



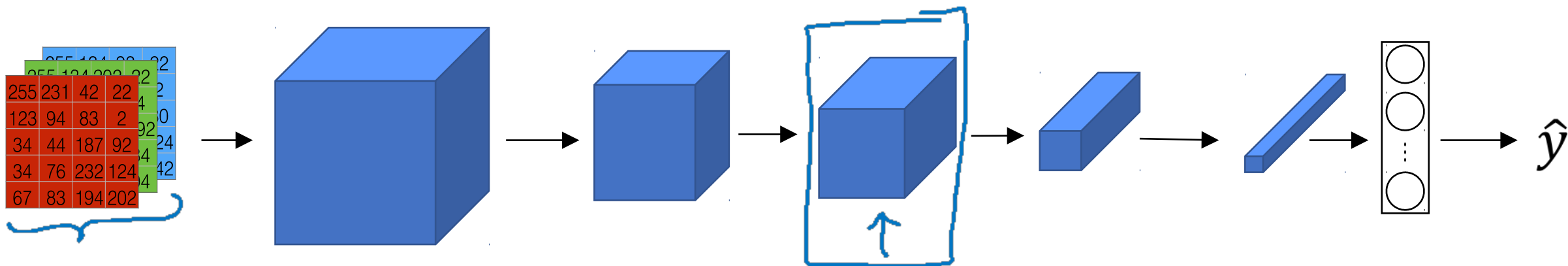
**deeplearning.ai**

# Neural Style Transfer

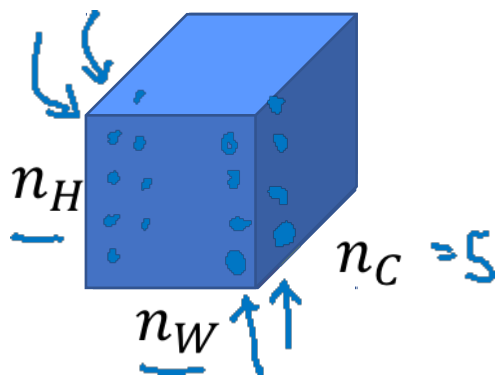
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Style cost  
function

# Meaning of the “style” of an image



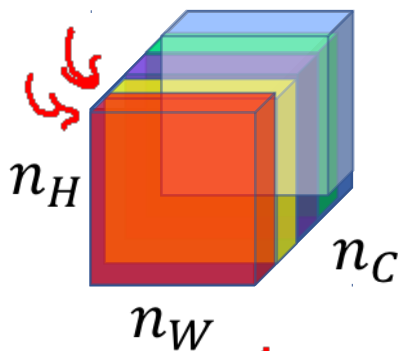
Say you are using layer's activation to measure “style.”  
Define style as correlation between activations across channels.



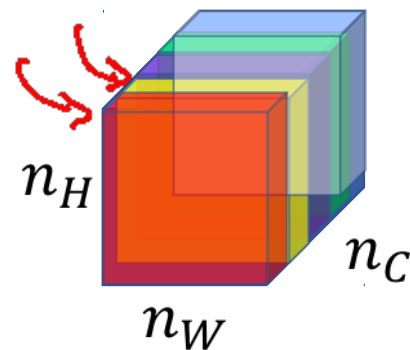
How correlated are the activations  
across different channels?

# Intuition about style of an image

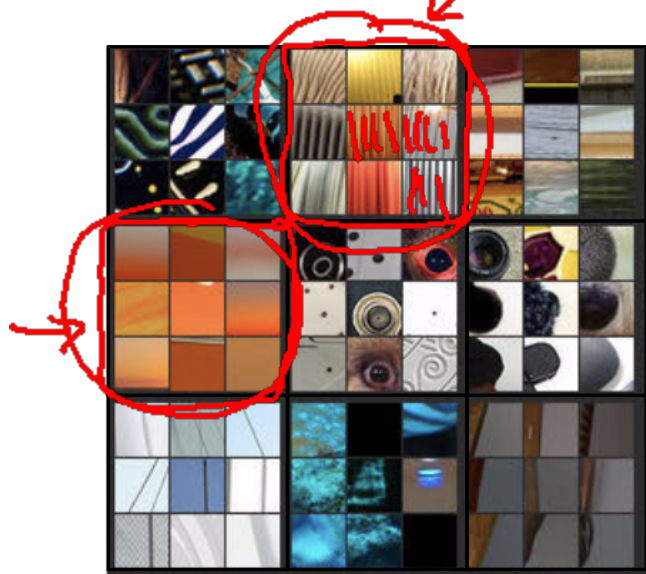
Style image



Generated Image



Correlated?  
Uncorrelated



# Style matrix

Let  $a_{i,j,k}^{[l]}$  = activation at  $G$  is  $n_c^{[l]} \times n_c^{[l]}$

H W C  
↓ ↓ ↙

$n_c$   
 $G_{kk'}^{[l]}$   
↑ ↑  
 $k = 1, \dots, n_c$

$$\begin{aligned} \rightarrow G_{kk'}^{[l](S)} &= \sum_{i=1}^{n_H^{[l]}} \sum_{j=1}^{n_W^{[l]}} a_{ijk}^{[l](S)} a_{ijk'}^{[l](S)} \\ \rightarrow G_{kk'}^{[l](G)} &= \sum_{i=1}^{n_H^{[l]}} \sum_{j=1}^{n_W^{[l]}} a_{ijk}^{[l](G)} a_{ijk}^{[l](G)} \end{aligned}$$

"Gram matrix"

$$\begin{aligned} \beta \uparrow J_{\text{style}}^{[l]}(S, G) &= \frac{1}{(\dots)} \|G^{[l](S)} - G^{[l](G)}\|_F^2 \\ &= \frac{1}{(2n_H^{[l]}n_W^{[l]}n_c^{[l]})^2} \sum_k \sum_{k'} (G_{kk'}^{[l](S)} - G_{kk'}^{[l](G)})^2 \end{aligned}$$

# Style cost function

$$\|G^{[l](S)} - G^{[l](G)}\|_F^2$$

$$J_{style}^{[l]}(S, G) = \frac{1}{\left(2n_H^{[l]}n_W^{[l]}n_C^{[l]}\right)^2} \sum_k \sum_{k'} (G_{kk'}^{[l](S)} - G_{kk'}^{[l](G)})^2$$

$$J_{style}(S, G) = \sum_l \lambda_l J_{style}^{[l]}(S, G)$$

$$\underbrace{J(G)}_G = \alpha J_{content}(G) + \beta J_{style}(S, G)$$