### Introduction to reinforcement learning

July 9, 2019

#### Introduction

► This morning we will study an important AI paradigm : Reinforcement learning (RL)

### Applications of RL

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- ▶ RL has many applications and is quite a hot topic.
- Especially Deep Reinforcement Learning has received a lot of attention recently.

### Applications of Deep Reinforcement Learning I

Atari games



Figure: Atari game

### Applications of Deep Reinforcement Learning II

► AlphaGo

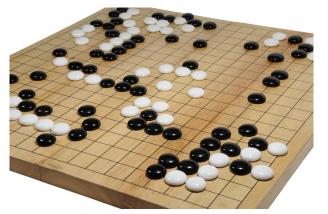


Figure: Go game, beaten by AlphaGo in 2017 [Silver et al., 2016]

### Applications of Reinforcement Learning III

► Reinforcement Learning is also begin used in the community of **Computationnal neuroscience**.

#### Ressources

- https://github.com/nlehir/summerschool contains our slides and exercices.
- ▶ When doing exercises, we will be using **python 3**

#### References

► [Andrew and Sutton, 1998]

#### Overview

#### The framework

Supervised learning Reinforcement learning

# Dynamic programming Value Iteration

### Supervised learning

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- MNIST demo

Supervised learning

# Supervised learning and Correction

- ▶ In **supervised learning**, the supervisor indicates the **expected answer** the agent should answer.
- ▶ With our mnist digit classificatino example, the actin of the agent is the **prediction of the class**.

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- ► The feedback does not depend on the action performed by the agent (for instance the prediction from the agent)
- ▶ We say that the agent receives an instructive feedback

#### Supervised learning Correction

- ▶ In **supervised learning**, the supervisor indicates the **expected answer** the agent should answer.
- ▶ The agent must then **correct its model** based on this answer.

## Cost sensitive learning

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#### Cost sensitive learning

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- ► The agent receives an evaluative feedback. The feedack depends on the action performed by the agent.
- Examples:
  - Al playing a game and receiving "victory" or "defeat" as a feedback
  - Child playing with an animal.

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- ▶ In reinforcement learning, the feedback is a **real number**
- **Example:** amount of coins won after a poker turn.

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- ▶ A reward of -10 good be good or bad depending on the other rewards that are possible to obtain.
- The objective of the agent will be to optimize the agregation of rewards

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- Examples:
  - world =  $\mathbb{R}^2$
  - ▶ state = position
  - actions = moving somewhere
  - reward = amount of food found

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#### Question

Are these hypothesis valid in the case of AlphaGo ?



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- Yes! So you can do crazy stuff in discrete spaces.
- However, please note that this is not always the case. Sometimes the possible actions are continuous, the available psitions are continuous, etc.

#### Let us continue with the formalization

- we will write :
  - $\triangleright$   $s_t$ : state at time t
  - a<sub>t</sub>: action performed at time t
  - r<sub>t</sub>: reward received at time t
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- ightharpoonup the actions are chosen according to a **policy**  $\pi$

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Reinforcement learning

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- ▶ The policy  $\pi$  depends on the current state.
- ▶ It can be **deterministic**: the action chosen is chosen with probability 1
- Or stochastic: the action performed in a given state is drawn from a distribution

#### Two levels of randomness

- ▶ The policy can be deterministic or stochastic.
- ▶ But the result of an action could also be stochastic! This is called a **stochastic transition function**.

The framework

Reinforcement learning

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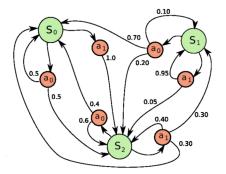


Figure: A stochastic policy with a stochastic transition function.

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### Exercise

▶ What is the probability of staying in state  $S_0$  when performing an action from  $S_0$ ? and from  $S_1$  and  $S_2$ ?

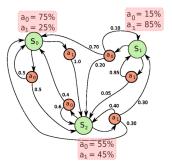


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## Agregation of rewards

- Remember that our agent want to optimize the agregation of the rewards.
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- ▶ However, what exactly does the agent maximise ?
- ▶ There are several ways to agregate the rewards.

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# Agregation of rewards

▶ If the horizon is finite, we can take the sum

$$V^{\pi}(s_0) = r_0 + \dots + r_N \tag{1}$$

# Agregation of rewards

▶ If the horizon is finite, we can take the sum

$$V^{\pi}(s_0) = r_0 + \dots + r_N \tag{2}$$

▶ We could also average a window. For instance a window of size 3 :

$$V^{\pi}(s_0) = \frac{r_0 + r_1 + r_2}{3} \tag{3}$$

## Agregation of rewards: discount factor

▶ the **discount factor**  $\gamma \in [0,1]$  allows you to weight the rewards  $r_k$ 

$$V^{\pi}(s_0) = \sum_{t=t_0}^{+\infty} \gamma^{t-t_0} r_t \tag{4}$$

Reinforcement learning

## More considerations

- ► The Markov hypothesis
- Exploitation exploration compromise

#### Art

"RL is a science, but dealing with the exploration-exploitation compromise is an art" (Sutton)

# Dynamic programming

- ► Today we will study a simple case of Reinforcement learning
- ▶ In that case, the result of our actions is deterministic.

### World

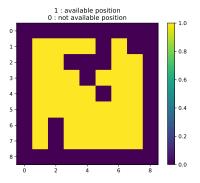


Figure: 2 dimensional world.

### Reward

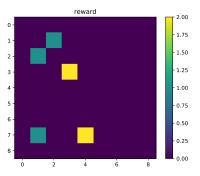


Figure: Reward function.

#### 2D world

- ▶ Our agent can move in the 4 directions, one step at a time.
- ▶ We will progressively build an agent that learns to evaluate the states and then learns how to go to the best state.

### Value function

► For each state (=position in the 2D world), we want to compute the **value function**.

$$V(s_0) = r_0 + \gamma r_1 + \gamma^2 r_2 \dots$$
 (5)

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► For each state (=position in the 2D world), we want to compute the **value function**.

$$V(s_0) = r_0 + \gamma r_1 + \gamma^2 r_2 \dots$$
 (6)

▶ Can you express  $V(s_0)$  as a function of  $V(s_1)$  ?

## Bellman equation

▶ This equation is the Bellman equation.

## Value Iteration

▶ First, the initial Value function for all the states is 0.

### Value Iteration

- First, the initial Value function for all the states is 0.
- ► Then we propagate the information about the rewards between the states, in order to **update the value function**
- We can find an optimal policy in the following way :

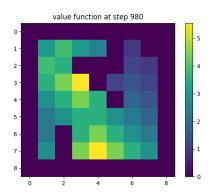
$$\forall s \in V(s_t) \leftarrow \max_{a_t} \left( r_{s_t} + \gamma V(s_{t+1}) \right) \tag{7}$$

 $(s_{t+1} \text{ depends on } a_t).$ 

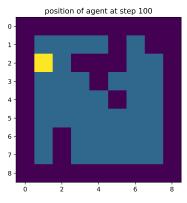
└─Value Iteration

#### Value iteration

► After learning, we will obtain a value function



└─Value Iteration



### Exercise 2A

- ▶ in the reinforcement learning folder
- Please use the file create\_world.py in order to generate your own environment.
- ▶ You can use the one that is already there if you prefer.
- ▶ We store the data about the world in .npy files.

## Exercise 2B

► In value\_iteration.py, modify the function move\_agent so that the agent is randomly moved.

└─Value Iteration

## Exercise 2C

In value\_iteration.py, modify the function update\_value\_function in order to modify the value function according to the Bellman equation.

## Exercise 2D

► Finally, make the alrogithm run in order to **converge to the optimal value function.** 

## Exercise 3

► Please use the file **value\_iteration\_policy** in order to design an optimal policy for our agent.

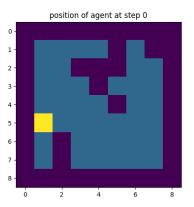


Figure: After learning, the agent can go to the reward.

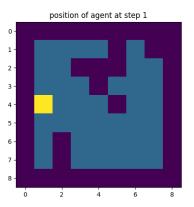


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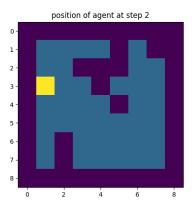


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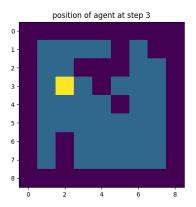


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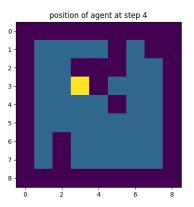


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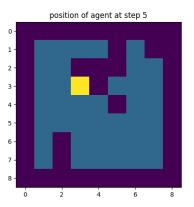


Figure: After learning, the agent can go to the reward.

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