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- MODULE actor -
EXTENDS TLC, Integers, Sequences
between 01 (n1, \ nb, \ n2) \ \stackrel{\Delta}{=} \ (nb \ge 0) \land (((n1 < n2) \land ((n1 < nb) \land (nb \le n2))) \lor ((n1 \ge n2) \land ((n1 < nb) \lor (nb \le n2))) \lor ((n1 \ge n2) \land ((n1 < nb) \lor (nb \le n2))) \lor ((n1 \ge n2) \land ((n1 < nb) \lor (nb \le n2))) \lor ((n1 \ge n2) \land ((n1 < nb) \lor (nb \le n2))) \lor ((n1 \le n2) \land ((n1 \le n2) 
between 00 (n1, \ nb, \ n2) \ \stackrel{\triangle}{=} \ (nb \ge 0) \land (((n1 < n2) \land ((n1 < nb) \land (nb < n2))) \lor ((n1 \ge n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \land ((n1 < nb) \lor (nb < n2))) \lor ((n1 \le n2) \lor ((n1 < n2) \lor (nb < n2))) \lor ((n1 \le n2) \lor ((n1 < n2) \lor (nb < n2))) \lor ((n1 \le n2) \lor ((n1 < n2) \lor (nb < n2))) \lor ((n1 \le n2) \lor ((n1 < n2) \lor (nb < n2))) \lor ((n1 \le n2) \lor ((n1 < n2) \lor (nb < n2))) \lor ((n1 \le n2) \lor ((n1 < n2) \lor ((n1 < n2) \lor (nb < n2)))) \lor ((n1 < n2) 
fingerStart(myId, k, m) \stackrel{\Delta}{=} (myId + (2^{(k-1)}))\%m
Constants m, bm, NULL
         --fair algorithm ActorStuff {
 variables actorInboxes = (0:> \langle \rangle) @@ (1:> \langle \rangle) @@ (3:> \langle \rangle);
                                                           triggered = FALSE;
                                                               make local
                                                         fingerTables = (0:> ((1:> 0) @@ (2:> 0) @@ (4:> 0)))
                                                            @@(1:>((2:>NULL)@@(3:>NULL)@@(5:>NULL)))
                                                           @@ (3:>((4:>NULL)) @@ (5:>NULL) @@ (7:>NULL)));
                                                          predecessors = (0:> 0) @@ (1:> NULL) @@ (3:> NULL);
fair process ( actor \in \{0, 1, 3\} )
 variables currentMessage = \langle "?", NULL, NULL \rangle;
          kind = "?";
          id = NULL;
          i;
          joined = FALSE;
          Join:+
                   if ( self = 0 ) {
                                         joined := TRUE;
                         } else {
                                                    actorInboxes[0] := Append(actorInboxes[0], \langle \text{"FindPredecessor"}, fingerStart(self, 1, bm), self \rangle);
            WaitFor Messages Before Join:+\\
                   if ( joined \neq TRUE ) {
                                          await actorInboxes[self] \neq \langle \rangle;
                                                currentMessage := Head(actorInboxes[self]);
                                                kind := Head(currentMessage);
                                                actorInboxes[self] := Tail(actorInboxes[self]);
                                               };
                                           ProcessMessageBeforeJoin:+
                                                              if ( kind = "Predecessor" ) {
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fingerTables[self][fingerStart(self, 1, bm)] := currentMessage[3];

predecessors[self] := currentMessage[2];

joined := TRUE;

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};
                 ReturnDefaultsBeforeJoin:+ {
                   currentMessage := \langle "?", NULL, NULL \rangle;
                   kind := "?";
                   id := NULL;
                      };
       } ;
Stabilize:+
    if ( joined ) {
                 actorInboxes[self] := Append(actorInboxes[self], \langle "Stabilize", 1 \rangle);
WaitFor Messages \colon\!\!\!+
    if ( joined )
     {
         await actorInboxes[self] \neq \langle \rangle;
                  currentMessage := Head(actorInboxes[self]);
                 kind := Head(currentMessage);
                  actorInboxes[self] := Tail(actorInboxes[self]);
                 };
                ProcessMessage:+
               {
                 if ( kind = \text{``FindPredecessor''} ) {
                              id := currentMessage[2];
                     await fingerTables[self][fingerStart(self, 1, bm)] \neq NULL;
                 if ( between 01 (self, id, finger Tables [self] [finger Start (self, 1, bm)]) ) {
                              actorInboxes[currentMessage[3]] :=
                              Append(actorInboxes[currentMessage[3]], \ ("Predecessor", self, fingerTables[self][fingerStart(self, fingerTables[self])] | Append(actorInboxes[self]) | Append(acto
                    } else {
                               i := m;
                                  await fingerTables[self] \neq NULL;
                                FindFirstSuitableI:
                               while (i > 0 \land \neg(fingerStart(self, i, bm) \in DOMAIN fingerTables[self])) {
                                       i := i - 1;
                                  };
                                   await fingerTables[self][fingerStart(self, i, bm)] \neq NULL;
                                MainLoop:
                                while ( i > 0 \land \neg(between 00(self, fingerTables[self][fingerStart(self, i, bm)], id)) ) {
                                          i := i - 1;
                                          Find Suitable I\colon
                                          while (i > 0 \land \neg(fingerStart(self, i, bm) \in DOMAIN fingerTables[self])) {
                                                     i := i - 1;
                                            };
```

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if ( i = 0 ) {
          actorInboxes[fingerTables[self][fingerStart(self, m, bm)]] :=
          Append(actorInboxes[fingerTables[self][fingerStart(self, m, bm)]], currentMessage);
      } else {
            actorInboxes[fingerTables[self][fingerStart(self, i, bm)]] :=
            Append(actorInboxes[fingerTables[self][fingerStart(self, i, bm)]], currentMessage);
      };
 };
 } else {
      {
         if ( kind =  "Stabilize" ) {
            actorInboxes[fingerTables[self][fingerStart(self, currentMessage[2], bm)]] :=
            Append(actorInboxes[fingerTables[self][fingerStart(self, currentMessage[2], bm)]], \langle \text{``GetPr}|
          } else {
              if (kind = "GetPredecessor") {
                   actorInboxes[currentMessage[2]] :=
                   Append(actorInboxes[currentMessage[2]], \langle "GotPredecessor", predecessors[self] \rangle);
               } else {
                    if (kind = "GotPredecessor") {
                      if (between 00 (current Message [2], finger Tables [self] [finger Start (self, 1, bm)], self
                           fingerTables[self][fingerStart(self, 1, bm)] := currentMessage[2];
                       actorInboxes[fingerTables[self][fingerStart(self, 1, bm)]] :=
                       Append(actorInboxes[fingerTables[self][fingerStart(self, 1, bm)]], \langle "Notify", self \rangle
                     } else {
                         if ( kind = "Notify" ) {
                             if ( predecessors[self] \neq NULL ) {
                                if ( between 00 (current Message [2], self, predecessors [self]) ) {
                                     predecessors[self] := currentMessage[2];
                                 };
                        };
                    }
              }
         }
      }
};
};
ReturnDefaults:+ \{
currentMessage := \langle "?", NULL, NULL \rangle;
kind := "?";
id := NULL;
 };
};
```

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} ;
 BEGIN TRANSLATION (chksum(pcal) = "e76f72bb" \land chksum(tla) = "6a8eed9d")
CONSTANT defaultInitValue
VARIABLES actorInboxes, triggered, fingerTables, predecessors, pc,
              currentMessage, kind, id, i, joined
vars \triangleq \langle actorInboxes, triggered, fingerTables, predecessors, pc, \rangle
           currentMessage, kind, id, i, joined⟩
ProcSet \stackrel{\triangle}{=} (\{0, 1, 3\})
Init \stackrel{\triangle}{=} Global variables
          \land actorInboxes = (0:> \langle \rangle) @@ (1:> \langle \rangle) @@ (3:> \langle \rangle)
          \land triggered = FALSE
                                                 (0:>((1:>0)@@(2:>0)@@(4:>0)))
          \land fingerTables =
                              @@ (1:> ((2:> NULL) @@ (3:> NULL) @@ (5:> NULL)))
                              @@(3:>((4:>NULL)@@(5:>NULL)@@(7:>NULL)))
          \land predecessors = (0:>0) @@ (1:> NULL) @@ (3:> NULL)
           Process actor
          \land currentMessage = [self \in \{0, 1, 3\} \mapsto \langle "?", NULL, NULL \rangle]
          \land kind = [self \in \{0, 1, 3\} \mapsto "?"]
          \wedge id = [self \in \{0, 1, 3\} \mapsto NULL]
          \land i = [self \in \{0, 1, 3\} \mapsto defaultInitValue]
          \land joined = [self \in \{0, 1, 3\} \mapsto FALSE]
          \land pc = [self \in ProcSet \mapsto "Join"]
Join(self) \stackrel{\triangle}{=} \land pc[self] = "Join"
                  \wedge IF self = 0
                        THEN \land joined' = [joined \ EXCEPT \ ![self] = TRUE]
                                 \land UNCHANGED actorInboxes
                         ELSE \land actorInboxes' = [actorInboxes \ EXCEPT \ ![0] = Append(actorInboxes[0], \langle "FindPre
                                 \land UNCHANGED joined
                  \land pc' = [pc \ EXCEPT \ ![self] = "WaitForMessagesBeforeJoin"]
                  \land UNCHANGED \langle triggered, fingerTables, predecessors,
                                      currentMessage, kind, id, i\rangle
WaitForMessagesBeforeJoin(self) \stackrel{\Delta}{=} \land pc[self] = \text{``WaitForMessagesBeforeJoin''}
                                               \land IF joined[self] \neq TRUE
                                                      THEN \land actorInboxes[self] \neq \langle \rangle
                                                              \land currentMessage' = [currentMessage \ Except \ ![self] = H
                                                              \land kind' = [kind \ EXCEPT \ ![self] = Head(currentMessage']self)
                                                              \land actorInboxes' = [actorInboxes \ EXCEPT \ ![self] = Tail(actorInboxes')
                                                              \land pc' = [pc \ \text{EXCEPT} \ ![self] = "ProcessMessageBeforeJoin"]
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ELSE $\land pc' = [pc \text{ EXCEPT } ! [self] = \text{"Stabilize"}]$

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\land UNCHANGED \langle actorInboxes,
                                                                                                                                                                  current Message,
                                                                                                                                                                  kind
                                                                                            \land UNCHANGED \langle triggered, fingerTables,
                                                                                                                                    predecessors, id, i, joined \rangle
ProcessMessageBeforeJoin(self) \stackrel{\Delta}{=} \land pc[self] = "ProcessMessageBeforeJoin"
                                                                                        \land IF kind[self] = "Predecessor"
                                                                                                     THEN \land predecessors' = [predecessors except ![self] = currentMes
                                                                                                                      \land fingerTables' = [fingerTables EXCEPT ![self]]fingerStart(set
                                                                                                                      \land joined' = [joined \ EXCEPT \ ![self] = TRUE]
                                                                                                     ELSE \land TRUE
                                                                                                                      \land UNCHANGED \langle finger Tables,
                                                                                                                                                            predecessors,
                                                                                                                                                             joined
                                                                                        \land pc' = [pc \ \text{EXCEPT} \ ![self] = "ReturnDefaultsBeforeJoin"]
                                                                                        \land UNCHANGED \langle actorInboxes, triggered,
                                                                                                                               currentMessage, kind, id, i\rangle
ReturnDefaultsBeforeJoin(self) \stackrel{\Delta}{=} \land pc[self] = "ReturnDefaultsBeforeJoin"
                                                                                        \land currentMessage' = [currentMessage \ Except \ ![self] = \langle "?", \ NULL, \ NU
                                                                                        \wedge kind' = [kind \text{ EXCEPT } ![self] = "?"]
                                                                                        \wedge id' = [id \text{ EXCEPT } ![self] = NULL]
                                                                                        \land pc' = [pc \text{ EXCEPT } ! [self] = \text{"Stabilize"}]
                                                                                        \land UNCHANGED \langle actorInboxes, triggered,
                                                                                                                               fingerTables, predecessors,
                                                                                                                               i, joined \rangle
Stabilize(self) \triangleq \land pc[self] = "Stabilize"
                                            \land IF joined[self]
                                                          THEN \land actorInboxes' = [actorInboxes \ EXCEPT \ ![self] = Append(actorInboxes[self], elements)
                                                           ELSE ∧ TRUE
                                                                          \land UNCHANGED actorInboxes
                                            \land pc' = [pc \ \texttt{EXCEPT} \ ![self] = "WaitForMessages"]
                                            \land UNCHANGED \langle triggered, fingerTables, predecessors,
                                                                                    currentMessage, kind, id, i, joined
WaitForMessages(self) \triangleq \land pc[self] = \text{``WaitForMessages''}
                                                                   \land IF joined[self]
                                                                                THEN \land actorInboxes[self] \neq \langle \rangle
                                                                                                 \land currentMessage' = [currentMessage \ Except \ ![self] = Head(actorIntMessage)]
                                                                                                 \land kind' = [kind \ EXCEPT \ ![self] = Head(currentMessage'[self])]
                                                                                                 \land actorInboxes' = [actorInboxes \ EXCEPT \ ! [self] = Tail(actorInboxes[self])
                                                                                                 \land pc' = [pc \text{ EXCEPT } ![self] = \text{"ProcessMessage"}]
                                                                                ELSE \land pc' = [pc \text{ EXCEPT } ![self] = \text{"Done"}]
                                                                                                 \land UNCHANGED \langle actorInboxes,
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currentMessage, kind \rangle
                                  \land UNCHANGED \langle triggered, fingerTables, predecessors,
                                                      id, i, joined
ProcessMessage(self) \triangleq \land pc[self] = "ProcessMessage"
                               \land IF kind[self] = "FindPredecessor"
                                      THEN \wedge id' = [id \text{ EXCEPT } ! [self] = currentMessage[self][2]]
                                               \land IF between01(self, id'[self], fingerTables[self][fingerStart(self, 1, bm)]
                                                     THEN \land actorInboxes' = [actorInboxes \ EXCEPT \ ! [currentMessage]]
                                                              \land pc' = [pc \text{ EXCEPT } ! [self] = \text{``ReturnDefaults''}]
                                                              \wedge i' = i
                                                     ELSE \wedge i' = [i \text{ EXCEPT } ! [self] = m]
                                                             \land pc' = [pc \ \text{EXCEPT} \ ![self] = \text{"FindFirstSuitablel"}]
                                                              \land \ \mathtt{UNCHANGED} \ \ actor Inboxes
                                               \land UNCHANGED \langle fingerTables, predecessors \rangle
                                      ELSE \wedge IF kind[self] = "Stabilize"
                                                     THEN \land actorInboxes' = [actorInboxes \ EXCEPT \ ![fingerTables[sel]]]
                                                              \land UNCHANGED \langle fingerTables,
                                                                                 predecessors \rangle
                                                     ELSE \land IF kind[self] = "GetPredecessor"
                                                                    THEN \land actorInboxes' = [actorInboxes \ EXCEPT \ ! [cur
                                                                             \land UNCHANGED \langle fingerTables,
                                                                                                predecessors \rangle
                                                                    ELSE \land IF kind[self] = "GotPredecessor"
                                                                                    Then \wedge if between 00 (current Message [see
                                                                                                   THEN \land fingerTables' = [fin
                                                                                                   ELSE \land TRUE
                                                                                                           ∧ UNCHANGED finger
                                                                                            \land actorInboxes' = [actorInboxes \ E
                                                                                            \land UNCHANGED predecessors
                                                                                    ELSE \land IF kind[self] = "Notify"
                                                                                                   THEN \land IF predecessors[self]
                                                                                                                  THEN \wedge IF betu
                                                                                                                                 TH
                                                                                                                                 ELS
                                                                                                                  ELSE \land TRUE
                                                                                                                          ∧ UNCHA
                                                                                                   ELSE \land TRUE
                                                                                                           ∧ UNCHANGED predec
                                                                                            \land UNCHANGED \langle actorInboxes,
                                                                                                                fingerTables
                                              \land pc' = [pc \text{ EXCEPT } ! [self] = \text{``ReturnDefaults''}]
                                              \land UNCHANGED \langle id, i \rangle
                               \land UNCHANGED \langle triggered, currentMessage, kind,
```

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joined \rangle
FindFirstSuitableI(self) \stackrel{\triangle}{=} \land pc[self] = \text{``FindFirstSuitableI''}
                                     \land IF i[self] > 0 \land \neg (fingerStart(self, i[self], bm) \in DOMAIN fingerTables[self])
                                            THEN \wedge i' = [i \text{ EXCEPT } ![self] = i[self] - 1]
                                                     \land pc' = [pc \text{ EXCEPT } ! [self] = \text{"FindFirstSuitablel"}]
                                            ELSE \land pc' = [pc \text{ EXCEPT } ! [self] = \text{"MainLoop"}]
                                                     \wedge i' = i
                                     \land UNCHANGED \langle actorInboxes, triggered,
                                                          fingerTables, predecessors,
                                                          currentMessage, kind, id, joined⟩
MainLoop(self) \triangleq \land pc[self] = \text{"MainLoop"}
                          \land IF i[self] > 0 \land \neg(between00(self, fingerTables[self][fingerStart(self, i[self], bm)], id[self])
                                 THEN \wedge i' = [i \text{ EXCEPT } ![self] = i[self] - 1]
                                          \land pc' = [pc \text{ EXCEPT } ! [self] = \text{"FindSuitablel"}]
                                          \land UNCHANGED actorInboxes
                                 ELSE \wedge IF i[self] = 0
                                                 THEN \land actorInboxes' = [actorInboxes \ EXCEPT \ ![fingerTables[self]]fing
                                                 ELSE \land actorInboxes' = [actorInboxes \ EXCEPT \ ![fingerTables[self]]fing
                                          \land pc' = [pc \text{ EXCEPT } ! [self] = \text{``ReturnDefaults''}]
                          \land UNCHANGED \langle triggered, fingerTables, predecessors,
                                               currentMessage, kind, id, joined
FindSuitableI(self) \stackrel{\Delta}{=} \land pc[self] = \text{``FindSuitableI''}
                               \land IF i[self] > 0 \land \neg(fingerStart(self, i[self], bm) \in DOMAIN fingerTables[self])
                                      THEN \wedge i' = [i \text{ EXCEPT } ! [self] = i[self] - 1]
                                              \land pc' = [pc \text{ EXCEPT } ! [self] = \text{"FindSuitablel"}]
                                      ELSE \land pc' = [pc \text{ EXCEPT } ! [self] = \text{"MainLoop"}]
                                              \wedge i' = i
                               \land UNCHANGED \langle actorInboxes, triggered, fingerTables,
                                                    predecessors, currentMessage, kind, id,
ReturnDefaults(self) \stackrel{\Delta}{=} \land pc[self] = "ReturnDefaults"
                                \land currentMessage' = [currentMessage \ Except \ ![self] = \langle "?", NULL, NULL \rangle]
                                \wedge kind' = [kind \text{ EXCEPT } ![self] = "?"]
                                \wedge id' = [id \text{ EXCEPT } ![self] = NULL]
                                \land pc' = [pc \text{ EXCEPT } ![self] = \text{"Done"}]
                                \land UNCHANGED \langle actorInboxes, triggered, fingerTables,
```

 $predecessors, i, joined \rangle$

 $\lor ReturnDefaultsBeforeJoin(self) \lor Stabilize(self)$

 $actor(self) \triangleq Join(self) \vee WaitForMessagesBeforeJoin(self)$

 $\lor ProcessMessageBeforeJoin(self)$

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\lor WaitForMessages(self) \lor ProcessMessage(self)
\vee FindFirstSuitableI(self) \vee MainLoop(self)
\vee FindSuitableI(self) \vee ReturnDefaults(self)
```

Allow infinite stuttering to prevent deadlock on termination.

$$\begin{array}{ll} \textit{Terminating} & \triangleq & \land \forall \, self \in \textit{ProcSet} : \textit{pc}[\textit{self}] = \text{``Done''} \\ & \land \, \texttt{UNCHANGED} \, \, \textit{vars} \\ \end{array}$$

$$\begin{array}{ccc} \textit{Next} & \triangleq & (\exists \textit{self} \in \{0,\,1,\,3\}: \textit{actor}(\textit{self})) \\ & \lor \textit{Terminating} \end{array}$$

$$\begin{array}{ll} Spec & \triangleq & \land Init \land \Box [Next]_{vars} \\ & \land \operatorname{WF}_{vars}(Next) \\ & \land \forall self \in \{0, 1, 3\} : \land \operatorname{WF}_{vars}(actor(self)) \end{array}$$

$$\wedge \operatorname{SF}_{vars}(Join(self)) \wedge \operatorname{S}$$

 $\wedge \operatorname{SF}_{vars}(Join(self)) \wedge \operatorname{SF}_{vars}(WaitForMessagesBeforeJoin(self)) \wedge \operatorname{SF}_{vars}(Pro$

 $Termination \stackrel{\triangle}{=} \Diamond(\forall self \in ProcSet : pc[self] = "Done")$

END TRANSLATION

$$\textit{Triggered} \ \stackrel{\triangle}{=} \ \textit{predecessors} = (0:>0) \ @@ \ (1:>0) \ @@ \ (3:>0)$$

 $Liveness \triangleq \Diamond Triggered$

 $LenStateConstraint \triangleq Len(actorInboxes[0]) \leq 0 \land Len(actorInboxes[1]) \leq 0 \land Len(actorInboxes[3]) \leq 0$

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