

Artificial Intelligence Lab Report



Submitted by

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Date: 9/11/22

Program 1: Implement Tic –Tac –Toe Game.

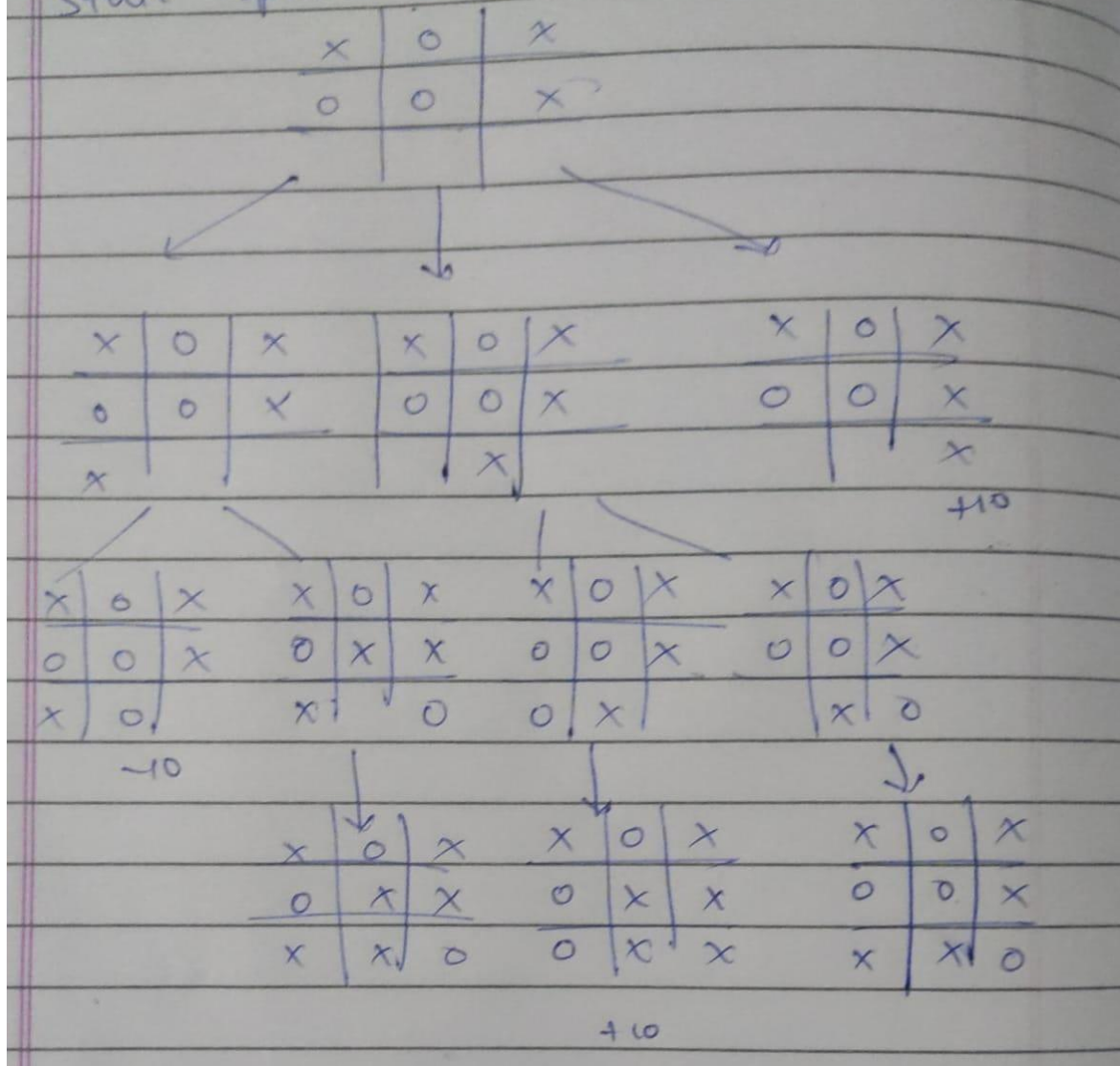
Algorithm:

Algorithm

```
int minimax (state, level) {  
    if (state is a solution) // base case  
        return states value  
  
    if (level is max) {  
        while (state has more children)  
            Minimax (child, level+1)  
            if value returned is > best so  
                far, store it & return it  
        } else { // level is a min value  
            while (state has more children)  
                Minimax (child, level+1)  
                if value returned is < best so  
                    far, store it  
            }  
        return minimum returned value  
    }  
}
```

Space state Tree

State space tree



Code

```

import numpy as np # linear algebra
import pandas as pd # data processing, CSV file I/O
import os
for dirname, _, filenames in os.walk('/kaggle/input'):
    for filename in filenames:
        print(os.path.join(dirname, filename))

#Tic Tac Toe Game Python

board = [' ' for x in range(10)]

def insertBoard(letter, pos):
    global board
    board[pos] = letter

def spaceIsFree(pos):
    return board[pos] == ' '

def isWinner(bo, le):
    # Given a board and a player's letter, this function returns True if
    # that player has won.
    # We use bo instead of board and le instead of letter so we don't
    # have to type as much.
    return ((bo[7] == le and bo[8] == le and bo[9] == le) or # across the
top
    (bo[4] == le and bo[5] == le and bo[6] == le) or # across the middle
    (bo[1] == le and bo[2] == le and bo[3] == le) or # across the bottom
    (bo[7] == le and bo[4] == le and bo[1] == le) or # down the left side
    (bo[8] == le and bo[5] == le and bo[2] == le) or # down the middle
    (bo[9] == le and bo[6] == le and bo[3] == le) or # down the right
side
    (bo[7] == le and bo[5] == le and bo[3] == le) or # diagonal
    (bo[9] == le and bo[5] == le and bo[1] == le)) # diagonal

def playerMove():
    run = True
    while run:
        move = input('Please select a position to place an \'X\' (1-9):')
        try:
            move = int(move)
            if move > 0 and move < 10:
                if spaceIsFree(move):

```

```

        run = False
        insertBoard('X', move)
    else:
        print('This position is already occupied!')
    else:
        print('Please type a number within the range!')
except:
    print('Please type a number!')

```

```

def selectRandom(li):
    import random
    ln = len(li)
    r = random.randrange(0, ln)
    return li[r]

```

```

def compMove():
    possibleMoves = [x for x, letter in enumerate(board) if letter == ' '
and x != 0]
    move = 0

```

```

    #Check for possible winning move to take or to block opponents
    winning move

```

```

    for let in ['O', 'X']:
        for i in possibleMoves:
            boardCopy = board[:]
            boardCopy[i] = let
            if isWinner(boardCopy, let):
                move = i
            return move

```

```

    #Try to take one of the corners

```

```

    cornersOpen = []
    for i in possibleMoves:
        if i in [1,3,7,9]:
            cornersOpen.append(i)
    if len(cornersOpen) > 0:
        move = selectRandom(cornersOpen)
        return move

```

```

    #Try to take the center

```

```

    if 5 in possibleMoves:
        move = 5
        return move

```

```

    #Take any edge

```

```

    edgesOpen = []

```

```

    for i in possibleMoves:
        if i in [2,4,6,8]:
            edgesOpen.append(i)

    if len(edgesOpen) > 0:
        move = selectRandom(edgesOpen)

    return move

def isBoardFull(board):
    if board.count(' ') > 1:
        return False
    else:
        return True

def printBoard():
    # "board" is a list of 10 strings representing the board (ignore
    index 0)
    print('    |    |')
    print(' ' + board[1] + ' | ' + board[2] + ' | ' + board[3])
    print('    |    |')
    print('-----')
    print('    |    |')
    print(' ' + board[4] + ' | ' + board[5] + ' | ' + board[6])
    print('    |    |')
    print('-----')
    print('    |    |')
    print(' ' + board[7] + ' | ' + board[8] + ' | ' + board[9])
    print('    |    |')

def main():
    #Main game loop
    print('Welcome to Tic Tac Toe, to win complete a straight line of
    your letter (Diagonal, Horizontal, Vertical). The board has positions 1-9
    starting at the top left.')
    printBoard()

    while not(isBoardFull(board)):
        if not(isWinner(board, 'O')):
            playerMove()
            printBoard()
        else:
            print('Os win this time...')
            break

    if not(isWinner(board, 'X')):
```

```
        move = compMove()
        if move == 0:
            print('Game is a Tie! No more spaces left to move.')
        else:
            insertBoard('O', move)
            print('Computer placed an O in position', move, ':')
            printBoard()
    else:
        print('X wins, good job!')
        break

if isBoardFull(board):
    print('Game is a tie! No more spaces left to move.')
```

Output:

Welcome to Tic Tac Toe, to win complete a straight line of your letter

Please select a position to place an \'X\' (1-9):1

X		

Computer placed an 0 in position 3 :

X		0

Please select a position to place an \'X\' (1-9):5

X	X	O
---	---	---

	X	
--	---	--

		O
--	--	---

Computer placed an O in position 6 :

X	X	O
---	---	---

	X	O
--	---	---

		O
--	--	---

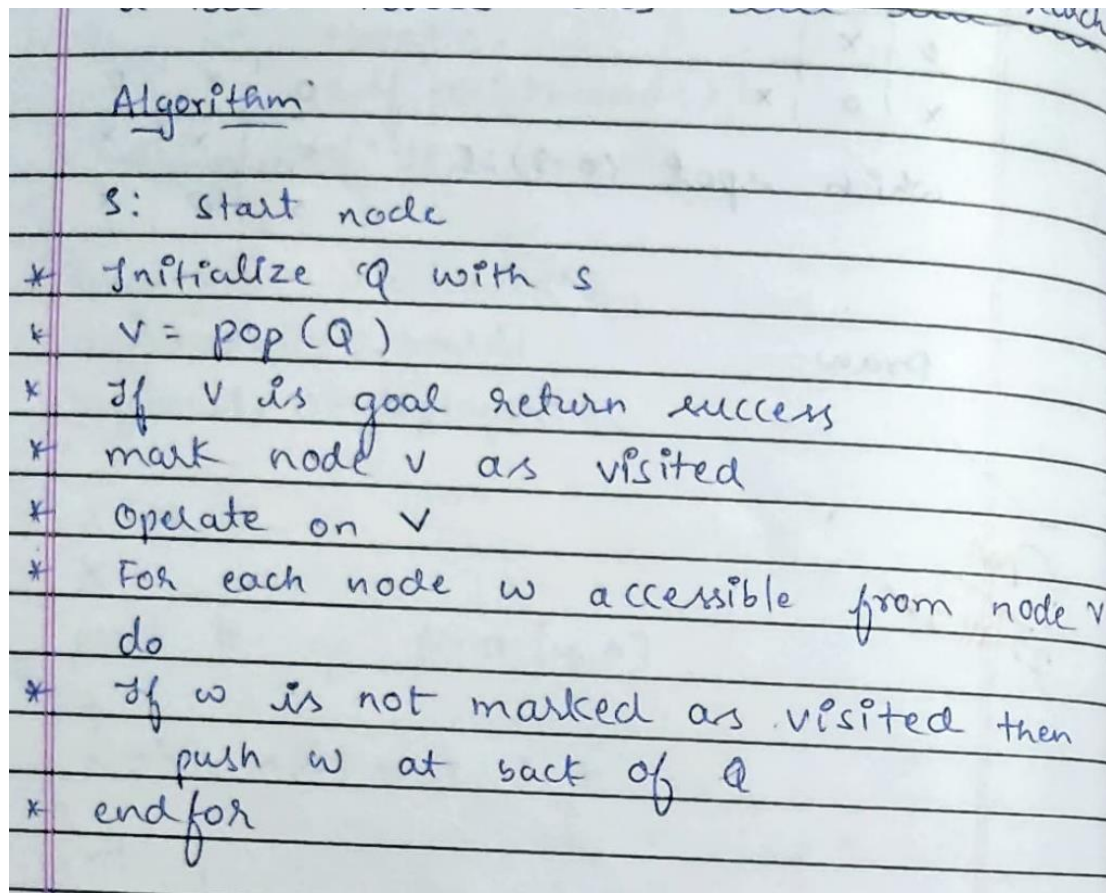
Os win this time...

Date: 16/11/22

Program 2: Solve 8 puzzle problem.

8

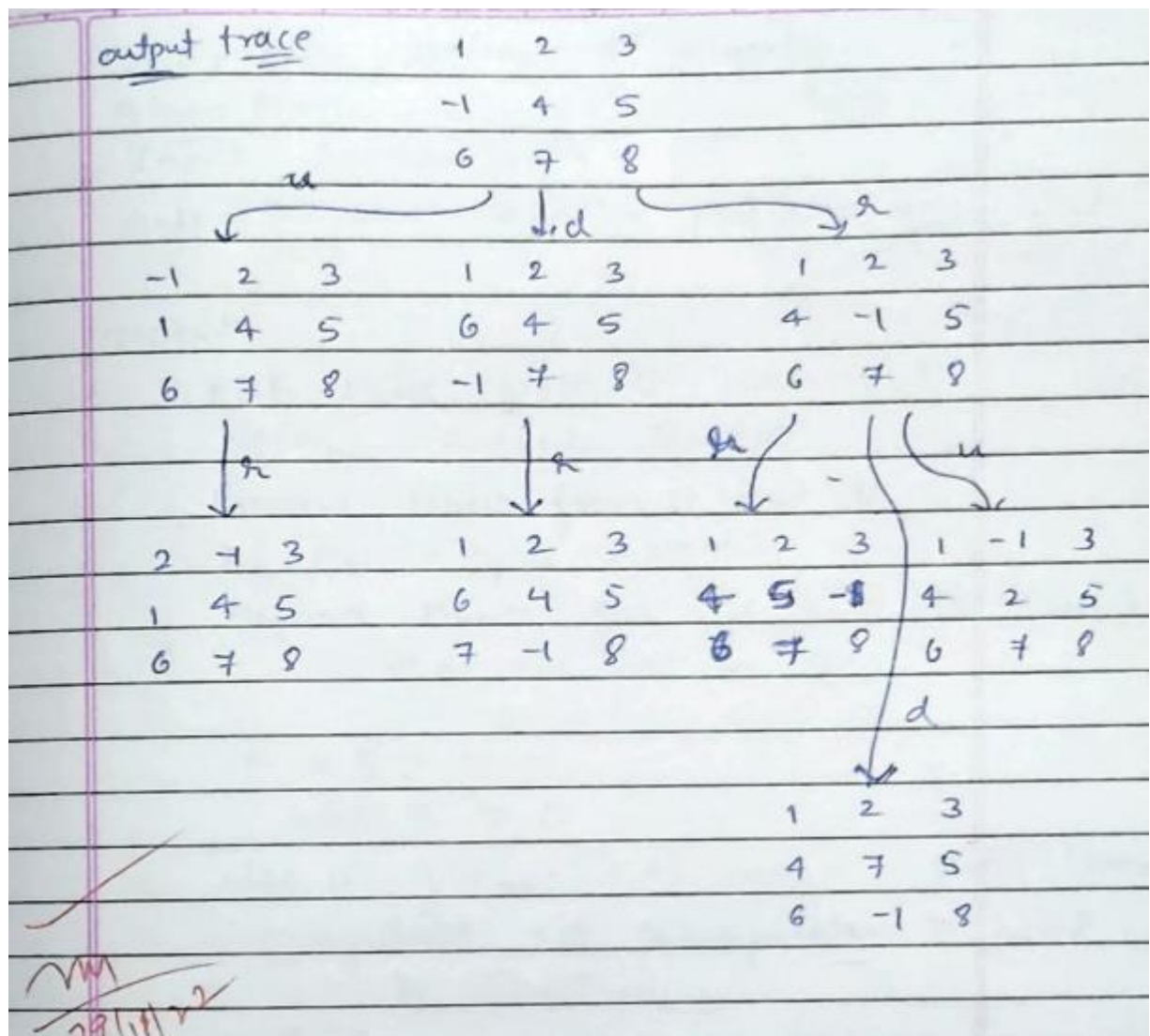
Algorithm:



The image shows a handwritten algorithm on lined paper. The word 'Algorithm' is underlined at the top. The steps are as follows:

- S: start node
- * Initialize Q with s
- * $v = \text{pop}(Q)$
- * If v is goal return success
- * mark node v as visited
- * Operate on v
- * For each node w accessible from node v do
- * If w is not marked as visited then push w at back of Q
- * endfor

State Space Tree:



Code:

```
def bsf(src,target):
    queue = []
    queue.append(src)

    exp = []

    while(len(queue)>0):
        source = queue.pop(0)
        exp.append(source)

        print(source)

        if source == target:
            print("Success")
            return
```

```

    poss_moves_to_do = []
    poss_moves_to_do = possible_moves(source,exp)

    for move in poss_moves_to_do:
        if move not in exp and move not in queue:
            queue.append(move)

def possible_moves(state,visited_states):
    b = state.index(-1)

    d = []
    if b not in [0,1,2]:
        d.append('u')
    if b not in [6,7,8]:
        d.append('d')
    if b not in [0,3,6]:
        d.append('l')
    if b not in [2,5,8]:
        d.append('r')

    poss_moves_it_can = []

    for i in d:
        poss_moves_it_can.append(gen(state,i,b))

    return [move_it_can for move_it_can in poss_moves_it_can if move_it_can not in
visited_states]

def gen(state,m,b):
    temp = state.copy()

    if m=='d':
        temp[b+3],temp[b] = temp[b],temp[b+3]
    if m=='u':
        temp[b-3],temp[b] = temp[b],temp[b-3]
    if m=='l':
        temp[b-1],temp[b] = temp[b],temp[b-1]
    if m=='r':
        temp[b+1],temp[b] = temp[b],temp[b+1]

    return temp

```

```
src = [1,2,3,-1,4,5,6,7,8]
target = [1,2,3,4,5,-1,6,7,8]
bsf(src,target)
```

Output:

```
OUTPUT

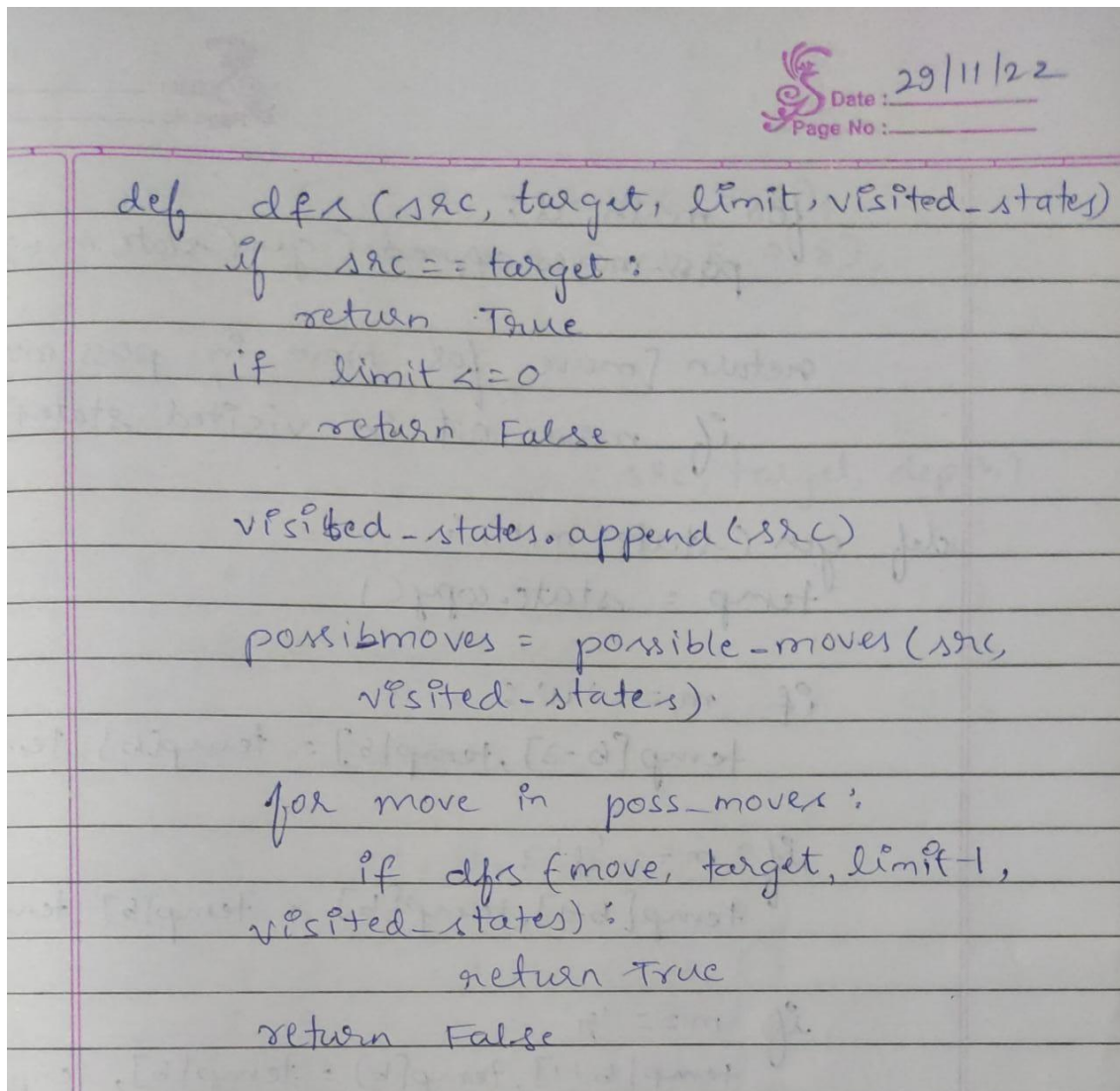
C:\Shashanka G\puzzle8>python 8puzzle.py
[1, 2, 3, -1, 4, 5, 6, 7, 8]
[-1, 2, 3, 1, 4, 5, 6, 7, 8]
[1, 2, 3, 6, 4, 5, -1, 7, 8]
[1, 2, 3, 4, -1, 5, 6, 7, 8]
[2, -1, 3, 1, 4, 5, 6, 7, 8]
[1, 2, 3, 6, 4, 5, 7, -1, 8]
[1, -1, 3, 4, 2, 5, 6, 7, 8]
[1, 2, 3, 4, 7, 5, 6, -1, 8]
[1, 2, 3, 4, 5, -1, 6, 7, 8]
Success

C:\Shashanka G\puzzle8>
```

Date: 23/11/22

Program 3: Implement Iterative deepening search algorithm.

Algorithm:



The image shows a handwritten implementation of the Iterative Deepening Search (IDS) algorithm in Python. The code is written on lined paper with a date stamp of 29/11/22 and a page number of 12. The algorithm is defined as a function `dfs(src, target, limit, visited_states)`. It checks if the source state is the target, and if the limit is zero, it returns False. It then appends the source state to the visited states, generates possible moves, and iterates through them, recursively calling `dfs` with a limit of `limit-1`. If any path leads to the target, it returns True; otherwise, it returns False.

```
def dfs(src, target, limit, visited_states):
    if src == target:
        return True
    if limit <= 0:
        return False

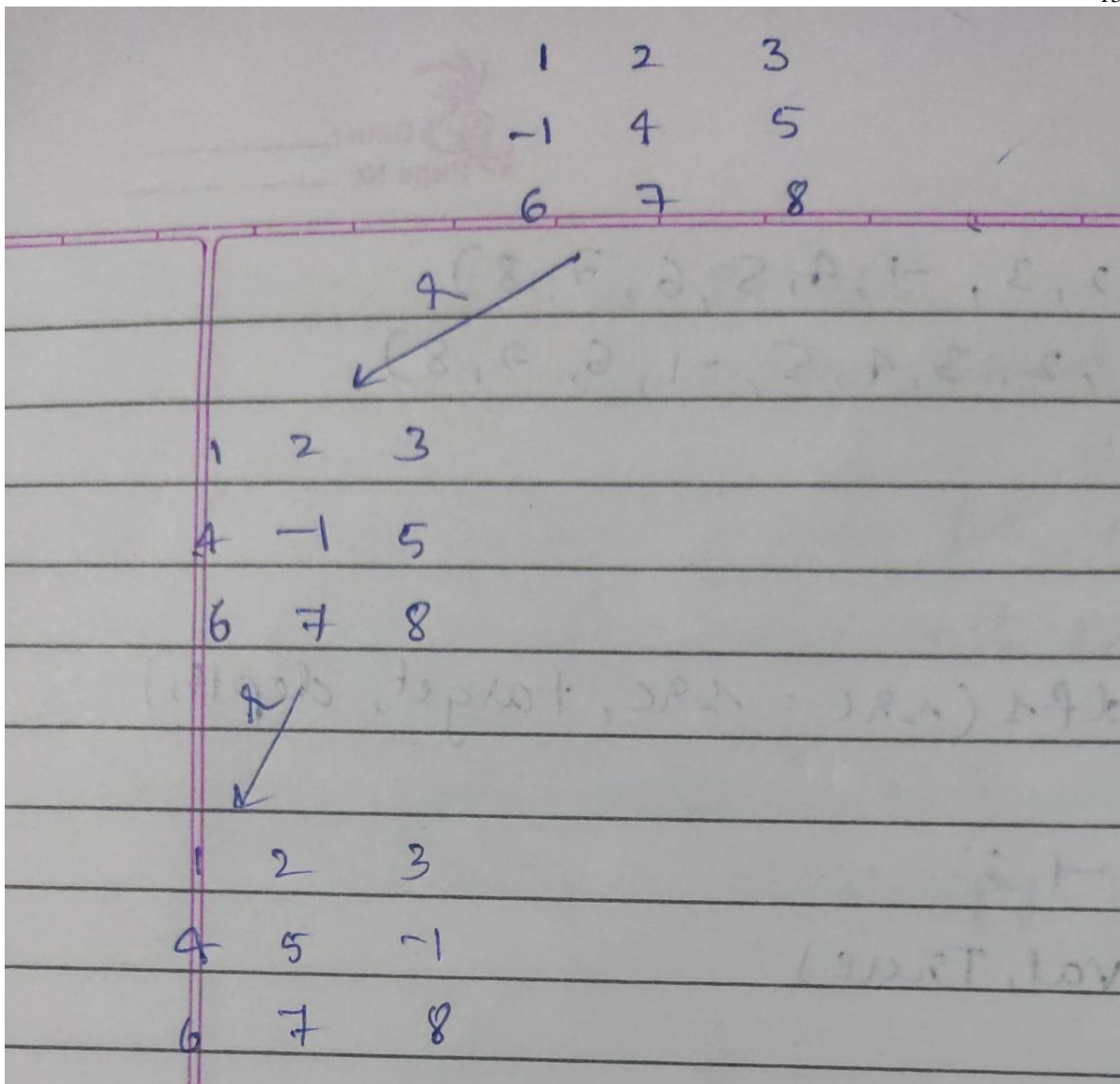
    visited_states.append(src)

    possible_moves = possible_moves(src,
        visited_states)

    for move in possible_moves:
        if dfs(move, target, limit-1,
            visited_states):
            return True

    return False
```

State Space Tree:

**Code:**

```
def dfs(src,target,limit,visited_states):
    print(visited_states)
    if src == target:
        return True
    if limit<=0:
        return False
    visited_states.append(src)
    poss_moves = possible_moves(src,visited_states)
```



```

for move in poss_moves:
    if dfs(move,target,limit-1,visited_states):
        return True
return False

```

```

def possible_moves(state,visited_states):
    b = state.index(-1)
    d = []
    if b not in [2,5,8]:
        d.append('r')
    if b-3 in range(9):
        d.append('u')
    if b not in [0,3,6]:
        d.append('l')
    if b+3 in range(9):
        d.append('d')
    pos_moves = []
    for m in d:
        pos_moves.append(gen(state,m,b))
    return [move for move in pos_moves if move not in visited_states]

```

```

def gen(state,m,b):
    temp = state.copy()
    if m == 'u':
        temp[b-3],temp[b] = temp[b],temp[b-3]
    if m == 'l':
        temp[b-1],temp[b] = temp[b],temp[b-1]
    if m == 'r':
        temp[b+1],temp[b] = temp[b],temp[b+1]
    if m == 'd':
        temp[b+3],temp[b] = temp[b],temp[b+3]
    return temp

```

```

def IDdfs(src,target,depth):
    visited_states = []

```

```

for i in range(1,depth+1):
    if dfs(src,target,i,visited_states):
        return i
return -1

src = [1,2,3,-1,4,5,6,7,8]
target = [1,2,3,4,5,-1,6,7,8]
depth = 25
val = IDdfs(src=src,target=target,depth=depth)
if val != -1:
    print(val,True)
else:
    print(False)

```

Output:

```

Initial state [1, 2, 3, -1, 4, 5, 6, 7, 8]
Finalstate [1, 2, 3, 4, 5, -1, 6, 7, 8]
[1, 2, 3, -1, 4, 5, 6, 7, 8]
[-1, 2, 3, 1, 4, 5, 6, 7, 8]
[2, -1, 3, 1, 4, 5, 6, 7, 8]
[1, 2, 3, 6, 4, 5, -1, 7, 8]
[1, 2, 3, 6, 4, 5, 7, -1, 8]
[1, 2, 3, 4, -1, 5, 6, 7, 8]
[1, -1, 3, 4, 2, 5, 6, 7, 8]
[1, 2, 3, 4, 7, 5, 6, -1, 8]
[1, 2, 3, 4, 5, -1, 6, 7, 8]
True

```

Date: 30/11/22

Program 4: Implement A* search algorithm

8 puzzle using A* Algorithm

Algorithm

Input: source state

Output: Best possible path to goal state

repeat

 Pick n_{best} from O such that

$f(n_{best}) \leq f(n), \forall n \in O$

 Remove n_{best} from O and to C

 If $n_{best} = g_{goal}$, EXIT

 Expand n_{best} : for all $x \in \text{star}(n_{best})$
 that are not in C

 if $x \notin O$ then

 add x to O

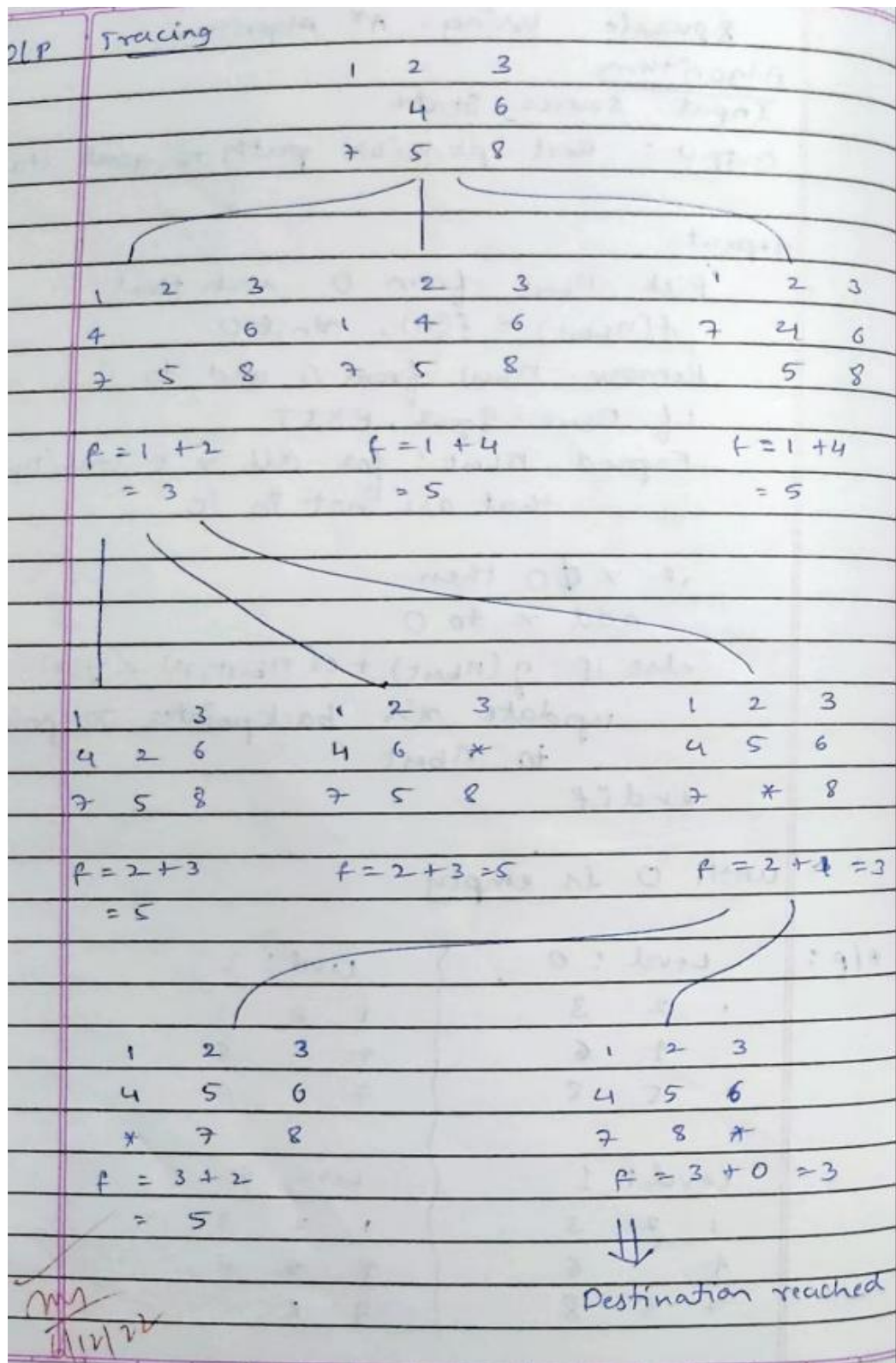
 else if $g(n_{best}) + c(n_{best}, x) < g(x)$ then

 update x 's backpointer to point
 to n_{best}

 endif

until O is empty

State Space Tree:



Code:

```

def print_b(src):

    state = src.copy()

    state[state.index(-1)] = ' '

    print(

        f"""

{state[0]} {state[1]} {state[2]}

{state[3]} {state[4]} {state[5]}

{state[6]} {state[7]} {state[8]}

        """

    )


def h(state, target):

    count=0

    for i in range(9):

```

```
if state[i] != target[i]:
```

```
    count=count+1
```

```
return count
```

```
def astar(state,target):# Add inputs if more are required
```

```
    states = [src]
```

```
    g = 0
```

```
    visited_states =[]
```

```
    while len(states):
```

```
        print(f"Level: {g}")
```

```
        moves = []
```

```
        for state in states:
```

```
            visited_states.append(state)
```

```
            print_b(state)
```

```
            if state == target:
```

```
                print("Success")
```

```
return
```

```
moves += [move for move in possible_moves(state, visited_states) if move not in moves]
```

```
costs = [ h(move, target) for move in moves]
```

```
states = [moves[i] for i in range(len(moves)) if costs[i] == min(costs)]
```

```
g += 1
```

```
print("Fail")
```

```
def possible_moves(state, visited_state): # Add inputs if more are required
```

```
# Find index of empty spot and assign it to b
```

```
b = state.index(-1)
```

```
# 'd' for down, 'u' for up, 'r' for right, 'l' for left - directions array
```

```
d = []
```

```
# Add all possible direction into directions array - Hint using if statements
```

```
if b - 3 in range(9):
```

```
    d.append('u')
```

```
if b not in [0, 3, 6]:
```

```
    d.append('l')
```

```
if b not in [2, 5, 8]:
```

```
    d.append('r')
```

```
if b + 3 in range(9):
```

```
    d.append('d')
```

```
# If direction is possible then add state to move
```

```
pos_moves = []
```

```
# for all possible directions find the state if that move is played
```

```
### Jump to gen function to generate all possible moves in the given directions
```

```
for m in d:
```

```
    pos_moves.append(gen(state, m, b))
```



```
# return all possible moves only if the move not in visited_states
```

```
return [move for move in pos_moves if move not in visited_state]
```

```
def gen(state, m, b):
```

```
    temp = state.copy()
```

```
    # if move is to slide empty spot to the left and so on
```

```
    if m == 'u': temp[b - 3], temp[b] = temp[b], temp[b - 3]
```

```
    if m == 'l': temp[b - 1], temp[b] = temp[b], temp[b - 1]
```

```
    if m == 'r': temp[b + 1], temp[b] = temp[b], temp[b + 1]
```

```
    if m == 'd': temp[b + 3], temp[b] = temp[b], temp[b + 3]
```

```
    # return new state with tested move to later check if "src == target"
```

```
    return temp
```

```
# Test 1
```

```
src = [1,2,3,-1,4,6,7,5,8]
```

```
target = [1,2,3,4,5,6,7,8,-1]
```

```
astar(src, target)
```

```
Output:
```

```
D:\Shashanka G\puzzle8_astart>python 8puzzle.py
```

```
Level: 0
```

```
1 2 3
```

```
4 6
```

```
7 5 8
```

```
Level: 1
```

```
1 2 3
```

```
4 6
```

```
7 5 8
```

```
Level: 2
```

```
1 2 3
```

```
4 5 6
```

```
7 8
```

```
Level: 3
```

```
1 2 3
```

```
4 5 6
```

```
7 8
```

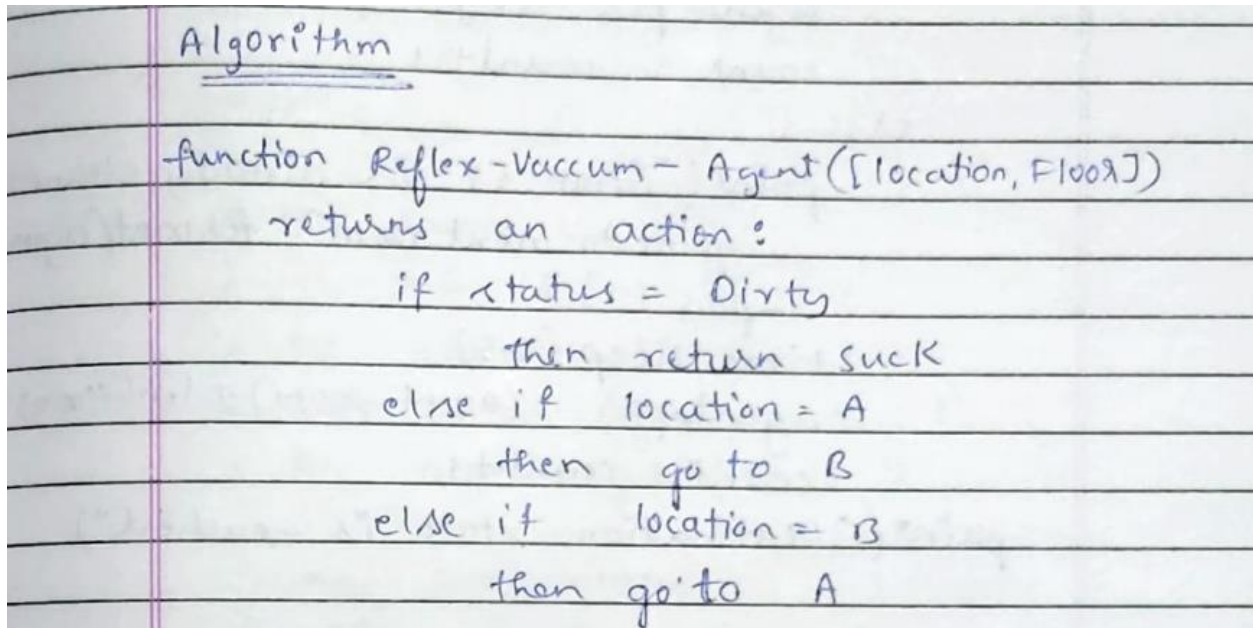
```
Success
```

```
D:\Shashanka G\puzzle8_astart>
```

Date: 7/12/22

Program 5: Implement vacuum cleaner agent.

Algorithm:



Algorithm

```

function Reflex-Vacuum-Agent([location, Floor])
  returns an action:
    if status = Dirty
      then return suck
    else if location = A
      then go to B
    else if location = B
      then go to A
  
```

CODE

```
import time
```

```

def clean(floor, agent_pos):
    count = 0
    print()
    print("Initial room status")
    print_floor(floor)
    agent_pos = (agent_pos - 1) % len(floor)
    while count < len(floor):
        if all([x == 0 for x in floor]):
            print()
            print("All rooms are cleaned")
            print()
            break
        # if room is dirty
        if floor[agent_pos] == 1:
            print()
            print("Room { } is dirty. Agent is cleaning now".format(agent_pos + 1))
            time.sleep(2.5)
            floor[agent_pos] = 0
    
```

```

    print_floor(floor)
    agent_pos = (agent_pos+1) % len(floor)
    count = count+1
# If room is cleaned
else:
    print("Room { } is already cleaned, going to next room".format(agent_pos+1))
    time.sleep(0.5)
    agent_pos = (agent_pos+1)%len(floor)
    count = count+1
print("Destination state is reached")

def print_floor(floor):
    status_map = {0:"CLEAN",1:"DIRTY"}
    for i in range(len(floor)):
        print("Room { } ".format(i+1),end=' ')
    print()
    for i in range(len(floor)):
        print(status_map[floor[i]],end='\t')
    print()

def main():
    #Entre initial condition
    floor = [None,None]
    print("Enter room status\nDirty-->1 Clean-->0")
    floor[0] = int(input("Enter status of room 1:"))
    floor[1] = int(input("Enter status of room 2:"))
    agent_pos = int(input("Enter agent position:"))
    clean(floor,agent_pos)

main()

```

Output:

```
D:\Shashanka G\vaccume_cleaner>python vaccume_cleaner.py
Enter room status
Dirty-->1 Clean-->0
Enter status of room 1:1
Enter status of room 2:1
Enter agent position:1

Initial room status
Room 1 Room 2
DIRTY DIRTY

Room 1 is dirty. Agent is cleaning now
Room 1 Room 2
CLEAN DIRTY

Room 2 is dirty. Agent is cleaning now
Room 1 Room 2
CLEAN CLEAN
Destination state is reached
```

```
D:\Shashanka G\vaccume_cleaner>python vaccume_cleaner.py
Enter room status
Dirty-->1 Clean-->0
Enter status of room 1:1
Enter status of room 2:0
Enter agent position:2

Initial room status
Room 1 Room 2
DIRTY CLEAN

Room 2 is already cleaned, going to next room

Room 1 is dirty. Agent is cleaning now
Room 1 Room 2
CLEAN CLEAN
Destination state is reached
```

Date: 28/12/22

Program 6: Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm and output



Date : _____

Page No : _____

Algorithm

function entailment(KB, α) return true or false

inputs KB , the knowledge base

symbols \leftarrow a list of preposition symbols

function checkall(KB, α , symbol, model)
returns true or false

if empty(symbols) then

if $PLTRUE ? (KB, model)$

then return true

else do

$p \leftarrow First(symbols)$

$rest \leftarrow REST(symbols)$

return checkall(KB, α , rest, model)

and

checkall(KB, α , rest, model)

O/p: Enter rule: $(p \vee q) \wedge (\neg q \vee r)$

Enter query: $p \wedge q$

knowledge base does not entail query

Code:

T = True

F = False

combinations = [

(T,T,T),

(T,T,F),

(T,F,T),

(T,F,F),

(F,T,T),

(F,T,F),

(F,F,T),

(F,F,F)]

variable = {"p":0,'q':1,"r":2}

kb=""

```
q=""
```

```
priority={'~':3,'^':2,'v':1}
```

```
def input_rules():
```

```
    global kb,q
```

```
    kb = input("Knowlwdge base:")
```

```
    q=input("query:")
```

```
def entailment():
```

```
    global kb,q
```

```
    print("*10+\"Truth table reference\"+\""*10)
```

```
    print('kb  $\alpha$ ')
```

```
    print("-"*10)
```

```
    for combination in combinations:
```

```
        s = evaluatePostfix(toPostfix(kb),combination)
```

```
f = evaluatePostfix(toPostfix(kb),combination)
```

```
print(s,f)
```

```
if s is True and f is False:
```

```
    return False
```

```
    return True
```

```
def isOperand(c):
```

```
    return c.isalpha() and c!='v'
```

```
def isLeftParanthesis(c):
```

```
    return ')' == c
```

```
def isRightParanthesis(c):
```

```
    return ')' == c
```

```
def isEmpty(stack):
```

```
return len(stack)==0
```

```
def peek(stack):
```

```
    return stack[-1]
```

```
def hasLessOrEqualPriority(c1,c2):
```

```
    try:
```

```
        return priority[c1]<=priority[c2]
```

except KeyError:

return False

def toPostfix(infix):

stack = []

postfix = ""

for c in infix:

if isOperand(c):

postfix += c

else:

if isLeftParanthesis(c):

stack.append(c)

elif isRightParanthesis(c):

operator = stack.pop()

while not isLeftParanthesis(operator):

postfix += operator

operator = stack.pop()

else:

while (not isEmpty(stack)) and hasLessOrEqualPriority(c, peek(stack)):

postfix += stack.pop()

stack.append(c)

while (not isEmpty(stack)):

postfix += stack.pop()

return postfix

```
def evaluatePostfix(exp, comb):
```

```
    stack = []
```

```
    for i in exp:
```

```
        if isOperand(i):
```

```
            stack.append(comb[variable[i]])
```

```
        elif i == '~':
```

```
            val1 = stack.pop()
```

```
            stack.append(not val1)
```

else:

val1 = stack.pop()

val2 = stack.pop()

stack.append(_eval(i, val2, val1))

return stack.pop()

def _eval(i, val1, val2):

if i == '^':

return val2 and val1

return val2 or val1

input_rules()

ans = entailment()

if ans:

print("The Knowledge Base entails query")

print(" KB \models α ")

else:

```
print("The Knowledge Base does not entail query")
```

```
print("\n")
```

30

Output:

```
D:\Shashanka G\27-12-2022>python main.py
```

```
Knowlwdge base: $p \wedge q \wedge r$ 
```

```
query: $p \vee q$ 
```

```
Truth table reference
```

```
kb    $\alpha$ 
```

```
-----
```

```
True True
```

```
False False
```

```
False False
```

```
False False
```

```
False False
```

```
False False
```

```
False False
```

```
False False
```

```
The Knowledge Base entails query
```

```
KB  $\models \alpha$ 
```


Date: 3/1/23

Program 7: Create a knowledge base using propositional logic and prove the given query using resolution

Algorithm:

Create KB using propositional logic and prove the given query using resolution.

Algorithm

function PL-RESOLUTION(KB, α)
returns true or false

inputs: KB, the knowledge base, a sentence in propositional logic

clause \leftarrow the set of clauses in CNF representation of KB and
new $\leftarrow \{\}$

loop do

for each pair of clauses (P, Q) in clause
resolvents \leftarrow PL-RESOLVE (P, Q)

if resolvent contains the priority clause then return true

new \leftarrow new \cup resolvents

if new clause then return false

clause \leftarrow clause \cup new

Code:

```
def disjunctify(clauses):
    disjuncts = []
    for clause in clauses:
        disjuncts.append(tuple(clause.split('v')))
    return disjuncts

def getResolvent(ci, cj, di, dj):
    resolvent = list(ci) + list(cj)
    resolvent.remove(di)
    resolvent.remove(dj)
    return tuple(resolvent)

def resolve(ci, cj):
    for di in ci:
        for dj in cj:
            if di == '~' + dj or dj == '~' + di:
                return getResolvent(ci, cj, di, dj)

def checkResolution(clauses, query):
    clauses += [query if query.startswith('~') else '~' + query]
    proposition = '^'.join(['(' + clause + ')'] for clause in clauses)
    print(f'Trying to prove {proposition} by contradiction....')

    clauses = disjunctify(clauses)
    resolved = False
    new = set()

    while not resolved:
        n = len(clauses)
        pairs = [(clauses[i], clauses[j]) for i in range(n) for j in range(i + 1, n)]
        for (ci, cj) in pairs:
            resolvent = resolve(ci, cj)
            if not resolvent:
                resolved = True
                break
            new = new.union(set(resolvents))
        if new.issubset(set(clauses)):
            break
        for clause in new:
            if clause not in clauses:
                clauses.append(clause)
```

```
if resolved:
    print('Knowledge Base entails the query, proved by resolution')
else:
    print("Knowledge Base doesn't entail the query, no empty set produced after resolution")
```

#Test Case 1

```
clauses = input('Enter the clauses ').split()
query = input('Enter the query: ')
checkResolution(clauses, query)
```

Output:

```
Enter the clauses ~Qv~PvR ~Q^P Q
Enter the query: Q
Trying to prove (~Qv~PvR)^(~Q^P)^(Q)^(~Q) by contradiction....
Knowledge Base entails the query, proved by resolution
```

Date: 10/1/23

Program 8: Implement unification in first order logic.

Algorithm:

17/01/2023

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Problem Statement: Implementing unification in first order logic

Algorithm

function $unify(x, y, \theta)$ returns a substitution to make x & y identical

Inputs: x : a variable, const, list or compound
 y : a variable, const, list or compound
 θ : the substitution built up so far

if $\theta = failure$ then return failure
else if $x = y$ then return θ
else if variable $?(x)$ then return $unify-var(x, y, \theta)$
else if variable $?(y)$ then return $unify-var(y, x, \theta)$
else if compound $?(x)$ and compound $?(y)$ then
return $unify(Args(x), Args(y), unify(OP(x), OP(y), \theta))$
else if List $?(x)$ and List $?(y)$ then
return $unify(REST(x), REST(y), unify(First(x), First(y), \theta))$
else return failure

function $unify-var(var, x, \theta)$ return a substitution

Inputs: var , a variable
 x , any expression
 θ , the substitution build up so far



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```
if { var/val } ∈ Θ then return unify(val,  
    x, Θ)  
else if { x/val } ∈ Θ then return unify(var,  
    val, Θ)  
else if occur-check?(var, x) then return  
    failure  
else return add { var/x } to Θ
```

a/p:

```
#1 exp1 = "pmof(c, p)" # c-country, p-person  
exp2 = "pmof(India, Modi)"  
subs = unify(exp1, exp2)  
print('Substitutions')  
&
```

Substitutions:

(India / c , modi / p)

```
#2 exp1 = "pmof(c, p)"  
exp2 = "pmof(c, p)"  
subs = unify(exp1, exp2)
```

Substitutions:

[] # Since no need to change

(x)

```
#3 exp1 = "King(x)"  
exp2 = "King(John)"
```

Substitutions:

[John / x]

✓
✓
✓

Code

```
import re
```

```
def getAttributes(expr):
```

```
    expr = expr.split("(")[1:]
```

```
    expr = "(" + ".join(expr)
```

```
    expr = expr[:-1]
```

```
    expr = re.split("(?<!.),(?!.)", expr)
```

```
    return expr
```

```
def getInitialPredicate(expr):
```

```
    return expr.split("(")[0]
```

```
def isConstant(char):
```

```
    return char.isupper() and len(char) == 1
```

```
def isVariable(char):
```

```
    return char.islower() and len(char) == 1
```

```
def replaceAttributes(expr, old, new):
```

```
    attr = getAttributes(expr)
```

```
    for index, val in enumerate(attr):
```

```
        if val == old:
```

```
            attr[index] = new
```

```
    predicate = getInitialPredicate(expr)
```

```
    return predicate + "(" + " ".join(attr) + ")"
```

```
def apply(expr, subs):
```

```
    for sub in subs:
```

```
        new, old = sub #substitution is a tuple of 2 values (new, old)
```

```
        expr = replaceAttributes(expr, old, new)
```

```
    return expr
```

```
def checkOccurs(var, expr):
```

```
    if expr.find(var) == -1:
```

```
        return False
```

```
    return True
```

```
def getFirstPart(expr):
```

```
    attr = getAttributes(expr)
```

```
    return attr[0]
```

```
def getRemainingPart(expr):
```

```
predicate = getInitialPredicate(expr)
attr = getAttributes(expr)
newExpr = predicate + "(" + ",".join(attr[1:]) + ")"
return newExpr
```

```
def unify(exp1, exp2):
    if exp1 == exp2:
        return []

    if isConstant(exp1) and isConstant(exp2):
        if exp1 != exp2:
            return False

    if isConstant(exp1):
        return [(exp1, exp2)]

    if isConstant(exp2):
        return [(exp2, exp1)]

    if isVariable(exp1):
        if checkOccurs(exp1, exp2):
            return False
        else:
            return [(exp2, exp1)]

    if isVariable(exp2):
        if checkOccurs(exp2, exp1):
            return False
        else:
            return [(exp1, exp2)]

    if getInitialPredicate(exp1) != getInitialPredicate(exp2):
        print("Cannot be unified")
        return False

    attributeCount1 = len(getAttributes(exp1))
    attributeCount2 = len(getAttributes(exp2))
    if attributeCount1 != attributeCount2:
        return False

    head1 = getFirstPart(exp1)
    head2 = getFirstPart(exp2)
    initialSub = unify(head1, head2)
    if not initialSub:
        return False
```

```

if attributeCount1 == 1:
    return initialSub

tail1 = getRemainingPart(exp1)
tail2 = getRemainingPart(exp2)

if initialSub != []:
    tail1 = apply(tail1, initialSub)
    tail2 = apply(tail2, initialSub)

remainingSub = unify(tail1, tail2)
if not remainingSub:
    return False

initialSub.extend(remainingSub)
res = []
for tup in initialSub:
    st = ' / '.join(tup)
    res.append(st)

return res

```

#Test Case 1

```

exp1 = "pmof(c,p)" # c--->country p--->person
exp2 = "pmof(c,p)"
subs = unify(exp1, exp2)
print("Substitutions:")
print(subs)

```


Output:

a/p:

#1 $exp1 = "pmof(c, p)"$ # c-country, p-person
 $exp2 = "pmof(India, modi)"$

$subs = unify(exp1, exp2)$

$print('substitutions')$

&

substitutions:

$(India / c, modi / p)$

#2 $exp1 = "pmof(c, p)"$

$exp2 = "pmof(c, p)"$

$subs = unify(exp1, exp2)$

substitutions:

$[]$ # Since no need to change

(x)

#3 $exp1 = "King(x)"$

$exp2 = "King(John)"$

substitutions:

$[John / x]$

Date: 10/1/23

Program 9: Convert given first order logic statement into Conjunctive Normal Form (CNF).

Algorithm:

FOL TO CNF Algorithm

8 FOL to CNF

1. Eliminate \leftrightarrow , replace $A \leftrightarrow B$ by
 $(A \Rightarrow B) \wedge (B \Rightarrow A)$

2. Eliminate \Rightarrow , replace $A \Rightarrow B$ by
 $\neg A \vee B$

3. Move \neg Inwards

$$\neg(\forall x p) \equiv \exists x \neg p$$

$$\neg(\exists x p) \equiv \forall x \neg p$$

$$\neg(\alpha \vee \beta) \equiv \neg \alpha \wedge \neg \beta$$

$$\neg(\alpha \wedge \beta) \equiv \neg \alpha \vee \neg \beta$$

$$\neg(\neg \alpha) \equiv \alpha$$

4. Standardize variables apart by them: each quantifier should use different variable.

5. Skolemization: Each existential variable is replaced by skolem constant or skolem function of the enclosing universally quantified variables.

eg: $\exists x \text{ Rich}(x)$ becomes $\text{Rich}(a)$

6. Drop universal quantifiers

eg: $\forall x \text{ Person}$ becomes $\text{Person}(x)$

7) Distribute \wedge over \vee :

$$(\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee \gamma) \wedge (\beta \vee \gamma)$$

Code:

```

def getAttributes(string):
    expr = '
    ,
    matches = re.findall(expr, string)
    return [m for m in str(matches) if m.isalpha()]

def getPredicates(string):
    expr = '[a-z~]+'
    ,
    return re.findall(expr, string)

def DeMorgan(sentence):
    string = ''.join(list(sentence).copy())
    string = string.replace('~~', '')
    flag = '[' in string
    string = string.replace('~[', '')
    string = string.strip(']')
    for predicate in getPredicates(string):
        string = string.replace(predicate, f'~{predicate}')
    s = list(string)
    for i, c in enumerate(string):
        if c == '|':
            s[i] = '&'
        elif c == '&':
            s[i] = '|'
    string = ''.join(s)
    string = string.replace('~~', '')
    return f'[{string}]' if flag else string

def Skolemization(sentence):
    SKOLEM_CONSTANTS = [f'{chr(c)}' for c in range(ord('A'), ord('Z')+1)]
    statement = ''.join(list(sentence).copy())
    matches = re.findall('[\forall\exists].', statement)
    for match in matches[:-1]:
        statement = statement.replace(match, '')
        statements = re.findall('
    ], statement)
    for s in statements:
        statement = statement.replace(s, s[1:-1])
    for predicate in getPredicates(statement):
        attributes = getAttributes(predicate)
        if ''.join(attributes).islower():
            statement = statement.replace(match[1], SKOLEM_CONSTANTS.pop(0))
        else:
            aL = [a for a in attributes if a.islower()]
            aU = [a for a in attributes if not a.islower()][0]
            statement = statement.replace(aU, f'{SKOLEM_CONSTANTS.pop(0)}({aL[0] if len(aL) else match[1]})')
    return statement

```

```
import re
```

```
def fol_to_cnf(fol):
```

```
    statement = fol.replace("<=>", "_")
```

```
    while '_' in statement:
```

```
        i = statement.index('_')
```

```
        new_statement = '[' + statement[:i] + '=>' + statement[i+1:] + ']&[' + statement[i+1:] + '=>' + statement[:i] + ']'
```

```
        statement = new_statement
```

```
    statement = statement.replace("=>", "-")
```

```
    expr = '
```

```
    statements = re.findall(expr, statement)
```

```
    for i, s in enumerate(statements):
```

```
        if '[' in s and ']' not in s:
```

```
            statements[i] += ']'
```

```
    for s in statements:
```

```
        statement = statement.replace(s, fol_to_cnf(s))
```

```
    while '-' in statement:
```

```
        i = statement.index('-')
```

```
        br = statement.index('[') if '[' in statement else 0
```

```
        new_statement = '~' + statement[br:i] + '|' + statement[i+1:]
```

```
        statement = statement[:br] + new_statement if br > 0 else new_statement
```

```
    while '~∀' in statement:
```

```
        i = statement.index('~∀')
```

```
        statement = list(statement)
```

```
        statement[i], statement[i+1], statement[i+2] = '∃', statement[i+2], '~'
```

```
        statement = ''.join(statement)
```

```
    while '~∃' in statement:
```

```
        i = statement.index('~∃')
```

```
        s = list(statement)
```

```
        s[i], s[i+1], s[i+2] = '∀', s[i+2], '~'
```

```
        statement = ''.join(s)
```

```
    statement = statement.replace('~[∀', '[~∀')
```

```
    statement = statement.replace('~[∃', '[~∃')
```

```
    expr = '([~∀|∃].)'
```

```
    statements = re.findall(expr, statement)
```

```
    for s in statements:
```

```
        statement = statement.replace(s, fol_to_cnf(s))
```

```
    expr = '~'
```

```
    statements = re.findall(expr, statement)
```

```
    for s in statements:
```

```
        statement = statement.replace(s, DeMorgan(s))
```

```
    return statement
```

```
#Interactive Test Cases
```

```
n = int(input())
```

```
while n:
```

```
    statement = input("Enter FOL statement: ")
```

```
    print(f"FOL converted to CNF: {Skolemization(fol_to_cnf(statement))} \n\n")
```

```
    n -= 1
```

Output

$$\alpha \Rightarrow \beta \equiv \neg \alpha \vee \beta$$

$$\alpha \Leftrightarrow \beta \equiv (\alpha \Rightarrow \beta) \wedge (\beta \Rightarrow \alpha)$$

$$= (\neg \alpha \vee \beta) \wedge (\neg \beta \vee \alpha)$$



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Q1P:

* FOL : $[\text{american}(x) \Rightarrow \text{white}(x)]$

CNF : $[\neg \text{american}(x) \vee \text{white}(x)]$

* FOL : $\forall x [\text{american}(x) \Rightarrow \text{white}(x)]$

CNF : $[\neg \text{american}(A) \vee \text{white}(A)]$

↳ substituting skolem constant

* FOL : $\text{likes}(n, x) \Leftrightarrow \text{likes}(s, x)$

CNF : $[\neg \text{likes}(n, x) \vee \neg \text{likes}(s, x)] \vee$
 $[\text{likes}(n, x) \vee \text{likes}(s, x)]$

Date: 10/1/23

Program 10: Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

Algorithm:

Forward Reasoning Algorithm.

function FOL-FC-ASK(KB, α) returns a
a substitution or false
repeat until new is empty
new $\leftarrow \{\}$

for each sentence α in KB do
 $(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{standardize-apart}(\alpha)$

for each θ such that $(p_1 \wedge \dots \wedge p_n)\theta$
 $= (p'_1 \wedge \dots \wedge p'_n)\theta$ for some
 $p'_1 \dots p'_n$ in KB

$q' \leftarrow \text{subst}(\theta, q)$

if q' is not a renaming of a
sentence already in KB or new then
do

add q' to new

$\phi \leftarrow \text{Unify}(q', \alpha)$

if ϕ is not fail then return ϕ

add new to KB

return false.

Code:

```

import re
def isVariable(x):
    return len(x) == 1 and x.islower() and x.isalpha()

def getAttributes(string):
    expr = '\([^)]+\)'
    matches = re.findall(expr, string)
    return matches

def getPredicates(string):
    expr = '([a-z~]+\)\([^&]+\)'
    return re.findall(expr, string)

class Fact:
    def __init__(self, expression):
        self.expression = expression
        predicate, params = self.splitExpression(expression)
        self.predicate = predicate
        self.params = params
        self.result = any(self.getConstants())

    def splitExpression(self, expression):
        predicate = getPredicates(expression)[0]
        params = getAttributes(expression)[0].strip('(').split(',')
        return [predicate, params]

    def getResult(self):
        return self.result

    def getConstants(self):
        return [None if isVariable(c) else c for c in self.params]

    def getVariables(self):
        return [v if isVariable(v) else None for v in self.params]

    def substitute(self, constants):
        c = constants.copy()
        f = f'{self.predicate}{'.'.join([constants.pop(0) if isVariable(p) else p for p in self.params])}'
        return Fact(f)

class Implication:
    def __init__(self, expression):
        self.expression = expression
        l = expression.split('=>')
        self.lhs = [Fact(f) for f in l[0].split('&')]
        self.rhs = Fact(l[1])

    def evaluate(self, facts):
        constants = {}

```

```

new_lhs = []
for fact in facts:
    for val in self.lhs:
        if val.predicate == fact.predicate:
            for i, v in enumerate(val.getVariables()):
                if v:
                    constants[v] = fact.getConstants()[i]
            new_lhs.append(fact)
    predicate, attributes = getPredicates(self.rhs.expression)[0],
str(getAttributes(self.rhs.expression)[0])
    for key in constants:
        if constants[key]:
            attributes = attributes.replace(key, constants[key])
    expr = f'{predicate}{attributes}'
    return Fact(expr) if len(new_lhs) and all([f.getResult() for f in new_lhs]) else None

```

```

class KB:
    def __init__(self):
        self.facts = set()
        self.implications = set()

    def tell(self, e):
        if '=>' in e:
            self.implications.add(Implication(e))
        else:
            self.facts.add(Fact(e))
        for i in self.implications:
            res = i.evaluate(self.facts)
            if res:
                self.facts.add(res)

    def query(self, e):
        facts = set([f.expression for f in self.facts])
        i = 1
        print(f'Querying {e}:')
        for f in facts:
            if Fact(f).predicate == Fact(e).predicate:
                print(f'\t{i}. {f}')
                i += 1

    def display(self):
        print("All facts: ")
        for i, f in enumerate(set([f.expression for f in self.facts])):
            print(f'\t{i+1}. {f}')

```

#Test Case 1

```

kb = KB()
kb.tell('missile(x)=>weapon(x)')
kb.tell('missile(M1)')
kb.tell('enemy(x,America)=>hostile(x)')
kb.tell('american(West)')
kb.tell('enemy(Nono,America)')

```

```
kb.tell('owns(Nono,M1)')
kb.tell('missile(x)&owns(Nono,x)=>sells(West,x,Nono)')
kb.tell('american(x)&weapon(y)&sells(x,y,z)&hostile(z)=>criminal(x)')
kb.query('criminal(x)')
kb.display()
```

#Test Case 2

```
kb_ = KB()
kb_.tell('king(x)&greedy(x)=>evil(x)')
kb_.tell('king(John)')
kb_.tell('greedy(John)')
kb_.tell('king(Richard)')
kb_.query('evil(x)')
```

Output:

```
Querying evil(x):
  1. evil(John)
```