$$0 = 1 - 1 = -1 + 1 = 0$$

From Elementary School to Higher Algebras

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IMB

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Your favorite equations?

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- $e^{i\pi} + 1 = 0$
- $\int_{\partial D} \omega = \int_D \mathrm{d}\omega$
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Question
Can you prove $0 = 0$, non-trivially?

Test your math level

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Hopf fibration