

# UIT2504 Artificial Intelligence

## Search and Non-determinism

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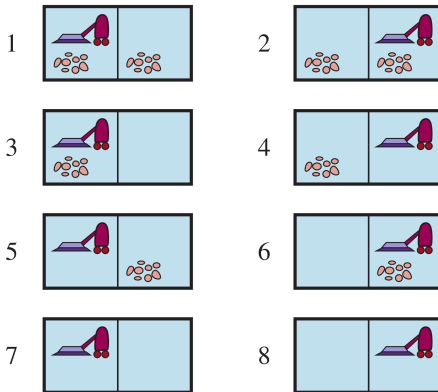
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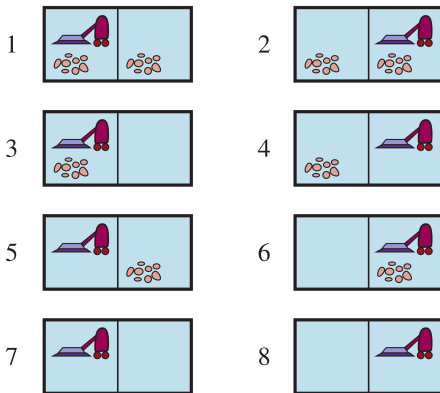
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- So, the agent is in one belief state and by performing an action moves to another belief state

# Vacuum World Revisited



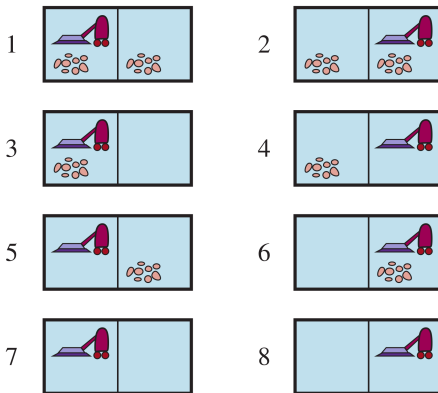
# Vacuum World Revisited



- Consider three possible actions — *Right*, *Left*, and *Suck*

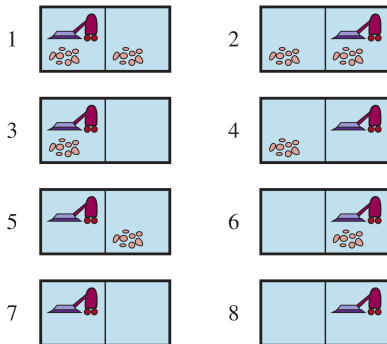


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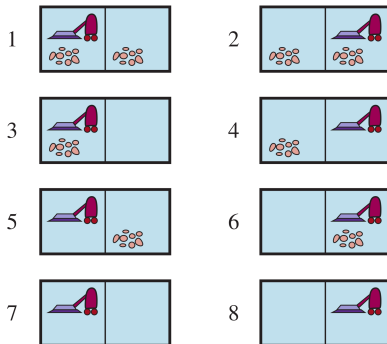


- Consider three possible actions — *Right*, *Left*, and *Suck*
- If the environment is simple, and the initial state is 1, then any search technique can be used to find a goal state (7 or 8) — *[Suck, Right, Suck]*

# Erratic Vacuum World

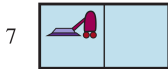
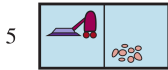
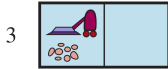
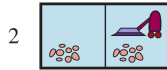
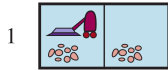


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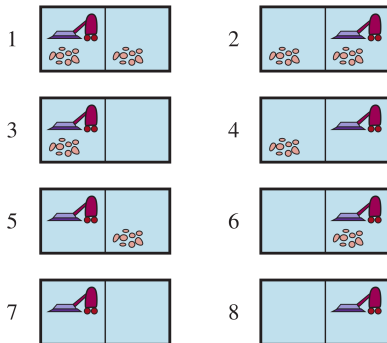


- Suppose, we introduce nondeterminism through erratic behavior of the *Suck* action:
  - When applied to a dirty square the action cleans the square and sometimes cleans up dirt in the adjacent square too
  - When applied to a clean square the action sometimes deposits dirt on the carpet

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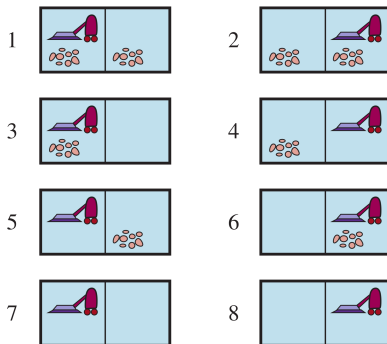


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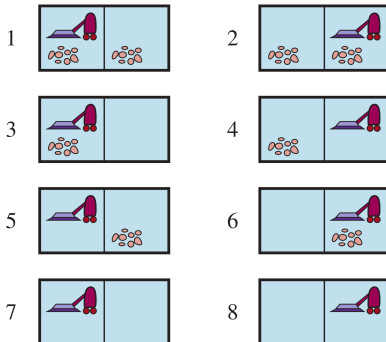
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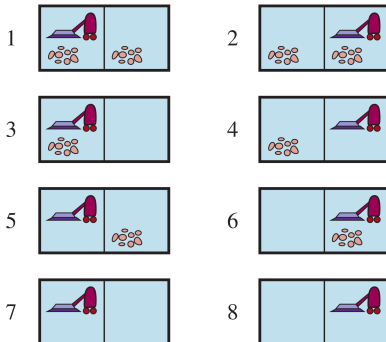


- This can be captured by appropriately modifying the **transition model**
- $RESULTS(1, Suck) = \{5, 7\}$

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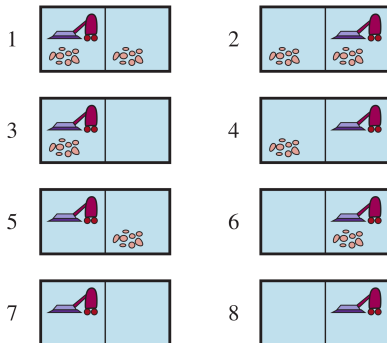
# Erratic Vacuum World



- Suppose, we start from state 1, what may be a solution? Is it a sequence of action?



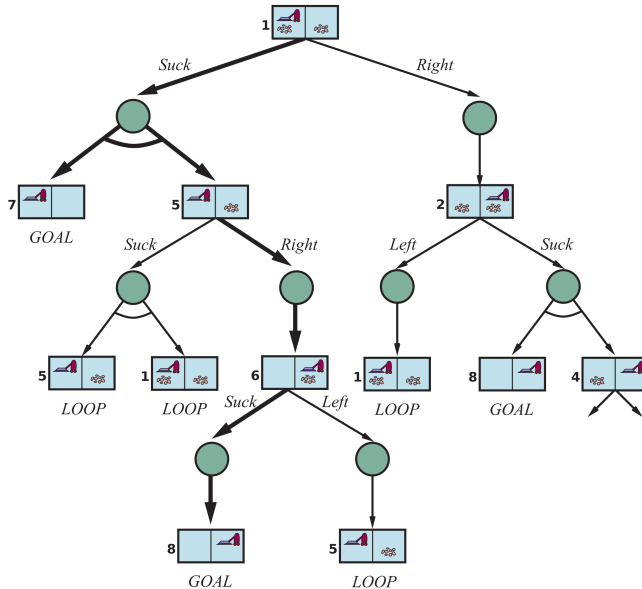
# Erratic Vacuum World



- Suppose, we start from state 1, what may be a solution? Is it a sequence of action?
- The solution now is a tree! It is called as a **condition plan** (also known as a contingency plan or a strategy)

*[Suck, if State = 5 then [Right, Suck] else []]*

# AND-OR Search Trees



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- As we can see, solution is no more a path in the search tree

# Solution in a AND–OR Tree

- As we can see, solution is no more a path in the search tree
- Solution is a subtree that
  - has a goal node at each leaf
  - specifies one action at each of its OR nodes
  - includes every outcome branch at each of its AND nodes

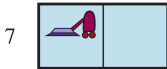
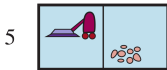
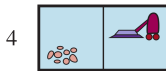
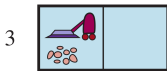
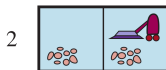
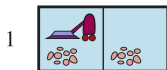
# AND-OR Search Algorithm

**function** AND-OR-SEARCH(*problem*) **returns** a conditional plan, or *failure*  
    **return** OR-SEARCH(*problem*, *problem*.INITIAL, [])

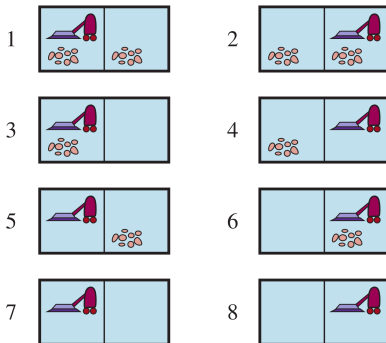
**function** OR-SEARCH(*problem*, *state*, *path*) **returns** a conditional plan, or *failure*  
    **if** *problem*.IS-GOAL(*state*) **then return** the empty plan  
    **if** IS-CYCLE(*path*) **then return** *failure*  
    **for each** *action* **in** *problem*.ACTIONS(*state*) **do**  
         $plan \leftarrow \text{AND-SEARCH}(\text{problem}, \text{RESULTS}(\text{state}, \text{action}), [\text{state}] + \text{path})$   
        **if**  $plan \neq \text{failure}$  **then return** [*action*] + *plan*  
    **return** *failure*

**function** AND-SEARCH(*problem*, *states*, *path*) **returns** a conditional plan, or *failure*  
    **for each**  $s_i$  **in** *states* **do**  
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        **if**  $plan_i = \text{failure}$  **then return** *failure*  
    **return** [**if**  $s_1$  **then**  $plan_1$  **else if**  $s_2$  **then**  $plan_2$  **else** ... **if**  $s_{n-1}$  **then**  $plan_{n-1}$  **else**  $plan_n$ ]

# Slippery Vacuum World

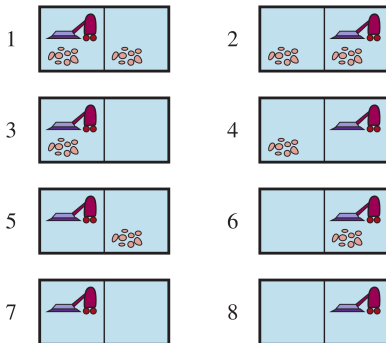


# Slippery Vacuum World



- Consider a different variation of the conventional vacuum world problem — movement actions sometimes fail, leaving the agent in the same location
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- Consider a different variation of the conventional vacuum world problem — movement actions sometimes fail, leaving the agent in the same location
- This can be captured by appropriately modifying the **transition model**
- $RESULTS(1, Right) = \{1, 2\}$ ,  $RESULTS(2, Left) = \{1, 2\}$ , and so on



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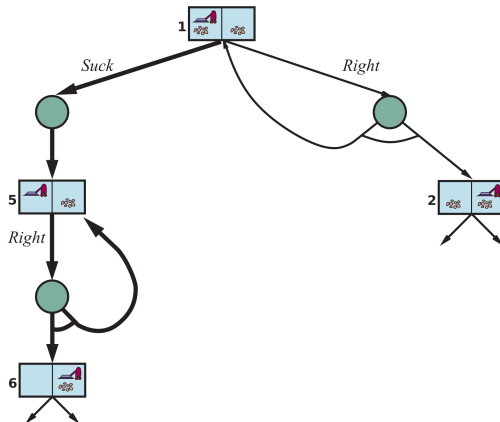
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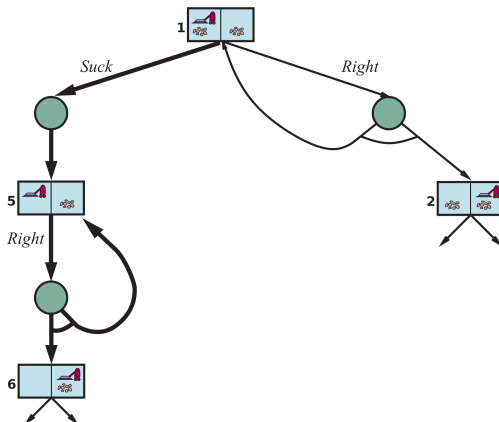
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- This idea works if the driving mechanism is just slippery and works otherwise. The plan does not work if the agent can never move right

# Cyclic Plans



# Cyclic Plans



- Solution is a “tree” with possible loops, where every leaf is a goal state and that a leaf is reachable from every point in the plan

# Questions?

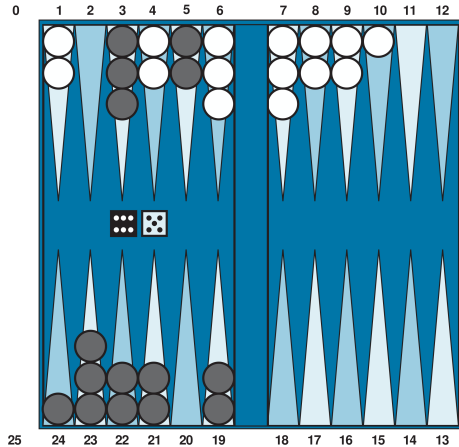
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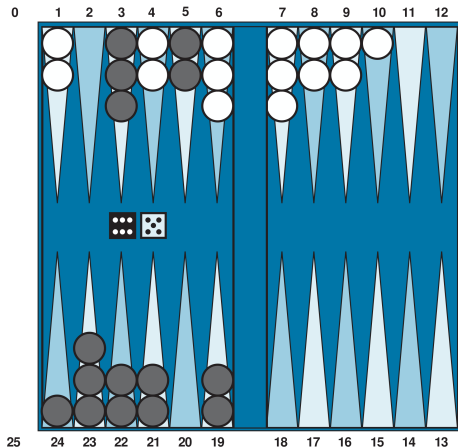


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- Depending on what has been rolled, a player, say Black, has certain choices of actions but can not think ahead as nobody knows what will be the result of White's dice roll
- The game tree is similar to the AND-OR tree, but basic probability knowledge can be used

# Stochastic Games



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- Black, which moves clockwise from 0 to 25, has four possible moves for this roll of dice (6-5): (5-11, 5-10), (5-11, 19-24), (5-10, 10-16), (5-11, 11-16)

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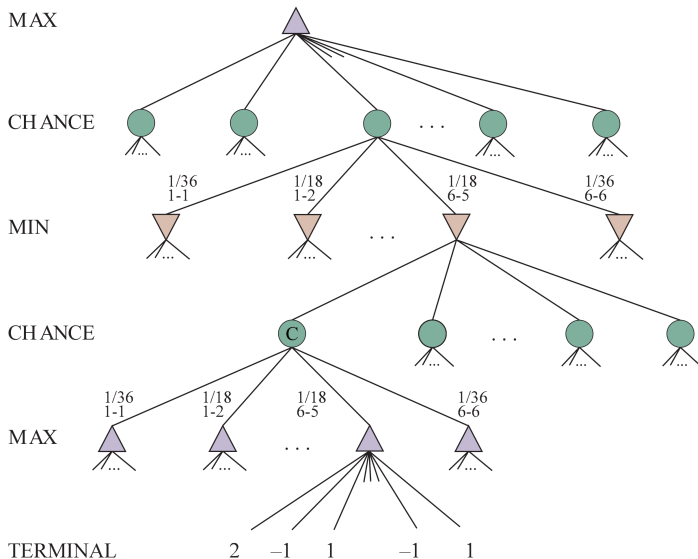
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- We make a weighted sum of utility values of all the children to get the **expected utility** of a chance node

# Game Tree with Chance Nodes



- Now, the idea of minimax value for deterministic games can be generalized to the **expectiminimax value** as follows:

EXPECTIMINIMAX( $s$ ) =

$$\begin{cases} \text{Utility}(s, \text{MAX}) & \text{if IS\_TERMINAL}(s) \\ \max_a \text{EMINIMAX}(\text{RESULT}(s, a)) & \text{if TO\_MOVE}(s) = \text{MAX} \\ \min_a \text{EMINIMAX}(\text{RESULT}(s, a)) & \text{if TO\_MOVE}(s) = \text{MIN} \\ \sum_r P(r) \text{EMINIMAX}(\text{RESULT}(s, r)) & \text{if TO\_MOVE}(s) = \text{CHANCE} \end{cases}$$

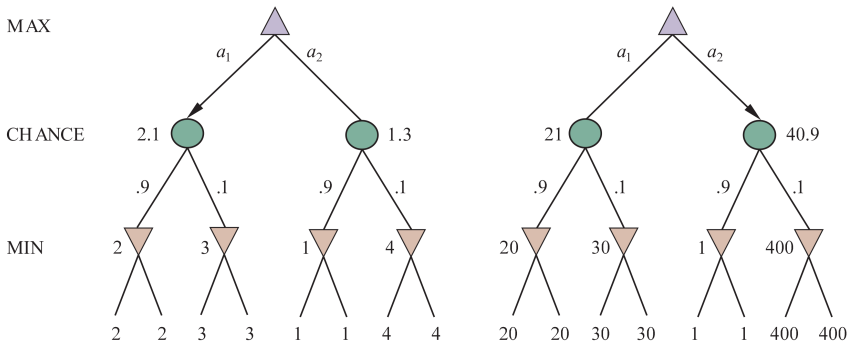
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- However, the estimated values should be in agreement with the probability of winning (or, of the expected utility)

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- Consider a game where 5 dices are rolled! The branching factor is too high. A Type B strategy of forward pruning may be applied
- Monte Carlo Tree Search is definitely possible as we can always take a random outcome for a dice roll!

# Questions?