Advanced Algorithmic Problem Solving(R1UC601B)

PRACTICE QUESTIONS FOR MTE

1. What is meant by time complexity and space complexity? Explain in detail.

Time Complexity and **Space Complexity** are two important aspects of evaluating the efficiency of an algorithm.

Time Complexity

Time Complexity is a measure of the amount of time an algorithm takes to run as a function of the size of the input to the program. It's usually expressed using Big O notation, which describes the upper bound of the time complexity in the worst-case scenario.

For example, for a simple for loop iterating over n elements, the time complexity would be O(n). This means that if the size of the input (n) doubles, the time taken for the algorithm also doubles.

Space Complexity

Space Complexity is a measure of the amount of memory an algorithm needs to run to completion. It's also expressed using Big O notation, which describes the upper bound of the space complexity in the worst-case scenario.

For instance, consider an algorithm that creates a new list and adds n elements to it. The space complexity for this algorithm is O(n). This means if the size of the input (n) doubles, the memory required by the algorithm also doubles.

In summary, time complexity and space complexity help us to estimate the worst-case scenario in terms of time and space respectively, for an algorithm. They are crucial in determining the scalability and efficiency of an algorithm. However, there's often a trade-off between the two. For example, an algorithm might be able to run faster (lower time complexity) by using more memory (higher space complexity), and vice versa. This trade-off is often referred to as the time-space trade-off.

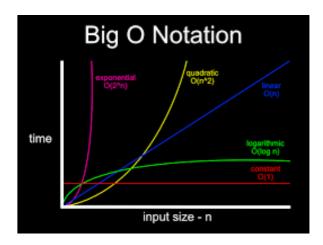
2. What are asymptotic notations? Define Theta, Omega, big O, small omega, and small o.

Asymptotic notations are mathematical tools used to describe the limiting behavior of functions when the argument tends towards a particular value or infinity, most often in terms of simpler functions. They are widely used in computer science to describe the time and space complexity of algorithms. Here are the definitions of the notations you asked about:

- 1. **Big O Notation (O)**: The Big O notation upper bounds a function to within a constant factor. It is used to describe the worst-case scenario of an algorithm's time or space complexity. For example, if we say a function f(n) is O(g(n)), it means there are some constant c and some value of n (n0) after which f(n) is always less than or equal to c*g(n).
- 2. **Omega Notation** (Ω): The Omega notation provides an asymptotic lower bound. It is used to describe the best-case scenario of an algorithm's time or space complexity. For example, if we say a function f(n) is $\Omega(g(n))$, it means there are some constant c and some value of n (n0) after which f(n) is always greater than or equal to c*g(n).
- 3. **Theta Notation (\Theta)**: The Theta notation bounds a function from above and below, so it defines exact asymptotic behavior. A function f(n) has a $\Theta(g(n))$ if it is both O(g(n)) and $\Omega(g(n))$.
- 4. **Small o notation (o)**: The small o notation is an upper bound that is not tight. If f(n) is o(g(n)), then for any constant c > 0, there exists a constant n > 0 such that $0 \le f(n) < c*g(n)$ for all n > n > 0. This means g(n) grows strictly faster than f(n).
- 5. **Small omega notation** (ω): The small omega notation is a lower bound that is not tight. If f(n) is $\omega(g(n))$, then for any constant c > 0, there exists a constant n > 0 such that $0 \le c * g(n) < f(n)$ for all n > n > 0. This means f(n) grows strictly faster than g(n).

Advanced Algorithmic Problem Solving (R1UC601B)

- 3. Explain the meaning of $O(2^n)$, $O(n^2)$, O(nlgn), O(lgn). Give one example of each.
 - 1. **O(2^n)**: This represents an algorithm whose growth doubles with each addition to the input data set. The growth curve of an O(2^n) function is exponential starting off very shallow, then rising meteorically. An example of an O(2^n) function is the recursive calculation of Fibonacci numbers.
 - 2. **O(n^2)**: This time complexity represents an algorithm whose performance is directly proportional to the square of the size of the input data set. This is common with algorithms that involve nested iterations over the data set. An example is bubble sort.
 - 3. **O(n log n)**: This is the time complexity of an algorithm that increases linearly with the size of the input, but also has a logarithmic aspect due to some divide and conquer aspect of the algorithm. Common algorithms with this time complexity include quicksort, mergesort, and heapsort.
 - 4. **O(log n)**: Logarithmic complexity arises when we reduce the size of the input data in each step of the algorithm (as in binary search). Here's a simple binary search algorithm:



4. Explain sliding window protocol.

The **Sliding Window Technique** is a method used in Data Structures and Algorithms (DSA). It's used to efficiently solve problems that involve defining a window or range in the input data (arrays or strings) and then moving that window across the data to perform some operation within the window. This technique is commonly used in algorithms like finding subarrays with a specific sum, finding the longest substring with unique characters, or solving problems that require a fixed-size window to process elements efficiently.

Here's a simple example to illustrate this: say we have an array of size N and also an integer K. Now, we have to calculate the maximum sum of a subarray having size exactly K. One way to do this is by taking each subarray of size K from the array and find out the maximum sum of these subarrays. This can be done using Nested loops which will result into O (N^2) Time Complexity.

But we can optimize this approach using the Sliding Window Technique. Instead of taking each K sized subarray and calculating its sum, we can just take one K size subarray from 0 to K-1 index and calculate its sum. Now shift our range one by one along with the iterations and update the result. This operation is optimal because it takes O (1) time to shift the range instead of recalculating.

There are basically two types of sliding window:

- 1. **Fixed Size Sliding Window**: Compute the result for the 1st window, i.e., include the first K elements of the data structure. Then use a loop to slide the window by 1 and keep computing the result window by window.
- 2. **Variable Size Sliding Window**: The steps to solve these questions are similar to the fixed size sliding window, but the window size can change based on certain conditions.

Advanced Algorithmic Problem Solving(R1UC601B)

5. Explain Naive String-Matching algorithm. Discuss its time and space complexity.

The Naive String-Matching Algorithm is a simple method used for pattern searching within a text. Given a text string of length n and a pattern of length m, the task is to print all occurrences of the pattern in the text. You may assume that n > m.

Here's how the algorithm works:

- 1. Slide the pattern over the text one by one.
- 2. For each character in the text string, check for a pattern match.
- 3. If a match is found, then slide by 1 again to check for subsequent matches.

Now, let's discuss its time and space complexity:

Time Complexity:

- **Best Case:** O(n) This is when the pattern is found at the very beginning of the text (or very early on). The algorithm will perform a constant number of comparisons, typically on the order of O(n) comparisons, where n is the length of the pattern.
- Worst Case: O(n*m) This is when the pattern doesn't appear in the text at all or appears
 only at the very end. The algorithm will perform O((n-m+1)*m) comparisons, where n is
 the length of the text and m is the length of the pattern. In the worst case, for each
 position in the text, the algorithm may need to compare the entire pattern against the
 text.

Space Complexity:

• The space complexity of the Naive String-Matching Algorithm is O(1). This is because it does not require any additional space that scales with input size.

```
def naive_string_matching(text, pattern):
 n = len(text)
 m = len(pattern)
 # Slide the pattern over the text one by one
 for i in range(n - m + 1):
   j = 0
   # For current index i, check for pattern match
    while(j < m):
     if (text[i + j] != pattern[j]):
        break
      j += 1
    # If pattern matches at index i
   if (j == m):
      print("Pattern found at index", i)
# Driver's Code
text = "AABAACAADAABAABA"
pattern = "AABA"
naive_string_matching(text, pattern)
```

6 Explain Rabin Karp String-Matching algorithm. Discuss its time and space complexity.

The Rabin-Karp Algorithm is a pattern searching algorithm that uses hashing to find any one of a set of pattern strings in a text. It uses a rolling hash to quickly filter out positions of the text that cannot match the pattern. This is why it's faster than the Naive String-Matching Algorithm for most cases.

Advanced Algorithmic Problem Solving(R1UC601B)

Here's how the algorithm works:

- 1. Calculate the hash value of the pattern.
- 2. Calculate the hash value of the first window of the text of the same length as the pattern.
- 3. Compare the hash value of the pattern with the hash value of the current substring of text.
- 4. If the hash values match, then only it starts matching individual characters.
- 5. Slide the window in the text one character at a time, updating the hash value of the text window at each step.

The hash value is calculated using a rolling hash function, which allows you to update the hash value for a new substring by efficiently removing the contribution of the old character and adding the contribution of the new character. This makes it possible to slide the pattern over the text and calculate the hash value for each substring without recalculating the entire hash from scratch.

Now, let's discuss its time and space complexity:

Time Complexity:

- **Best Case:** O(n + m) This is when the pattern is found at the very beginning of the text (or very early on). The algorithm will perform a constant number of comparisons, typically on the order of O(n + m) comparisons, where n is the length of the text and m is the length of the pattern.
- Worst Case: O(nm) This is when all characters of pattern and text are the same as the
 hash values of all the substrings of T[] match with the hash value of P[]. The algorithm will
 perform O((n-m+1)*m) comparisons, where n is the length of the text and m is the length
 of the pattern¹.

Space Complexity:

• The space complexity of the Rabin-Karp Algorithm is O(1). This is because it does not require any additional space that scales with input size².

```
function RabinKarp(string s[1..n], string pattern[1..m])
  hpattern := hash(pattern[1..m]); hs := hash(s[1..m])
  for i from 1 to n-m+1
    if hs = hpattern
    if s[i..i+m-1] = pattern[1..m]
        return i
    hs := hash(s[i+1..i+m])
    return not found
```

Explain Knuth Morris and Pratt String-Matching algorithm. Discuss its time and space complexity.

It's a linear time algorithm used for pattern searching in strings.

The KMP algorithm uses the observation that when a mismatch occurs, the pattern itself contains enough information to determine where the next match could begin. This avoids unnecessary comparisons in the future.

Advanced Algorithmic Problem Solving(R1UC601B)

Here's a high-level overview of how it works:

- 1. **Preprocessing Step**: Compute a **prefix table (also known as failure function or pi array)** for the pattern. This table will be used to decide the next characters to match.
- 2. **Matching Step**: Slide the pattern over the text one character at a time. When a mismatch is found, use the prefix table to skip over characters that we know will anyway match.

The preprocessing step takes O(m) time, where m is the length of the pattern. The matching step takes O(n) time, where n is the length of the text. Therefore, the KMP algorithm has a time complexity of O(m + n).

The space complexity of the KMP algorithm is **O(m)**, as it requires storing the prefix table for the pattern.

```
function KMP(string s[1..n], string pattern[1..m])

Compute prefix table for pattern
i := 0; j := 0

while i < n

if s[i] = pattern[j]

i++; j++

if j = m

return i - j (match found)

else if j > 0

j := prefix[j-1] (use prefix table to skip characters)
else
i++

return not found
```

What is a sliding window? Where this technique is used to solve the programming problems.

ANS 4

9 What are bit manipulation operators? Explain and, or, not, ex-or bit-wise operators.

Bit manipulation operators are used to perform operations at the bit level. These operators are commonly used in low-level programming such as kernel or driver development, as well as in performance-critical code. Here's a brief explanation of the bit manipulation operators you asked about:

1. **AND (&)**: The bitwise AND operator takes two numbers as operands and does AND on every bit of two numbers. The result of AND is 1 only if both bits are 1.

For example, 12 (1100 in binary) & 10 (1010 in binary) will give 8 (1000 in binary).

2. **OR (|)**: The bitwise OR operator takes two numbers as operands and does OR on every bit of two numbers. The result of OR is 1 if any of the two bits is 1.

For example, 12 (1100 in binary) | 10 (1010 in binary) will give 14 (1110 in binary).

3. NOT (~): The bitwise NOT operator takes one number and inverts all bits of it.

For example, $^{\sim}12$ (which is 1100 in binary) will give -13 (which is 0011 in binary in 2's complement form).

4. **XOR (^)**: The bitwise XOR (exclusive OR) operator takes two numbers as operands and does XOR on every bit of two numbers. The result of XOR is 1 if the two bits are different.

For example, 12 (1100 in binary) ^ 10 (1010 in binary) will give 6 (0110 in binary).

Advanced Algorithmic Problem Solving(R1UC601B)

```
10
            Why are the benefits for linked list over arrays.
           benefits of linked lists over arrays:
               1. Dynamic Size: Unlike arrays, linked lists do not have a fixed size. This makes them flexible
                   for situations where the amount of data is not known in advance.
               2. Ease of Insertion/Deletion: Linked lists can insert or delete nodes at any point with O(1)
                   time complexity (if we have a pointer to the node), unlike arrays which require shifting
                   elements.
               3. Efficient Memory Utilization: Linked lists use memory more efficiently when elements
                   are frequently added and removed. In an array, all elements need to be moved to fill or
                   open up space, which can be costly in terms of time.
                   No Memory Wastage: In linked lists, nodes can be allocated as and when required, thus
                   reducing memory waste. In contrast, in arrays, we need to allocate memory beforehand.
               5. Implementation of Stacks and Queues: Linked lists are used to implement other abstract
                   data types like stacks and queues.
11
            Implement singly linked list.
            class Node:
              def __init__(self, data=None):
                 self.data = data
                 self.next = None
            class LinkedList:
              def __init__(self):
                 self.head = None
              def insert(self, data):
                 if not self.head:
                   self.head = Node(data)
                 else:
                   cur = self.head
                   while cur.next:
                      cur = cur.next
                   cur.next = Node(data)
              def display(self):
                 cur = self.head
                 while cur:
                   print(cur.data, end=' ')
                   cur = cur.next
                 print()
            # Usage
            11 = LinkedList()
            ll.insert(1)
            ll.insert(2)
            ll.insert(3)
            ll.display() # Outputs: 1 2 3
            Implement stack with singly linked list.
11
            class Node:
              def __init__(self, data=None):
                 self.data = data
                 self.next = None
            class Stack:
              def __init__(self):
                 self.top = None
              def push(self, data):
                 new node = Node(data)
```

 $new_node.next = self.top$

```
self.top = new\_node
              def pop(self):
                 if self.top is None:
                   return None
                   popped\_data = self.top.data
                   self.top = self.top.next
                   return popped_data
              def peek(self):
                 return self.top.data if self.top else None
            # Usage
            s = Stack()
            s.push(1)
            s.push(2)
            s.push(3)
            print(s.pop()) # Outputs: 3
            print(s.peek()) # Outputs: 2
            Implement queue with singly linked list.
12
            class Node:
              def init (self, data=None):
                self.data = data
                self.next = None
            class Queue:
              def init (self):
                self.front = self.rear = None
              def is_empty(self):
                return self.front is None
              def enqueue(self, data):
                new_node = Node(data)
                if self.rear is None:
                  self.front = self.rear = new_node
                self.rear.next = new_node
                self.rear = new_node
              def dequeue(self):
                if self.is empty():
                   return None
                temp = self.front
                self.front = temp.next
                if self.front is None:
                  self.rear = None
                return temp.data
            # Usage
            q = Queue()
            q.enqueue(1)
            q.enqueue(2)
            q.enqueue(3)
            print(q.dequeue()) # Outputs: 1
12
            Implement doubly linked list.
            class Node:
              def __init__(self, data=None):
                self.data = data
                self.next = None
```

```
self.prev = None
            class DoublyLinkedList:
              def __init__(self):
                self.head = None
              def append(self, data):
                if self.head is None:
                   self.head = Node(data)
                   new_node = Node(data)
                  cur = self.head
                   while cur.next:
                     cur = cur.next
                   cur.next = new_node
                   new_node.prev = cur
              def prepend(self, data):
                if self.head is None:
                   self.head = Node(data)
                else:
                   new_node = Node(data)
                   new node.next = self.head
                   self.head.prev = new node
                   self.head = new_node
              def print_list(self):
                cur = self.head
                while cur:
                   print(cur.data)
                   cur = cur.next
13
            Implement circular linked list.
            class Node:
              def __init__(self, data=None):
                 self.data = data
                 self.next = None
            class CircularLinkedList:
              def __init__(self):
                 self.head = None
              def append(self, data):
                 if not self.head:
                   self.head = Node(data)
                   self.head.next = self.head
                 else:
                   new\_node = Node(data)
                   cur = self.head
                   while cur.next != self.head:
                     cur = cur.next
                   cur.next = new node
                   new\_node.next = self.head
              def print_list(self):
                 cur = self.head
                 while True:
                   print(cur.data)
                   cur = cur.next
                   if cur == self.head:
                     break
14
            Implement circular queue with linked list.
```

Advanced Algorithmic Problem Solving (R1UC601B)

```
class Node:
  def __init__(self, data):
     self.data = data
     self.next = None
class CircularQueue:
  def init (self):
     self.front = self.rear = None
  def enqueue(self, data):
     temp = Node(data)
     if self.rear == None:
       self.front = self.rear = temp
       self.rear.next = self.front
     else:
       self.rear.next = temp
       self.rear = temp
       self.rear.next = self.front
  def dequeue(self):
     if self.front == None:
       print("Circular Queue is empty")
       return
     temp = self.front
     self.front = temp.next
     self.rear.next = self.front
     if self.front == self.rear:
       self.front = self.rear = None
  def display(self):
     temp = self.front
     while temp:
       print(temp.data, end=" ")
       temp = temp.next
       if temp == self.front:
          break
```

15 What is recursion? What is tail recursion?

Recursion is a process in which a function calls itself as a subroutine. This allows the function to be broken down into smaller, more manageable problems that are easier to solve1. It's a method of solving a computational problem where the solution depends on solutions to smaller instances of the same problem2. Recursion has some important properties1:

The ability to solve a problem by breaking it down into smaller sub-problems. A recursive function must have a base case or stopping criteria to avoid infinite recursion. Recursive functions may be less efficient than iterative solutions in terms of memory and performance.

Tail recursion is a special case of recursion where the recursive call is the last operation in the recursive function3. What this means is that all calculations are performed first, and the execution of the recursive call is the final operation3. This is important because it allows certain compilers to optimize the recursion, using a loop construct instead of a function call for the recursive step3. This can result in significant savings in both processing time and stack space3.

Here's an example of a tail-recursive function in Python:

Advanced Algorithmic Problem Solving(R1UC601B)

```
Python

def factorial(n, acc=1):
    if n == 0:
        return acc
    else:
        return factorial(n-1, n*acc)
```

In this example, factorial(n-1, n*acc) is the last operation in the recursive function, making it tail recursive. The acc parameter accumulates the result of the factorial calculation, which is returned when n reaches 0. This is the base case of the recursion. The advantage of this tail-recursive version is that it uses constant stack space and is more efficient.

What is the tower of Hanoi problem? Write a program to implement the Tower of Hanoi problem. Find the time and space complexity of the program.

The **Tower of Hanoi** problem is a classic problem in the field of computer science and mathematics. It consists of three rods and a number of disks of different sizes which can slide onto any rod. The puzzle starts with the disks in a neat stack in ascending order of size on one rod, the smallest at the top, thus making a conical shape.

The objective of the puzzle is to move the entire stack to another rod, obeying the following simple rules:

- 1. Only one disk can be moved at a time.
- 2. Each move consists of taking the upper disk from one of the stacks and placing it on top of another stack or on an empty rod.
- 3. No disk may be placed on top of a smaller disk.

```
def TowerOfHanoi(n , source, destination, auxiliary):
    if n==1:
        print("Move disk 1 from source", source, "to destination", destination)
        return
    TowerOfHanoi(n-1, source, auxiliary, destination)
    print("Move disk", n, "from source", source, "to destination", destination)
    TowerOfHanoi(n-1, auxiliary, destination, source)

# Driver code
n = 4
TowerOfHanoi(n, 'A', 'B', 'C')
# A. C. B are the name of rods
```

The **time complexity** of the Tower of Hanoi problem is **O(2^n)**, where n is the number of disks. This is because with each increase in the number of disks, the number of steps required to solve the problem doubles.

The **space complexity** of the Tower of Hanoi problem is **O(n)**, where n is the number of disks. This is due to the recursive nature of the problem, which results in n recursive calls, and thus n items in the call stack. Each recursive call requires a constant amount of space.

What is backtracking in algorithms? What kind of problems are solved with this technique?

Backtracking is a general algorithmic technique that involves finding a solution incrementally by trying different options and undoing them if they lead to a dead end1. It is commonly used in situations where you need to explore multiple possibilities to solve a problem, like searching for a path in a maze or solving puzzles like Sudoku1.

A backtracking algorithm works by recursively exploring all possible solutions to a problem. It

Advanced Algorithmic Problem Solving (R1UC601B)

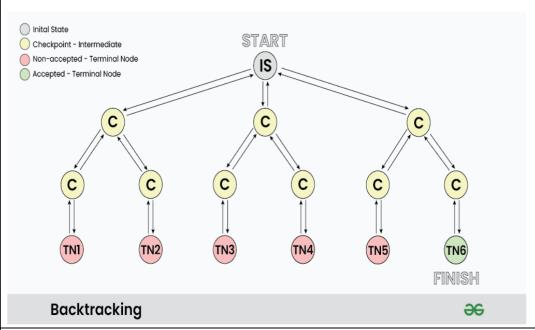
starts by choosing an initial solution, and then it explores all possible extensions of that solution. If an extension leads to a solution, the algorithm returns that solution. If an extension does not lead to a solution, the algorithm backtracks to the previous solution and tries a different extension1.

Backtracking can be applied to a wide range of problems. Here are some examples of problems that can be solved using backtracking:

Puzzles: Such as the N-Queens problem, Sudoku, and the Knight's tour problem12. Path Finding: Finding the shortest path through a maze or finding all paths from source to destination in a matrix12.

Combinatorial Problems: Generating all possible combinations of a set of items3.

Constraint Satisfaction Problems: Finding a specific solution that satisfies a set of constraints3. Remember, while backtracking can solve these problems, it may not always be the most efficient method, especially for problems with large input sizes or many potential solutions. Other techniques like dynamic programming might be more suitable in such cases4.



18 Implement N-Queens problem. Find the time and space complexity.

The N-Queens problem is a classic example of a problem that can be solved using backtracking. The problem is to place N queens on an N x N chessboard such that no two queens threaten each other. Thus, a solution requires that no two queens share the same row, column, or diagonal.

```
def isSafe(board, row, col, N):
    # Check this row on left side
    for i in range(col):
        if board[row][i] == 1:
            return False

# Check upper diagonal on left side
    for i, j in zip(range(row, -1, -1), range(col, -1, -1)):
        if board[i][j] == 1:
            return False

# Check lower diagonal on left side
    for i, j in zip(range(row, N, 1), range(col, -1, -1)):
        if board[i][j] == 1:
            return False

return True
```

def solveNQUtil(board, col, N):

```
# base case: If all queens are placed
  if col >= N:
     return True
  # Consider this column and try placing this queen in all rows one by one
  for i in range(N):
     if isSafe(board, i, col, N):
       # Place this queen in board[i][col]
       board[i][col] = 1
       # recur to place rest of the queens
       if solveNQUtil(board, col + 1, N):
          return True
       # If placing queen in board[i][col] doesn't lead to a solution, then remove queen from
board[i][col]
       board[i][col] = 0
  # If the queen cannot be placed in any row in this column col then return false
  return False
def solveNQ(N):
  board = [[0 \text{ for } \_ \text{ in } range(N)] \text{ for } \_ \text{ in } range(N)]
  if not solveNQUtil(board, 0, N):
     print("Solution does not exist")
     return False
  printSolution(board)
  return True
def printSolution(board):
  for i in range(N):
     for j in range(N):
       print(board[i][j], end = " ")
     print()
# Driver Code
N = 4
solveNQ(N)
```

- 1. def isSafe (board, row, col, N): This function checks if a queen can be placed at board[row][col]. It returns False if there's a queen in the same row or in the upper or lower diagonal. Otherwise, it returns True.
- 2. def solveNQUtil(board, col, N): This function is a recursive utility that solves the N-Queens problem. It returns False if queens cannot be placed, otherwise, it returns True and prints placements in the form of 1s. Please note that there may be more than one solutions, this function prints one of the feasible solutions.
- 3. def solveNQ(N): This function solves the N-Queens problem using solveNQUtil(). It mainly uses solveNQUtil() to solve the problem. It returns False if queens cannot be placed, otherwise, True and prints placements in the form of 1s.
- 4. def printSolution(board): This function prints the final solution. It prints the board matrix where the queens are placed.
- 5. N = 4 This is where you define the size of the board and the number of queens.
- 6. solveNQ(N) This is where the program starts. It calls the solveNQ function to solve the problem.

Advanced Algorithmic Problem Solving(R1UC601B)

What is subset sum problem? Write a recursive function to solve the subset sum problem?

The Subset Sum Problem is a classic computer science problem that falls under the category of NP-Complete problems. It is a decision problem that can be stated as follows:

Given a set of integers and an integer **S**, does any subset of the given set add up to **S**?

```
def is_subset_sum(set, n, sum):
  # Base Cases
  if sum == 0:
    return True
  if n == 0 and sum != 0:
    return False
  # If last element is greater than sum, then ignore it
  if set[n-1] > sum:
    return is_subset_sum(set, n-1, sum)
  # Else, check if sum can be obtained by any of the following:
  # (a) including the last element
  # (b) excluding the last element
  return is_subset_sum(set, n-1, sum) or is_subset_sum(set, n-1, sum-set[n-1])
# Test the function
set = [3, 34, 4, 12, 5, 2]
sum = 9
n = len(set)
if (is subset sum(set, n, sum) == True):
  print("Found a subset with given sum")
else:
  print("No subset with given sum")
```

Implement a function that uses the sliding window technique to find the maximum sum of any contiguous subarray of size K.

```
def max_sum_subarray_size_k(arr, k):
  window sum = 0
  max_sum = 0
  window_start = 0
  for window_end in range(len(arr)):
    window_sum += arr[window_end] # add the next element
    # slide the window, we don't need to slide if we've not hit the required window size of 'k'
    if window_end >= k-1:
       max_sum = max(max_sum, window_sum)
       window_sum -= arr[window_start] # subtract the element going out
       window_start += 1 # slide the window ahead
  return max_sum
# Test the function
arr = [2, 3, 4, 1, 5]
k = 3
print("Maximum sum of a subarray of size K: ", max_sum_subarray_size_k(arr, k))
```

```
21
          Write a recursive function to generate all possible subsets of a given set.
          def generate_subsets(s, current_subset=[], index=0):
             if index == len(s):
               print(current_subset)
             else:
               # Two possibilities for each element, it's either in the subset or not
               # First, we select the element to be in the subset
               generate_subsets(s, current_subset + [s[index]], index + 1)
               # Then, we do not select the element to be in the subset
               generate subsets(s, current subset, index + 1)
          # Test the function
          s = [1, 2, 3]
          generate_subsets(s)
22
          Write a program to find the first occurrence of repeating character in a given
          string.
          def first_repeating_char(s):
             char count = {}
             for char in s:
               if char in char_count:
                  return char
                else:
                  char_count[char] = 1
             return None
          # Test the function
          s = "interviewquery"
          print("The first repeating character is: ", first_repeating_char(s))
23
          Write a program to print all the LEADERS in the array. An element is a leader if
          it is greater than all the elements to its right side. And the rightmost element is
          always a leader.
          def print_leaders(arr):
             max_from_right = arr[-1] # The rightmost element is always a leader
             print(max_from_right, end=' ')
             for i in range(len(arr)-2, -1, -1):
                if max from right <= arr[i]: # If this element is greater than the max from
          right
                  print(arr[i], end=' ') # This element is a leader
                  max_from_right = arr[i] # Update the max from right
          # Test the function
          arr = [16, 17, 4, 3, 5, 2]
          print("Leaders in the array are: ", end=")
          print_leaders(arr)
24
          Write a program to find the majority element in the array. A majority element in
          an array A[] of size n is an element that appears more than n/2 times.
          def find_majority_element(arr):
             majority_element = 0
             count = 0
             # Boyer-Moore Voting Algorithm
             for i in range(len(arr)):
                if count == 0:
                  majority element = arr[i]
                if arr[i] == majority_element:
                  count += 1
```

```
else:
                  count -= 1
             # Verify if the majority_element appears more than n/2 times
             count = arr.count(majority_element)
             if count > len(arr) // 2:
                return majority_element
                return "No Majority Element"
          # Test the function
          arr = [2, 2, 1, 1, 1, 2, 2]
          print(find_majority_element(arr))
25
          Given an integer k and a queue of integers, write a program to reverse the order
          of the first k elements of the queue, leaving the other elements in the same
          relative order.
          from queue import Queue
          from collections import deque
          def reverse_first_k(queue, k):
             if queue.empty() or k > queue.qsize():
               return "Invalid input"
             stack = deque()
             for _ in range(k):
                stack.append(queue.get())
             while stack:
                queue.put(stack.pop())
             for _ in range(queue.qsize() - k):
                queue.put(queue.get())
             return queue
          # Test the function
          queue = Queue()
          for i in range(1, 11):
             queue.put(i)
          reverse_first_k(queue, 5)
          while not queue.empty():
             print(queue.get(), end=' ')
26
          Write a program to implement a stack using queues.
          class Stack:
            def __init__(self):
               self.q1 = []
               self.q2 = []
             def push(self, x):
               self.q1.append(x)
            def pop(self):
               if not self.q1:
                  return "Stack is empty"
               while len(self.q1) > 1:
                  self.q2.append(self.q1.pop(0))
               item = self.q1.pop()
               self.q1, self.q2 = self.q2, self.q1
               return item
```

```
# Test the Stack
           stack = Stack()
           stack.push(1)
           stack.push(2)
           stack.push(3)
           print(stack.pop()) # prints 3
           print(stack.pop()) # prints 2
27
            Wrire a program to implement queue using stacks.
           class Queue:
              def init (self):
                 self.s1 = []
                 self.s2 = []
              def enqueue(self, x):
                 self.s1.append(x)
              def dequeue(self):
                 if not self.s1 and not self.s2:
                    return "Queue is empty"
                 if not self.s2:
                    while self.s1:
                      self.s2.append(self.s1.pop())
                 return self.s2.pop()
           # Test the Queue
           queue = Queue()
           queue.enqueue(1)
           queue.enqueue(2)
           queue.enqueue(3)
           print(queue.dequeue()) # prints 1
           print(queue.dequeue()) # prints 2
28
            Given a string S of lowercase alphabets, write a program to check if string is
           isogram or not. An Isogram is a string in which no letter occurs more than once.
           def is_isogram(string):
              # Convert the string to lowercase for uniformity
              string = string.lower()
              # Create a set from the string. In a set, duplicate elements are not allowed.
              # So, if the length of the set is equal to the length of the string, it means all characters were unique.
              return len(string) == len(set(string))
           # Test the function
           print(is_isogram("subdermatoglyphic")) # This should return True
           print(is_isogram("hello")) # This should return False
29
            Given a sorted <u>array</u>, arr[] consisting of N integers, write a program to
           find the frequencies of each array element.
           def count frequencies(arr):
              # Initialize the count and the element
              count = 1
              element = arr[0]
              # Iterate over the array
              for i in range(1, len(arr)):
                 # If the current element is the same as the previous one, increment the
           count
                 if arr[i] == element:
                    count += 1
                 else:
                    # Print the element and its frequency
                    print(f"Element {element} occurs {count} times")
```

```
# Update the element and reset the count
                   element = arr[i]
                   count = 1
              # Print the last element and its frequency
              print(f"Element {element} occurs {count} times")
           # Test the function
           arr = [1, 1, 2, 2, 2, 3, 4, 4, 4, 4]
           count_frequencies(arr)
30
           Write a program to delete middle element from stack.
           def delete middle(stack, n, curr=0):
              # Base case: If stack is empty or all items are traversed
              if not stack or curr == n:
                return
              # Remove current item
              temp = stack.pop()
              # Remove remaining items
              delete_middle(stack, n, curr+1)
             # Put all items back except middle
             if curr != n//2:
                stack.append(temp)
           # Test the function
           stack = [1, 2, 3, 4, 5]
           delete_middle(stack, len(stack))
           print(stack) # This should print [1, 2, 4, 5]
31
           Write a program to remove consecutive duplicates from string.
           def remove_consecutive_duplicates(s):
              # Initialize the result
              result = ""
              # Iterate over the string
              for i in range(len(s)):
                # If the current character is not the same as the previous one, add it to the result
                if i == 0 or s[i] != s[i-1]:
                   result += s[i]
              return result
           # Test the function
           print(remove_consecutive_duplicates("aaabbbccdaaa")) # This should print "abcda"
33
           Write a program to display next greater element of all element given in array.
           def print_next_greater(arr):
             stack = []
             for i in range(len(arr)):
                while stack and stack[-1] < arr[i]:
                   print(f"Next greater element for {stack.pop()} is {arr[i]}")
                stack.append(arr[i])
              while stack:
                print(f"Next greater element for {stack.pop()} is -1")
           # Test the function
           arr = [4, 5, 2, 25]
           print_next_greater(arr)
```

```
34
           Write a program to evaluate a postfix expression.
           def evaluate_postfix(expression):
             stack = []
             for char in expression:
                if char.isdigit():
                   stack.append(int(char))
                   operand2 = stack.pop()
                   operand1 = stack.pop()
                   if char == '+':
                     result = operand1 + operand2
                   elif char == '-':
                     result = operand1 - operand2
                   elif char == '*':
                     result = operand1 * operand2
                   elif char == '/':
result = operand1 / operand2
                   stack.append(result)
             return stack[0]
           # Test the function
           expression = "231*+9-"
           print(evaluate_postfix(expression))
```

```
35
           Write a program to get MIN at pop from stack.
           class MinStack:
              def __init__(self):
                self.stack = []
                self.min_stack = []
              def push(self, x):
                self.stack.append(x)
                if not self.min_stack or x <= self.min_stack[-1]:
                   self.min stack.append(x)
              def pop(self):
                if self.stack:
                   top = self.stack.pop()
                   if self.min_stack and self.min_stack[-1] == top:
                      self.min_stack.pop()
                   return top
              def get_min(self):
                return self.min_stack[-1] if self.min_stack else None
           # Test the MinStack
           min stack = MinStack()
           min_stack.push(3)
           min_stack.push(5)
           print(min_stack.get_min()) # prints 3
           print(min_stack.pop()) # prints 5
           print(min_stack.get_min()) # prints 3
36
           Write a program to swap kth node from ends in given single linked list.
           class Node:
             def __init__(self, data):
               self.data = data
               self.next = None
           class LinkedList:
             def __init__(self):
               self.head = None
             def push(self, data):
                new node = Node(data)
               new node.next = self.head
               self.head = new_node
             def print_list(self):
               node = self.head
               while node:
                  print(node.data, end=" ")
                  node = node.next
               print()
             def swap_kth_node(self, k):
               n = 0
               node = self.head
               while node:
                 n += 1
                  node = node.next
               if n < k:
                  return
               x = self.head
               x_prev = None
```

```
for i in range(k - 1):
                  x_prev = x
                  x = x.next
                y = self.head
                y_prev = None
                for i in range(n - k):
                  y_prev = y
                  y = y.next
                if x_prev:
                  x prev.next = y
                  self.head = y
                if y_prev:
                  y_prev.next = x
                else:
                  self.head = x
                temp = x.next
                x.next = y.next
                y.next = temp
           # Test the LinkedList
           llist = LinkedList()
           for i in range(8, 0, -1):
              llist.push(i)
           print("Original linked list:")
           llist.print list()
           llist.swap_kth_node(3)
           print("Linked list after swapping 3rd node from both ends:")
           llist.print_list()
37
           Write a program to detect loop in linked list
           class Node:
              def __init__(self, data):
                 self.data = data
                 self.next = None
           class LinkedList:
              def __init__(self):
                 self.head = None
              def push(self, data):
                 new_node = Node(data)
                 new_node.next = self.head
                 self.head = new_node
              def detect_loop(self):
                 slow_p = self.head
                 fast_p = self.head
                 while slow_p and fast_p and fast_p.next:
                    slow_p = slow_p.next
                    fast_p = fast_p.next.next
                    if slow p == fast p:
                      return True
                 return False
           # Test the LinkedList
           llist = LinkedList()
           for i in range(5, 0, -1):
```

```
llist.push(i)
           # Create a loop for testing
           llist.head.next.next.next.next.next = llist.head.next.next
           print("Loop detected:" if llist.detect_loop() else "No loop detected")
38
           Write a program to find Intersection point in Y shaped Linked list.
           class Node:
             def init (self, data):
               self.data = data
               self.next = None
           def getIntersectionNode(head1, head2):
             curr1 = head1
             curr2 = head2
             # Traverse through both lists. If one list ends, start at the beginning of the other list.
              # If there is an intersection, the pointers should meet at the intersection point after 2
           traversals.
             while curr1 != curr2:
               curr1 = curr1.next if curr1 else head2
                curr2 = curr2.next if curr2 else head1
              return curr1.data # Return the intersection node
           # Test the function with an example
           # Create a Y shaped linked list
           head1 = Node(3)
           head1.next = Node(6)
           head1.next.next = Node(9)
           head1.next.next.next = Node(15)
           head1.next.next.next.next = Node(30)
           head2 = Node(10)
           head2.next = head1.next.next.next # Intersection point
           print("Intersection point is", getIntersectionNode(head1, head2))
39
           Write a program to merge two sorted linked list.
           class Node:
              def __init__(self, data):
                self.data = data
                 self.next = None
           def mergeLists(head1, head2):
              # A dummy node to store the result
              dummyNode = Node(0)
              # last stores the last node
              last = dummyNode
              while True:
                 # If either list runs out, use the other list
                 if head1 is None:
                   last.next = head2
                   break
                 if head2 is None:
                   last.next = head1
                   break
                 # Compare the data of the lists and whichever is smaller is appended to the last's
           next and the head is changed
```

```
if head1.data <= head2.data:
                  last.next = head1
                  head1 = head1.next
               else:
                  last.next = head2
                  head2 = head2.next
               # Update the last for next insertion
               last = last.next
             # Returns the head of the merged list
             return dummyNode.next
          # Test the function with an example
          # Create two sorted linked lists
          head1 = Node(1)
          head1.next = Node(2)
          head1.next.next = Node(4)
          head2 = Node(1)
          head2.next = Node(3)
          head2.next.next = Node(4)
          merged_head = mergeLists(head1, head2)
          # Print the merged list
          while merged_head is not None:
             print(merged head.data, end=" ")
             merged head = merged head.next
40
          Write a program to find max and second max of array.
          def find_max_and_second_max(arr):
             if len(arr) < 2:
               return "Invalid input. Array should have at least two elements."
             max1 = max2 = float('-inf')
             for num in arr:
               if num > max1:
                 max2 = max1
                  max1 = num
               elif num > max2 and num != max1:
                  max2 = num
             if max2 == float('-inf'):
               return "No second max value, all elements are the same."
             else:
               return max1, max2
          # Test the function with an example
          arr = [2, 3, 6, 6, 5]
          print("Max and second max of array:", find_max_and_second_max(arr))
41
          Write a program to find Smallest Positive missing number. You are given an
          array arr[] of N integers. The task is to find the smallest positive number missing
          from the array. Positive number starts from 1.
          def find_smallest_missing_positive(arr):
             if not arr:
               return 1
             arr = set(arr)
             smallest_positive = 1
             while smallest_positive in arr:
```

```
smallest positive += 1
             return smallest_positive
           # Test the function with an example
           arr = [0, 10, 2, -10, -20, 1, 3]
           print("Smallest positive missing number:", find_smallest_missing_positive(arr))
           Given a non-negative integer N. The task is to check if N is a power of 2. More
42
           formally, check if N can be expressed as 2x for some integer x. Return true if N
           is power of 2 else return false.
           def is_power_of_two(n):
             if n \le 0:
                return False
                return (n & (n - 1)) == 0
           # Test the function with an example
           print("Is", n, "a power of 2?", is_power_of_two(n))
             1. If n is less than or equal to 0: The function returns False. This is because powers
                  of 2 are always positive and non-zero.
             2. If n is greater than 0: The function checks if n AND n-1 is equal to 0. This is a
                  bitwise operation.
                         The bitwise AND operation (&) compares each bit of the first operand (n)
                          to the corresponding bit of the second operand (n-1). If both bits are 1,
                          the corresponding result bit is set to 1. Otherwise, the corresponding
                          result bit is set to 0.
                      o For numbers that are powers of 2, their binary representation has a single
                          '1' bit and the rest are '0'. For example, 2 is 10 in binary and 4 is 100 in
                          binary.
                         When you subtract 1 from these numbers, you get a binary number with
                          the '1' bit turned to '0' and all bits to the right of it turned to '1'. For
                          example, 2-1 is 1 which is 01 in binary and 4-1 is 3 which is 011 in
                          binary.
                         So, when you perform a bitwise AND operation between a power of 2 and
                          one less than it, you get 0 because there are no positions where both
                          numbers have a '1' bit.
                      o Therefore, (n \& (n - 1)) == 0 is a quick way to check if a number is
                          a power of 2.
43
           Write a program to Count Total Digits in a Number using recursion. You are
           given a number n. You need to find the count of digits in n.
           def count_digits(n):
             if n == 0:
                return 0
             return 1 + count_digits(n // 10)
           # Test the function with an example
           n = 12345
           print("The number of digits in", n, "is", count_digits(n))
44
           Check whether K-th bit is set or not. Given a number N and a bit number K,
           check if Kth index bit of N is set or not. A bit is called set if it is 1. Position of set
           bit '1' should be indexed starting with 0 from LSB side in binary representation
           of the number. Index is starting from 0. You just need to return true or false.
```

```
def is_kth_bit_set(n, k):
             if n & (1 << k):
                return True
             else:
                return False
           # Test the function with an example
           n = 5 # binary: 101
           print("Is the", k, "th bit of", n, "set?", is_kth_bit_set(n, k))
45
           Write a program to print 1 To N without loop
           def print_numbers(n):
             if n > 0:
                print_numbers(n - 1)
                print(n)
           # Test the function with an example
           N = 10
           print("Printing numbers from 1 to", N)
           print_numbers(N)
```