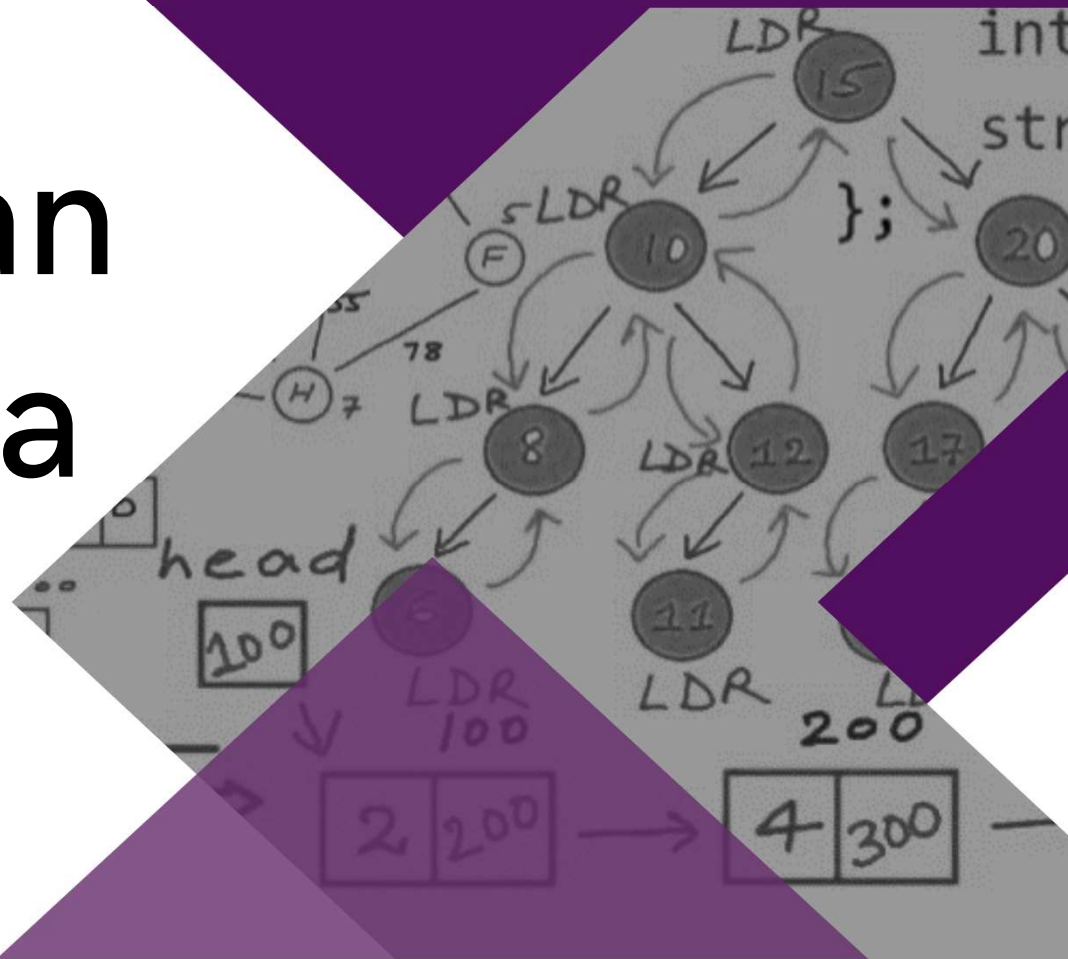


# Algoritma dan Struktur Data



# Pekan 11

Array dan  
Struct

Alokasi  
Memori

Varian  
*Linked List*

Studi Kasus

Tree

**Binary  
Tree**

Advanced  
Tree

Hash Table

Pointer

List

Stack dan  
Queue

UTS

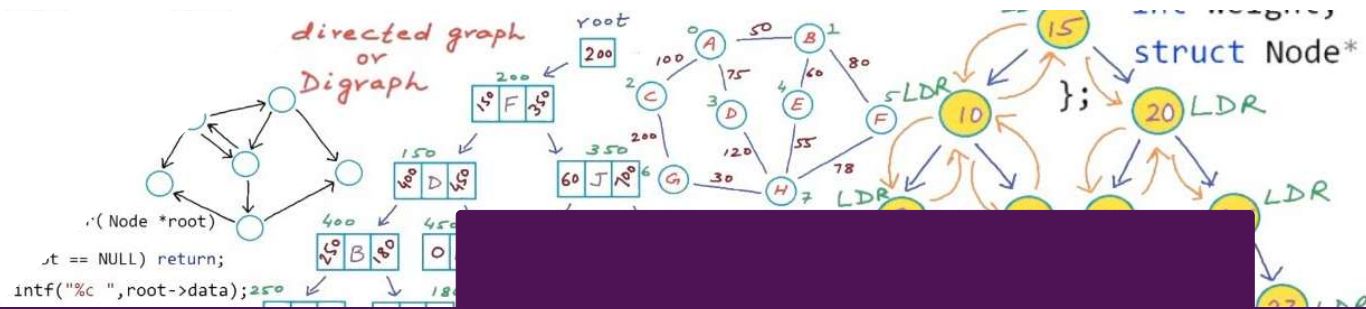
Non-Binary  
Tree

Extended  
Tree

Heap

UAS

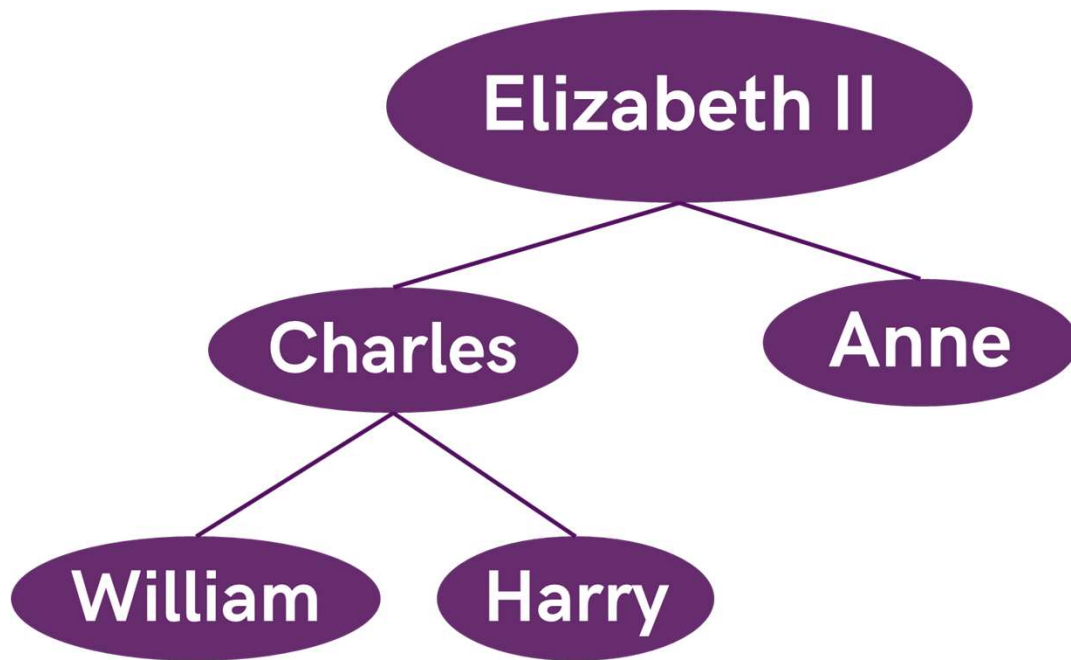
# Tujuan



1	Mahasiswa memahami perbedaan non-binary dan binary tree
2	Mahasiswa mampu mengimplementasikan ADT Tree menggunakan array
3	Mahasiswa mampu mengimplementasikan ADT Tree menggunakan linked list

# Binary Tree

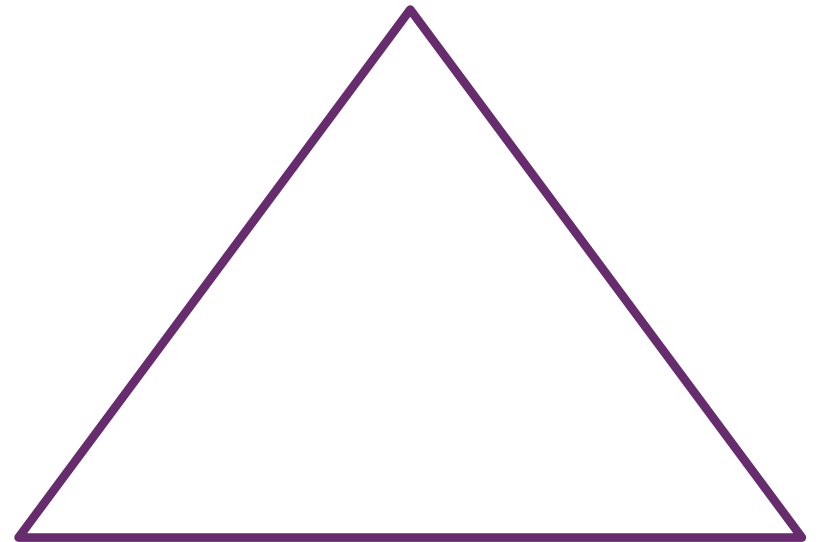
# Binary Tree



Any parent can have **at most** two children

# Full Binary Tree

A binary tree in which all the leaves are located on the same level and every non-leaf node has two children



# Complete Binary Tree

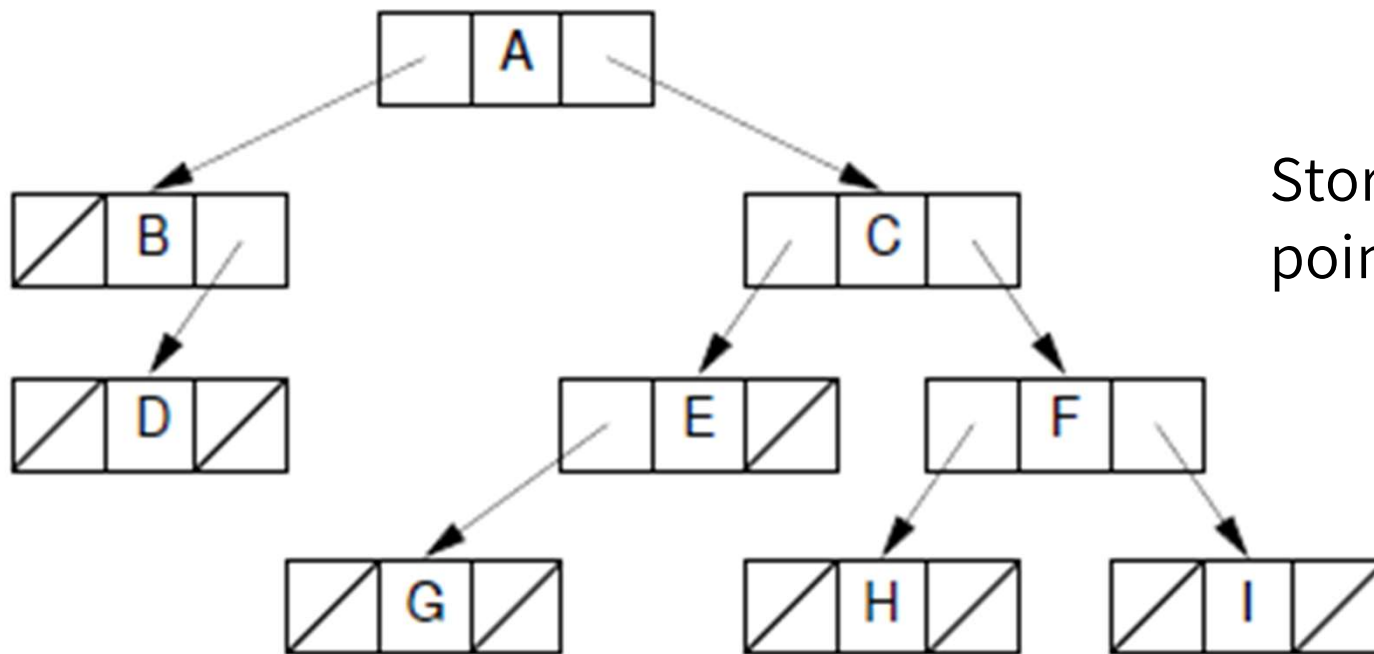
A binary tree that is either full or full through the next-to-last level, with the leaves on the last level located as far to the left as possible



# Implementasi Menggunakan Linked List



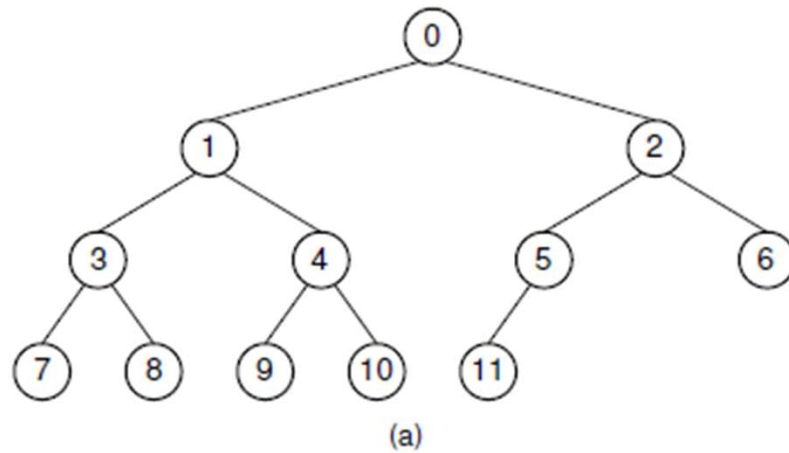
# Pointer-Based Node



Store a linked list of child pointers with each node.

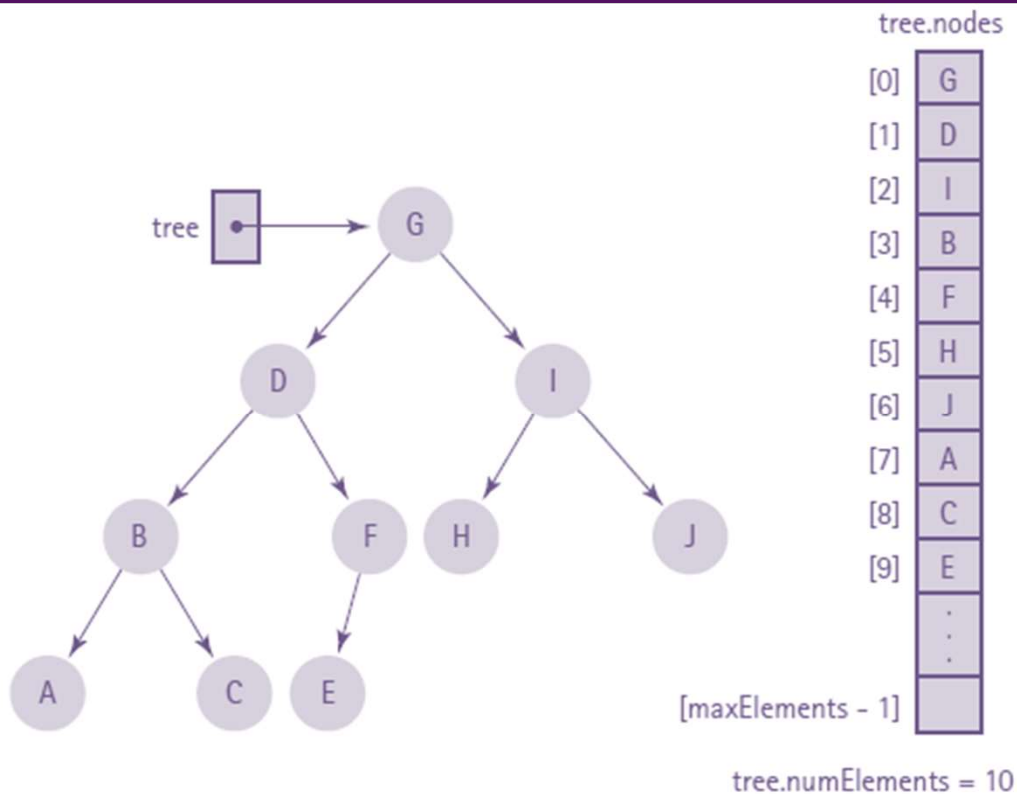
# Implementasi Menggunakan Array

# Array Implementation



Position	0	1	2	3	4	5	6	7	8	9	10	11
Parent	–	0	0	1	1	2	2	3	3	4	4	5
Left Child	1	3	5	7	9	11	–	–	–	–	–	–
Right Child	2	4	6	8	10	–	–	–	–	–	–	–
Left Sibling	–	–	1	–	3	–	5	–	7	–	9	–
Right Sibling	–	2	–	4	–	6	–	8	–	10	–	–

# Array Implementation



- $\text{Parent}(r) = \left\lfloor \frac{(r-1)}{2} \right\rfloor$  if  $r \neq 0$ .
- $\text{Left child}(r) = 2r + 1$  if  $2r + 1 < n$ .
- $\text{Right child}(r) = 2r + 2$  if  $2r + 2 < n$ .
- $\text{Left sibling}(r) = r - 1$  if  $r$  is even.
- $\text{Right sibling}(r) = r + 1$  if  $r$  is odd and  $r + 1 < n$ .

# Binary Search Tree

# Binary Search Tree (BST)

A binary tree in which the key value in any node is greater than the key value in its left child and any of its left children (the node in the left subtree) and less than the key value in its right child and any of its children (the nodes in the right subtree)

# BST Operations

isFull  
IsEmpty  
LengthIs

RetrieveItem  
InsertItem  
DeleteItem

CopyTree  
ResetTree  
GetNextItem

# BST Operations - isFull

```
bool isFull()
{
    tree_t* location;
    try
    {
        location = new tree_t;
        delete location;
        return false;
    }
    catch (bad_alloc)
    {
        return true;
    }
}
```



# BST Operations - isEmpty

```
bool isEmpty(tree_t* tree)
{
    return tree == nullptr;
}
```

# BST Operations - Lengths

```
int lengthIs(tree_t* tree)
{
    if (tree == nullptr)
        return 0;
    else
        return 1 + lengthIs(tree->left) + lengthIs(tree->right);
}
```

# BST Operations – RetrieveItem

```
void retrieveItem(char& item, bool& found, tree_t* tree)
{
    if (tree == nullptr)
        found = false;
    else if (item < tree->info)
        retrieveItem(item, found, tree->left);
    else if (item > tree->info)
        retrieveItem(item, found, tree->right);
    else
    {
        found = true;
        item = tree->info;
    }
}
```

# BST Operations – InsertItem

```
void insertItem(char item, tree_t*& tree)
{
    if (tree == nullptr)
    {
        tree = new TreeNode;
        tree->info = item;
        tree->left = nullptr;
        tree->right = nullptr;
    }
    else if (item < tree->info)
        insertItem(item, tree->left);
    else
        insertItem(item, tree->right);
}
```

# BST Operations – DeleteItem

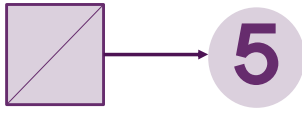
```
void deleteItem(char item, tree_t*& tree)
{
    if (tree == nullptr)
        return;

    if (item < tree->info)
        deleteItem(item, tree->left);
    else if (item > tree->info)
        deleteItem(item, tree->right);
    else
    {
        deleteNode(tree);
    }
}
```

# Insert

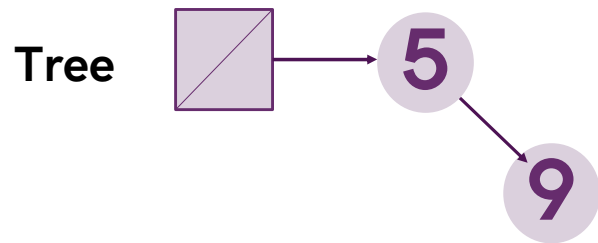
Insert 5

Tree



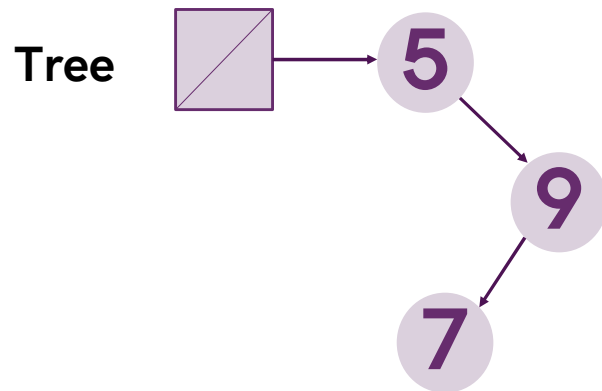
# Insert

Insert 9



# Insert

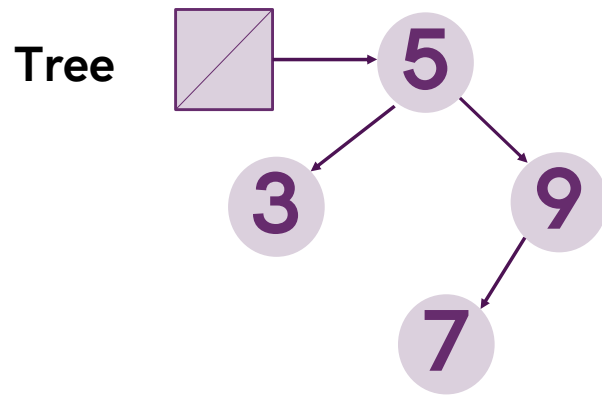
Insert 7





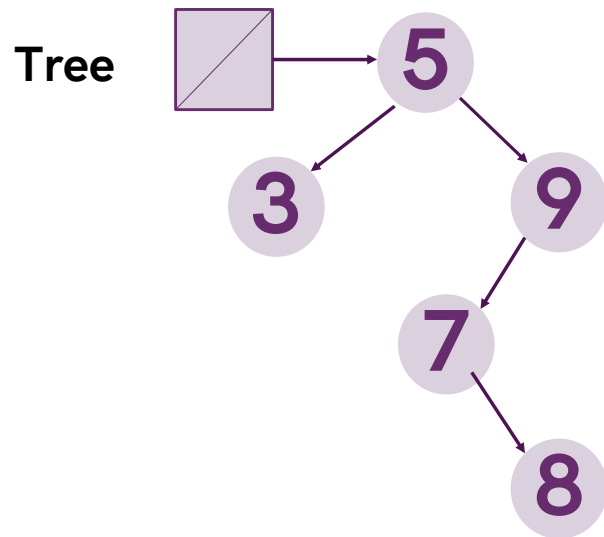
# Insert

Insert 3



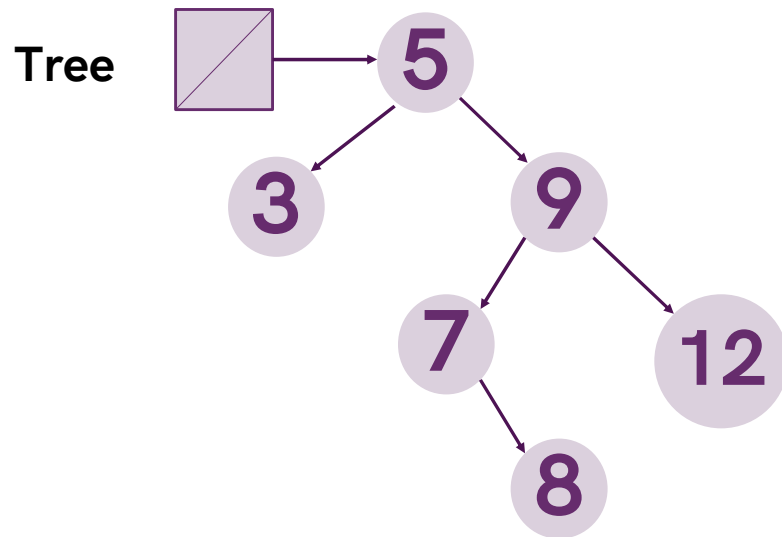
# Insert

Insert 8



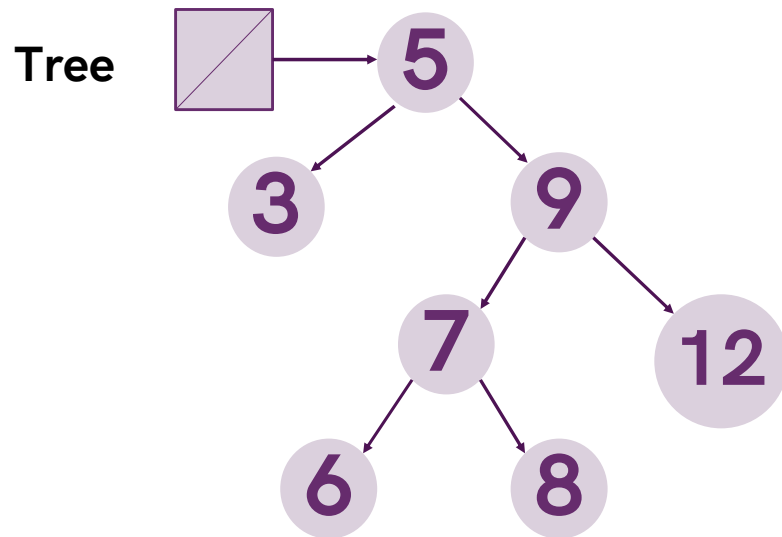
# Insert

Insert 12



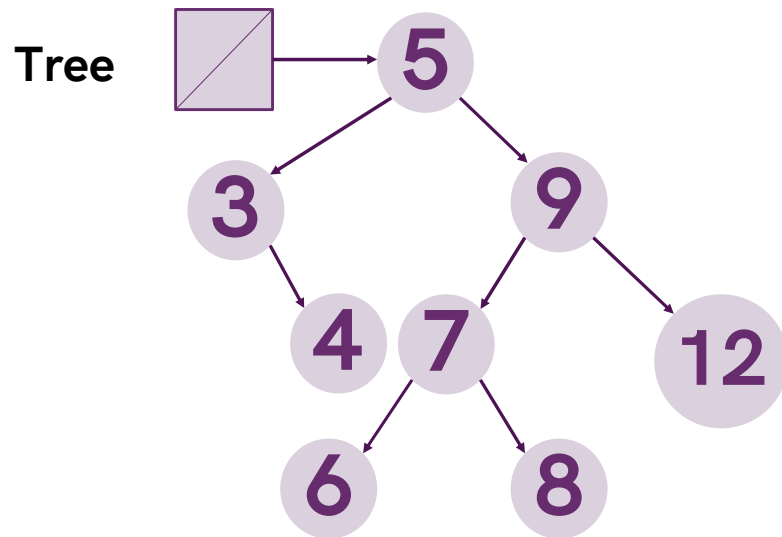
# Insert

Insert 6



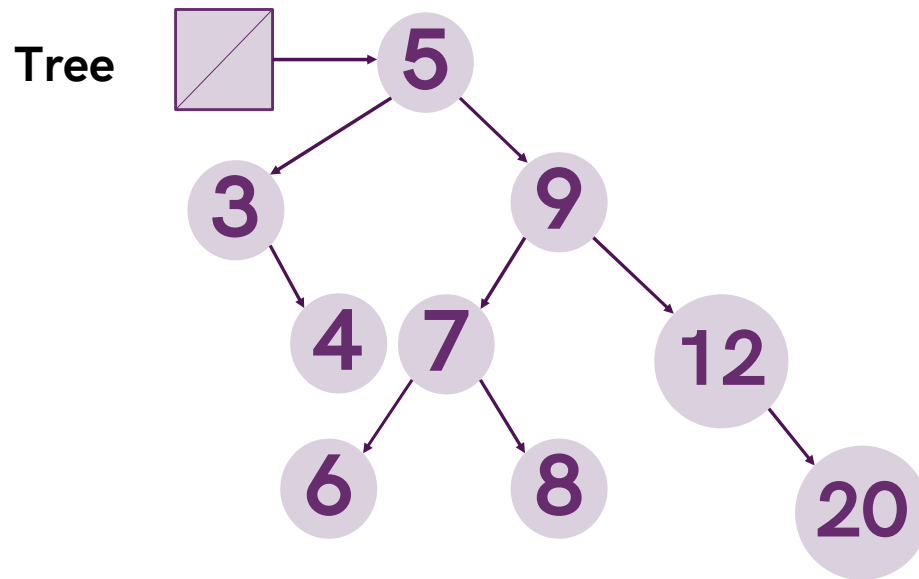
# Insert

Insert 4



# Insert

Insert 20

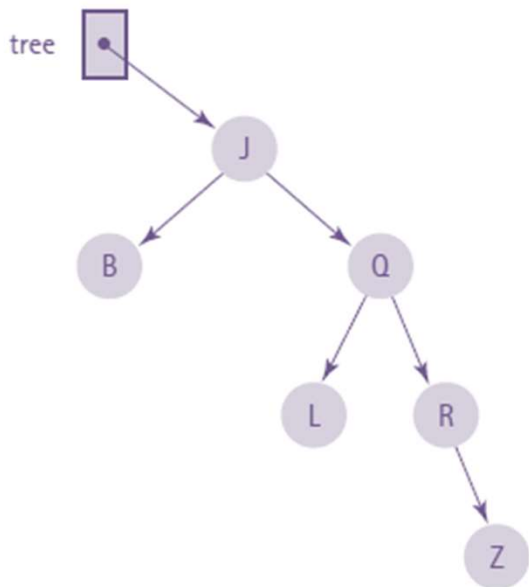


# Delete

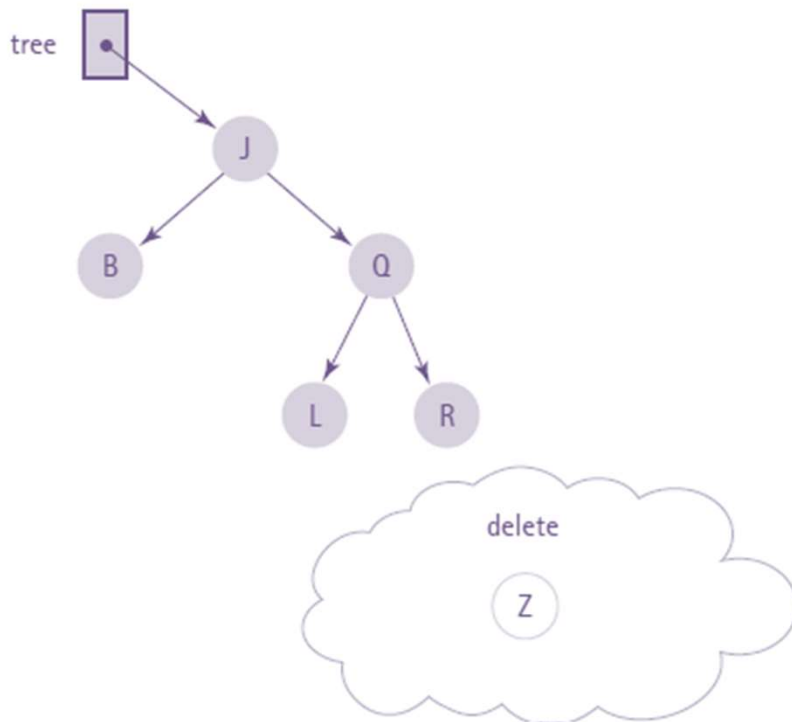
- Deleting a leaf (no children)
- Deleting a node with only one child
- Deleting a node with two children

# Delete a leaf

BEFORE



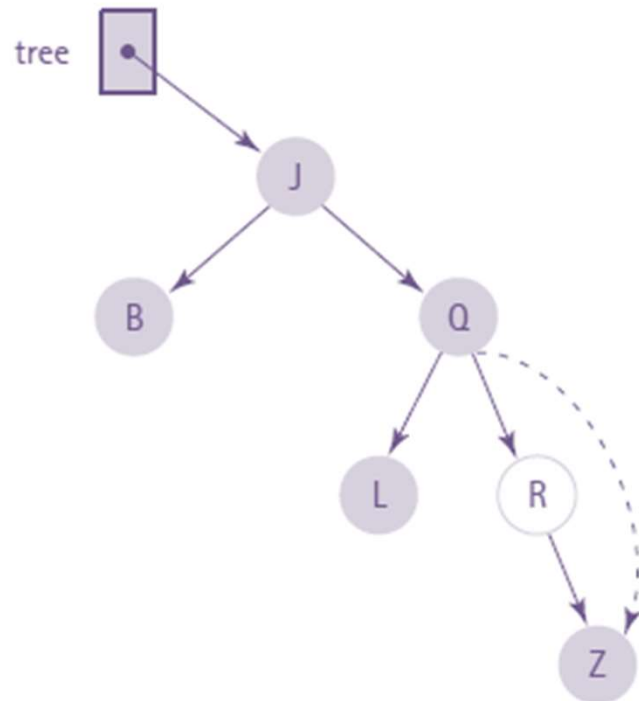
AFTER



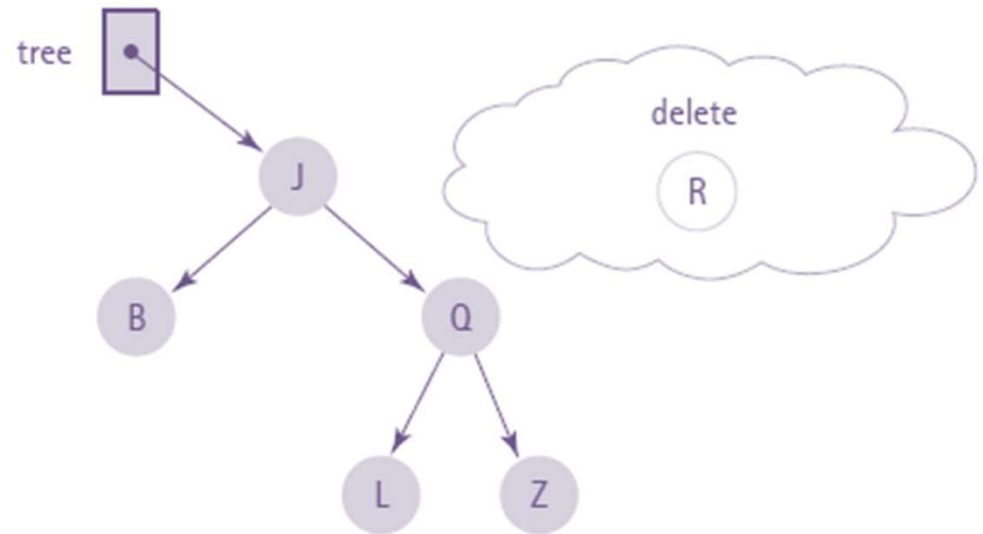


# Delete a node with only one child

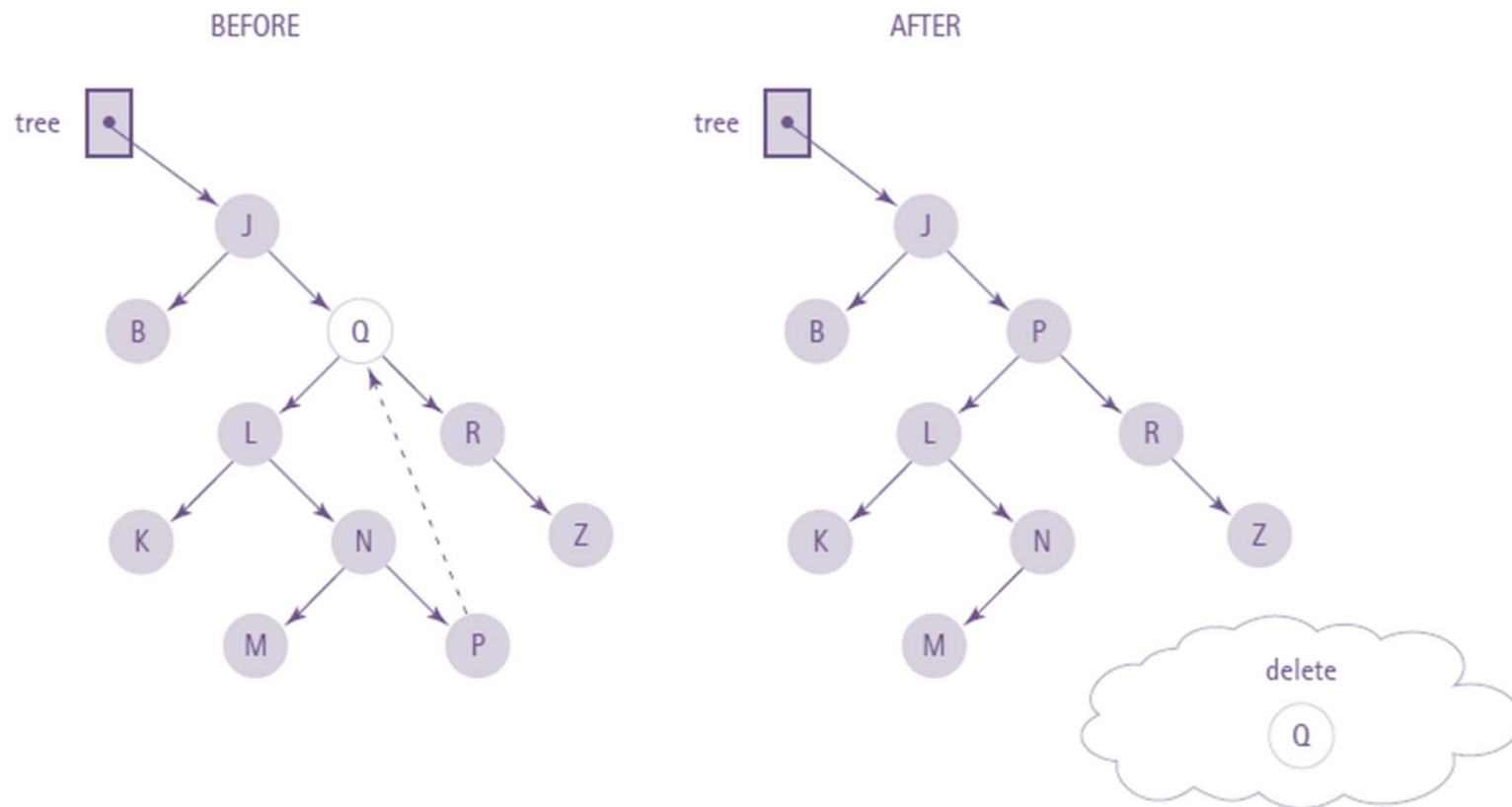
BEFORE



AFTER

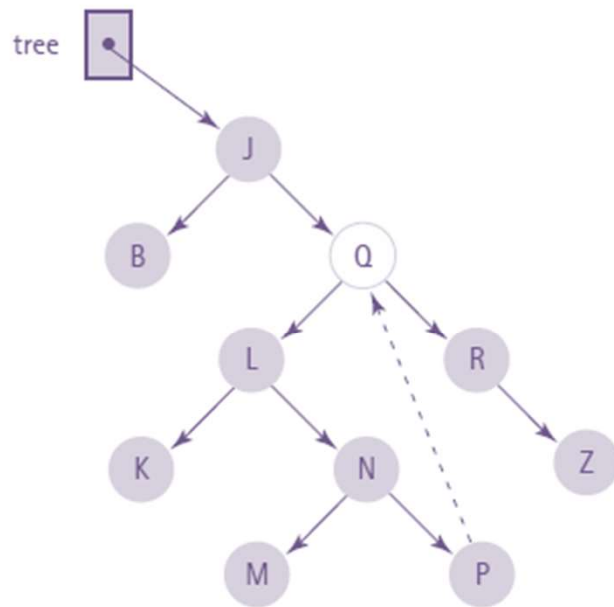


# Delete a node with two child

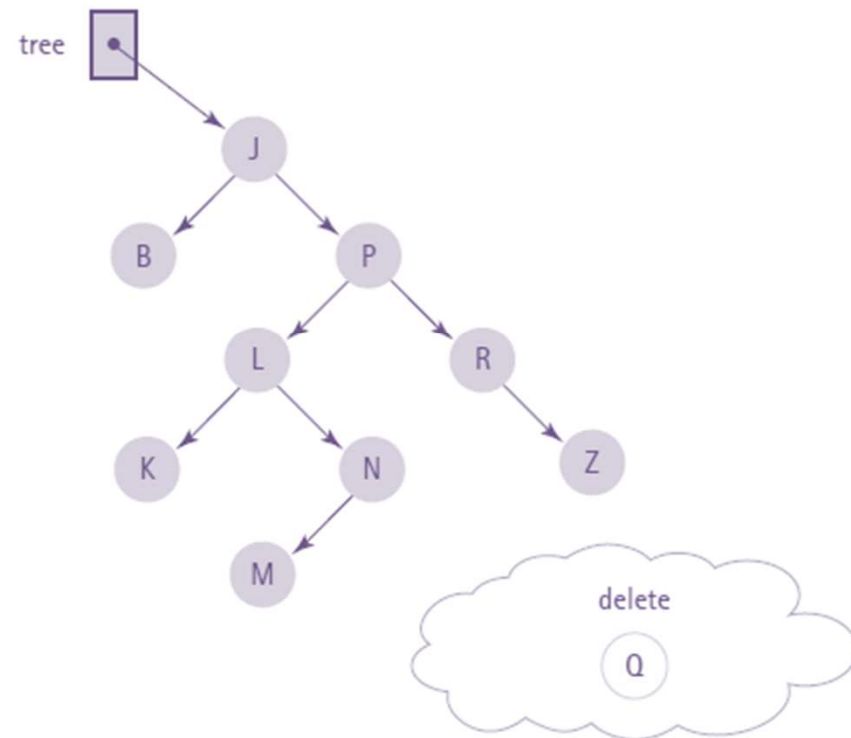


# Print Tree

BEFORE



AFTER



# Insert Algorithm

## *InsertItem*

Create a node to contain the new item.

Find the insertion place.

Attach the new node.

# Delete Algorithm

## *DeleteNode*

```
if (Left(tree) is NULL) AND (Right(tree) is NULL)
    Set tree to NULL
else if Left(tree) is NULL
    Set tree to Right(tree)
else if Right(tree) is NULL
    Set tree to Left(tree)
else
    Find predecessor
    Set Info(tree) to Info(predecessor)
    Delete predecessor
```

# Kompleksitas Algoritma

	Binary Search Tree	Array-Based Linear List	Linked List
Class constructor	$O(1)$	$O(1)$	$O(1)$
Destructor	$O(N)$	$O(1)^*$	$O(N)$
MakeEmpty	$O(N)$	$O(1)^*$	$O(N)$
LengthIs	$O(N)$	$O(1)$	$O(1)$
IsFull	$O(1)$	$O(1)$	$O(1)$
IsEmpty	$O(1)$	$O(1)$	$O(1)$
RetrieveItem			
Find	$O(\log_2 N)$	$O(\log_2 N)$	$O(N)$
Process	$O(1)$	$O(1)$	$O(1)$
Total	$O(\log_2 N)$	$O(\log_2 N)$	$O(N)$
InsertItem			
Find	$O(\log_2 N)$	$O(\log_2 N)$	$O(N)$
Process	$O(1)$	$O(N)$	$O(1)$
Total	$O(\log_2 N)$	$O(N)$	$O(N)$
DeleteItem			
Find	$O(\log_2 N)$	$O(\log_2 N)$	$O(N)$
Process	$O(1)$	$O(N)$	$O(1)$
Total	$O(\log_2 N)$	$O(N)$	$O(N)$

\*If the items in the array-based list could possibly contain pointers, the items must be deallocated, making this an  $O(N)$  operation.