

i) Since  $h$  matrix is separable into column vectors  $u$  and  $v$  given by the below formula

$$h_{kl} = u_k v_l \quad (\text{Given as per statement})$$

$$\sum_l h_{kl} = \sum_l u_k v_l \quad (\text{Adding summation sign both sides})$$

$$\sum_R \sum_l h_{kl} = \sum_R \sum_l u_k v_l \quad (\text{2 summations can be computed as independent summation})$$

$$\sum_R \sum_l h_{kl} = \sum_l \sum_R u_k v_l \quad (\text{because order of summation can be changed})$$

$$\sum_R u_k = \sum_l v_l = 1; \quad \text{~~also given~~}$$

$$\sum_R \sum_l h_{kl} = \sum_l 1 \cdot v_l$$

$$\Rightarrow \sum_R \sum_l h_{kl} = 1 \cdot 1 = 1$$