



Unit V

Backtracking Problems



Tackling Difficult Combinatorial Problems

- *exhaustive search* (brute force)
 - useful only for small instances
- *dynamic programming*
 - applicable to some problems (e.g., the knapsack problem)
- *backtracking*
 - eliminates some unnecessary cases from consideration
 - yields solutions in reasonable time for many instances but worst case is still exponential
- *branch-and-bound*
 - further refines the backtracking idea for optimization problems



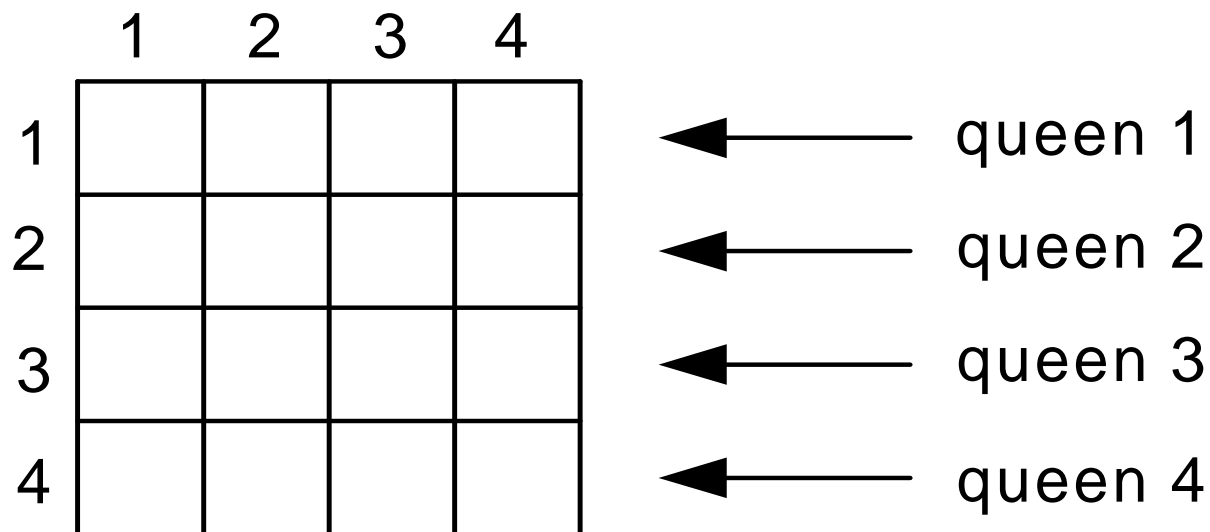
Backtracking

- Construct the state-space tree
 - nodes: partial solutions
 - edges: choices in extending partial solutions
- Explore the state space tree using depth-first search
- “Prune” nonpromising nodes
 - dfs stops exploring subtrees rooted at nodes that cannot lead to a solution and backtracks to such a node’s parent to continue the search

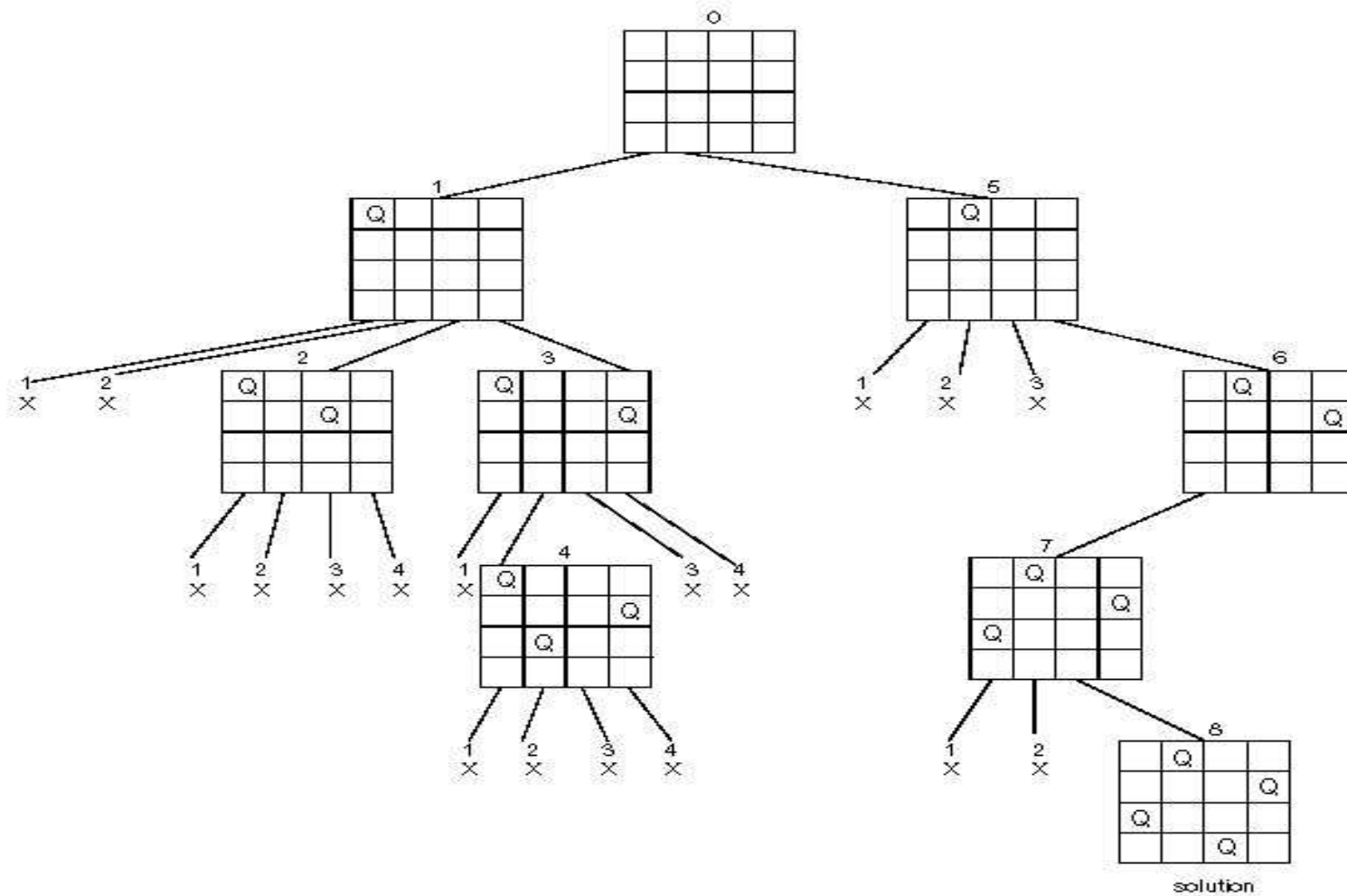


Example: n -Queens Problem

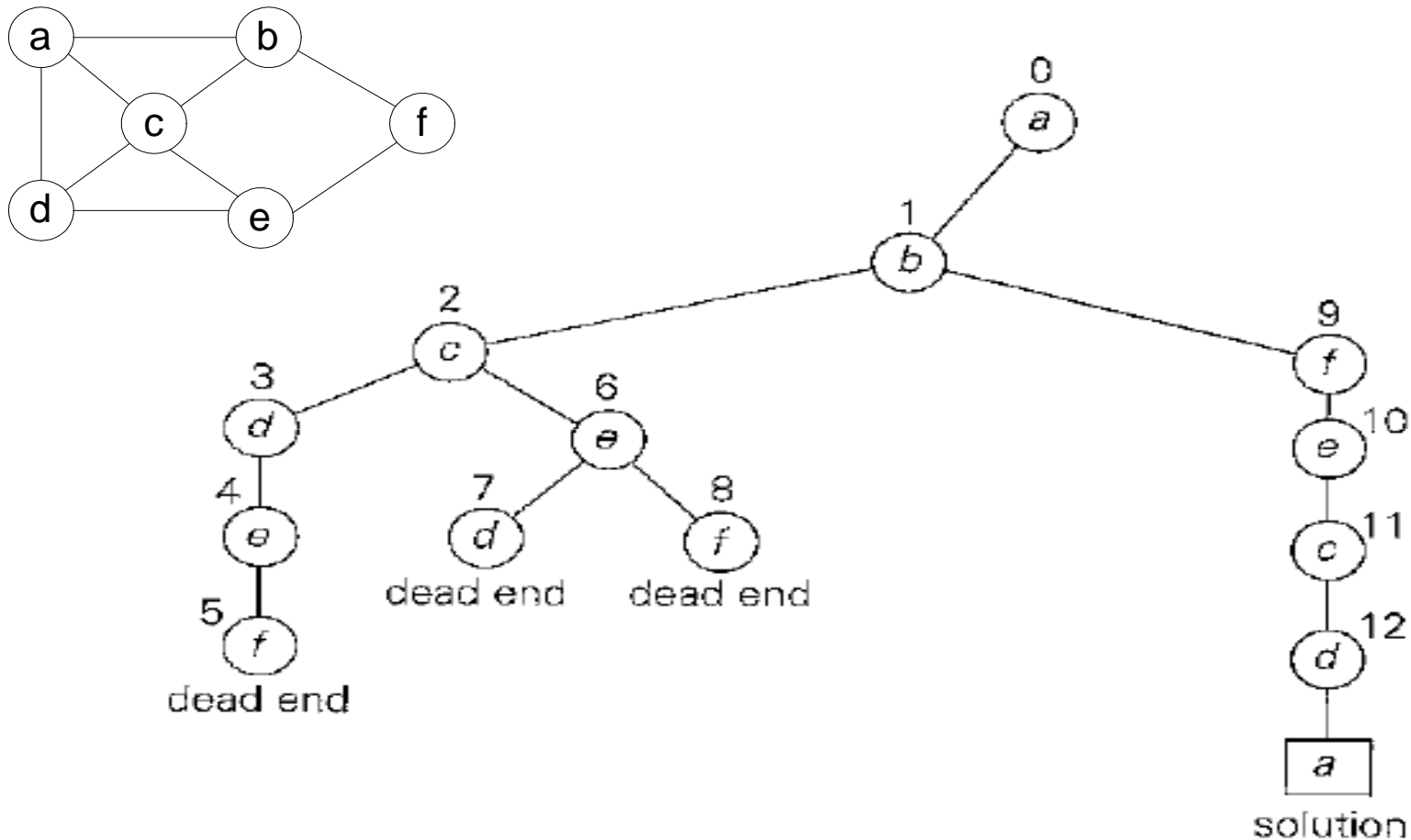
Place n queens on an n -by- n chess board so that no two of them are in the same row, column, or diagonal



State-Space Tree of the 4-Queens Problem

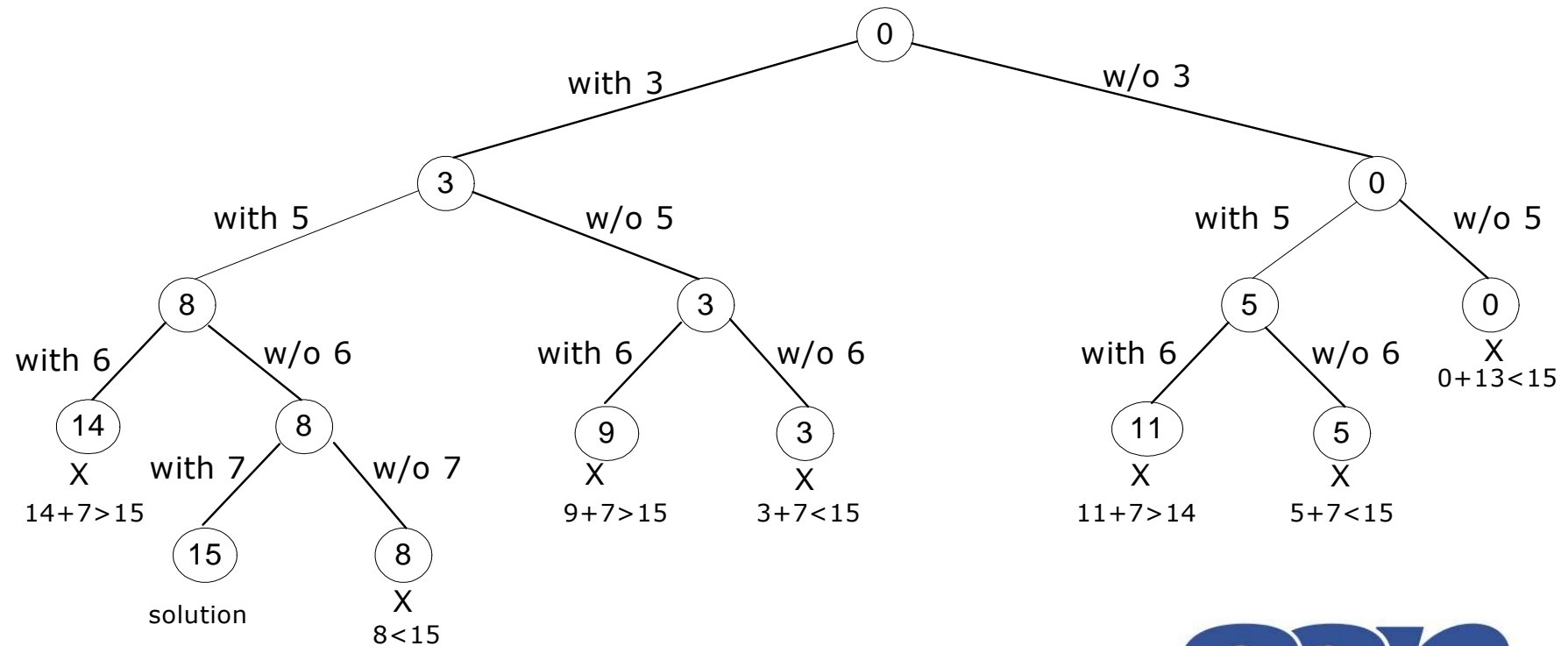


Example: Hamiltonian Circuit Problem



Example: Subset Sum Problem

$A = \{3, 5, 6, 7\}$ and $d = 15$



Backtracking – Generic Algorithm

ALGORITHM *Backtrack*($X[1..i]$)

//Gives a template of a generic backtracking algorithm

//Input: $X[1..i]$ specifies first i promising components of a solution

//Output: All the tuples representing the problem's solutions

if $X[1..i]$ is a solution **write** $X[1..i]$

else //see Problem 9 in this section's exercises

for each element $x \in S_{i+1}$ consistent with $X[1..i]$ and the constraints **do**

$X[i + 1] \leftarrow x$

Backtrack($X[1..i + 1]$)

