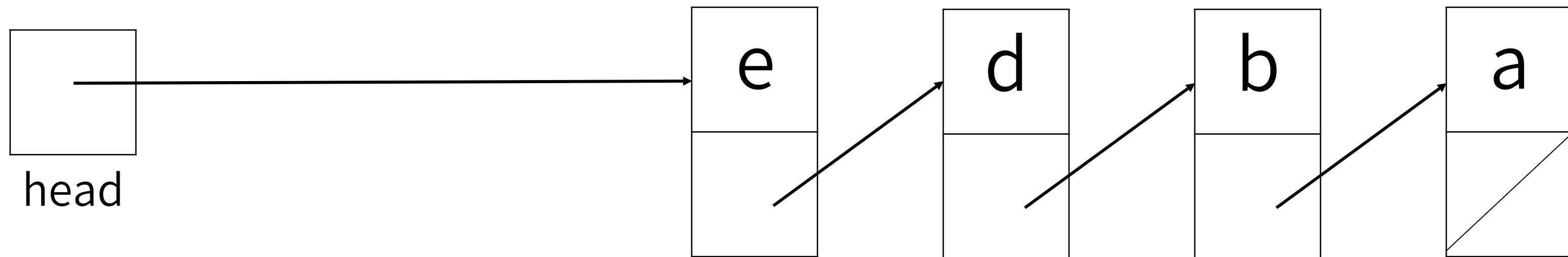


Stack Implementation with Linked List



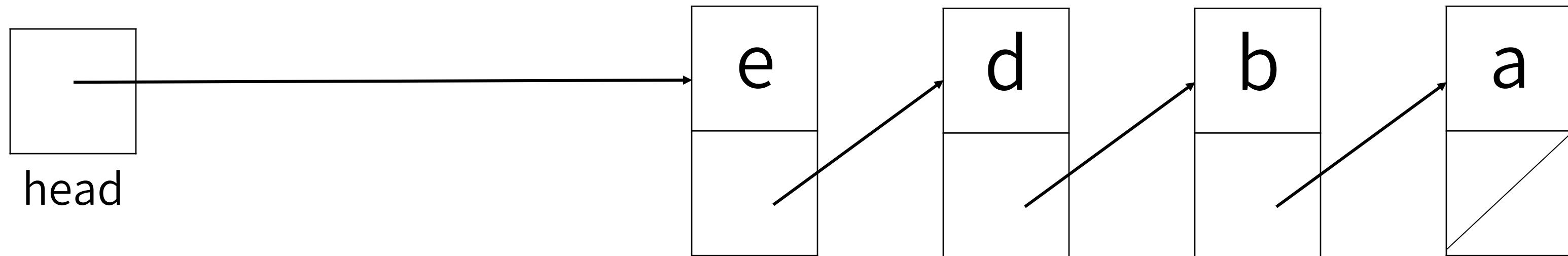
Push (e)

Stack Implementation with Linked List

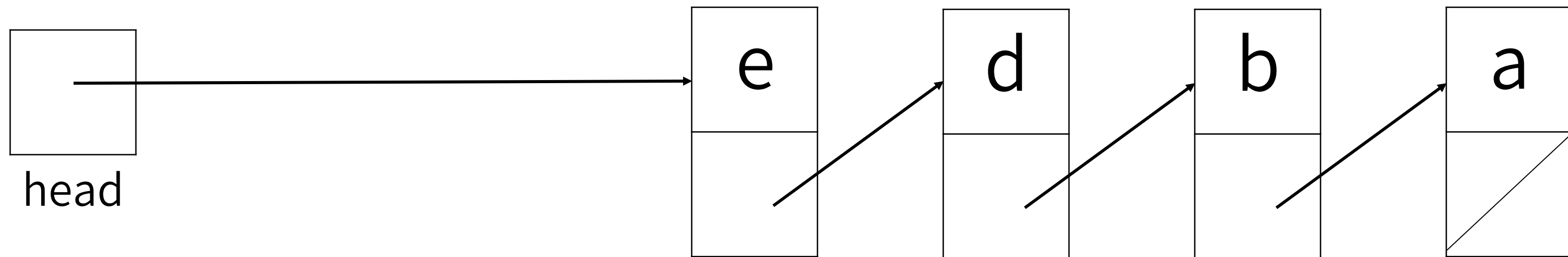


Push (e)

Stack Implementation with Linked List

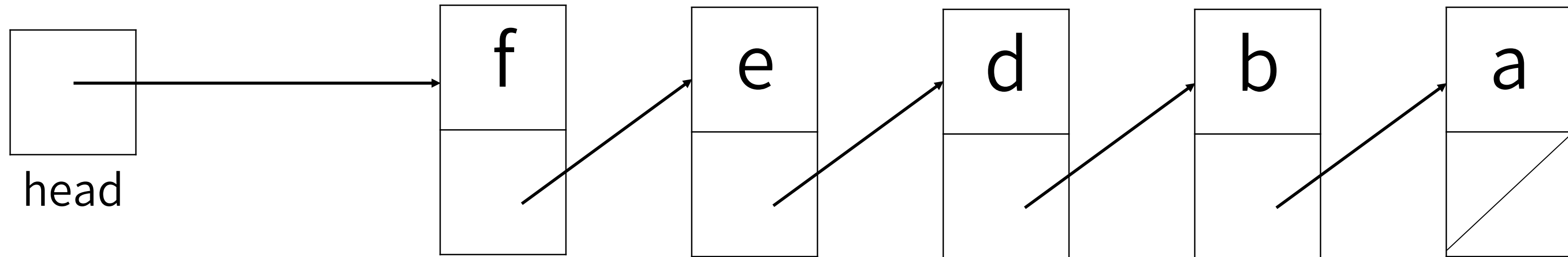


Stack Implementation with Linked List



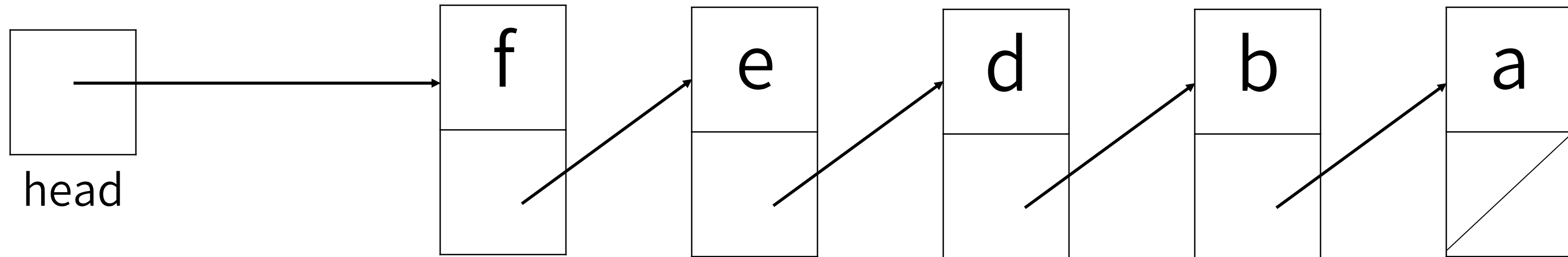
Push (f)

Stack Implementation with Linked List

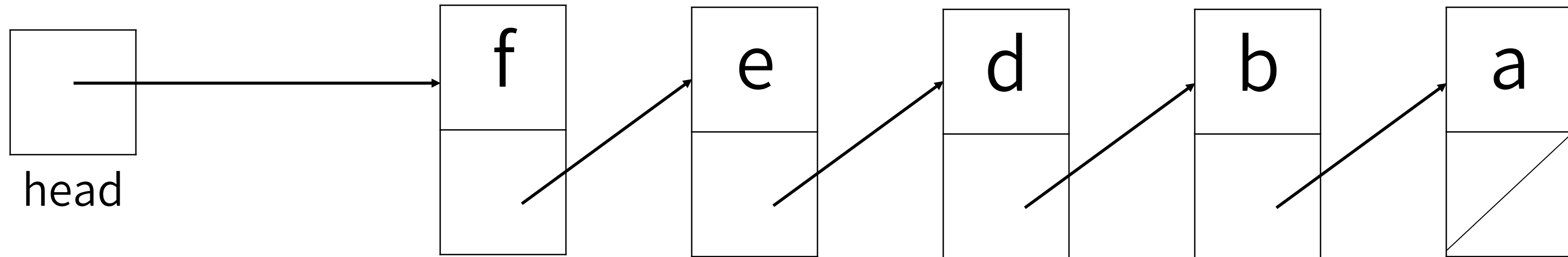


Push (f)

Stack Implementation with Linked List

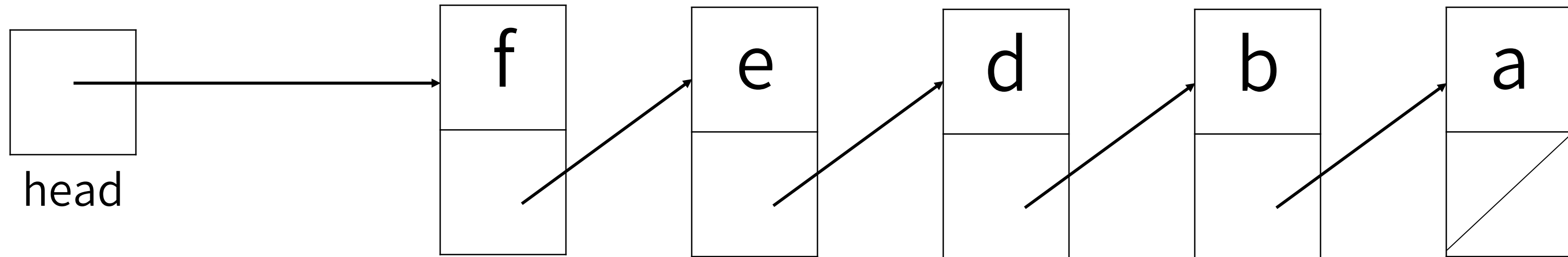


Stack Implementation with Linked List



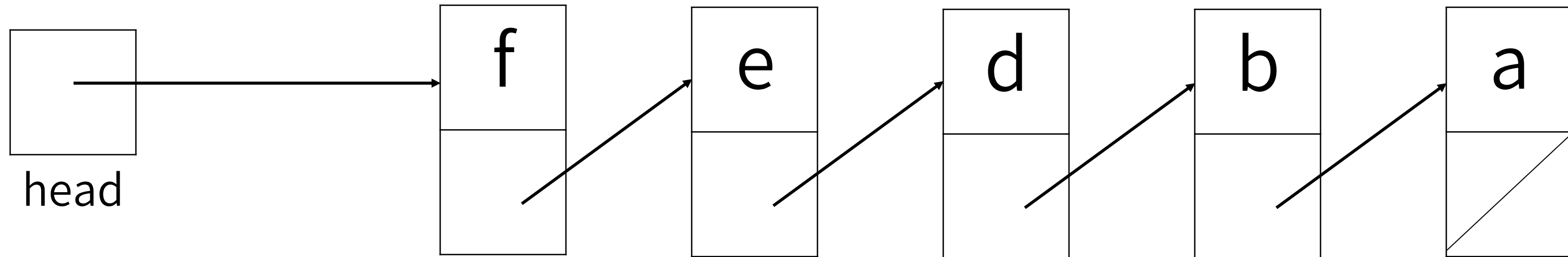
`Empty()`

Stack Implementation with Linked List



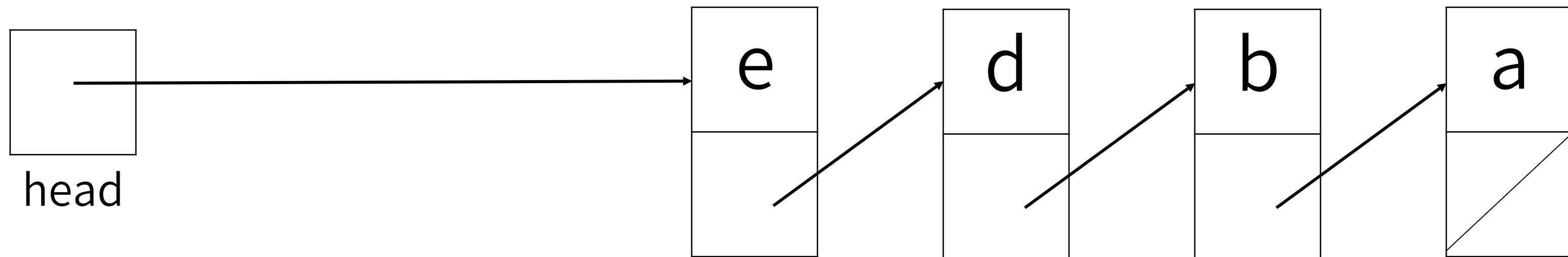
`Empty() → False`

Stack Implementation with Linked List



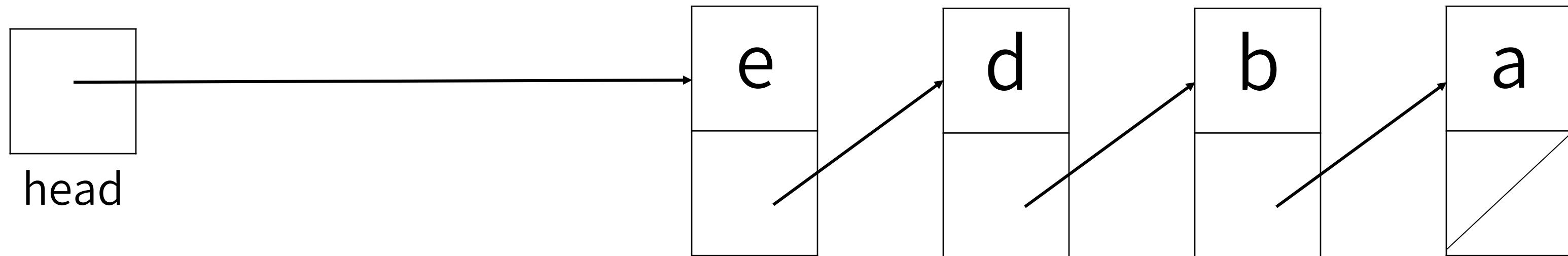
Pop ()

Stack Implementation with Linked List

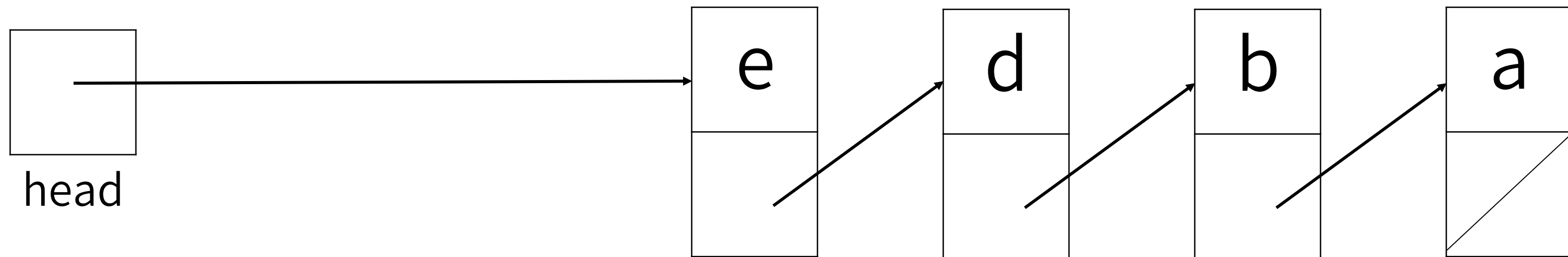


Pop () → f

Stack Implementation with Linked List



Stack Implementation with Linked List



Pop ()

Stack Implementation with Linked List



Pop () → e

Stack Implementation with Linked List



Stack Implementation with Linked List



Pop ()

Stack Implementation with Linked List



Pop () → d

Stack Implementation with Linked List

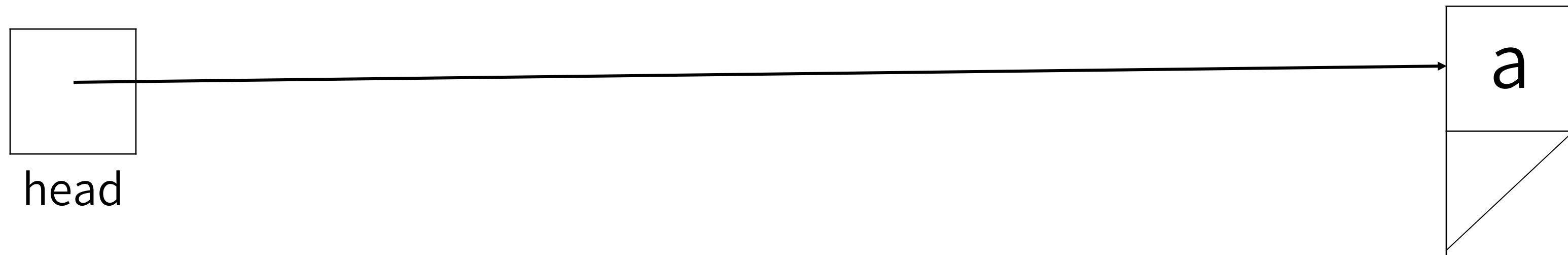


Stack Implementation with Linked List



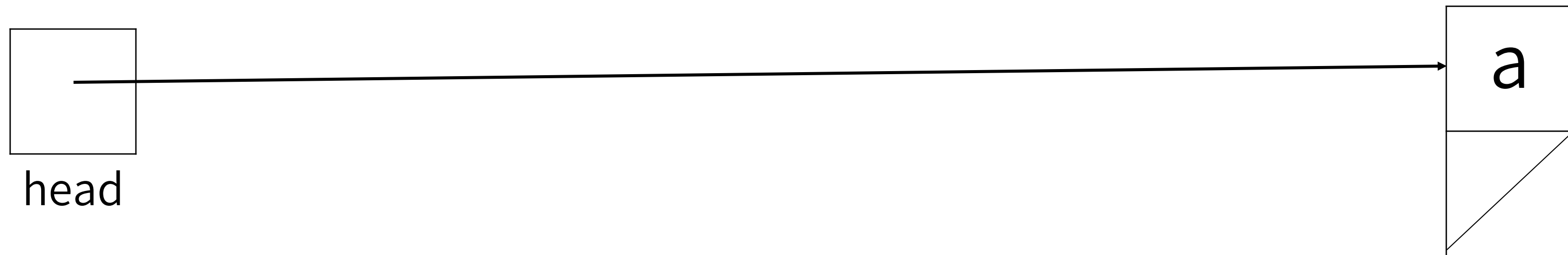
Pop ()

Stack Implementation with Linked List



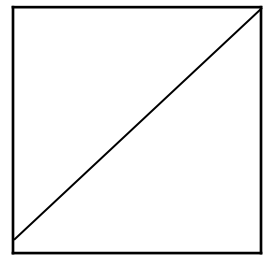
Pop () → b

Stack Implementation with Linked List



Pop ()

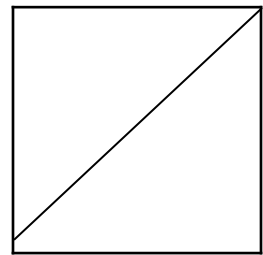
Stack Implementation with Linked List



head

Pop () → a

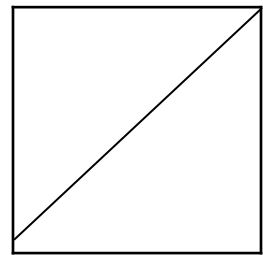
Stack Implementation with Linked List



head

Empty ()

Stack Implementation with Linked List



head

`Empty() → True`

Summary

- Stacks can be implemented with either an array or a linked list.
- Each stack operation is $O(1)$: Push, Pop, Top, Empty.
- Implementation with linked list:
 - Push : `PushFront()`
 - Top : `TopFront()`
 - Pop : `TopFront() + PopFront()`
- Stacks are occasionally known as LIFO queues.

ADT - Queue



Queue



Queue

An abstract data type in which element are added to the rear and remove from the front; a “first in, first out” (FIFO) structure.

A queue is a first-in, first-out (FIFO) data structure that operates like the line at your favorite coffee shop: we add new elements at the back of the queue and remove old elements from the front.

A list data structure in which elements are inserted at one end and removed from the other end.

Queue Operations

Enqueue(key)

Add a new element to the back of the queue.

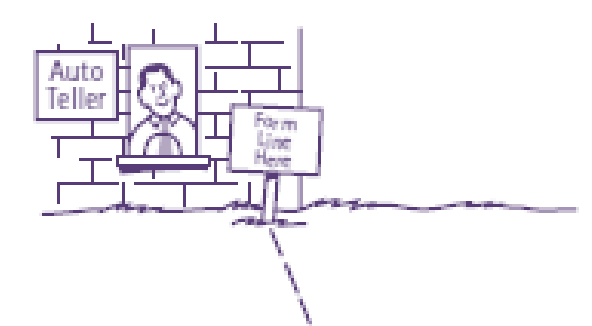
Dequeue(key)

Remove the element from the front of the queue and return it.

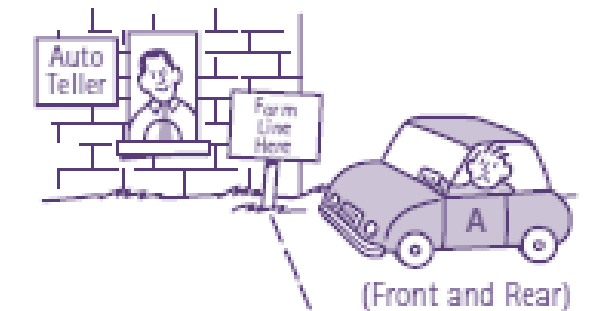
IsEmpty()

Check whether there are any elements

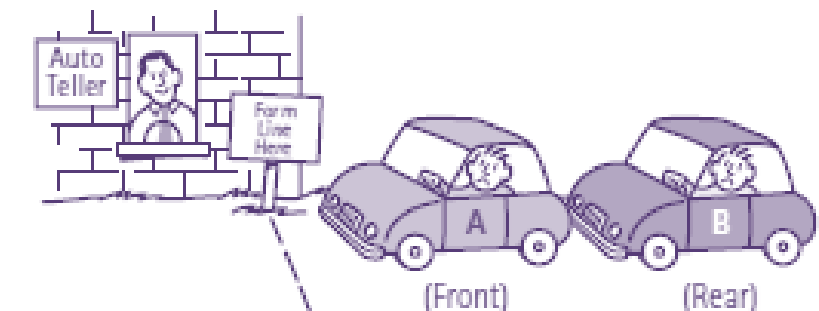
`QueueType queue;`
`queue.IsEmpty() == true`



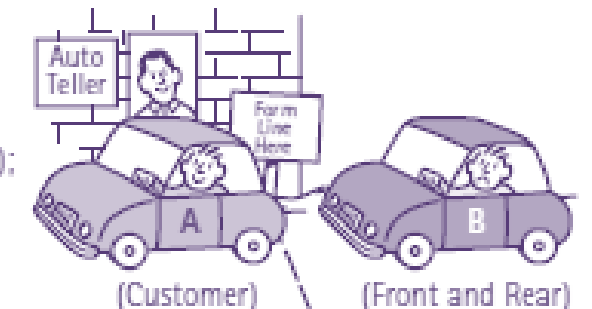
`queue.Enqueue(A);`
`queue.IsEmpty() == false`



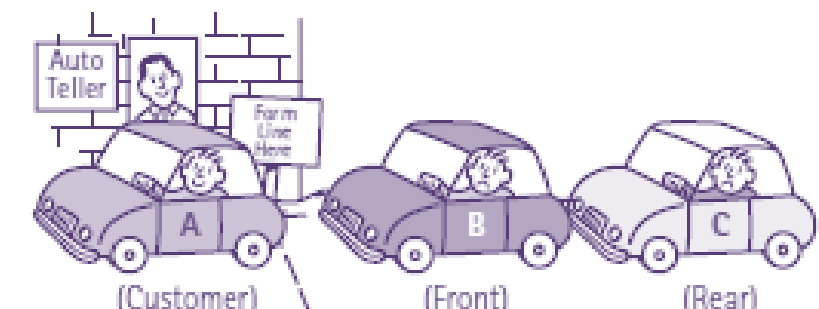
`queue.Enqueue(B);`



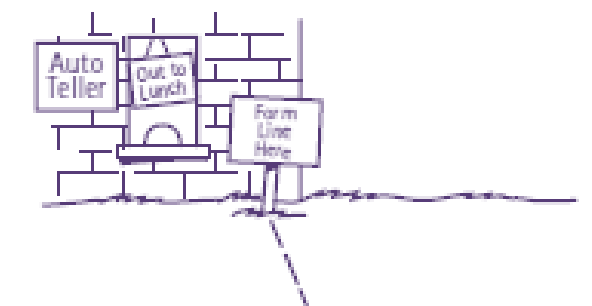
`queue.Dequeue(Customer);`



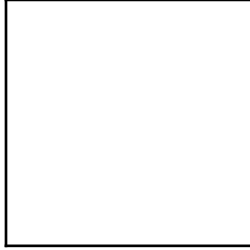
`queue.Enqueue(C);`

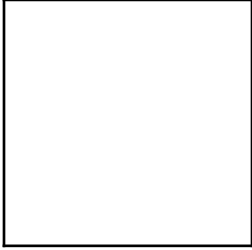


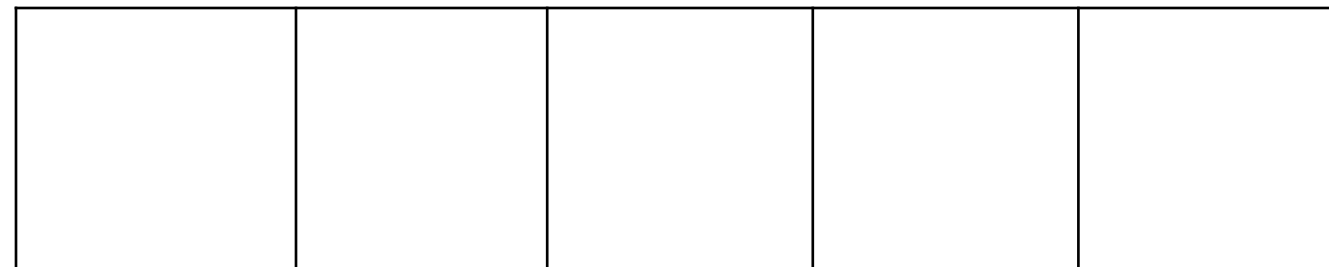
`queue.MakeEmpty();`
`queue.IsEmpty() == true`



Queue Implementation with Arrays


read/ front


write/back/rear



Queue Implementation with Arrays

0

front

0

rear



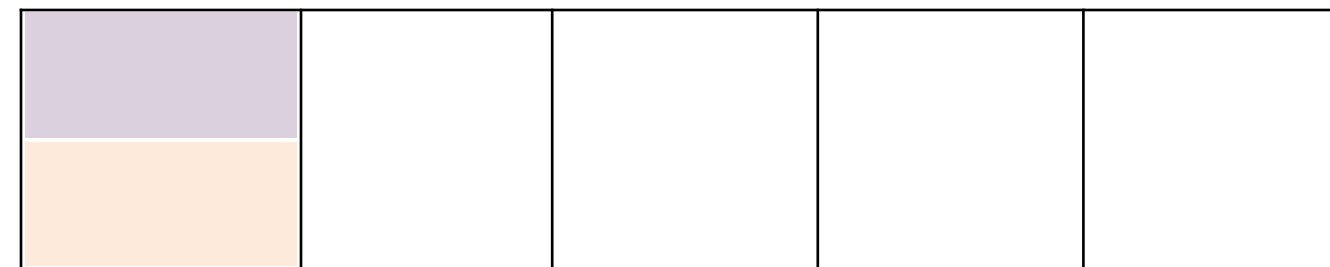
Queue Implementation with Arrays

0

front

0

rear



Enqueue (a)

Queue Implementation with Arrays

0

front

1

rear



Enqueue (a)

Queue Implementation with Arrays

0

front

1

rear



Queue Implementation with Arrays

0

front

1

rear



Enqueue (b)

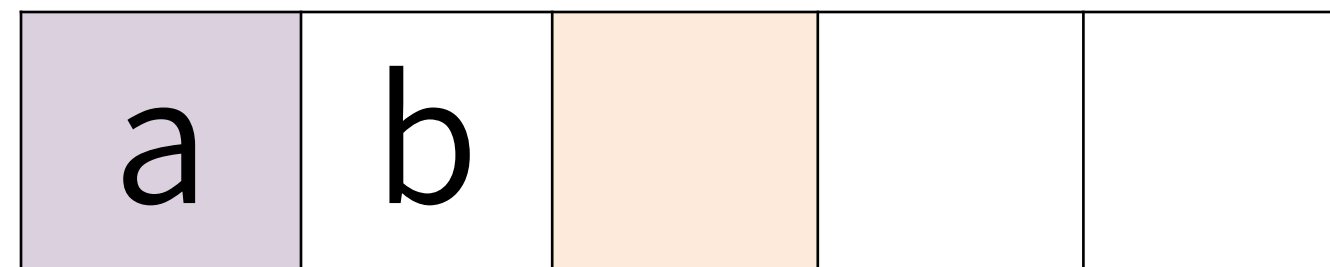
Queue Implementation with Arrays

0

front

2

rear



Enqueue (b)

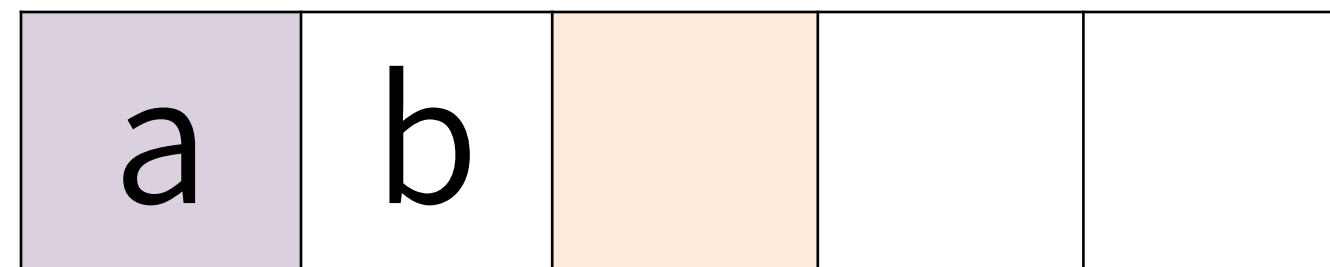
Queue Implementation with Arrays

0

front

2

rear



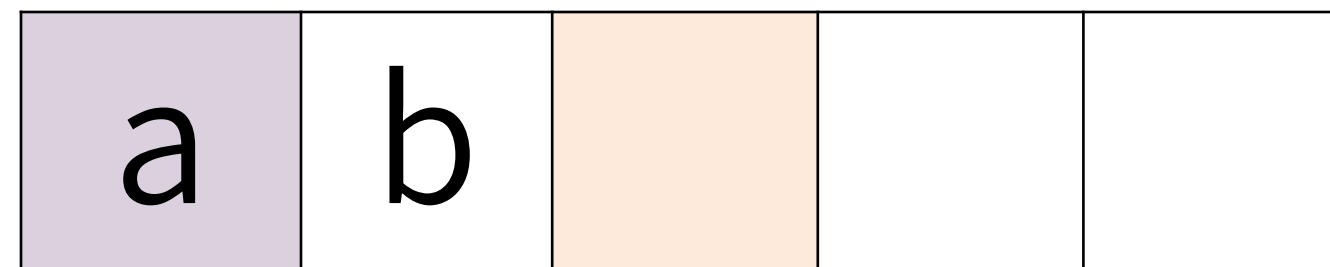
Queue Implementation with Arrays

0

front

2

rear



Empty ()

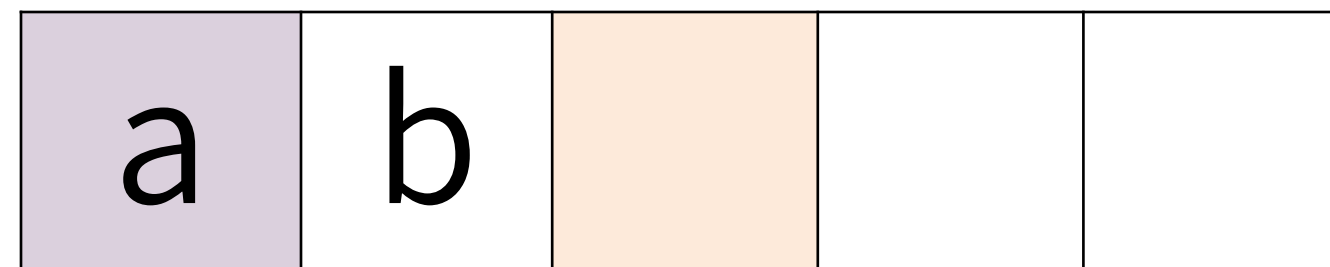
Queue Implementation with Arrays

0

front

2

rear



`Empty()` \rightarrow `False`

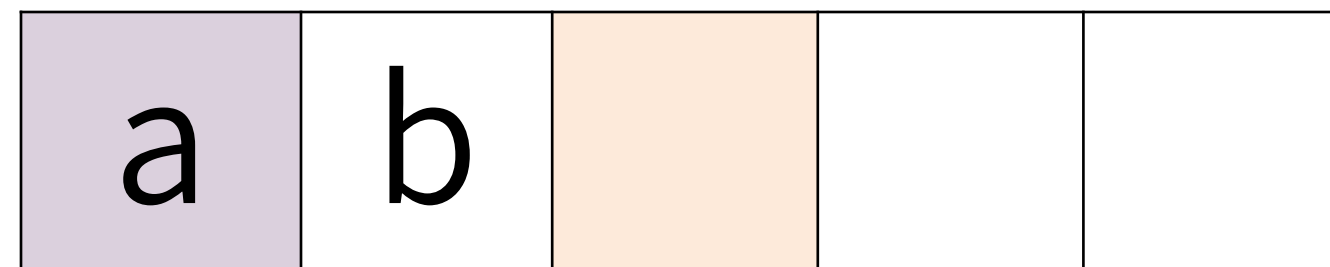
Queue Implementation with Arrays

0

front

2

rear



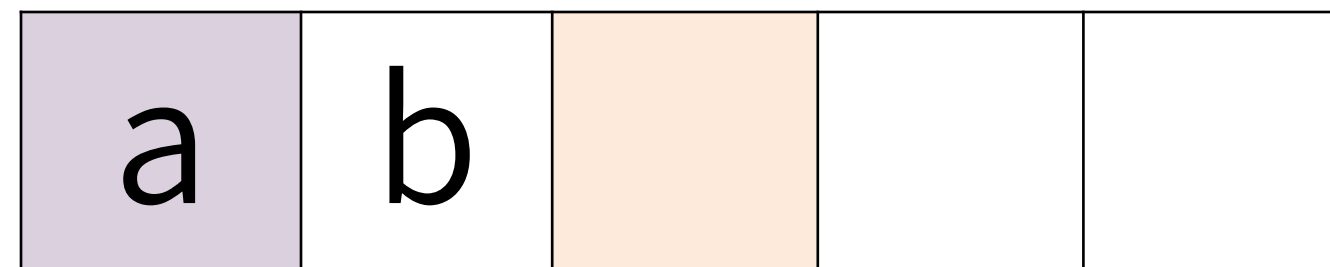
Queue Implementation with Arrays

0

front

2

rear



Enqueue (c)

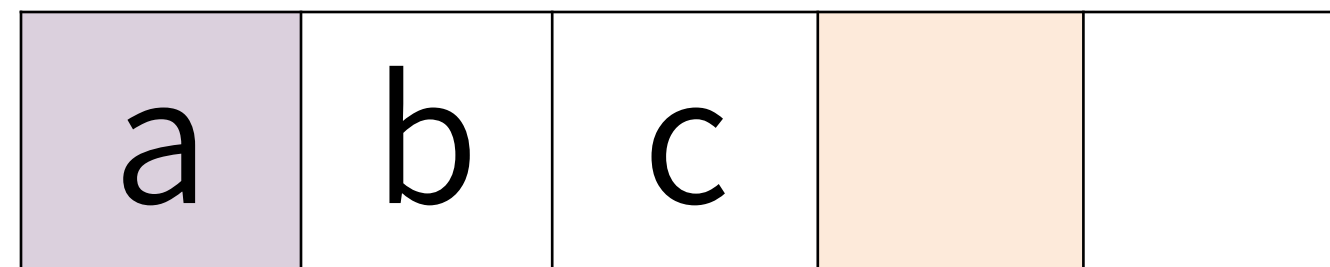
Queue Implementation with Arrays

0

front

3

rear



Enqueue (c)

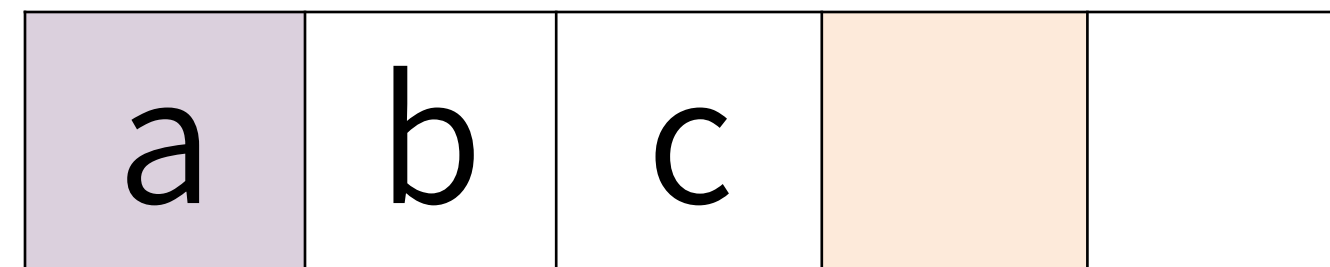
Queue Implementation with Arrays

0

front

3

rear



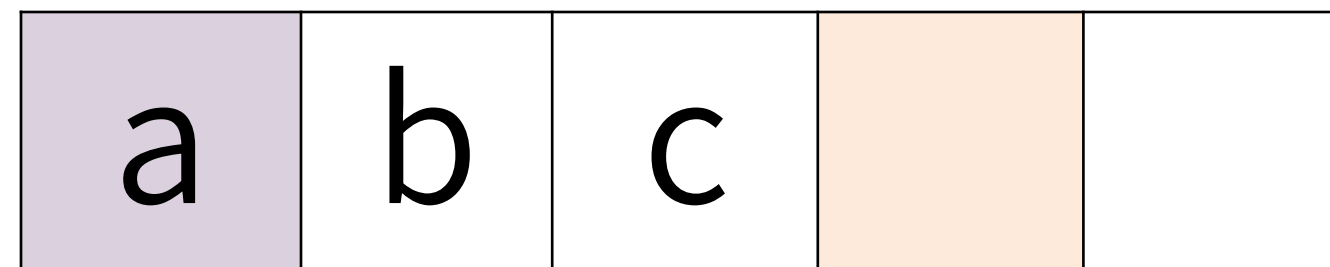
Queue Implementation with Arrays

0

front

3

rear



Dequeue ()

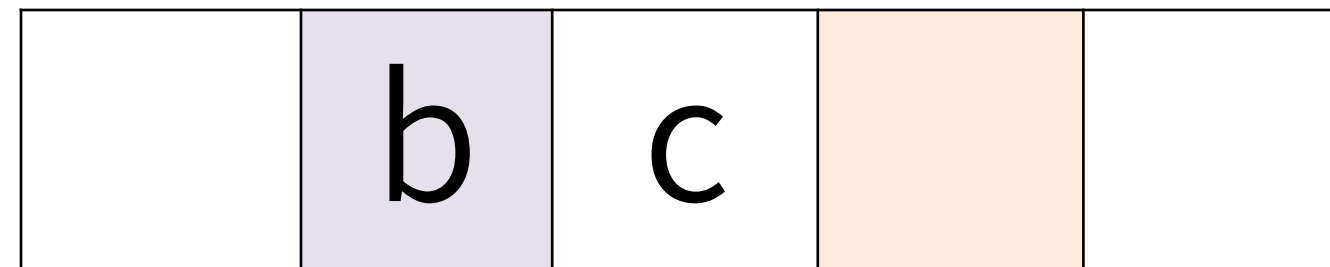
Queue Implementation with Arrays

1

front

3

rear



Dequeue () → a

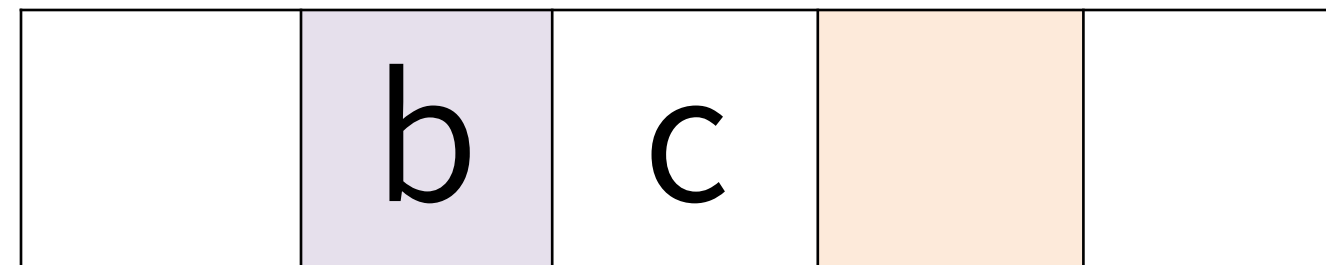
Queue Implementation with Arrays

1

front

3

rear



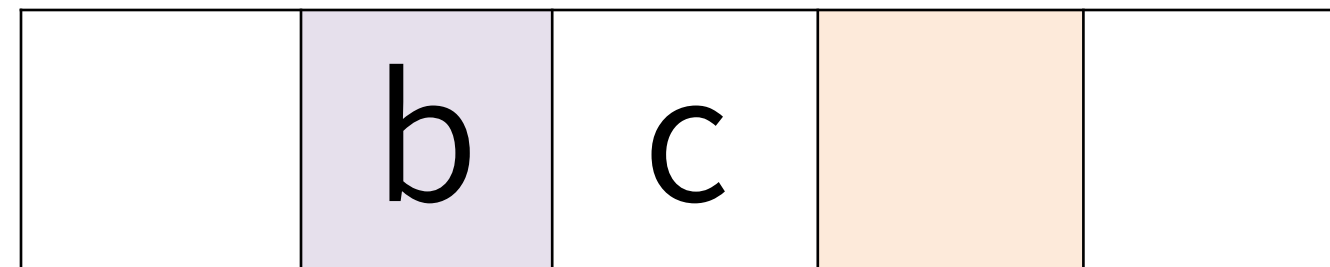
Queue Implementation with Arrays

1

front

3

rear



Dequeue ()

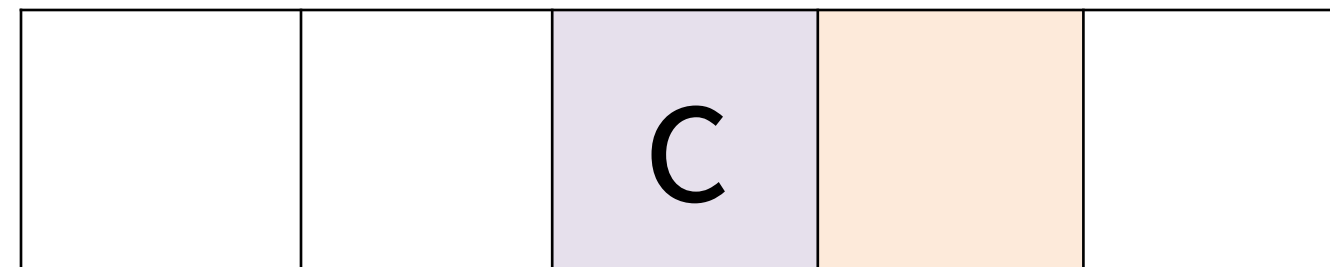
Queue Implementation with Arrays

2

front

3

rear



Dequeue () → b

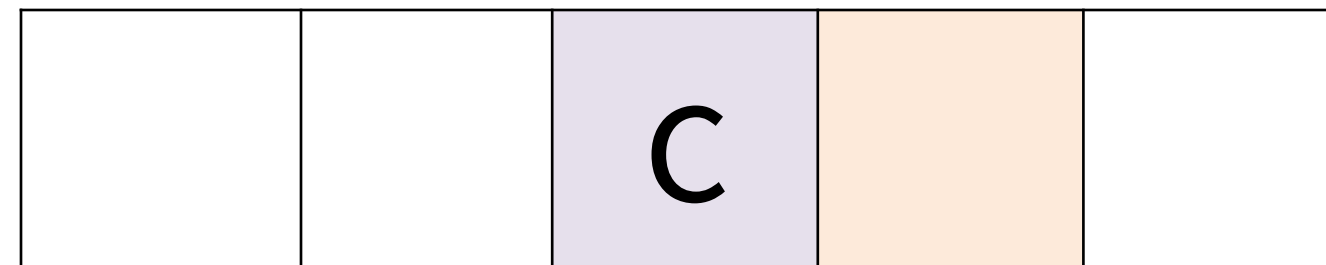
Queue Implementation with Arrays

2

front

3

rear



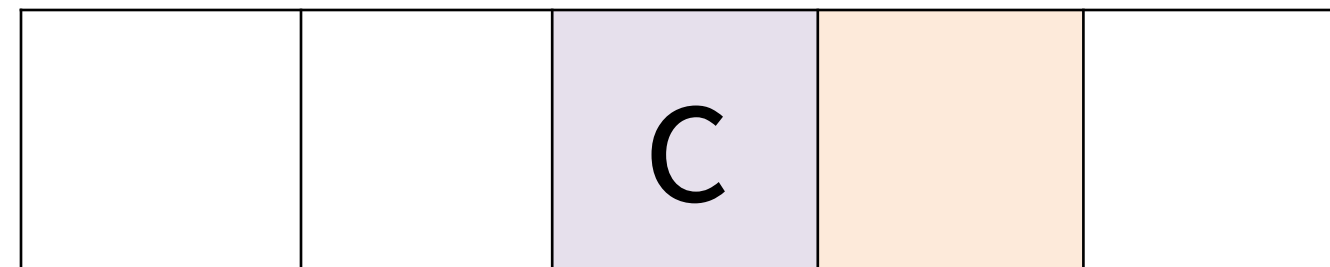
Queue Implementation with Arrays

2

front

3

rear



Enqueue (d)

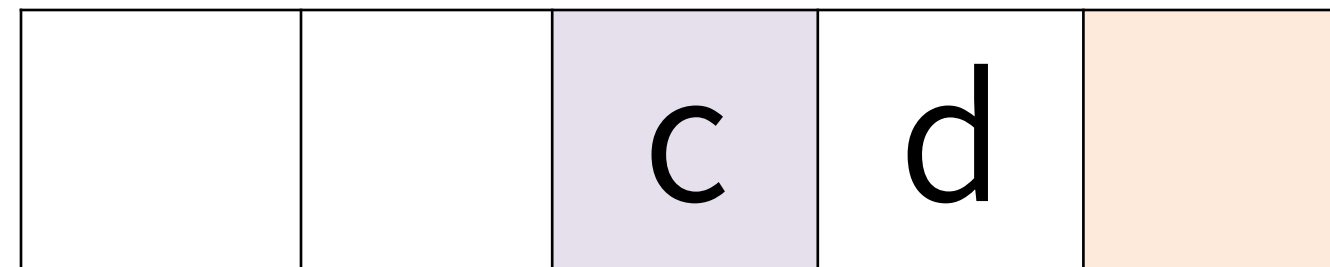
Queue Implementation with Arrays

2

front

4

rear



Enqueue (d)

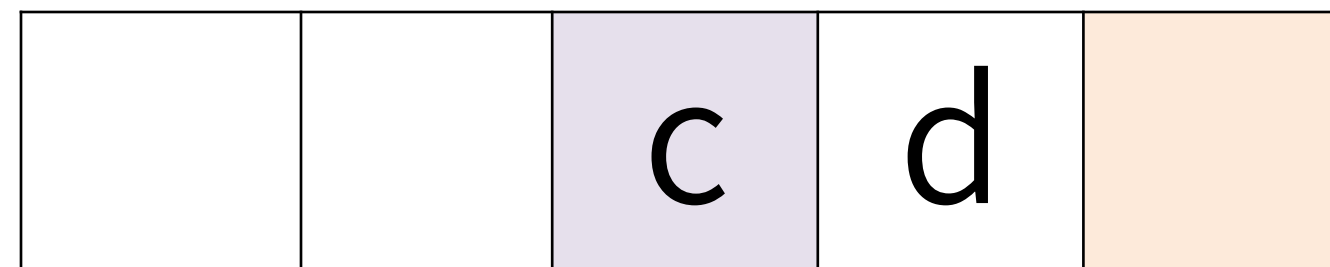
Queue Implementation with Arrays

2

front

4

rear



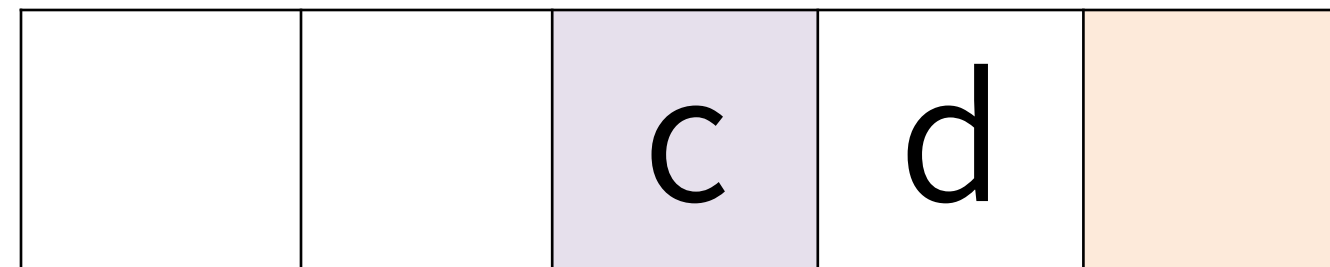
Queue Implementation with Arrays

2

front

4

rear



Enqueue (e)

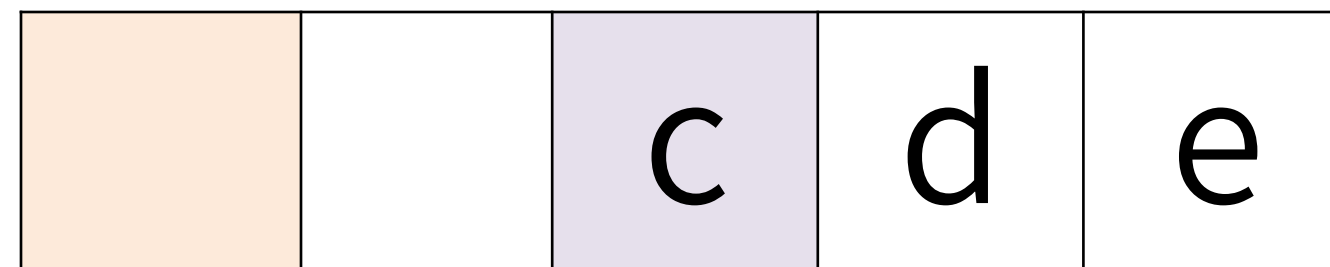
Queue Implementation with Arrays

2

front

0

rear



Enqueue (e)

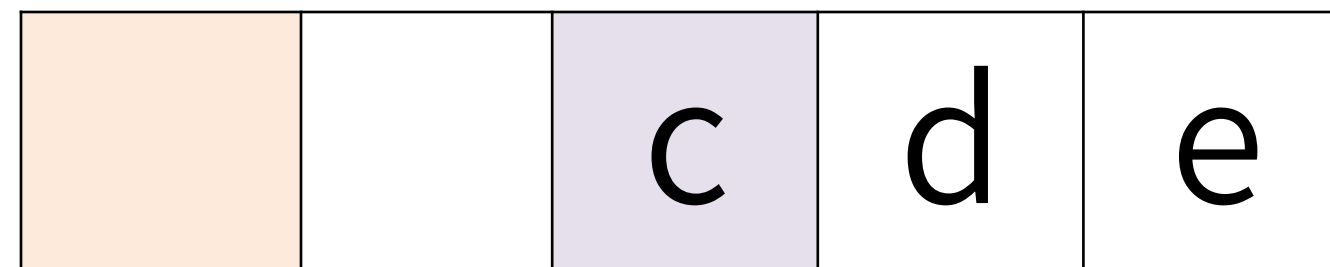
Queue Implementation with Arrays

2

front

0

rear



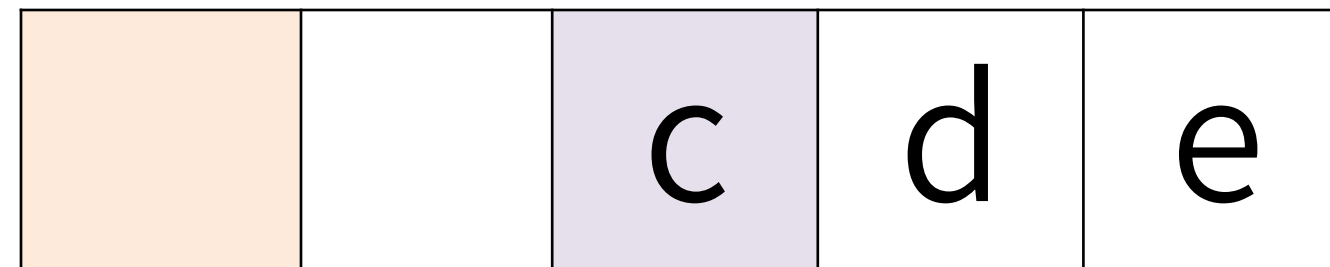
Queue Implementation with Arrays

2

front

0

rear



Enqueue (f)

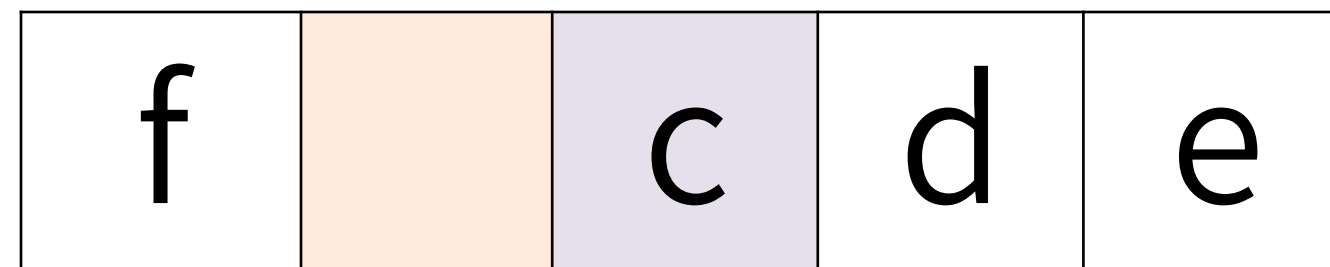
Queue Implementation with Arrays

2

front

1

rear



Enqueue (f)

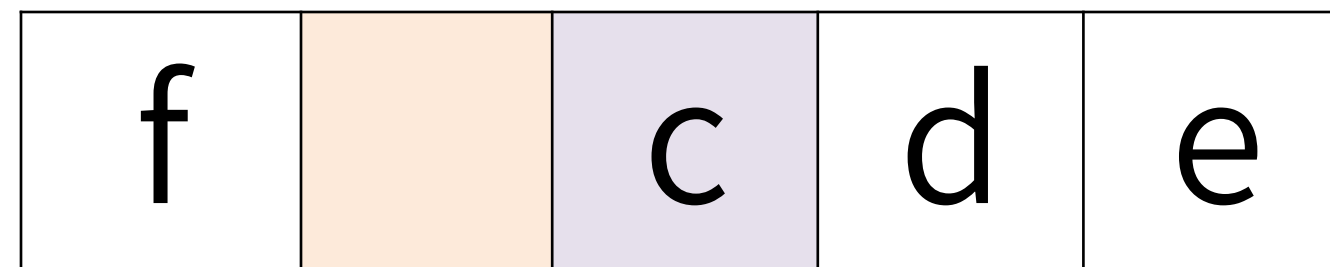
Queue Implementation with Arrays

2

front

1

rear



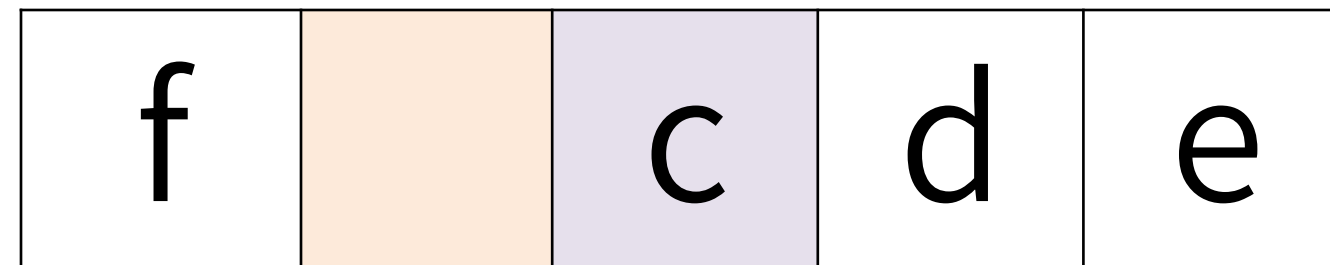
Queue Implementation with Arrays

2

front

1

rear



Enqueue (g)

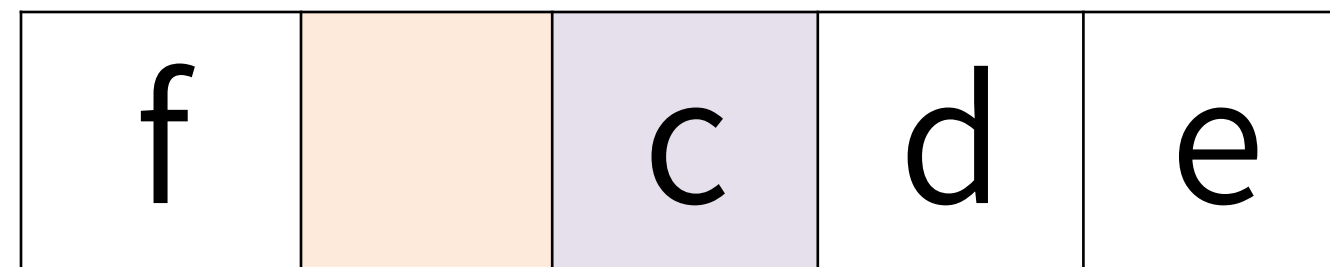
Queue Implementation with Arrays

2

front

1

rear



Enqueue (g) → ERROR

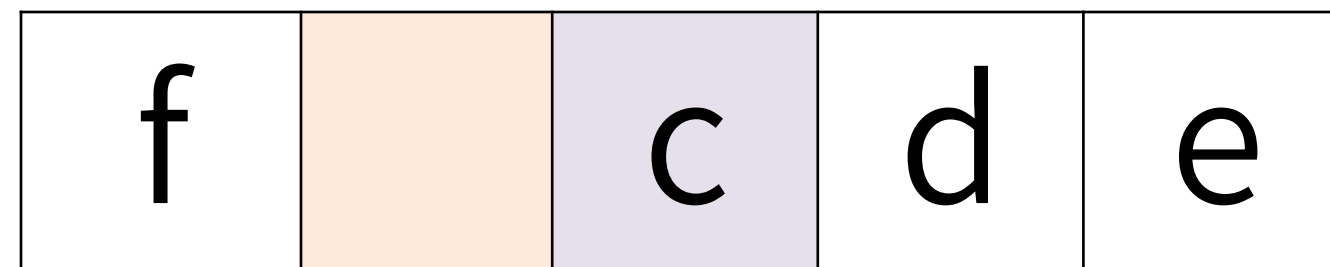
Queue Implementation with Arrays

2

front

1

rear



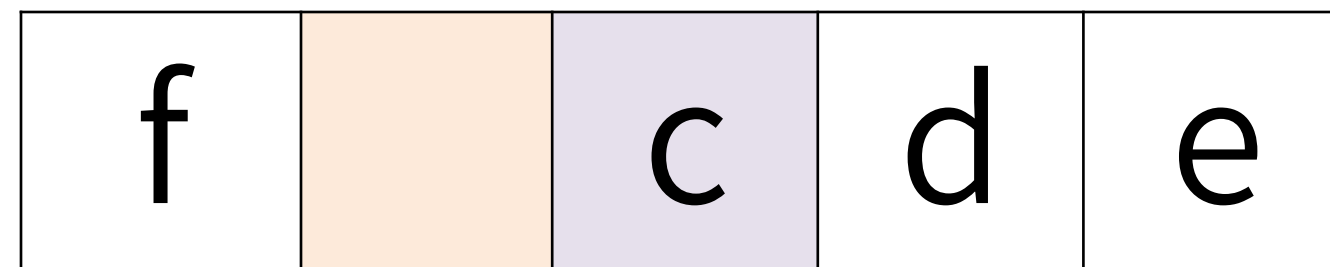
Queue Implementation with Arrays

2

front

1

rear



Dequeue ()

Queue Implementation with Arrays

3

front

1

rear



Dequeue () → c

Queue Implementation with Arrays

3

front

1

rear



Queue Implementation with Arrays

3

front

1

rear



Dequeue ()

Queue Implementation with Arrays

4

front

1

rear



Dequeue () → d

Queue Implementation with Arrays

4

front

1

rear



Queue Implementation with Arrays

4

front

1

rear



Dequeue ()

Queue Implementation with Arrays

0

front

1

rear



Dequeue () → e

Queue Implementation with Arrays

0

front

1

rear



Queue Implementation with Arrays

0

front

1

rear



Dequeue ()

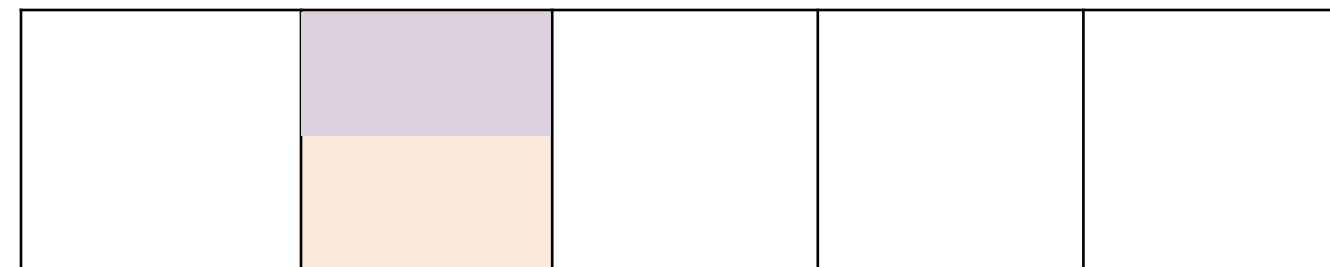
Queue Implementation with Arrays

1

front

1

rear



Dequeue () \rightarrow f

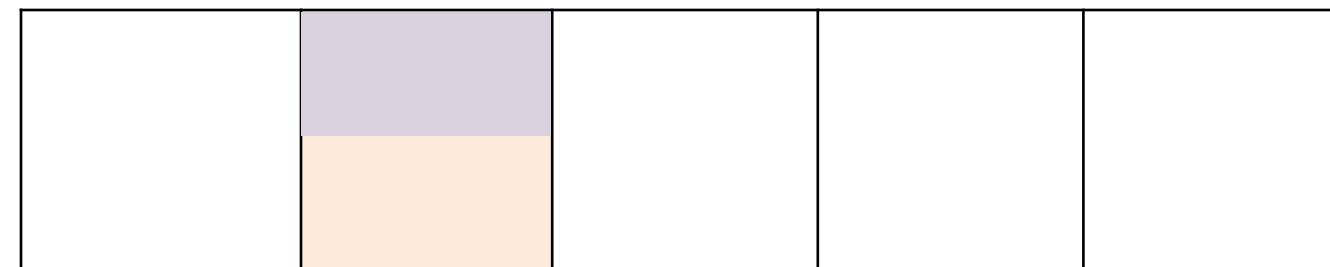
Queue Implementation with Arrays

1

front

1

rear



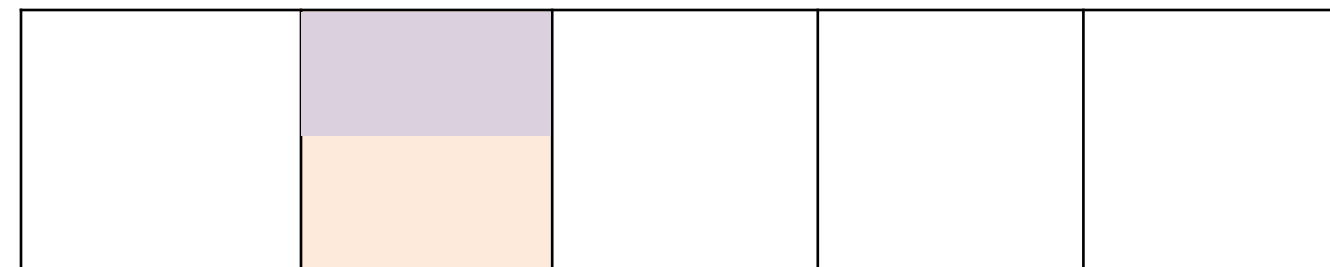
Queue Implementation with Arrays

1

front

1

rear



Empty ()

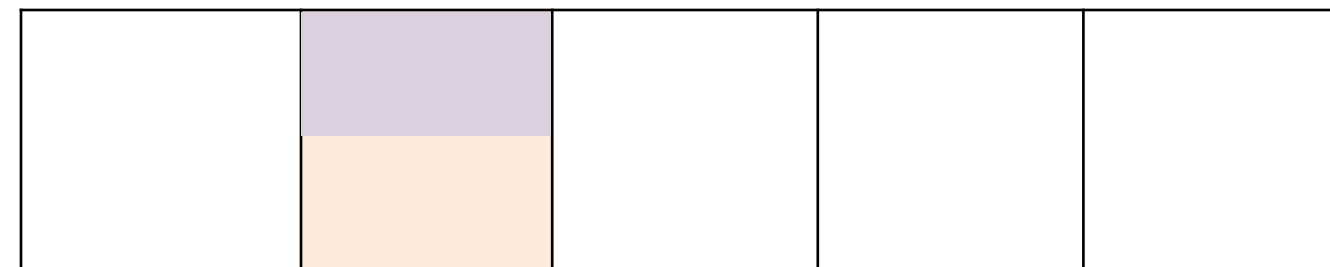
Queue Implementation with Arrays

1

front

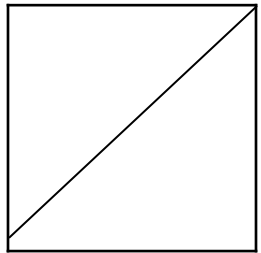
1

rear

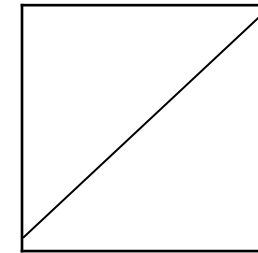


`Empty() → True`

Queue Implementation with Linked List

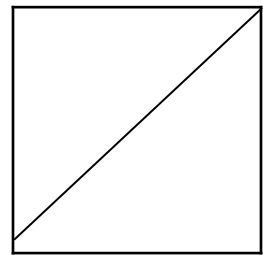


head

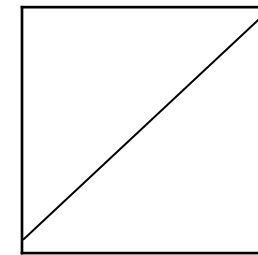


tail

Queue Implementation with Linked List



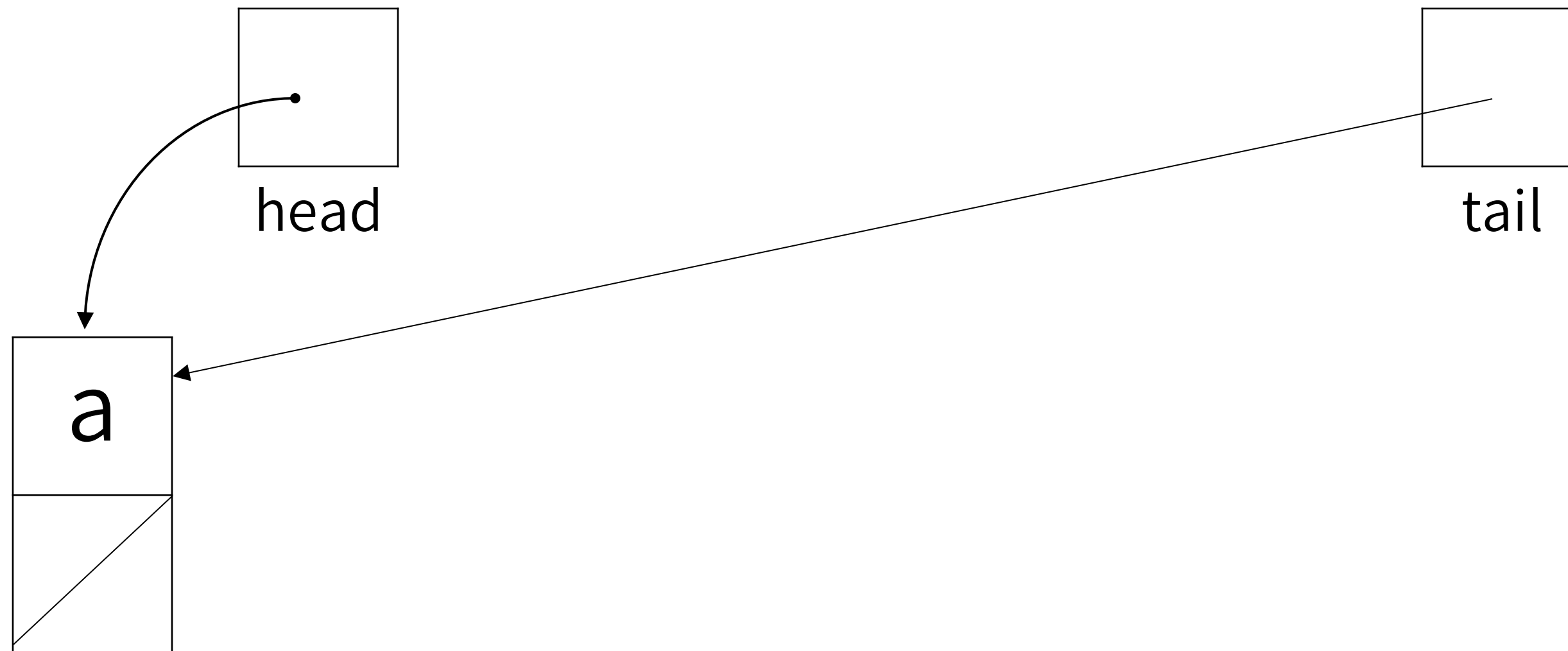
head



tail

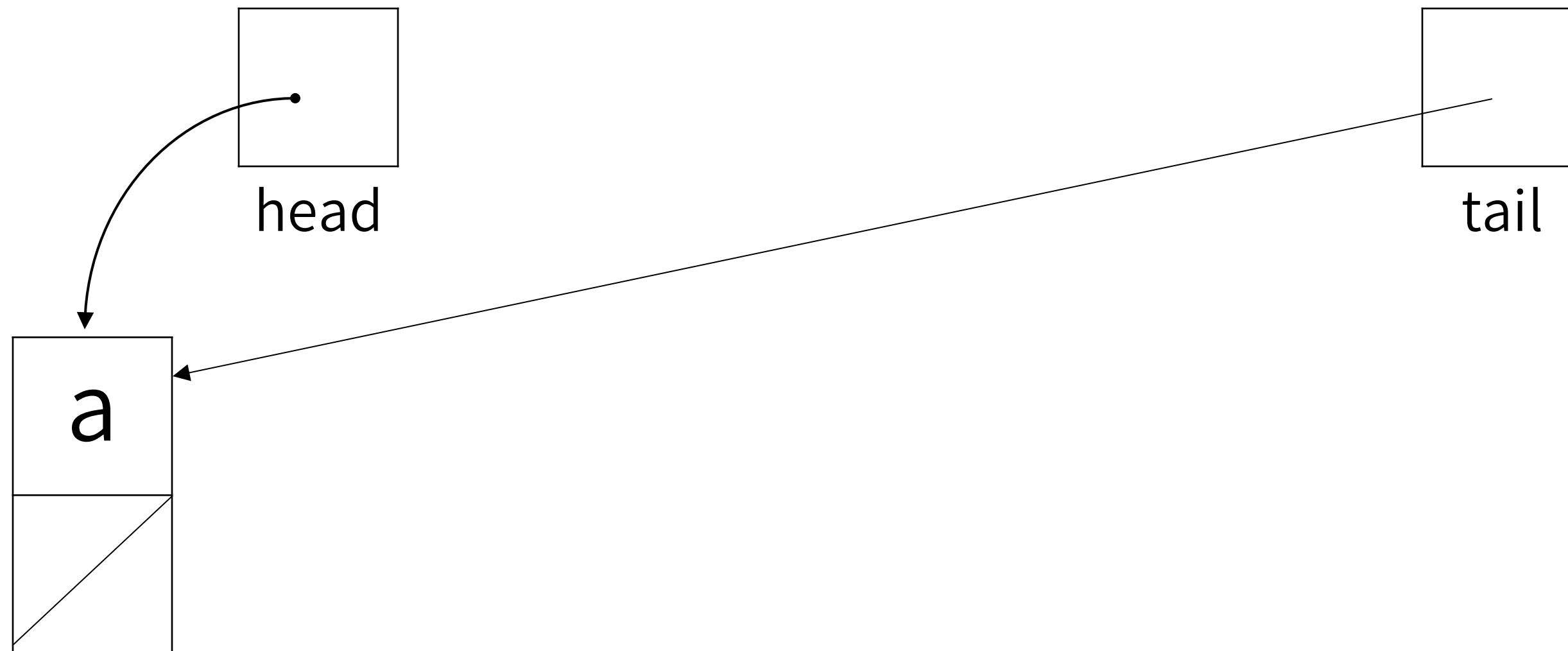
Enqueue (a)

Queue Implementation with Linked List

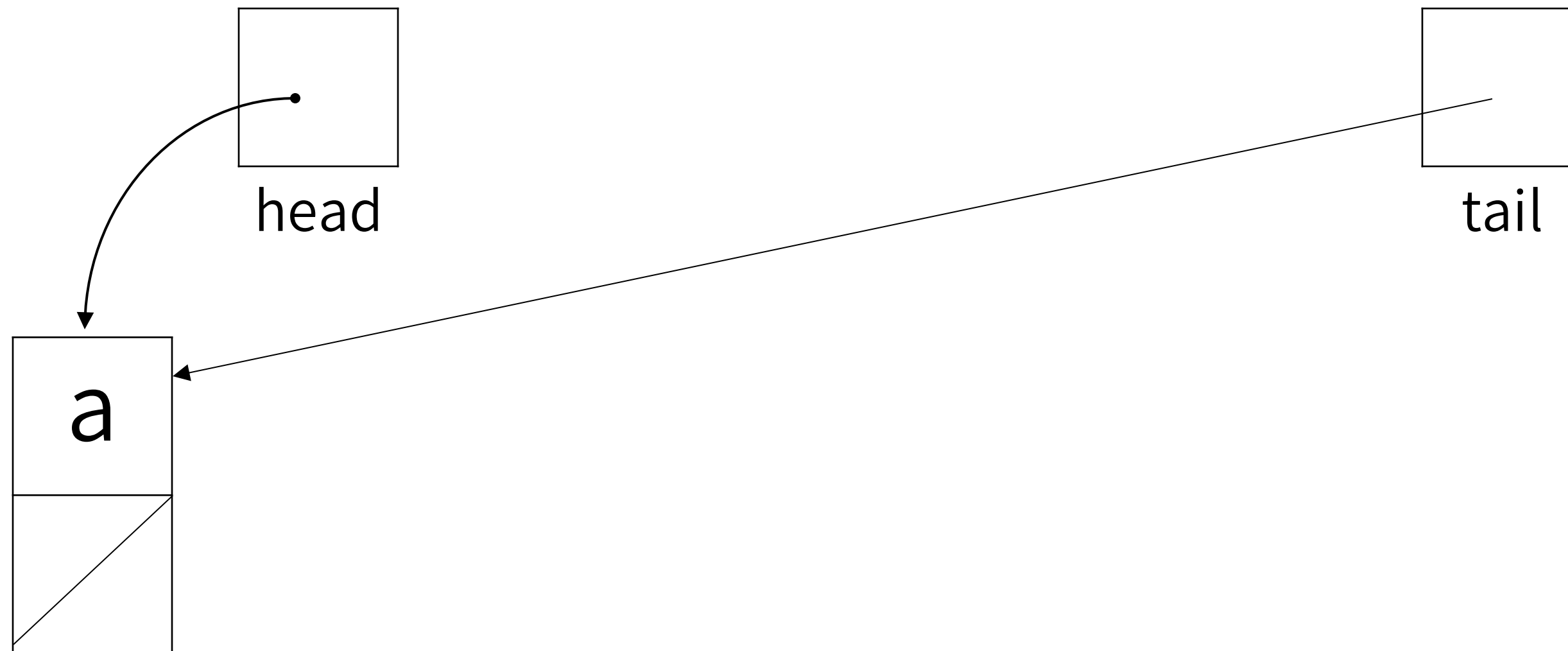


Enqueue (a)

Queue Implementation with Linked List

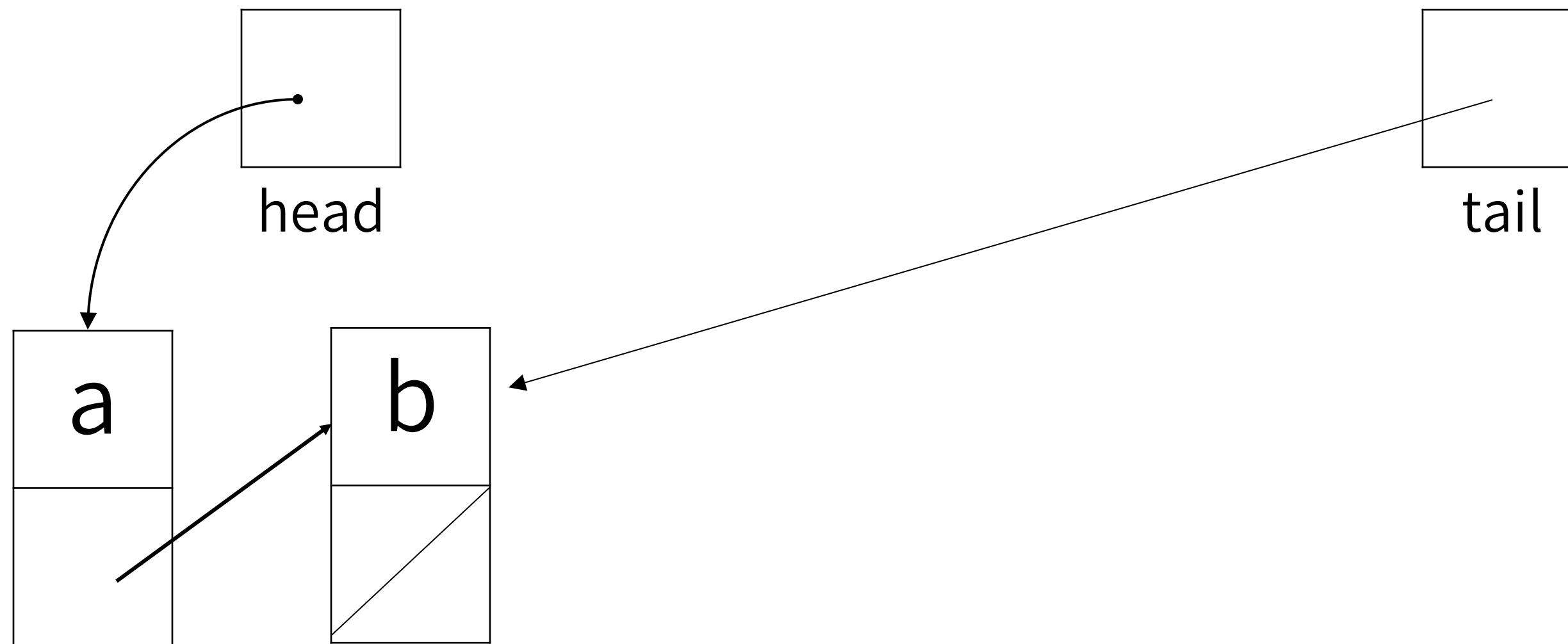


Queue Implementation with Linked List



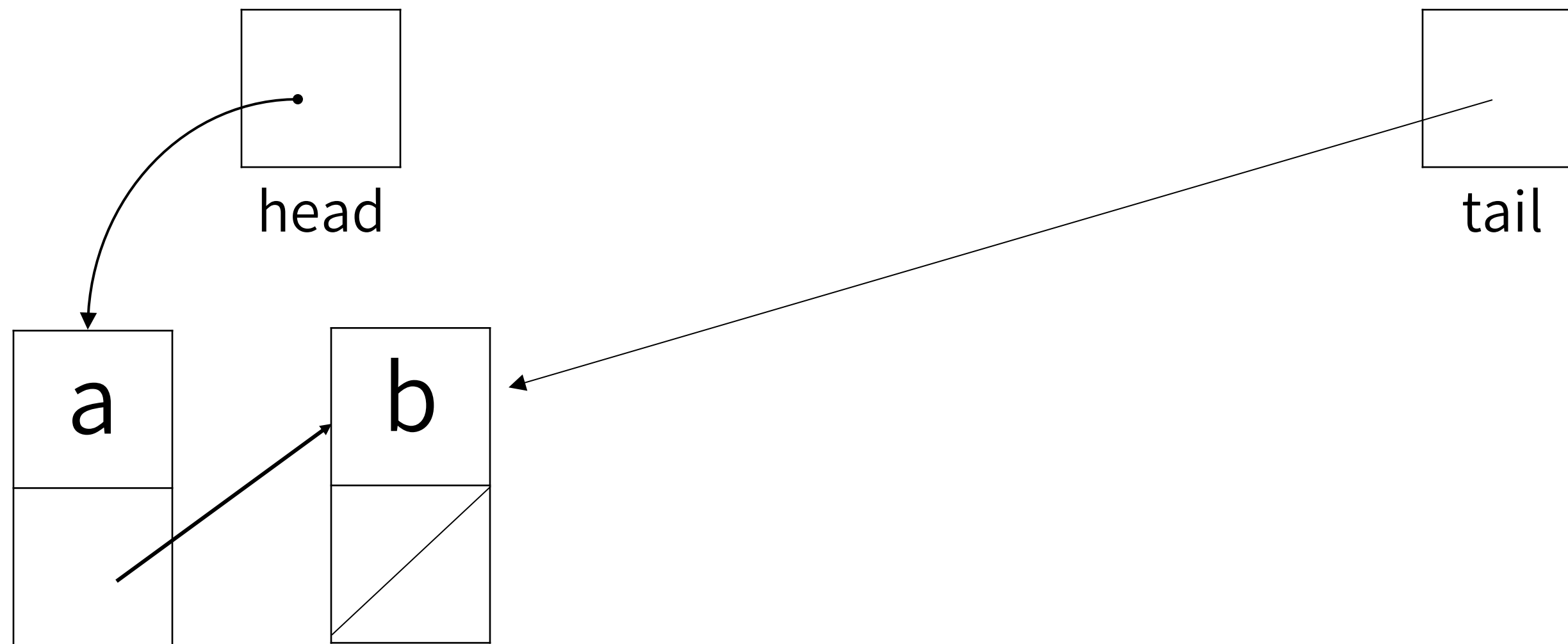
Enqueue (b)

Queue Implementation with Linked List

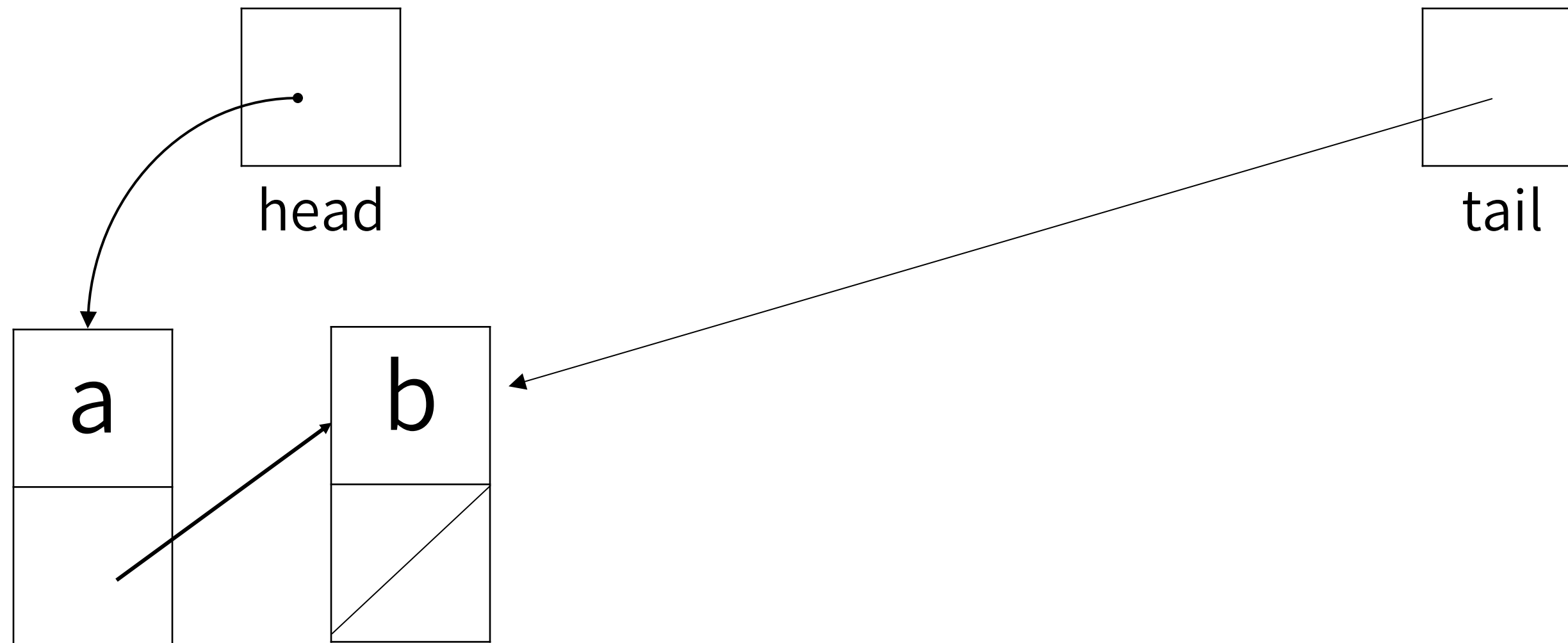


Enqueue (b)

Queue Implementation with Linked List

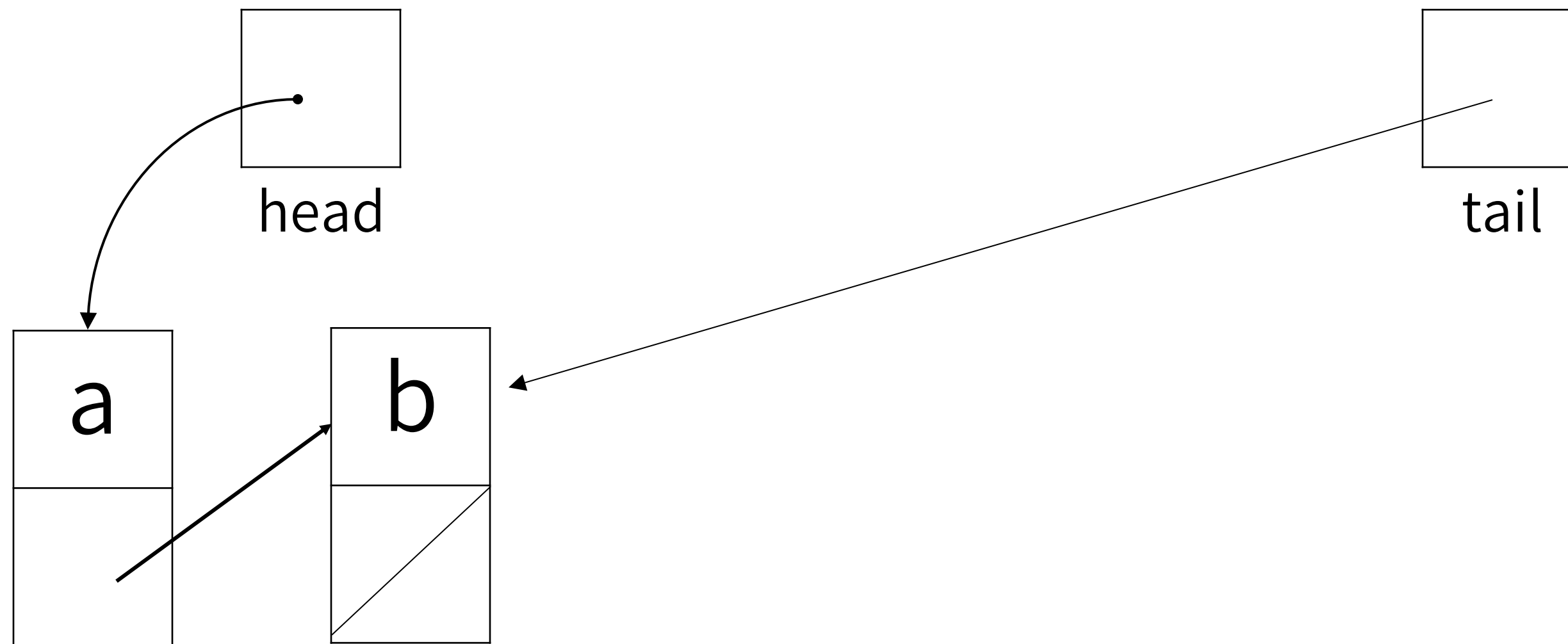


Queue Implementation with Linked List



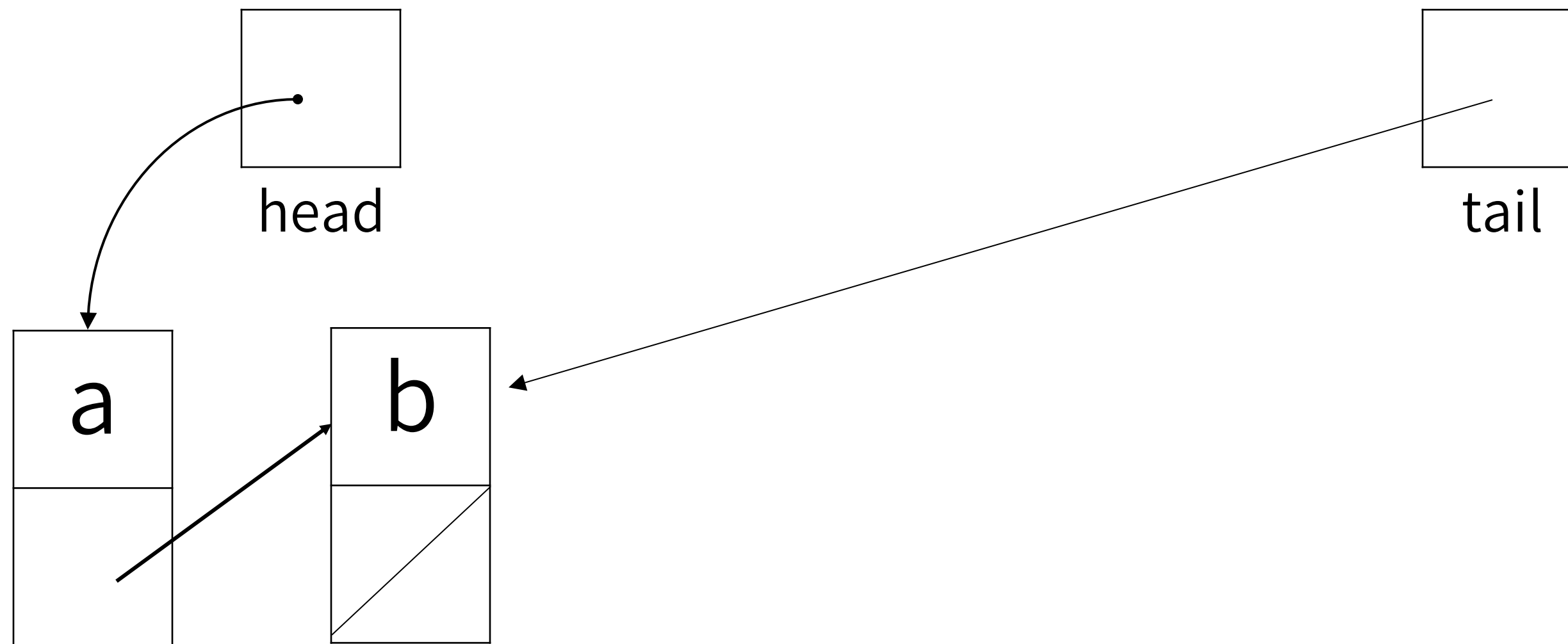
Empty ()

Queue Implementation with Linked List

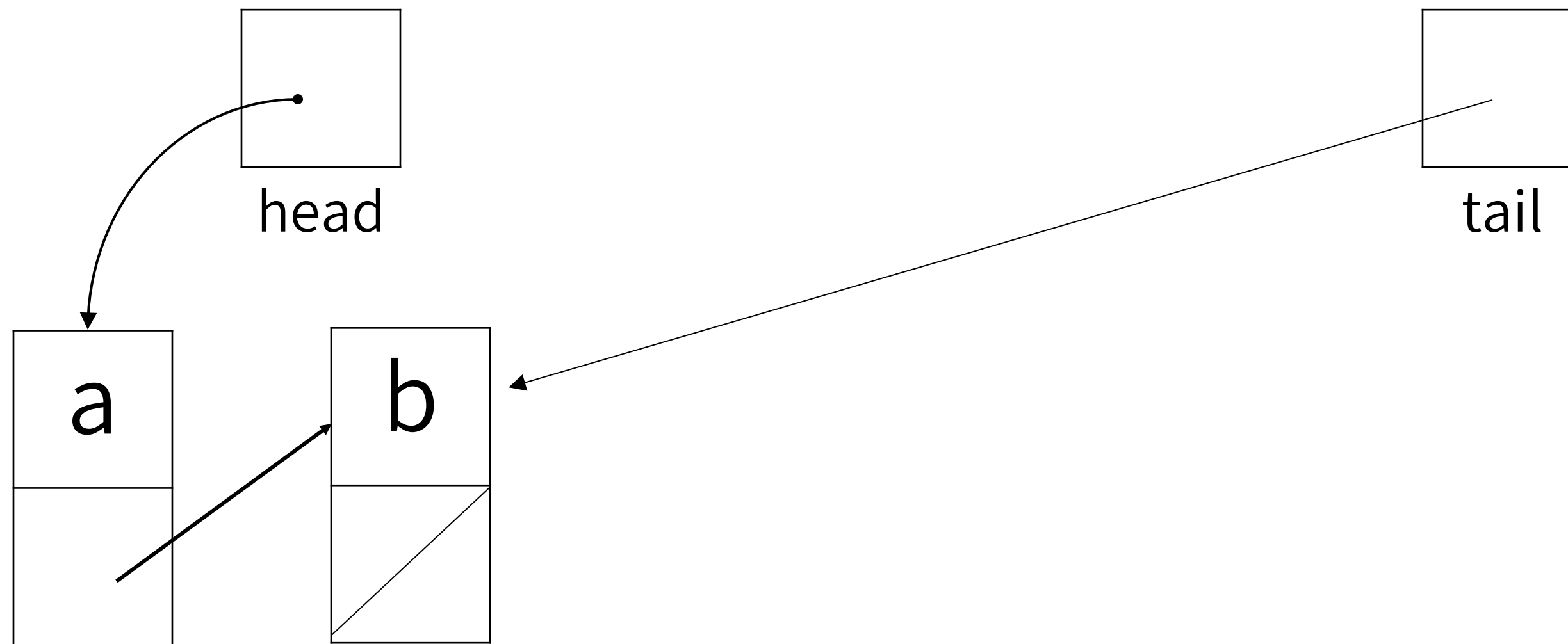


`Empty() → False`

Queue Implementation with Linked List

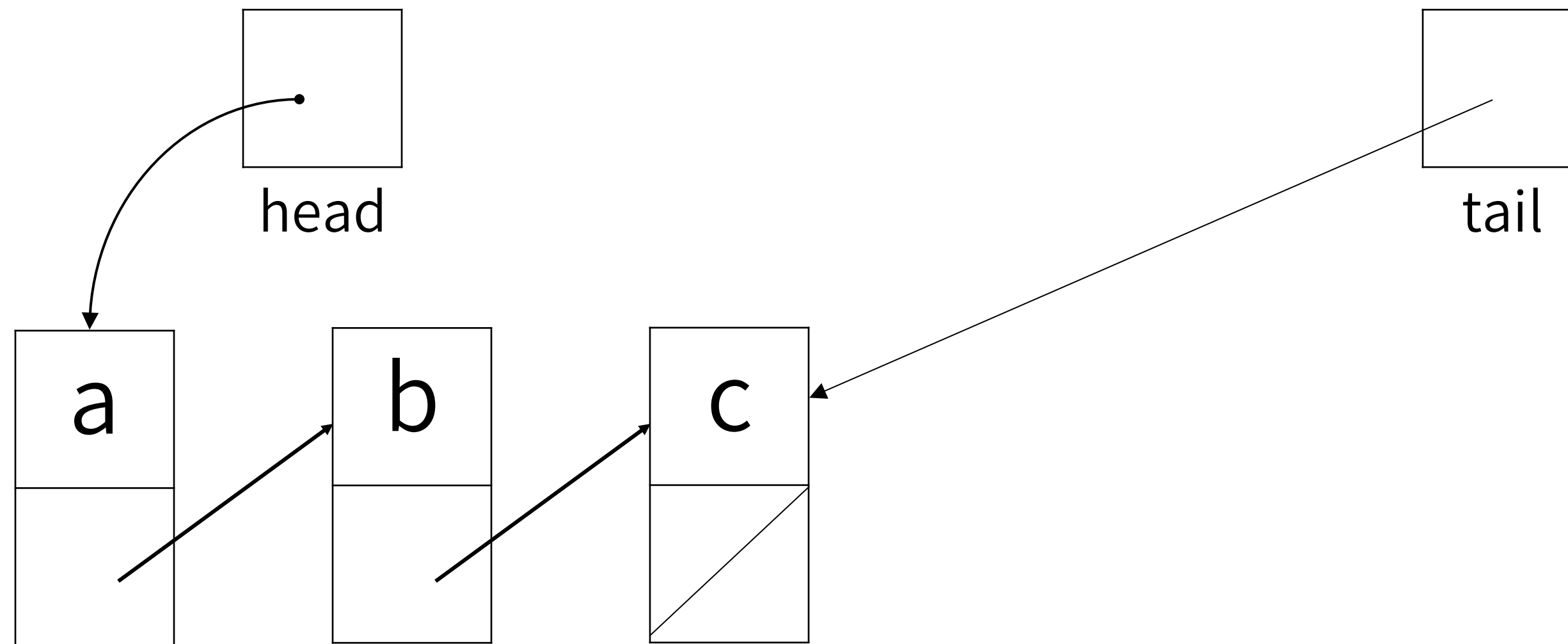


Queue Implementation with Linked List



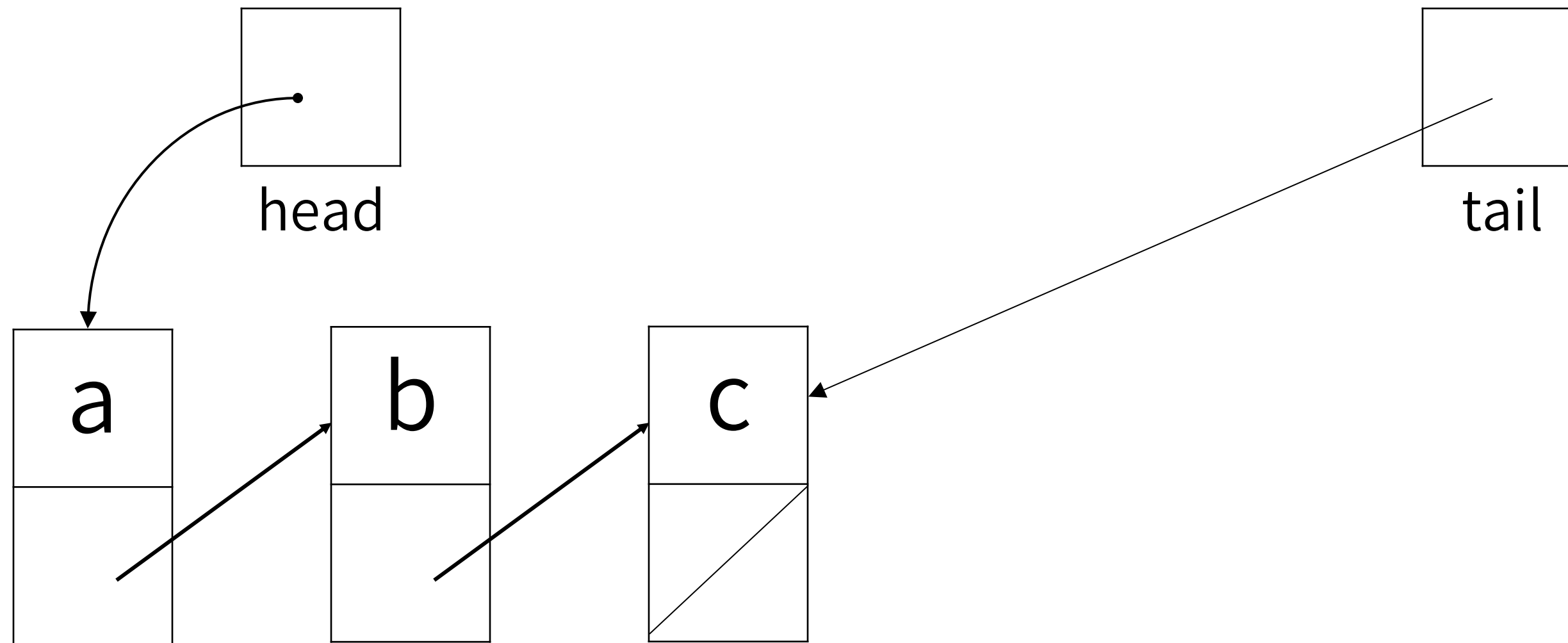
Enqueue (c)

Queue Implementation with Linked List

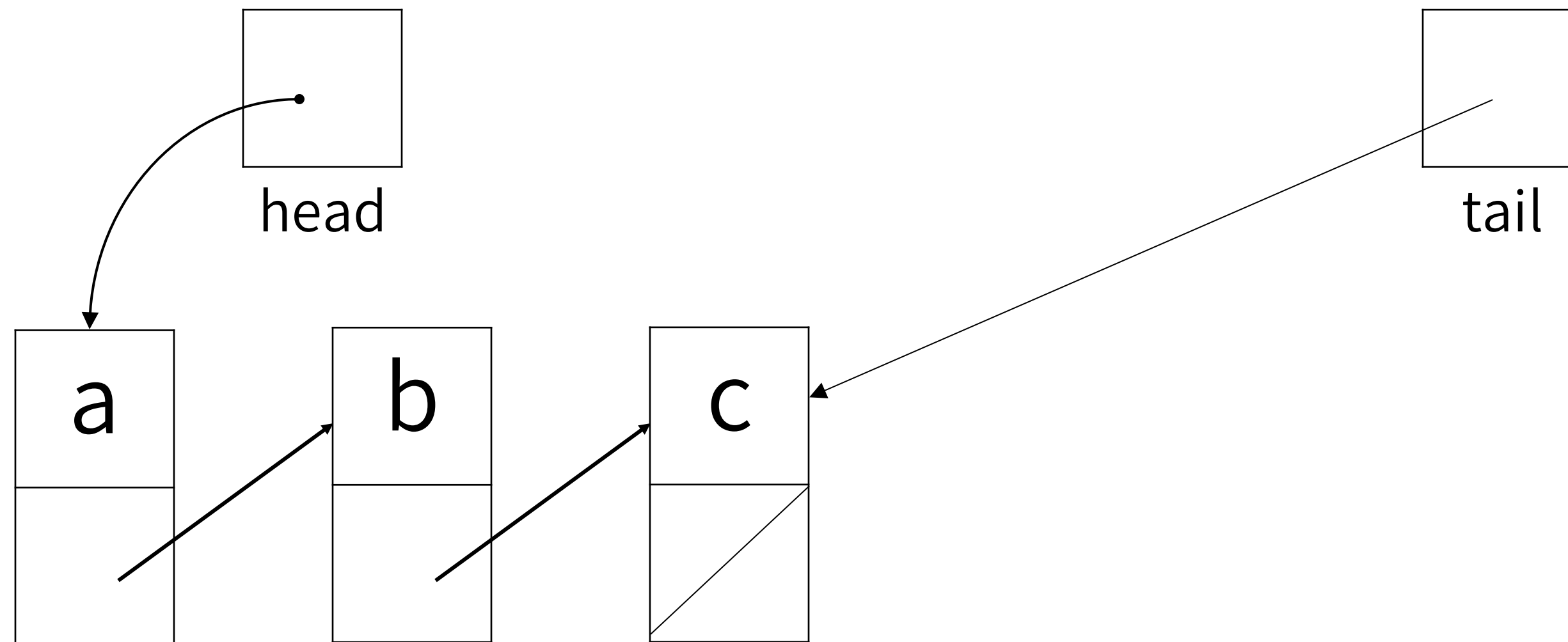


Enqueue (c)

Queue Implementation with Linked List

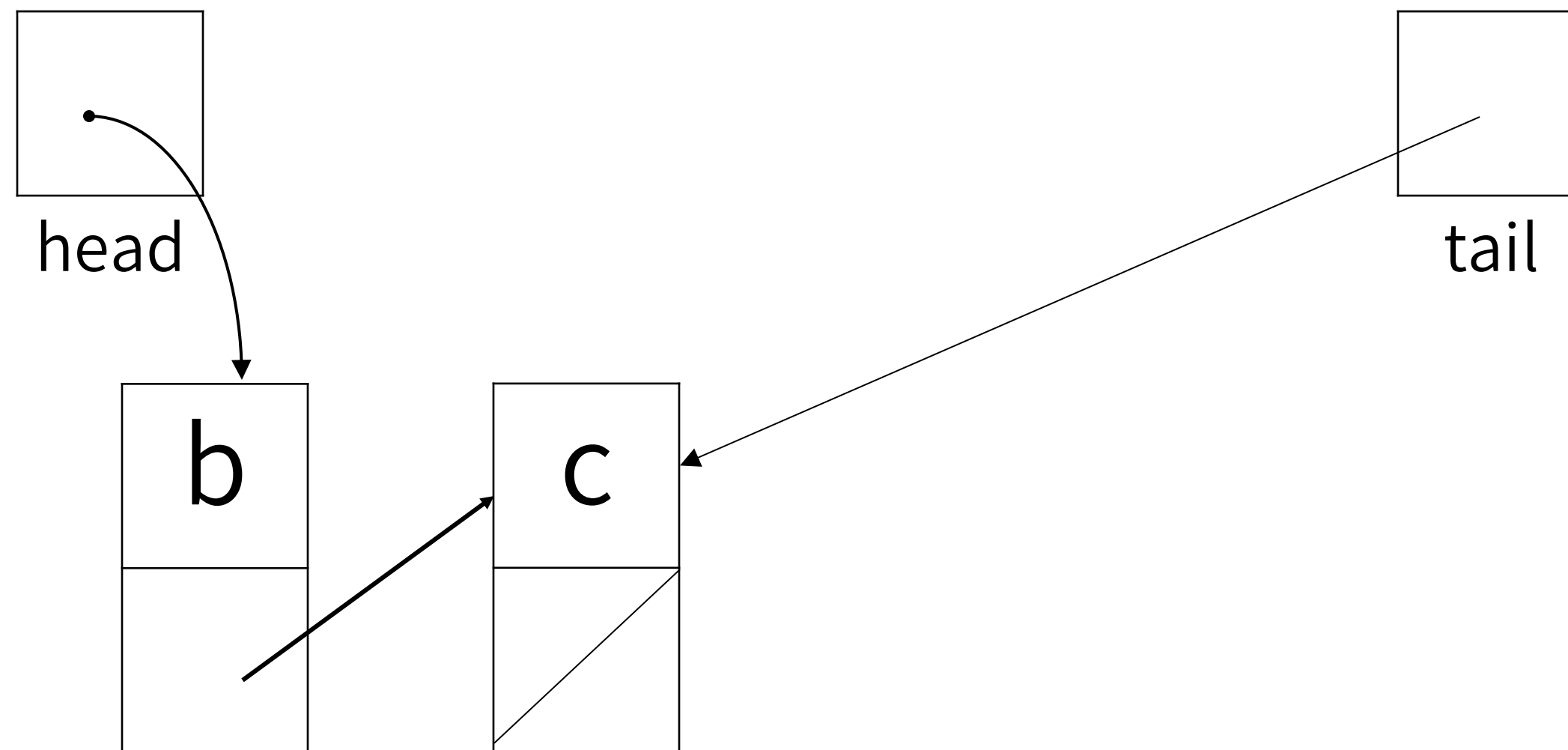


Queue Implementation with Linked List



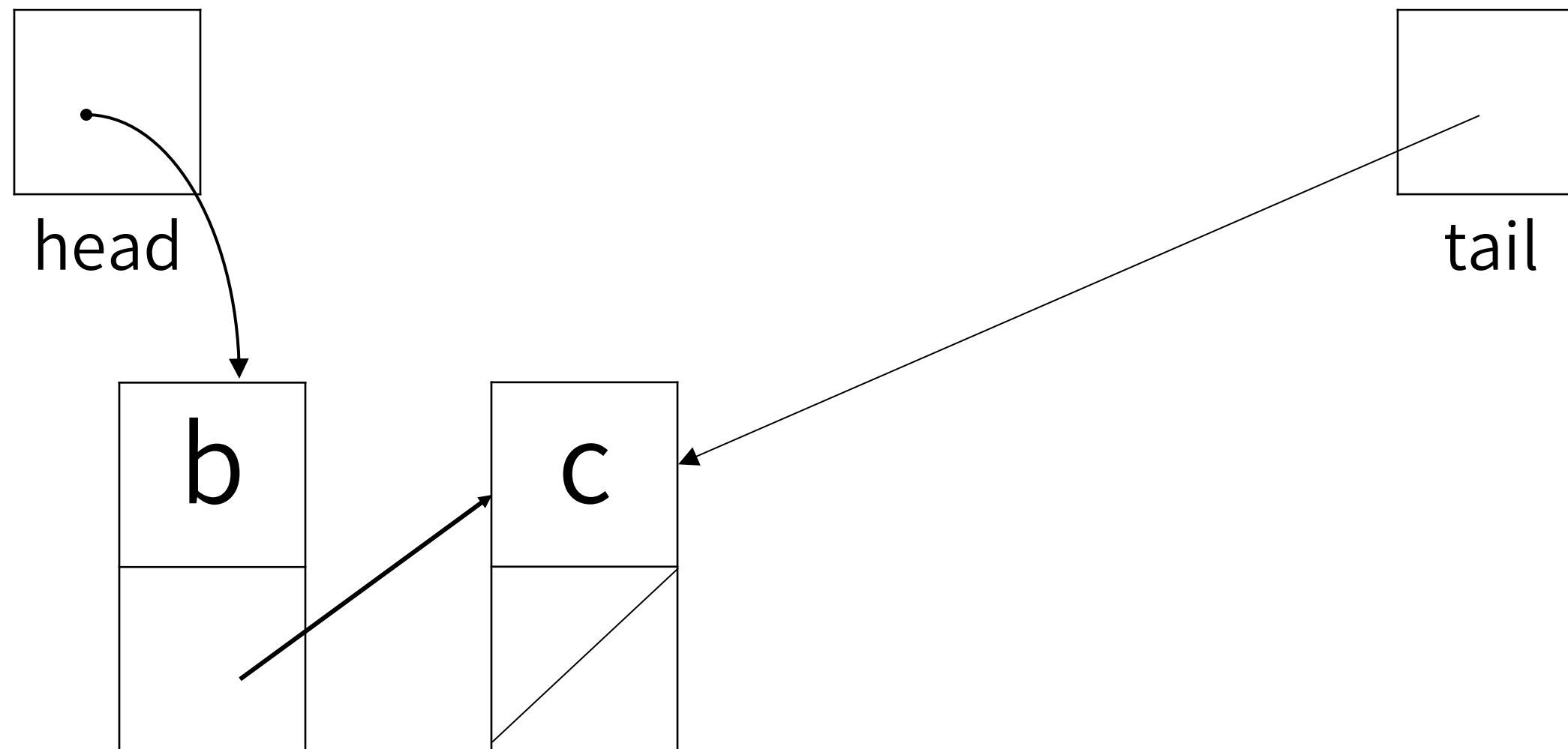
Dequeue ()

Queue Implementation with Linked List

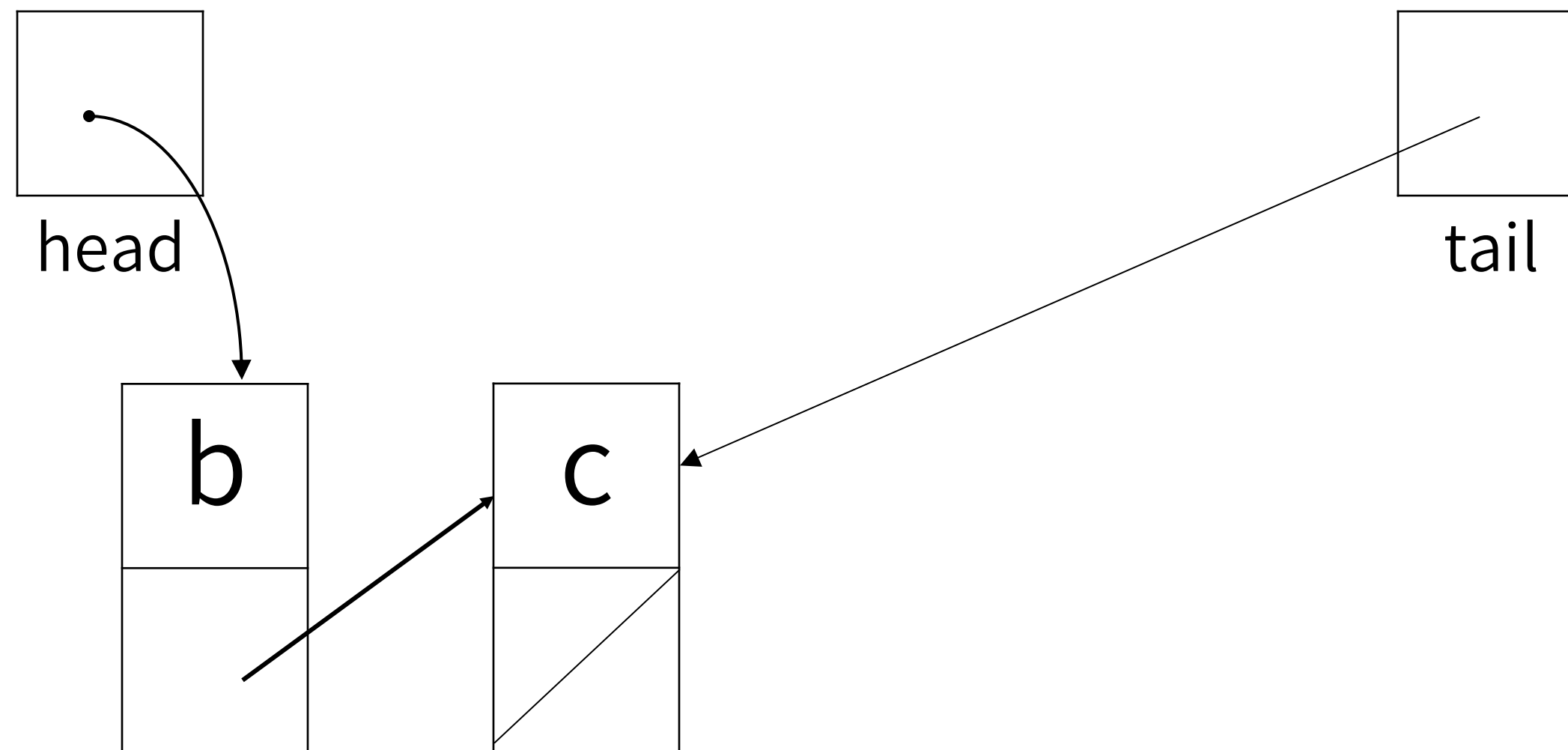


Dequeue () → a

Queue Implementation with Linked List

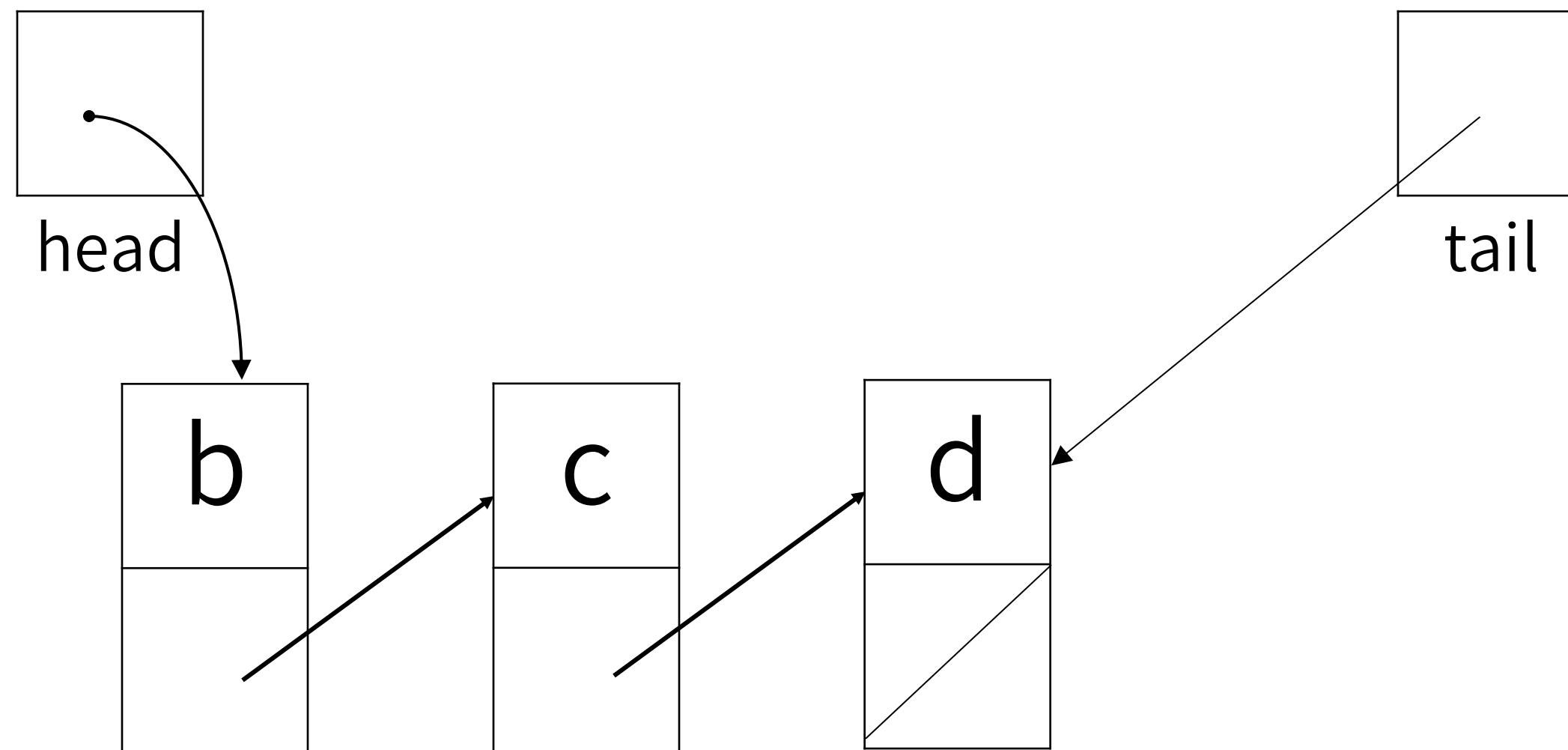


Queue Implementation with Linked List



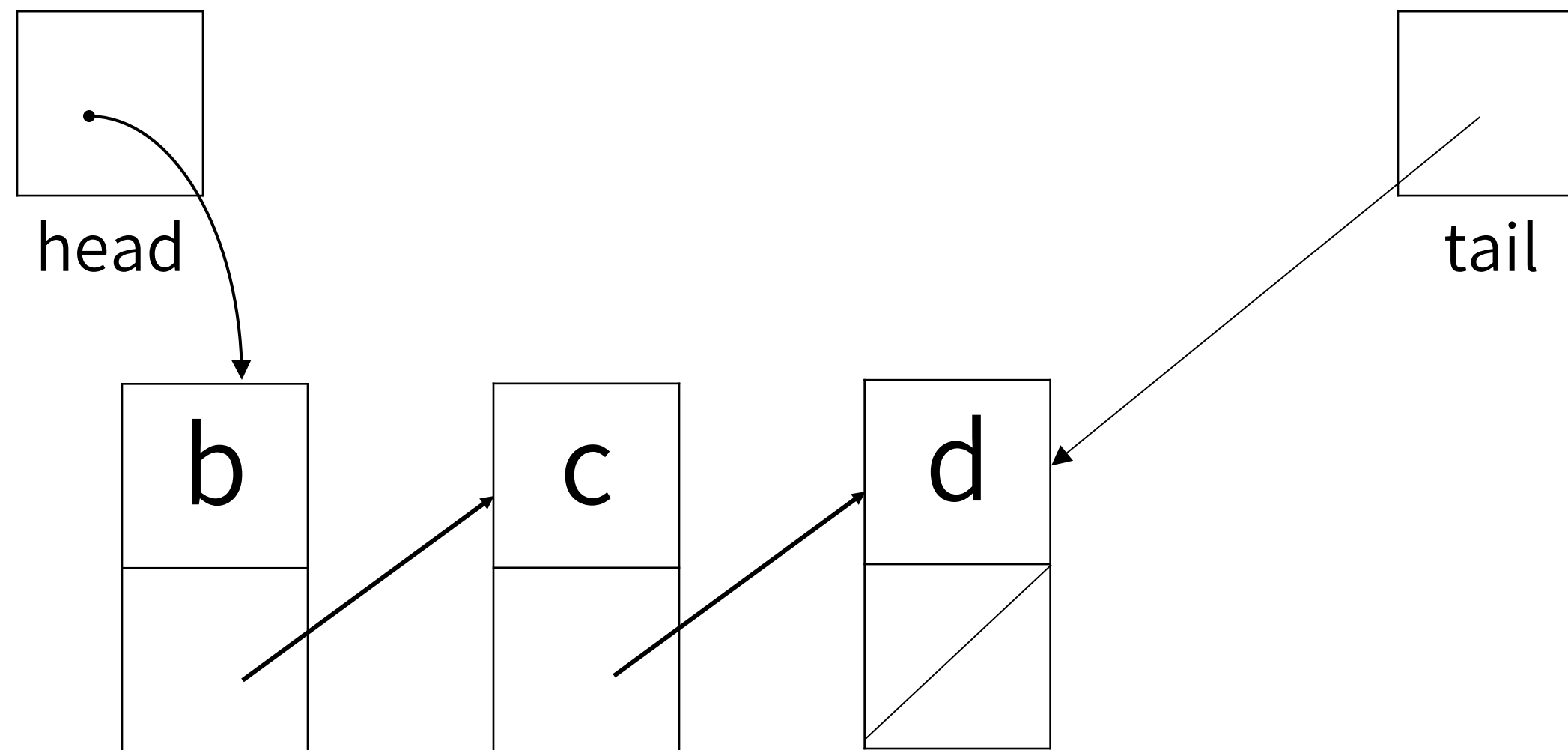
Enqueue (d)

Queue Implementation with Linked List

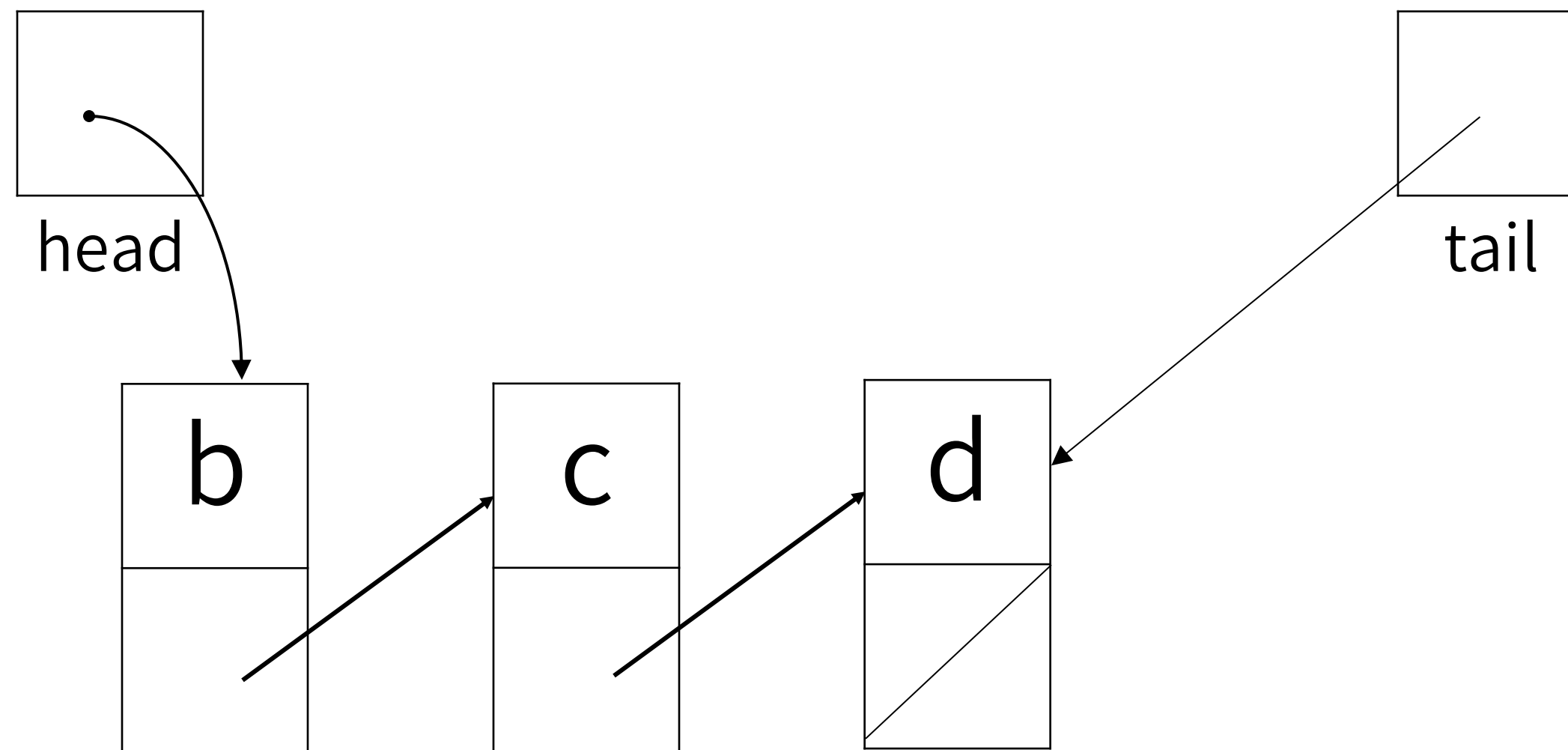


Enqueue (d)

Queue Implementation with Linked List

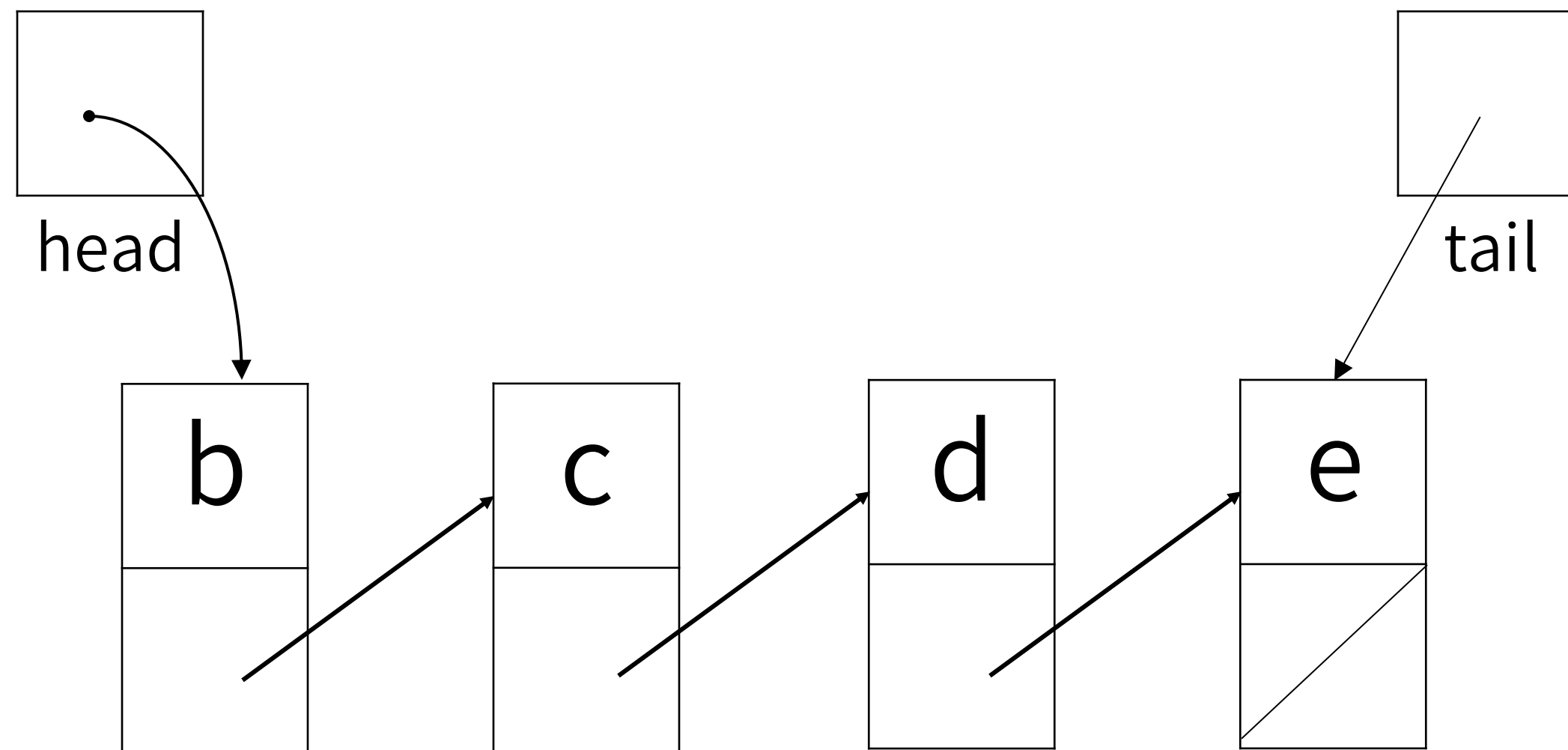


Queue Implementation with Linked List



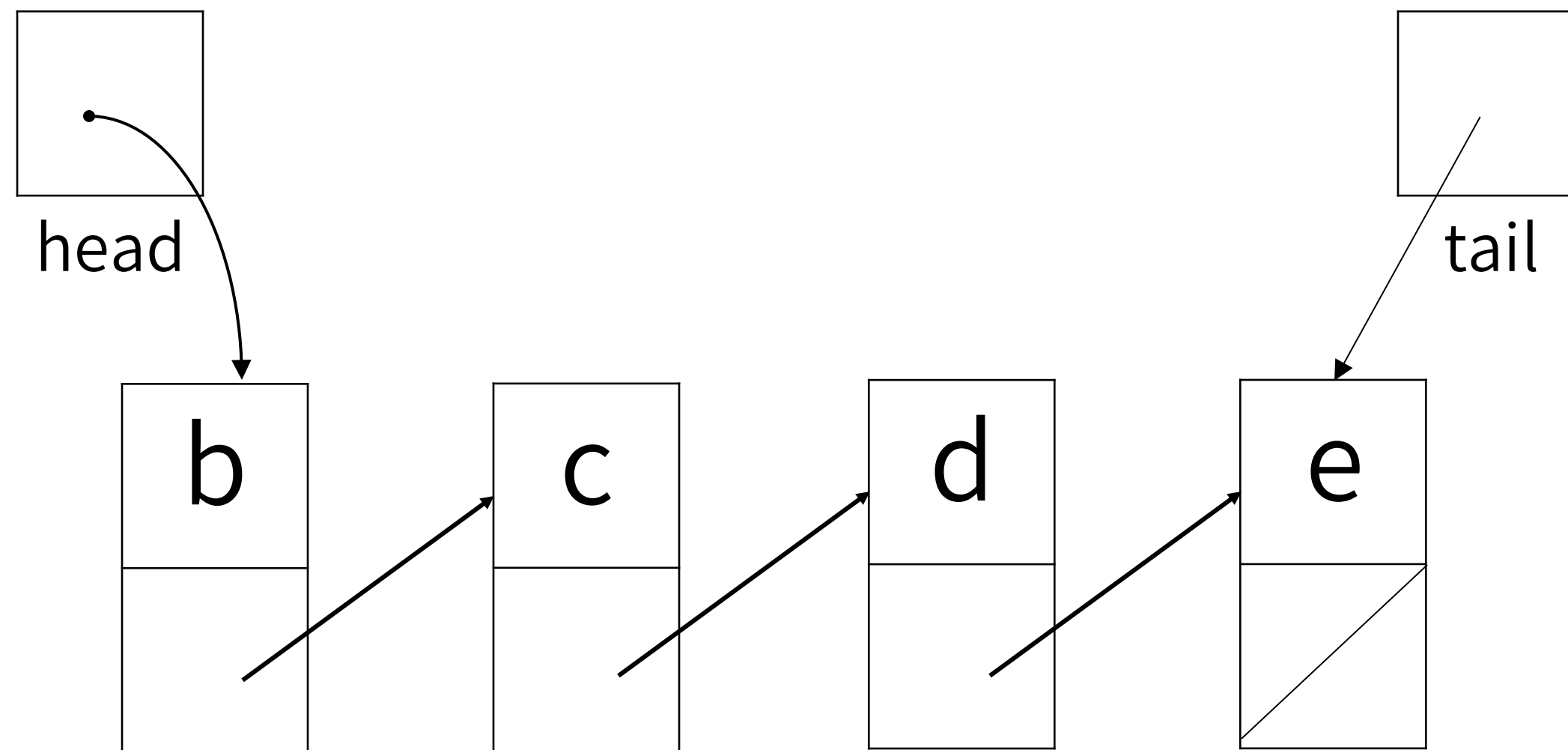
Enqueue (e)

Queue Implementation with Linked List

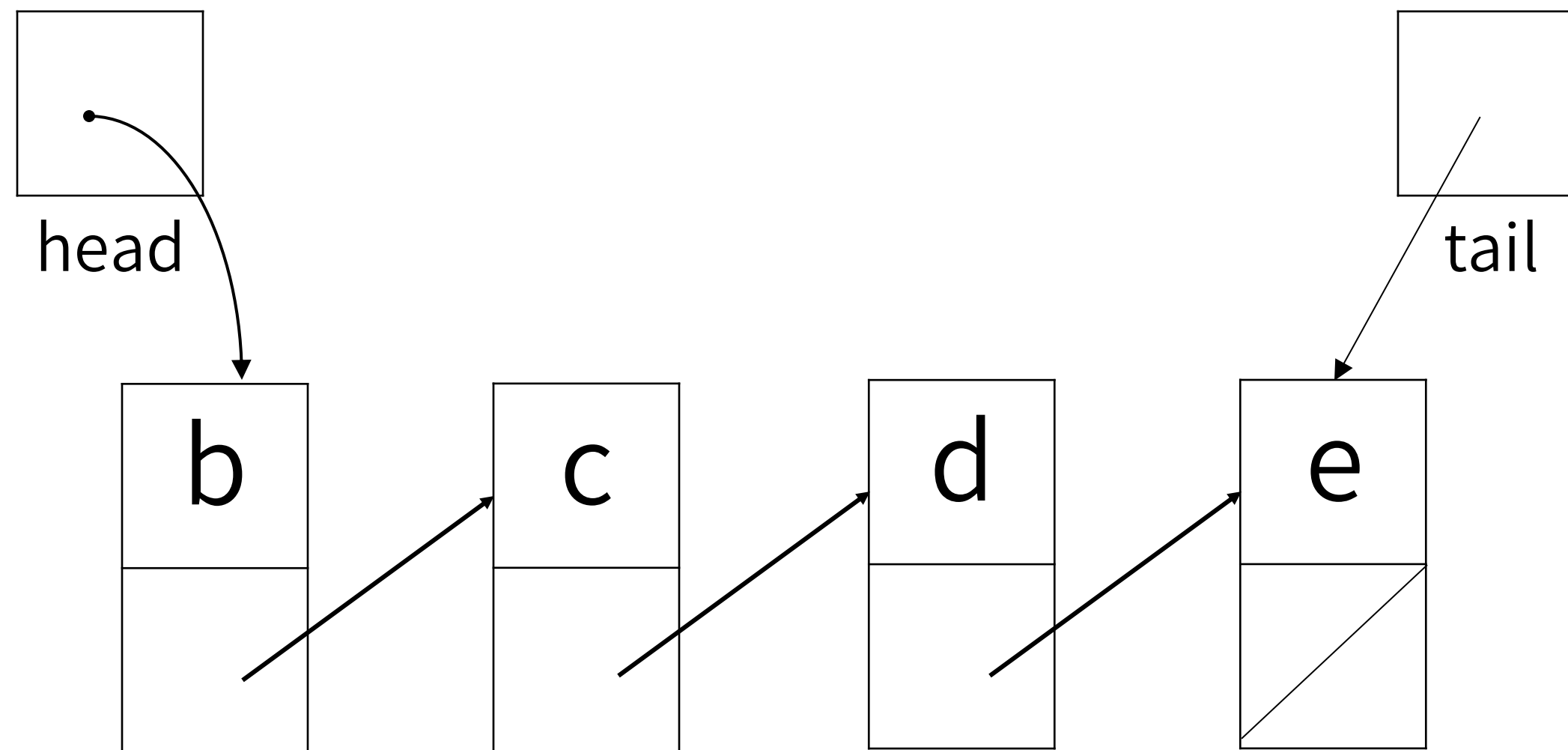


Enqueue (e)

Queue Implementation with Linked List

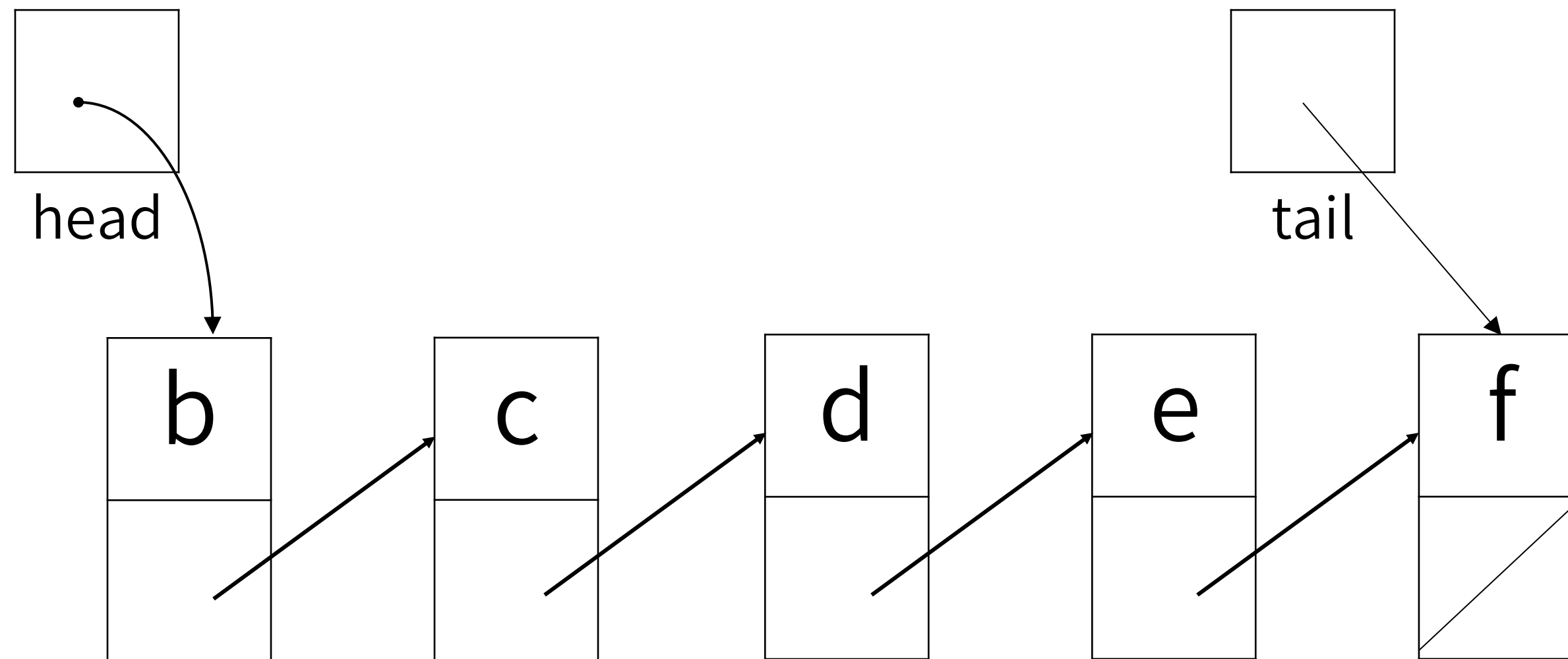


Queue Implementation with Linked List



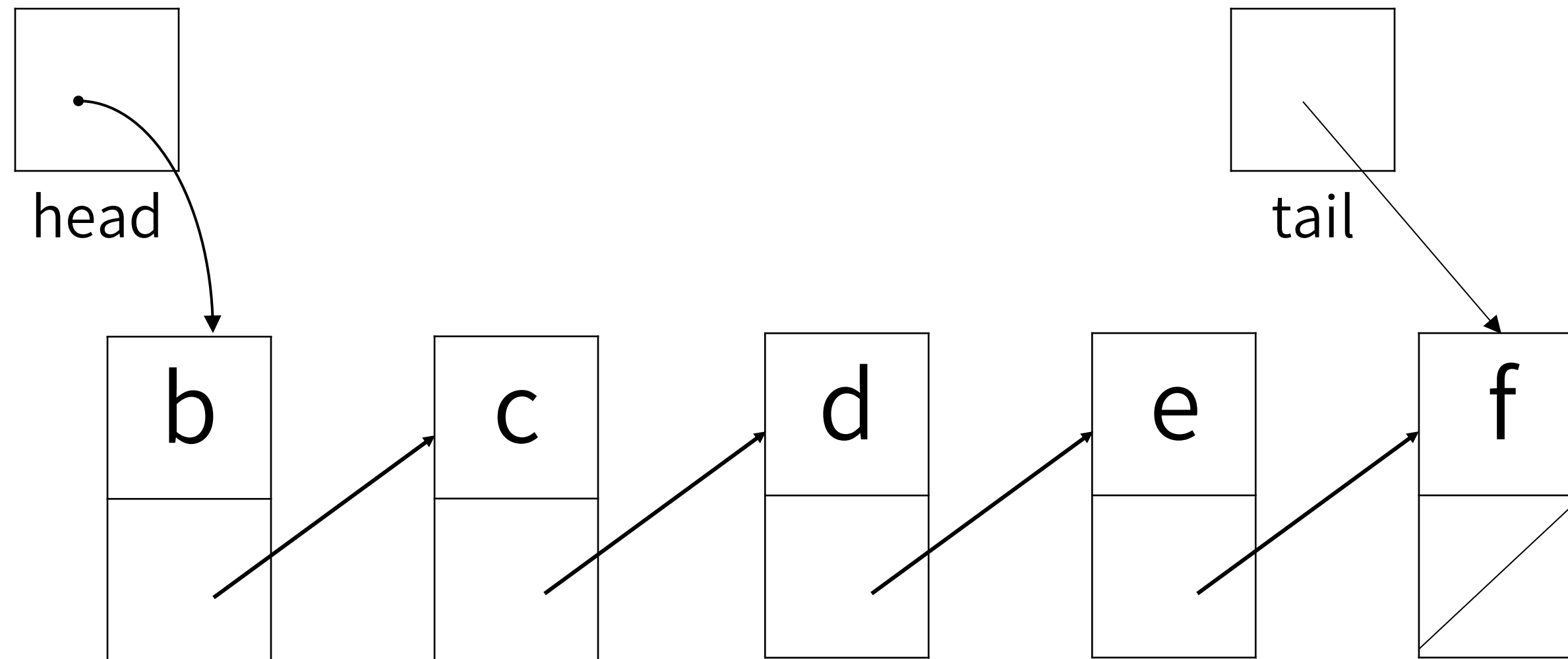
Enqueue (f)

Queue Implementation with Linked List

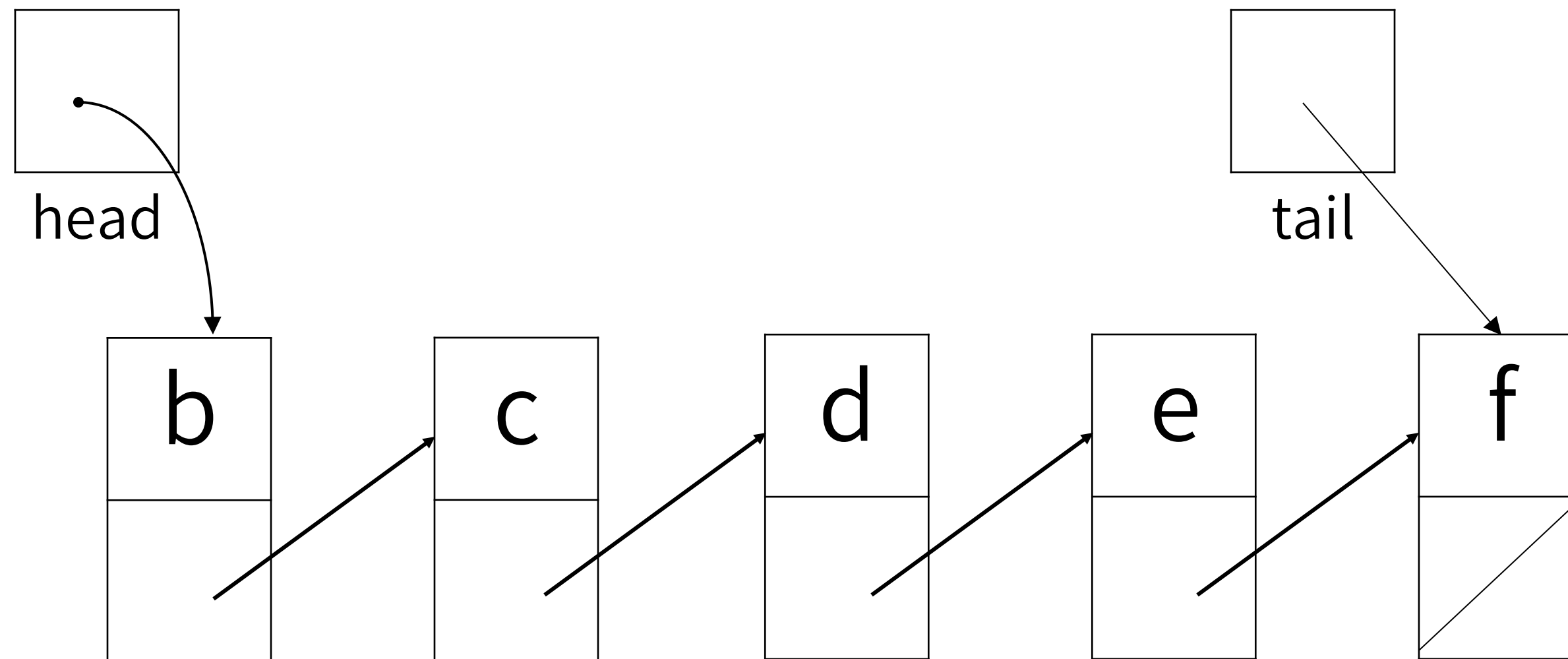


Enqueue (f)

Queue Implementation with Linked List

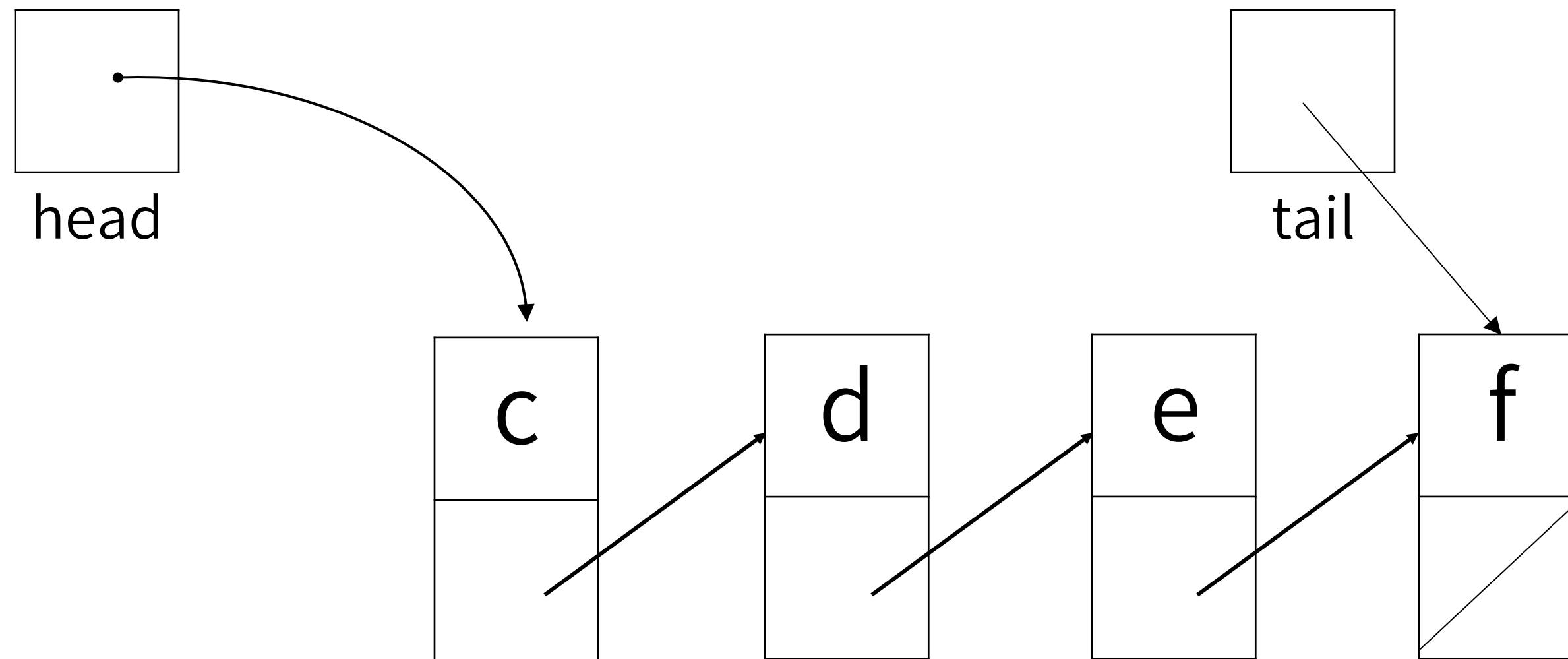


Queue Implementation with Linked List



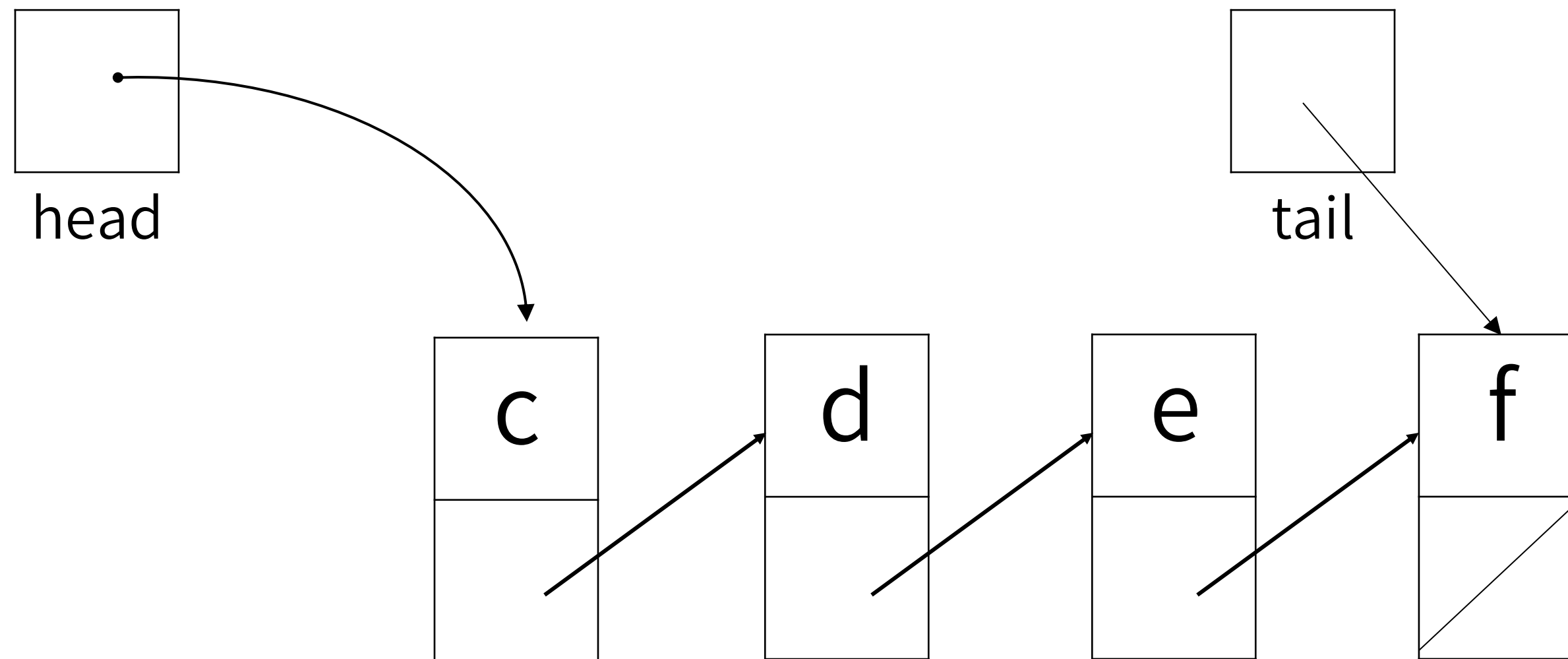
Dequeue ()

Queue Implementation with Linked List



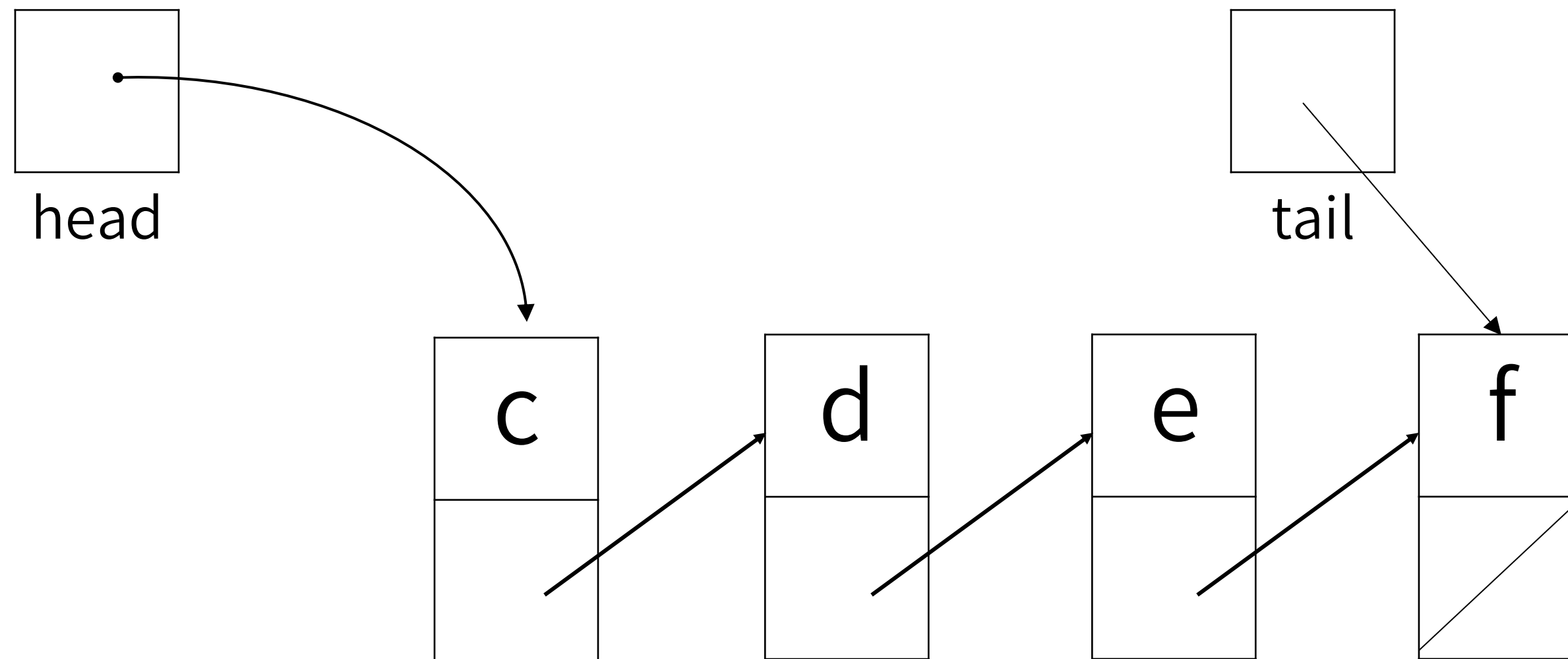
Dequeue () → b

Queue Implementation with Linked List



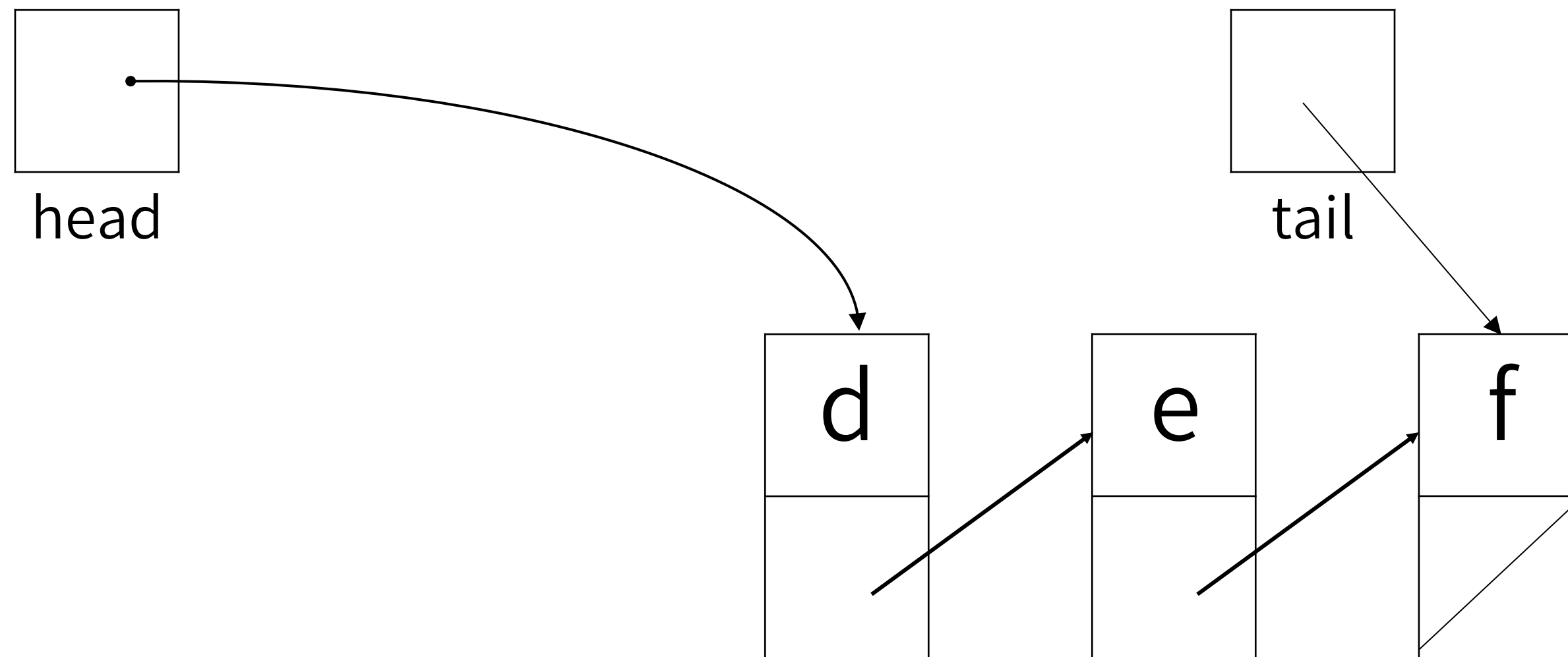
Dequeue () → b

Queue Implementation with Linked List



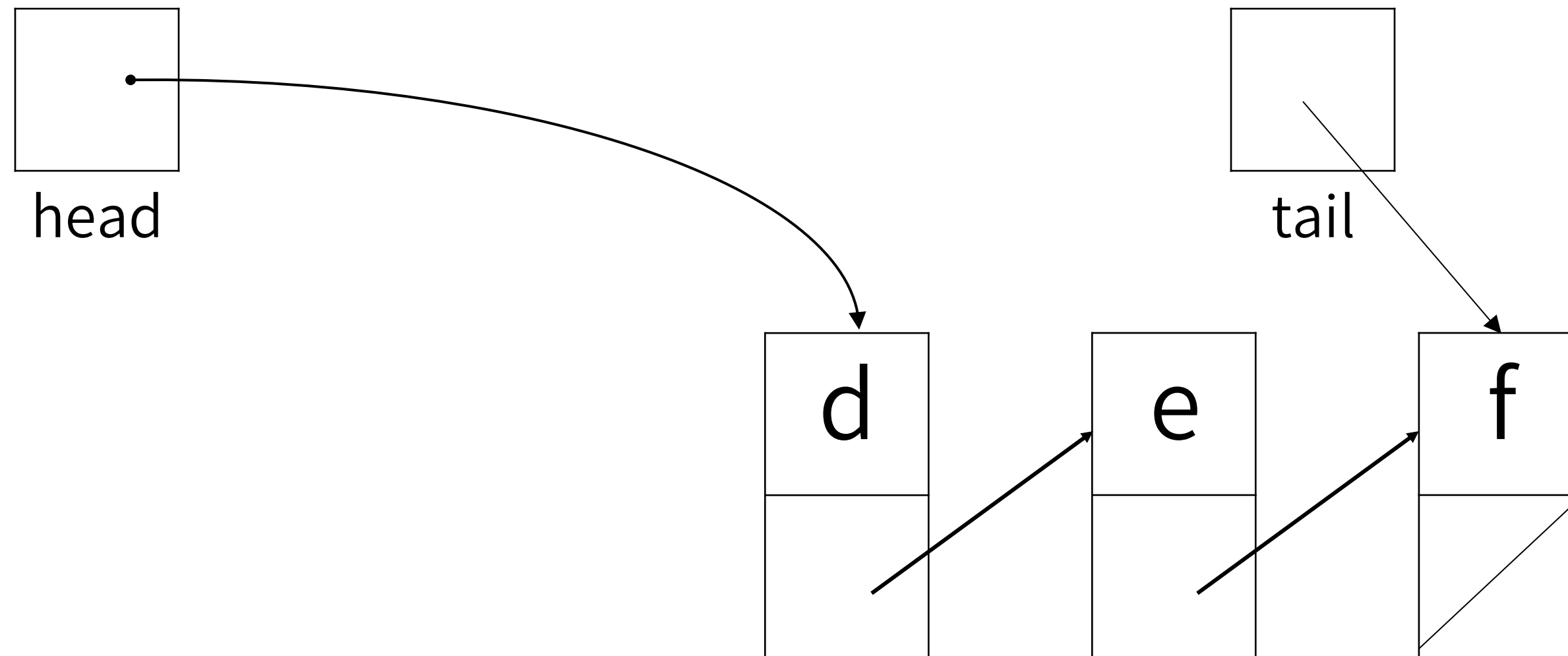
Dequeue ()

Queue Implementation with Linked List

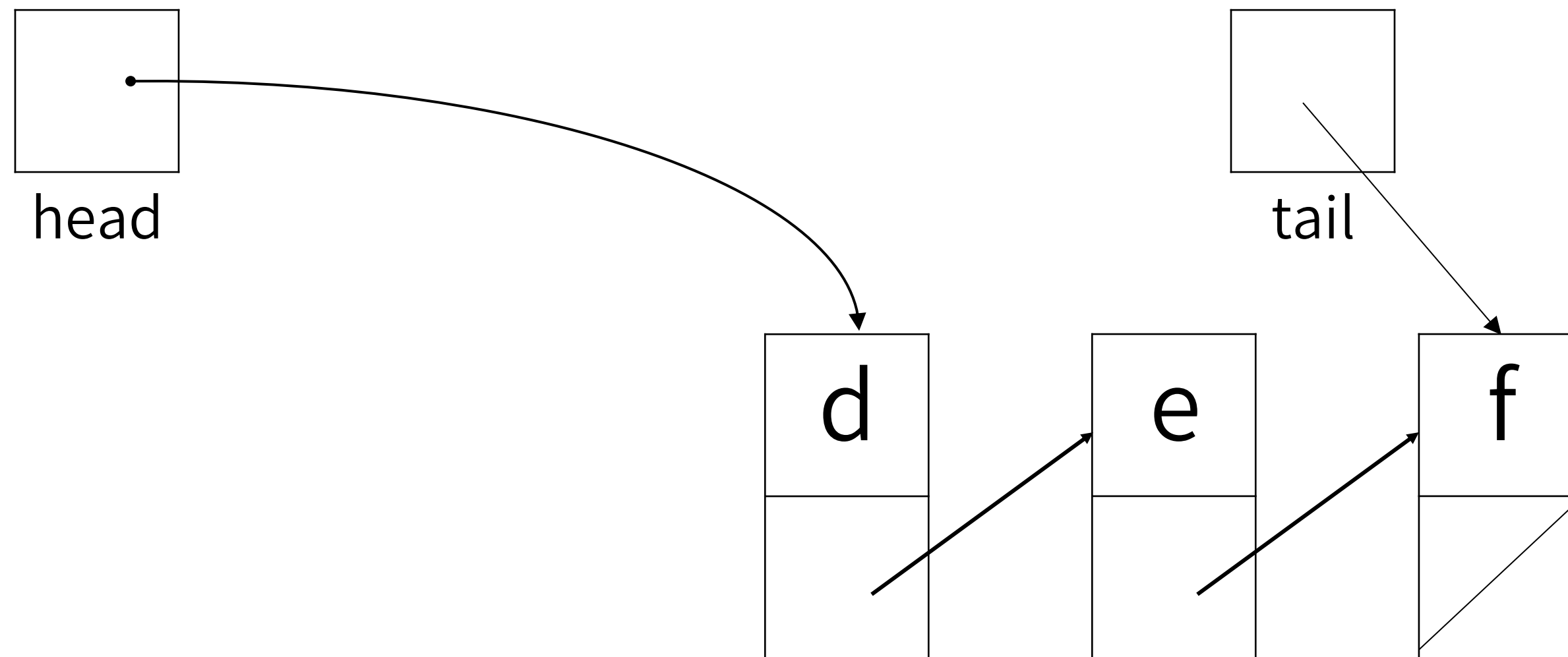


Dequeue () → c

Queue Implementation with Linked List

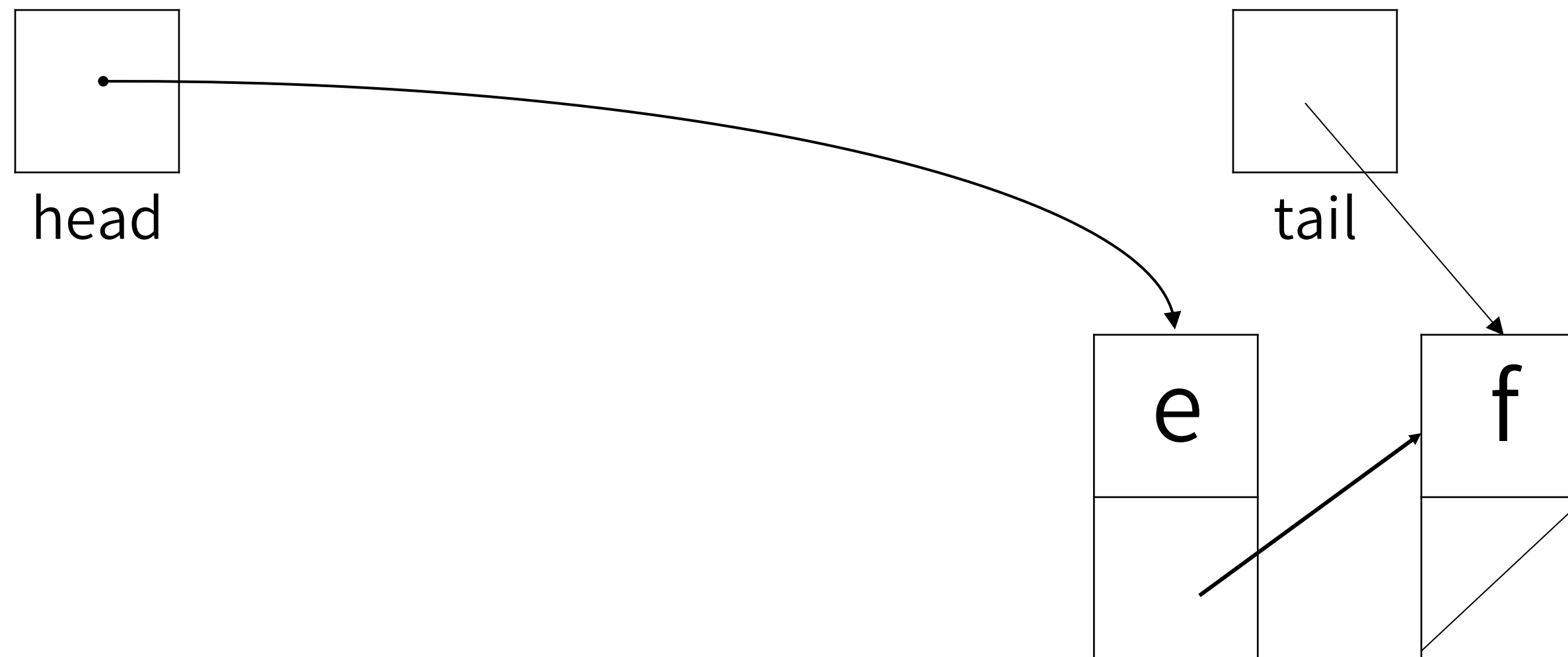


Queue Implementation with Linked List



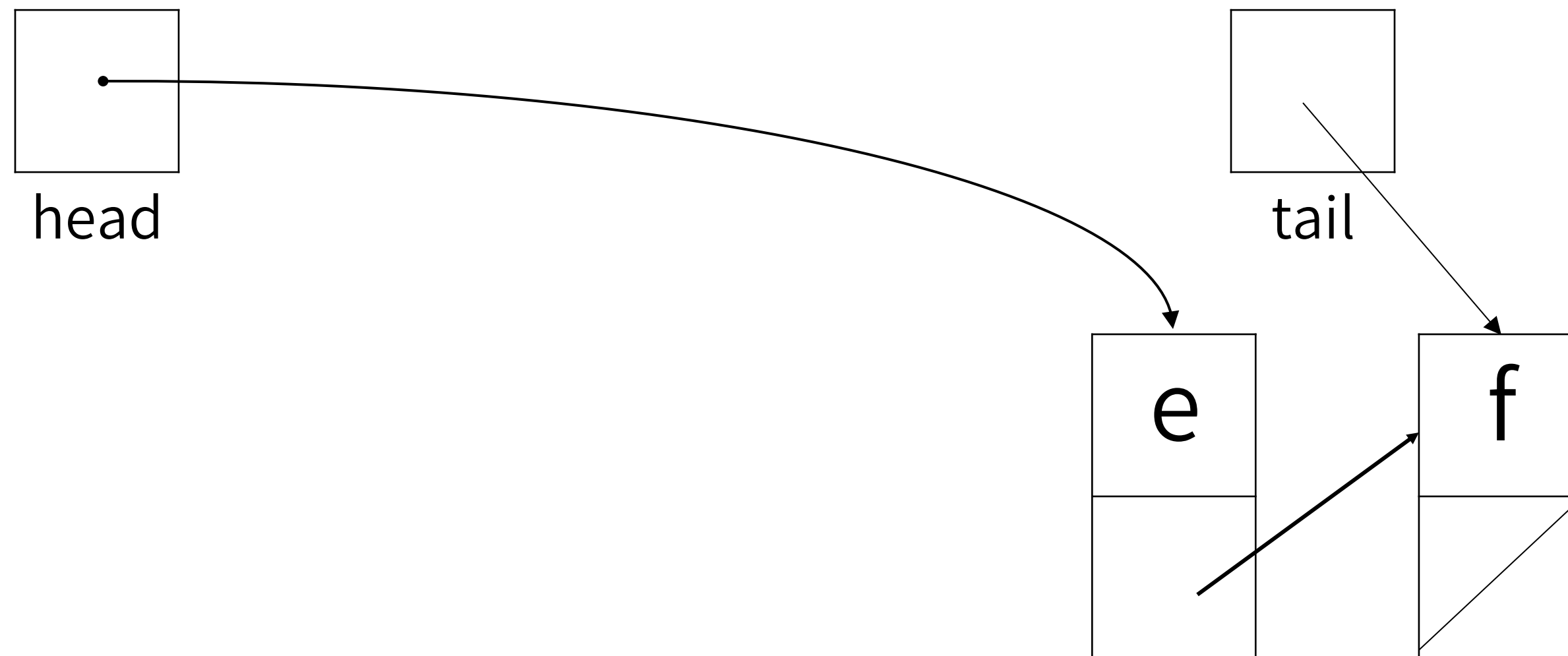
Dequeue ()

Queue Implementation with Linked List

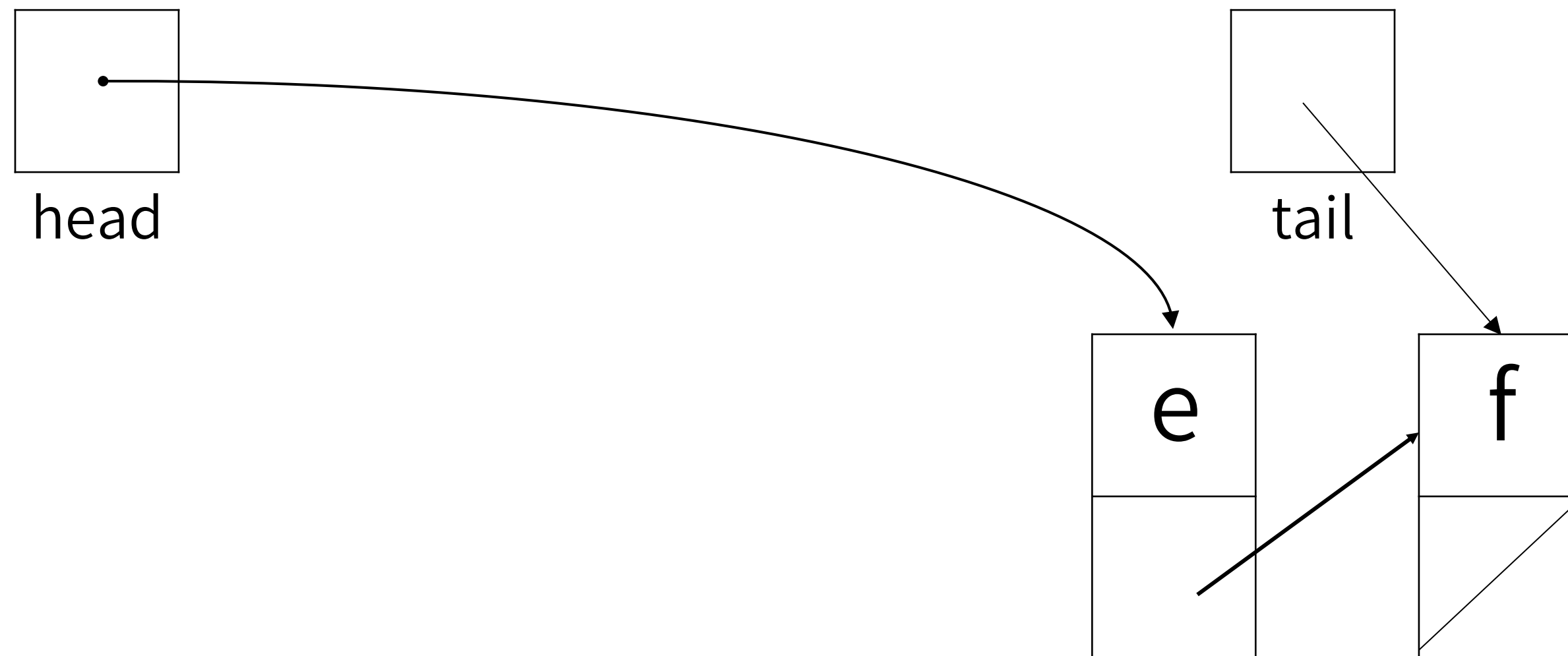


Dequeue () → d

Queue Implementation with Linked List

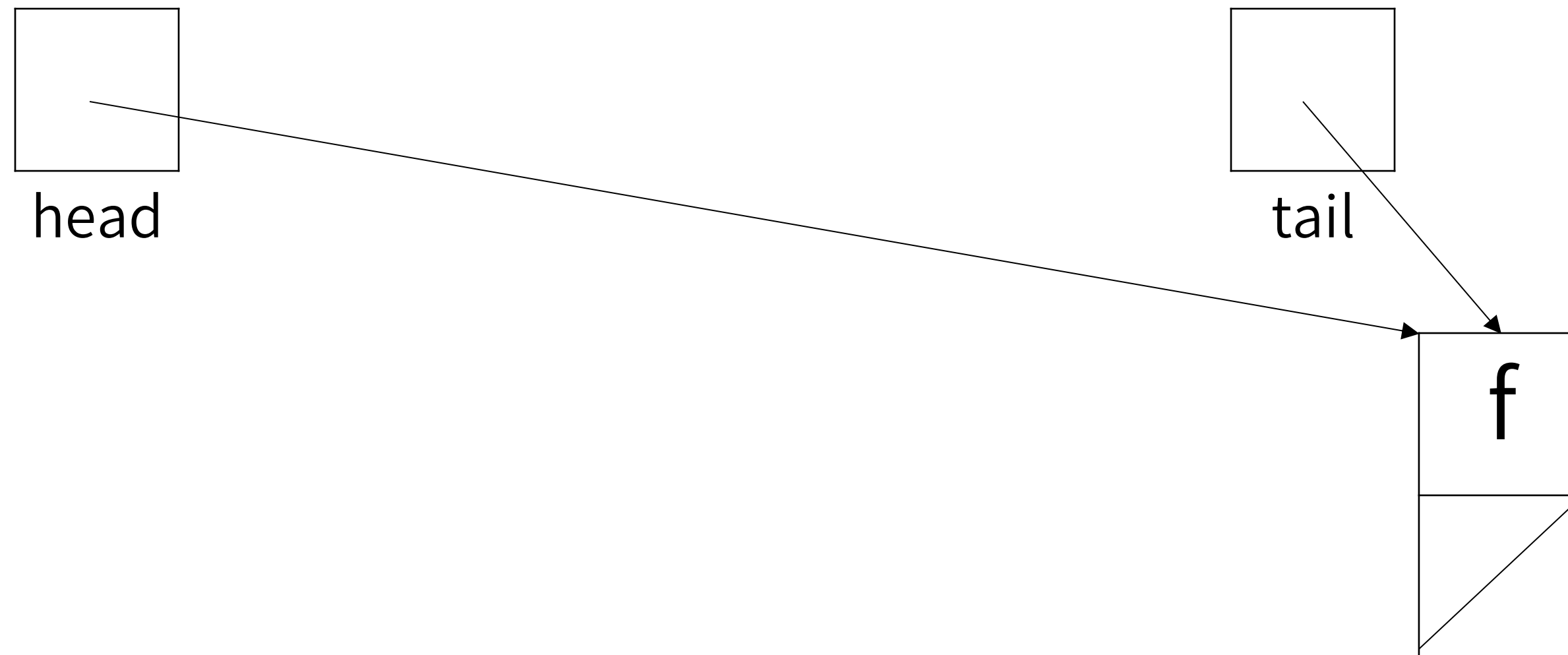


Queue Implementation with Linked List



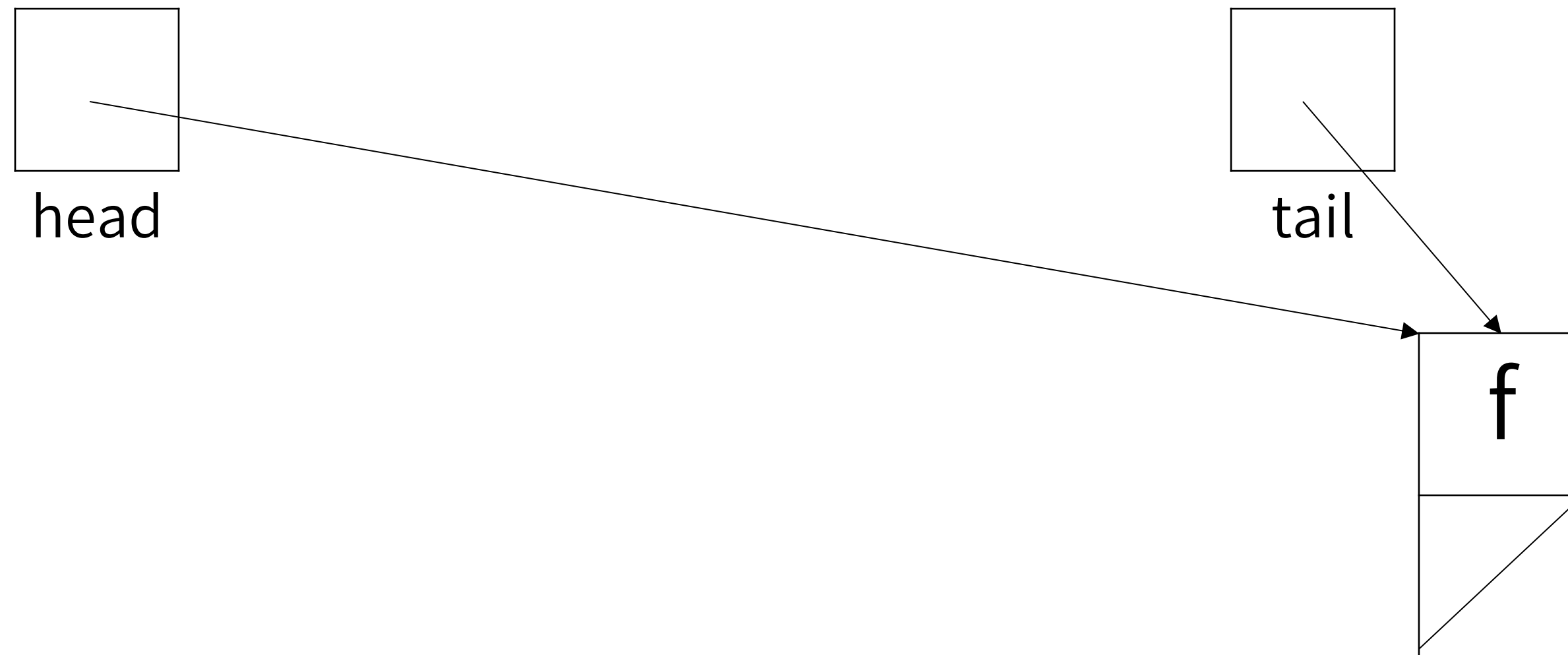
Dequeue ()

Queue Implementation with Linked List

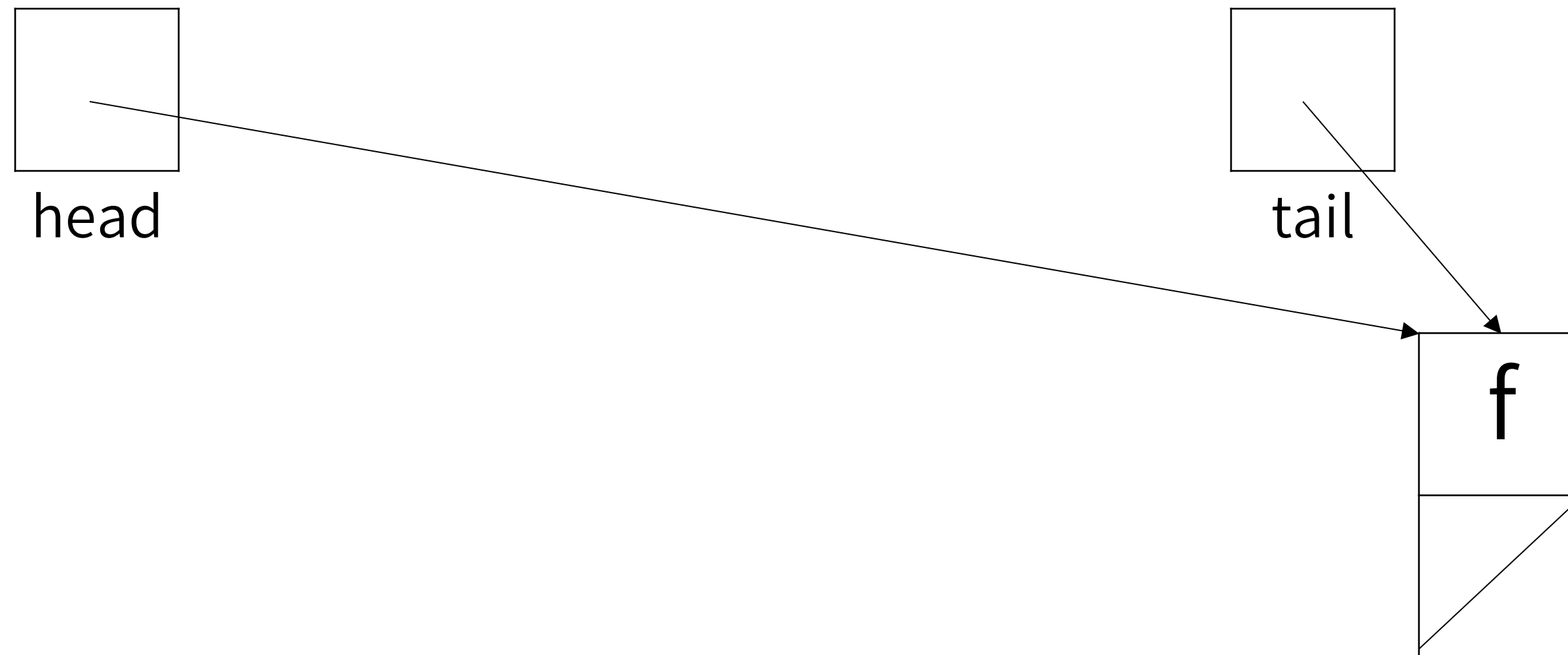


Dequeue () → e

Queue Implementation with Linked List

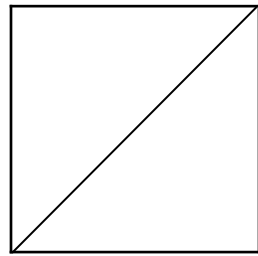


Queue Implementation with Linked List

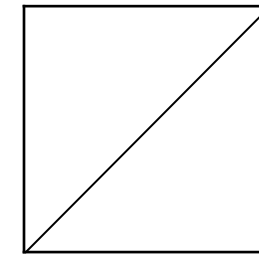


Dequeue ()

Queue Implementation with Linked List



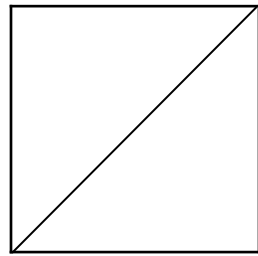
head



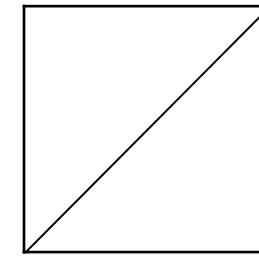
tail

Dequeue () \rightarrow f

Queue Implementation with Linked List



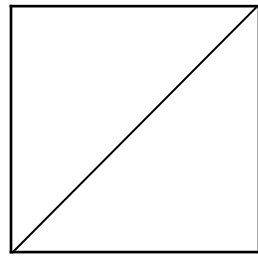
head



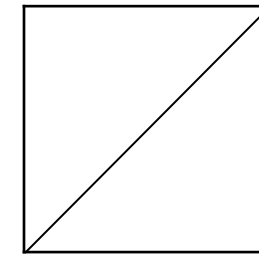
tail

Empty ()

Queue Implementation with Linked List



head



tail

`Empty() → True`

Summary

- Queues can be implemented with either an array or a linked list (with tail pointer).
- Each stack operation is $O(1)$: Enqueue, dequeue, empty.
- Implementation with linked list:
 - Enqueue : `PushBack()`
 - Dequeue : `TopFront()` + `PopFront()`
- Stacks are occasionally known as FIFO queues.