

Stack

(LIFO ordering structure)

Stack ADT

```
template <class T>
class Stack {
public:
    Stack();

    bool IsEmpty() const;

    // T& Top() const;

    void Push(const T& data);

    T Pop();

private:
    Not yet!!

};
```

```
int main() {
    List<int> mystack;
    mystack.Push(9);
    mystack.Push(3);
    mystack.Push(2);
    mystack.Pop();
    mystack.Push(4);
    . . . .
}
```

Linked list based implementation

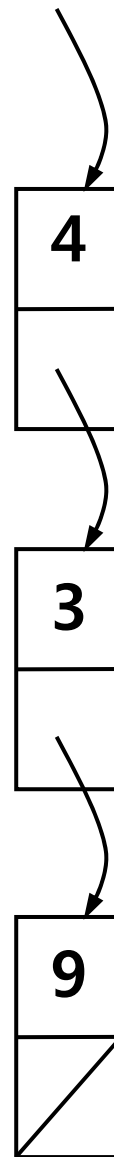
```
template <class T>
class Stack {
public:
    Stack();

    bool IsEmpty() const;

    void Push(const T& d);

    T Pop();

private:
    struct stackNode {
        T data;
        stackNode *next;
        stackNode();
    };
    stackNode *top;
    int size;
};
```



```
template<class T>
void Stack<T>::Push(const T & d)
{
    stackNode *newNode =
        new stackNode(d);

    newNode->next = top;
    top = newNode;
    size++;
}
```

```
// Assume stack is not empty
template<class T>
T Stack<T>::Pop() {
}
```

Array based implementation

```
template <class T>
class Stack {
public:
    Stack();

    bool IsEmpty() const;

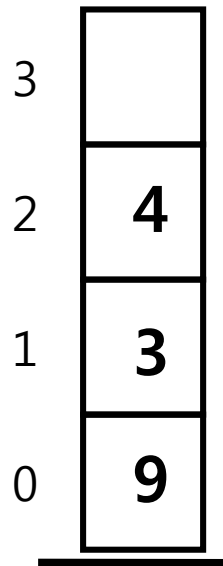
    void Push(const T& d);

    T Pop();

private:
    int capacity;
    int size;
    T *stack;
};
```

size = 3

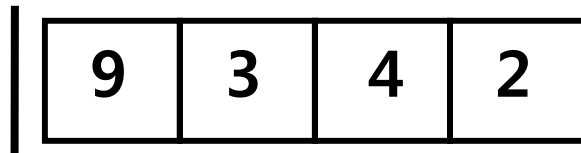
```
template <class T>
void Stack<T>::Push(const T &d) {
    if (size == capacity) {
        // resize stack array
    }
    stack[size] = d;
    size++;
}
```



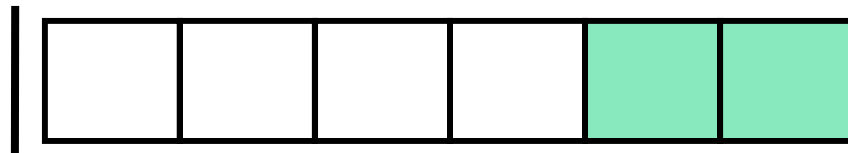
```
template <class T>
Stack<T>::Stack() {
    capacity = 4;
    size = 0;
    stack = new T[capacity];
}
```

Array resizing when inserting (pushing), but the array is full

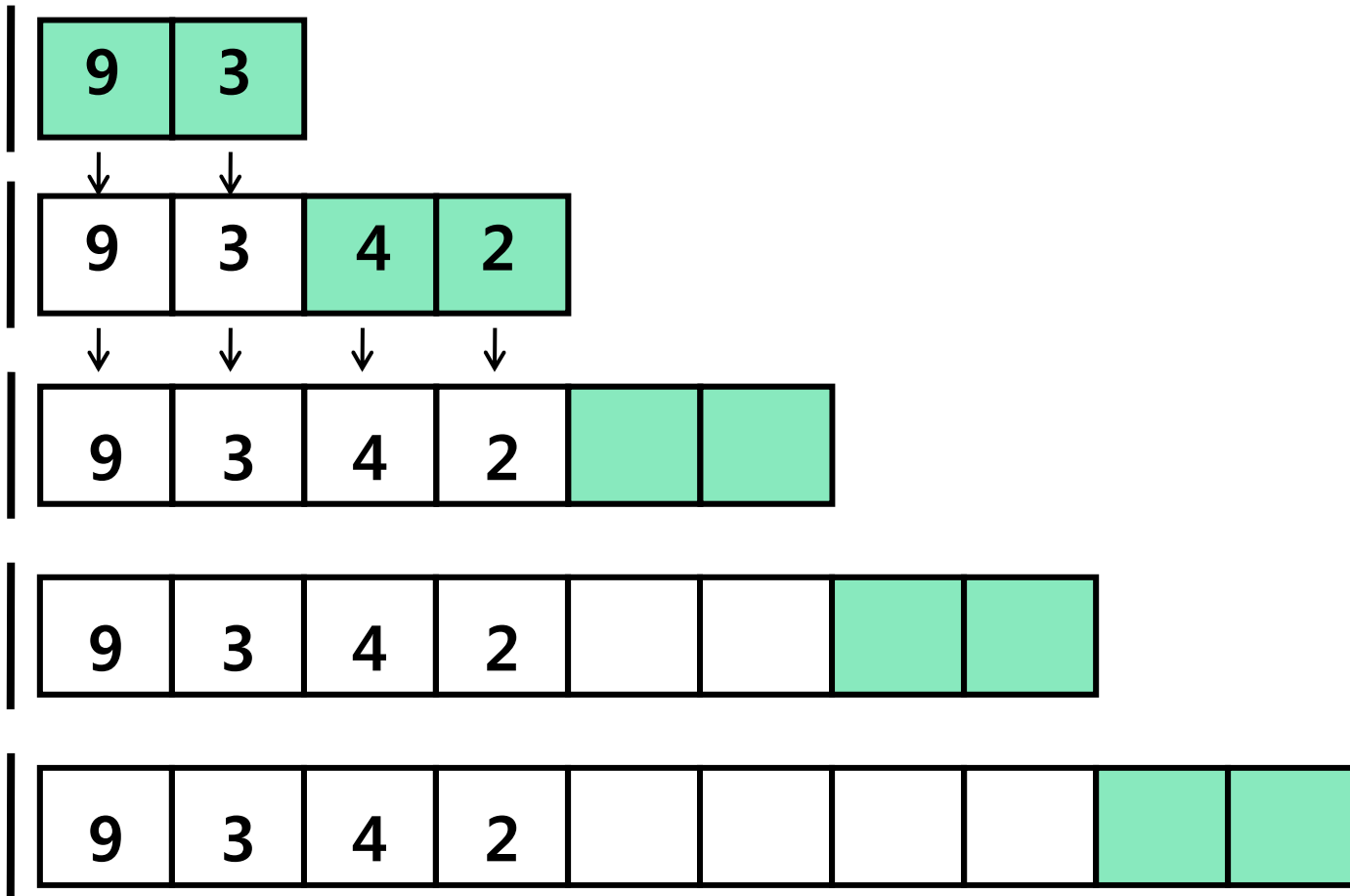
Steps.



How much do we need to increase?

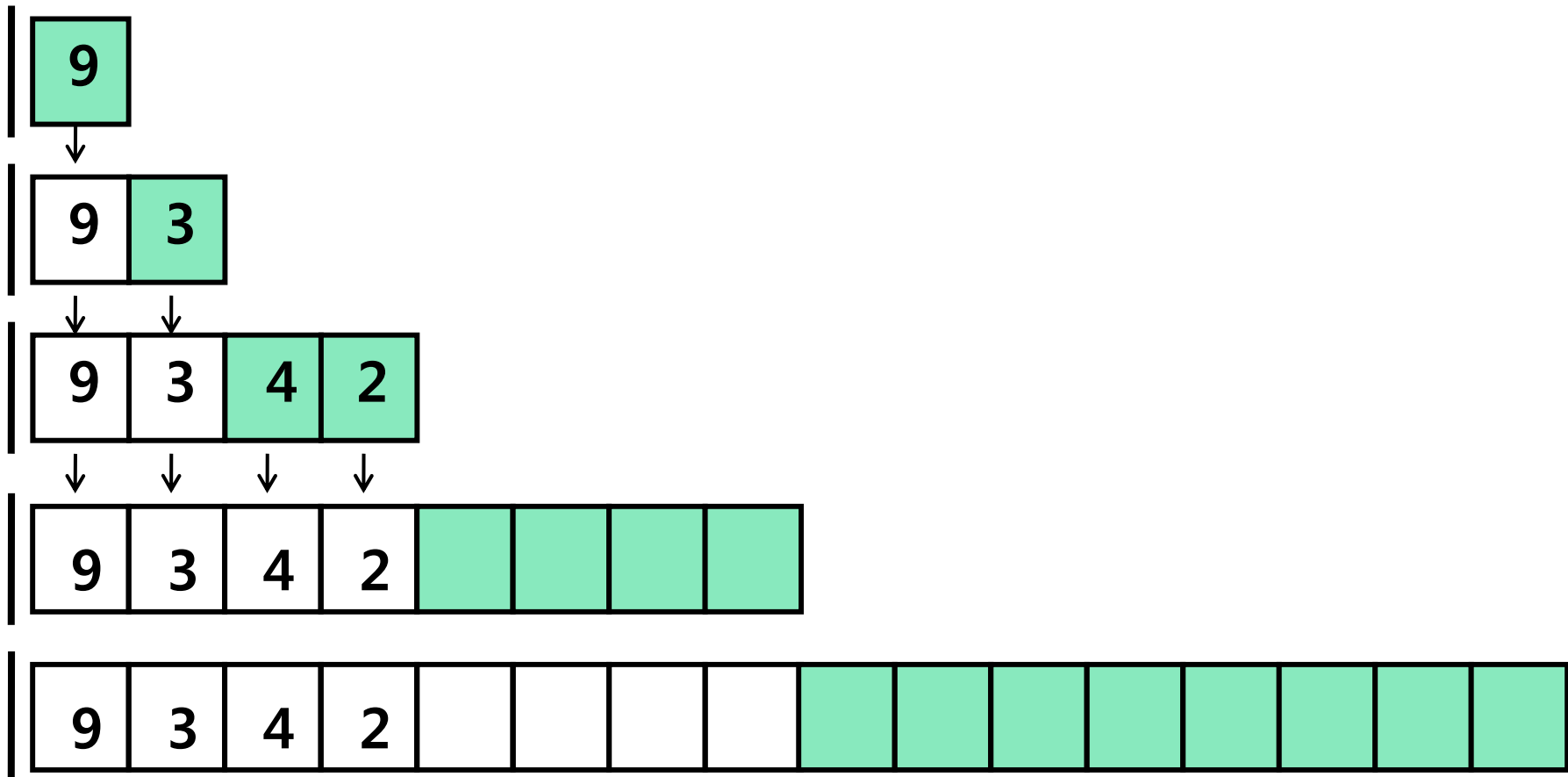


Strategy 1: Increase array size by a constant amount



How much is the cost by this strategy on a sequence of n pushes?

Strategy 2: Double the array size



How much is the cost by this strategy on a sequence of n pushes?

Run time summary

- Linked list based implementation
 - $O(1)$ per push, pop
- Array based implementation
 - $O(1)$ per pop
 - $O(1)$ per push if capacity exists.
 - Cost over n pushes is $O(n)$ for an average of $O(1)$ per push.
- Which implementation we choose?

Queue

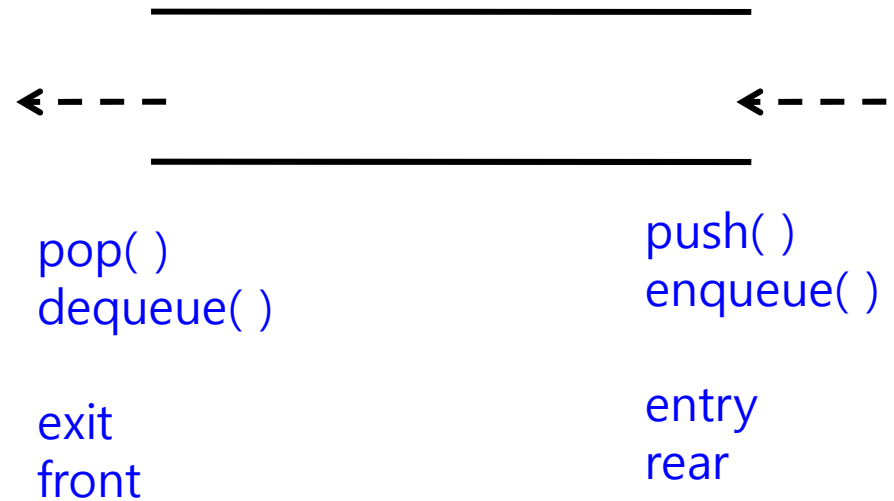
(FIFO ordering structure)

Queue ADT

```
template <class T>
class Queue
{
public:
    Queue ();
    Boolean IsEmpty() const;

    // T& Front() const ;
    // T& Rear() const;
    void Push(const T& item);
    T Pop();

Private:
    // not yet
};
```



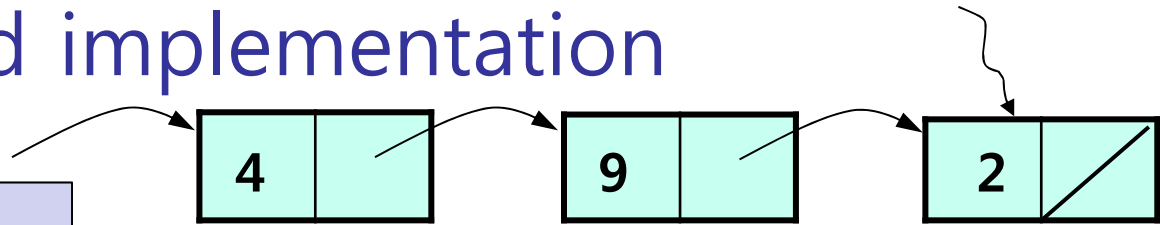
Linked list based implementation

```
template <class T>
class Queue {
public:
    Queue();

    bool IsEmpty() const;
    void Push(const T& d);
    T Pop();

private:

};
```



Which pointer is "entry" ("rear") and which is "exit" ("front")?

Running time of Push?

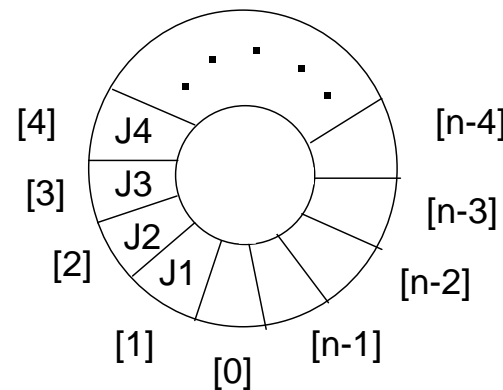
Running time of Pop?

Array based implementation

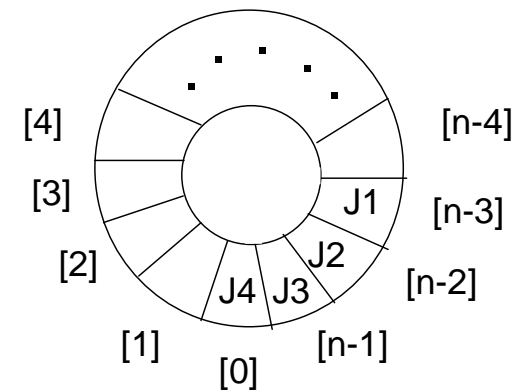
```
template <class T>
class Queue {
public:
    Queue();

    bool IsEmpty() const;
    void Push(const T& d);
    T Pop();

private:
    T *queue;
    int capacity;
    int front;
    int rear;
};
```



front = 0; rear = 4



front = n - 4; rear = 0

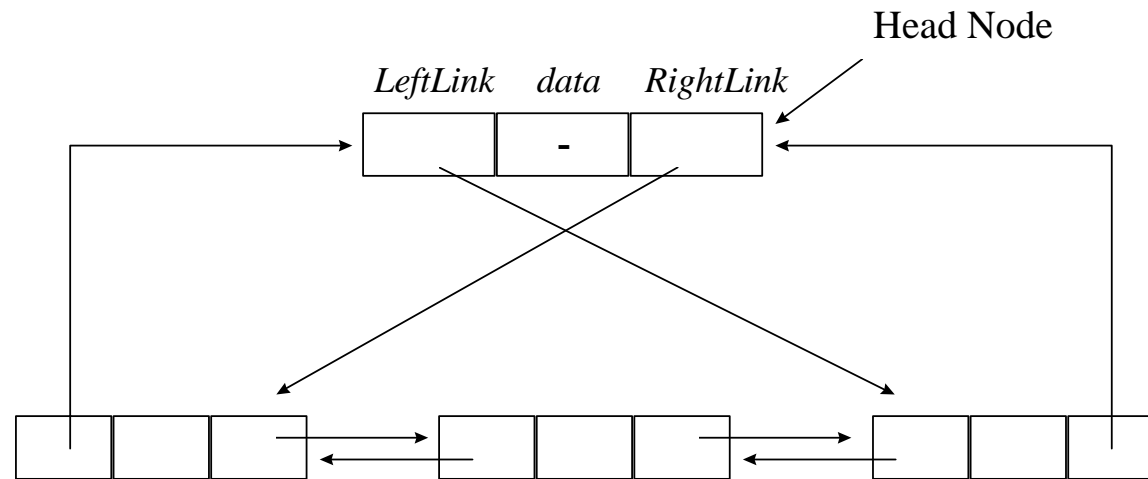
Modeling as a circular list

DLL

(Doubly Linked Lists)

- Problems with singly linked lists
 - can move only in the direction of the links
 - deletion requires knowing the preceding node
- Node
 - at least three fields :
data, llink (left link), rlink (right link)

DLL with sentinel node



- Head node
 - convenient for algorithms
 - data field usually contains no information
- Essential virtue
 - one can go back and forth with equal ease
 - $p == p \rightarrow \text{llink} \rightarrow \text{rlink} == p \rightarrow \text{rlink} \rightarrow \text{llink}$

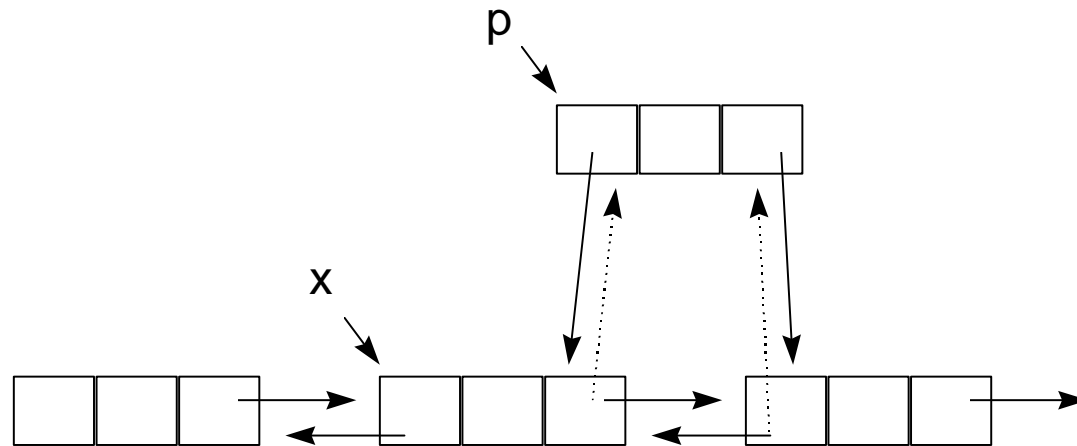
Implementation

```
class DbList;
class DbListNode {
// Dblist functions are allowed to access
friend class DbList;
private:
    int data;
    DbListNode *left, *right;
};

class DbList {
public:
    // List manipulation operations
    :
private:
    DbListNode *first; // points to head node
};
```


Insert a node

```
void DbList::Insert(DbListNode *p, DbListNode *x)
// insert node p to the right of node x
{
    p->left = x; p->right = x->right;
    x->right->left = p; x->right = p;
}
```



Delete a node

```
void DbList::Delete(DbListNode *x)
{
    if ( x == first ) throw "Deletion of headnode not permitted";
    else {
        x->left->right = x->right;
        x->right->left = x->left;
        delete x;
    }
}
```