### **DATA STRUCTURES**

Неар

Ву

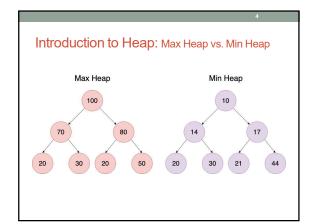
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- · Introduction to Heap
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- · Priority Queue
- · Heap Sort

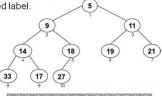
### Introduction to Heap

- · A heap is binary tree that satisfies the following properties
- · Shape property: Heap must be a complete binary tree
- · Order property: It must be either Max heap or Min heap
- Max hear
- For every node in the heap, the value stored in that node is greater than or equal to the value in each of its children
- Min heap
- For every node in the heap, the value stored in that node is less than or equal to the value in each of its children



### Heap Representation

- Heap is a Complete Binary Tree. This property of Binary Heap makes it suitable to be stored in a linear array.
- Each node is assigned a numeric label and a node is stored in an array at a position with same index as its associated label.



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### Operations on Heaps

- ${\scriptstyle \bullet}$  On heaps, only two operations are performed
- Insertion
- Deletion

### Heap Operation: Insertion(item)

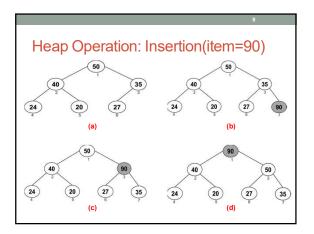
- Item is always inserted as last (bottom) child of the original heap.
- After insertion, shape property remain undisturbed, but the order may get violated if a larger item (incase of Max Heap) or smaller item (incase of Min Heap) is inserted.
- To satisfy the order property, heap needs to be readjusted in terms of its structure (reheapifyUpward)
- · ReheapifyUpward:
- It involves moving the items up from the last (bottom) position until either it ends up in a position where the order property satisfied or it hits the root node.

### Heap Operation: Insertion(item)

- Insert(item,n,heap):
- 1. Set n=n+1
- Set heap[n]=item
- 3. Call reheapifyUpward(heap n)
- 4. Return
- ReheapifyUpward(heap, start)
- If heap[start] is not a root node then
- If(heap[parent]<=heap[start]) then
- Set index = index of the child with largest value
   Swap heap[parent] and heap[index]
- 5. Call repheapifyUpward(heap, parent)

Endif Endif

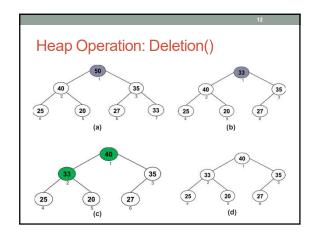
5. Return



### Heap Operation: Deletion()

- · Element is always deleted from the root of the heap
- When the element is deleted from the root, it creates a vacant space in the root position
- As heap must be a complete binary tree, so the vacant space is filled by last (bottom right) element of the heap
- Like insertion, this replacement ensures the shape property but disturbs the order property that needs to be satisfied by mean of reheapify (reheapifyDownward).
- · reheapifyDownward:
  - It involves moving the element down from the root position until either it ends up in a position where order property is satisfied or it hits the leaf node.

## Heap Operation: Deletion() Delete(n,heap): Set item=heap[root] Set heap[root]=heap[n] Set n=n-1 Call reheapifyDownward(heap,root) Return item ReheapifyDownward(heap, start) If heap[start] is not a leaf node then Set index = index of the child with largest value If(heap[start]<=heap[index)] then Swap heap[index] and heap[start] Call repheapifyDownward(heap, index) Endif Endif Return



### Applications of Heap • Priority Queue • Heap Sort

### Priority Queue using Heap

- Each Node in a heap have two types of information i.e. the content and an associated priority
- Heap is build with respect to priority which means that the element with highest priority will be at root node.
- As in heap we always delete from the root therefore, whenever a node will be removed for processing it will be of highest priority

Priority Heap Operation: Insertion(item)

Insert(item,n,heap)://item must be an object of Element containing both content and priority

Set n=n+1

Set n=n+1

Set heap[n]=item
Call reheapifyUpward(heap n)
Return

ReheapifyUpward(heap, start)
If heap[start] is not a root node then
If(heap[parent].priority:=heap[start].priority) then
Set index = index of the child with largest priority value
Swap heap[parent] and heap[index]
Call repheapifyUpward(heap, parent)
Endif
Endif
S. Return

Priority Heap Operation: Deletion()

Delete(n,heap):
Set item=heap[root]
Set heap[root]=heap[n]
Set n=n-1
Call reheapifyDownward(heap,root)
Return item

ReheapifyDownward(heap, start)
If heap[start] is not a leaf node then
Set index = index of the child with largest priority value
If(heap[start], priority<=heap[index], priority) then
Swap heap[index] and heap[start]
Call repheapifyDownward(heap, index)
Endif
Endif
Return

Applications of Heap

Priority Queue
Heap Sort

# Heap Sort HeapSort(a,n) //a is a linear array and n is the last element of a Heapify(a, n) Repeat Step 3 and 4 For i=n to 1 in steps of -1 Swap elements a[1] with a[i] Call ReheapifyDownward(a,1) (see slide # 11) Endfor Return Heapify(a,n) Set index=Parent of node with index n Repeat step 3 For i=index to 1 in setp of -1 Call reheapifyDownward(a,i) (see slide # 8) Endif Return

