## Unification Algorithm in Al

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#### Unification

- Any substitution that makes two or more expressions equal is called a unifier for the expressions.
- In propositional logic, it is easy to determine that two literals cannot both be true at the same time. Simply look for L and ~L.
- In predicate logic, this matching process is more complicated, since binding of variables must be considered.

- For example MAN (john) and ~MAN(john) is a contradiction, while MAN (john) and MAN(Himalayas) is not.
- Thus in order to determine contradictions, we need a matching procedure that compares two literals and discovers whether there exist a set of substitutions that makes them identical.
- There is a recursive procedure that does this matching. It is called Unification algorithm.

- In Unification algorithm each literal is represented as a list, where first element is the name of a predicate and the remaining elements are arguments. The argument may be a single element (atom) or may be another list.
- For example, we can have literals as
- TRYASSASSINATE(Marcus, Caesar)
- TRYASSASSINATE(Marcus, Ruler of Rome)

- To unify two literals, first check if their first elements are same. If so proceed. Otherwise they cannot be unified.
- For example the literals
  - TRYASSASSINATE (Marcus, Caesar)
  - HATE (Marcus, Caesar)

#### Can not be Unified.

 The unification algorithm recursively matches pairs of elements, one pair at a time.

- The Unification algorithm is listed below as a procedure UNIFY (L1, L2). It returns a list representing the composition of the substitutions that were performed during the match.
- An empty list NIL indicates that a match was found without any substitutions. If the list contains a single value FAIL, it indicates that the unification procedure failed.

- Algorithm UNIFY (L1, L2)
- 1. if L1 or L2 are both variable or constants, then:
  - □ (a). if L1 or L2 are identical then return NIL.
  - □ (b). else if L1 is a variable then if L1 occurs in L2 then return {FAIL} else return (L2/L1).
  - ☐ (c). else if L2 is a variable then if L2 occurs in L1 then return {FAIL} else return (L1/L2).
  - $\Box$ (d). else return {FAIL}.

- 2. If the initial predicate symbols in L1 and L2 are not identical, then return {FAIL}.
- 3. If L1 and L2 have a different number of arguments, then return {FAIL}.
- 4. Set SUBST to NIL.

- 5. For i← 1 to number of arguments in L1:
  - □(a). Call Unify with the ith argument of L1 and the ith argument of L2, putting result in S.
  - $\Box$ (b). If S contains FAIL then return {FAIL}.
  - $\square$ (c). If S is not equal to NIL then:
    - (i). Apply S to the remainder of both L1 and L2.
    - ➤(ii). SUBST:=APPEND(SUBST).
- 6. Return SUBST.

## Example#1

- Let's say there are two different expressions,
  P(x, y), and P(a, f(z)).
- we need to make both above statements identical to each other.
- Perform the substitution.

- Substitute x with a, and y with f(z) in the first expression, and it will be represented as a/x and f(z)/y.
- With both the substitutions, the first expression will be identical to the second expression and the substitution set will be: [a/x, f(z)/y].

#### **Conditions for Unification**

 Predicate symbol must be same, atoms or expression with different predicate symbol can never be unified.

tryassassinate (Marcus, Caesar)

hate (Marcus, Caesar)

Number of Arguments in both expressions must be identical.

hate (Marcus, Caesar)

 Unification will fail if there are two similar variables present in the same expression.

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