

Q.1 - Q.5 carry one mark each.

Q.1 The expenditure on the project _____ as follows: equipment Rs.20 lakhs, salaries Rs.12 lakhs, and contingency Rs.3 lakhs.

- | | |
|----------------|-----------------|
| (A) break down | (C) breaks down |
| (B) break | (D) breaks |

Q.2 The search engine's business model _____ around the fulcrum of trust.

- | | |
|--------------|------------|
| (A) revolves | (C) sinks |
| (B) plays | (D) bursts |

Q.3 Two cars start at the same time from the same location and go in the same direction. The speed of the first car is 50 km/h and the speed of the second car is 60 km/h. The number of hours it takes for the distance between the two cars to be 20 km is _____.

- | | |
|-------|-------|
| (A) 1 | (C) 3 |
| (B) 2 | (D) 6 |

Q.4 Ten friends planned to share equally the cost of buying a gift for their teacher. When two of them decided not to contribute, each of the other friends had to pay Rs. 150 more. The cost of the gift was Rs. _____.

- | | |
|----------|-----------|
| (A) 666 | (C) 6000 |
| (B) 3000 | (D) 12000 |

Q.5 A court is to a judge as _____ is to a teacher.

- | | |
|------------------|----------------|
| (A) a student | (C) a syllabus |
| (B) a punishment | (D) a school |

Q.6 to Q.10 carry two marks each.

Q.6. The police arrested four criminals P, Q, R, and S. The criminals knew each other. They made the following statements:

P says "Q committed the crime"

Q says "S committed the crime"

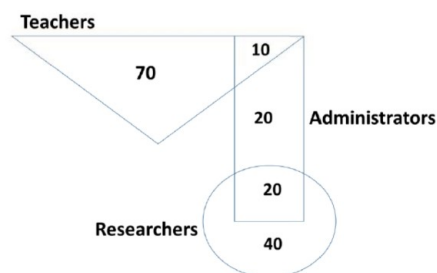
R says "I did not do it."

S says "What Q said about me is false."

Assume only one of the arrested four committed the crime and only one of the statements made above is true. Who committed the crime?

- (A) P (C) S
(B) R (D) Q

Q.7. In the given diagram, teachers are represented in the triangle, researchers in the circle and administrators in the rectangle. Out of the total number of the people, the percentage of administrators shall be in the range of ----.



- (A) 0 to 15 (C) 31 to 45
(B) 16 to 30 (D) 46 to 60
- Q.8.** "A recent High Court judgement has sought to dispel the idea of begging as a disease which leads to its stigmatization and criminalization and to regard it as a symptom. The underlying disease is the failure of the state to protect citizens who fall through the social security net."
- Which one of the following statements can be inferred from the given passage?
- (A) Beggars are lazy people who beg because they are unwilling to work
(B) Beggars are created because of the lack of social welfare schemes
(C) Begging is an offence that has to be dealt with firmly
(D) Begging has to be banned because it adversely affects the welfare of the state
- Q.9.** In a college, there are three student clubs. Sixty students are only in the Drama club, 80 students are only in the Dance club, 30 students are only in the Maths club, 40 students are in both Drama and Dance clubs, 12 students are in both Dance and Maths clubs, 7 students are in both Drama and Maths clubs, and 22 students are in all the clubs. If 75% of the students in the college are not in any of these clubs, then the total number of students in the college is ----.
- (A) 1000 (C) 900
(B) 975 (D) 225

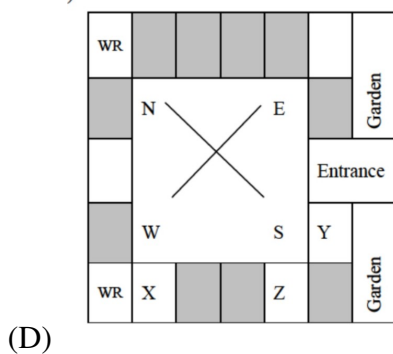
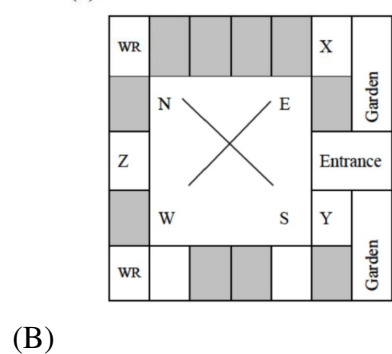
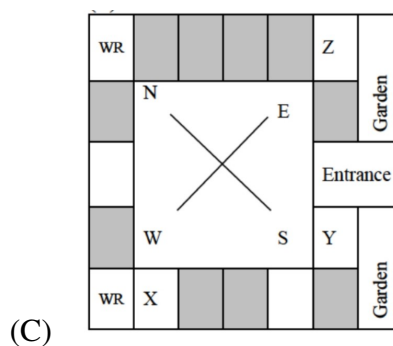
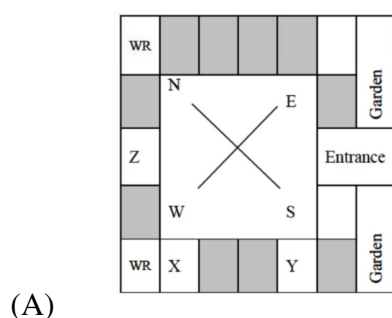
Q.10. Three of the five students allocated to a hostel put in special requests to the warden. Given the floor plan of the vacant rooms, select the allocation plan that will accommodate all their requests.

Request by X: Due to pollen allergy, I want to avoid a wing next to the garden.

Request by Y: I want to live as far from the washrooms as possible, since I am very sensitive to smell.

Request by Z: I believe in Vaastu and so want to stay in the South-west wing.

The shaded rooms are already occupied. WR is washroom.



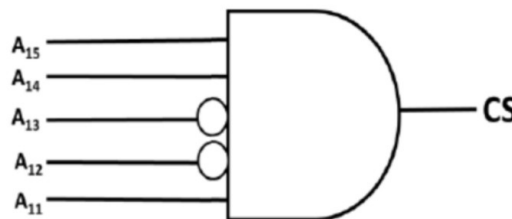
END OF THE QUESTION PAPER

Q.1 - Q.25 carry one mark each.

Q.1 A certain processor uses a fully associative cache of size 16 kB. The cache block size is 16 bytes. Assume that the main memory is byte addressable and uses a 32-bit address. How many bits are required for the *Tag* and the *Index* fields respectively in the addresses generated by the processor?

- (A) 24 bits and 0 bits (C) 28 bits and 1 bit
(B) 25 bits and 4 bits (D) 28 bits and 0 bits

Q.2 The chip select logic for a certain DRAM chip in a memory system design is shown below. Assume that the memory system has 16 address lines denoted by A_{15} to A_0 . What is the range of addresses (in hexadecimal) of the memory system that can get enabled by the chip select (CS) signal?



- (A) C800 to CFFF (C) C800 to C8FF
(B) CA00 to CAFF (D) D400 to DFFF

Q.3 Which one of the following kinds of derivation is used by LR parsers?

- (A) Leftmost (C) Rightmost
(B) Leftmost in reverse (D) Rightmost in reverse

Q.4 In 16-bit 2's complement representation, the decimal number -28 is:

- (A) 1111 1111 0001 1100 (C) 1111 1111 0001 1101
(B) 0000 0000 1110 0011 (D) 1000 0000 0001 1100

Q.5 Let $U = \{1, 2, \dots, n\}$. Let $A = \{(x, X) | x \in X, X \subseteq U\}$. Consider the following two statements on $|A|$.

I. $|A| = n2^{n-1}$

II. $|A| = \sum_{k=1}^n k \binom{n}{k}$

Which of the above statements is/are TRUE?

- (A) Only I (C) Both I and II
 (B) Only II (D) Neither I nor II

Q.6 Which one of the following is *NOT* a valid identity?

- (A) $(x \oplus y) \oplus z = x \oplus (y \oplus z)$ (C) $x \oplus y = x + y$, if $xy = 0$
 (B) $(x + y) \oplus z = x \oplus (y + z)$ (D) $x \oplus y = (xy + x'y')'$

Q.7 If L is a regular language over $\Sigma = \{a, b\}$, which one of the following languages is NOT regular?

- (A) $L \cdot L^R = \{xy \mid x \in L, y^R \in L\}$
 (B) $\{ww^R \mid w \in L\}$
 (C) Prefix $(L) = \{x \in \Sigma^* \mid \exists y \in \Sigma^* \text{ such that } xy \in L\}$
 (D) Suffix $(L) = \{y \in \Sigma^* \mid \exists x \in \Sigma^* \text{ such that } xy \in L\}$

Q.8 Consider $Z = X - Y$, where X , Y and Z are all in sign-magnitude form. X and Y are each represented in n bits. To avoid overflow, the representation of Z would require a minimum of:

- (A) n bits (C) $n + 1$ bits
 (B) $n - 1$ bits (D) $n + 2$ bits

Q.9 Let X be a square matrix. Consider the following two statements on X .

- I. X is invertible.
 II. Determinant of X is non-zero.

Which one of the following is TRUE?

- (A) I implies II; II does not imply I. (C) I does not imply II; II does not imply I.
 (B) II implies I; I does not imply II. (D) I and II are equivalent statements.

Q.10 Let G be an arbitrary group. Consider the following relations on G :

$$R_1: \forall a, b \in G, a R_1 b \iff \exists g \in G \text{ such that } a = g^{-1}bg \quad (1)$$

$$R_2: \forall a, b \in G, a R_2 b \iff a = b^{-1} \quad (2)$$

$$(3)$$

Which of the above is/are equivalence relation/relation(s)?

- (A) R_1 and R_2 (C) R_2 only
 (B) R_1 only (D) Neither R_1 nor R_2

Q.11 Consider the following two statements about database transaction schedules:

- I. Strict two-phase locking protocol generates conflict serializable schedules that are also recoverable.
 II. Timestamp-ordering concurrency control protocol with Thomas' Write Rule can generate view serializable schedules that are not conflict serializable.

Which of the above statements is/are TRUE?

- (A) I only (C) Both I and II
 (B) II only (D) Neither I nor II

Q.12 Let G be an undirected complete graph on n vertices, where $n > 2$. Then, the number of different Hamiltonian cycles in G is equal to

- (A) $n!$ (C) 1
 (B) $(n-1)!$ (D) $\frac{(n-1)!}{2}$

Q.13 Compute

$$\lim_{x \rightarrow 3} \frac{x^4 - 81}{2x^2 - 5x - 3}$$

- (A) 1 (C) 108/7
 (B) 53/12 (D) Limit does not exist

Q.14 Which one of the following statements is *NOT* correct about the B+ tree data structure used for creating an index of a relational database table?

- (A) B+ Tree is a height-balanced tree (C) Key values in each node are kept in sorted order
 (B) Non-leaf nodes have pointers to data records (D) Each leaf node has a pointer to the next leaf node

Q.15 For $\Sigma = \{a, b\}$, let us consider the regular language $L = \{x \mid x = a^{2+3k} \text{ or } x = b^{10+12k}, k \geq 0\}$. Which one of the following can be a pumping length (the constant guaranteed by the pumping lemma) for L ?

- (A) 3 (C) 9
(B) 5 (D) 24

Q.16 Which of the following protocol pairs can be used to send and retrieve e-mails (in that order)?

- (A) IMAP, POP3 (C) SMTP, MIME
(B) SMTP, POP3 (D) IMAP, SMTP

Q.17 The following C program is executed on a Unix/Linux system:

```
#include <unistd.h>
int main()
{
    int i;
    for (i = 0; i < 10; i++)
        if (i % 2 == 0) fork();
    return 0;
}
```

The total number of child processes created is _____.

Q.18 Consider the following C program:

```
#include <stdio.h>
int jumble(int x, int y){
    x = 2 * x + y;
    return x;
}

int main(){
    int x = 2, y = 5;
    y = jumble(y, x);
    x = jumble(y, x);
    printf("%d\n", x);
    return 0;
}
```

The value printed by the program is _____.

Q.19 Consider the grammar given below:

$$S \rightarrow Ab$$

$$A \rightarrow BD$$

$$B \rightarrow b \mid \epsilon$$

$$D \rightarrow d \mid \epsilon$$

Let a, b, d , and $\$$ be indexed as follows:

Symbol	a	b	d	$\$$
Index	3	2	1	0

Compute the FOLLOW set of the non-terminal B and write the index values for the symbols in the FOLLOW set in the descending order. (For example, if the FOLLOW set is $a, b, d, \$$, then the answer should be 3210)

Answer: _____

Q.20 An array of 25 distinct elements is to be sorted using quicksort. Assume that the pivot element is chosen uniformly at random. The probability that the pivot element gets placed in the worst possible location in the first round of partitioning (rounded off to 2 decimal places) is _____.

Q.21 The value of $3^{31} \bmod 5$ is _____.

Q.22 Two numbers are chosen independently and uniformly at random from the set $\{1, 2, \dots, 13\}$. The probability (rounded off to 3 decimal places) that their 4-bit (unsigned) binary representations have the same most significant bit is _____.

Q.23 Consider three concurrent processes P1, P2 and P3 as shown below, which access a shared variable D that has been initialized to 100.

P1	P2	P3
$D = D + 20$	$D = D - 50$	$D = D + 10$

The processes are executed on a uniprocessor system running a time-shared operating system. If the minimum and maximum possible values of D after the three processes have completed execution are X and Y respectively, then the value of $Y - X$ is _____.

Q.24 Consider the following C program:

```
#include <stdio.h>
```



```
int main() {
    int arr[] = {1,2,3,4,5,6,7,8,9,0,1,2,5}, *ip=arr+4;
    printf("%d\n", ip[1]);
    return 0;
}
```

The number that will be displayed on execution of the program is

Q.25 Consider a sequence of 14 elements: $A = [-5, -10, 6, 3, -1, -2, 13, 4, -9, -1, 4, 12, -3, 0]$.

The subsequence sum $S(i, j) = \sum_{k=i}^j A[k]$. Determine the maximum of $S(i, j)$, where $0 \leq i \leq j < 14$. (Divide and conquer approach may be used.)

Answer:

Q.26 Consider the following C function:

```
void convert(int n) {
    if (n <= 0)
        printf("%d", n);
    else {
        convert(n/2);
        printf("%d", n%2);
    }
}
```

Which one of the following will happen when the function convert is called with any positive integer n as argument?

- (A) It will print the binary representation of n and terminate
- (B) It will print the binary representation of n in the reverse order and terminate
- (C) It will print the binary representation of n but will not terminate
- (D) It will not print anything and will not terminate

Q.27 Consider the following C program:

```
#include <stdio.h>
int f() {
    static int num=7;
    return num--;
}

int main() {
```

```
for (f(); f(); f())  
    printf("%d", f());  
return 0;  
}
```

Which one of the following values will be displayed on execution of the program?

- (A) 41
- (B) 52
- (C) 63
- (D) 630

Q.28 Consider three machines M, N, and P with IP addresses 100.10.5.2, 100.10.5.5, and 100.10.5.6 respectively. The subnet mask is set to 255.255.255.252 for all three machines. Which one of the following is true?

- (A) M, N, and P all belong to the same subnet
- (B) Only M and N belong to the same subnet
- (C) Only M and P belong to the same subnet
- (D) M, N, and P belong to three different subnets

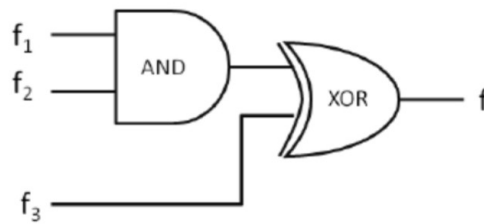
Q.29 Suppose that in an IP-over-Ethernet network, a machine X wishes to find the MAC address of another machine Y in its subnet. Which one of the following techniques can be used for this?

- (A) X sends an ARP request packet to the local gateway's IP address which then finds the MAC address of Y and sends to X
- (B) X sends an ARP request packet to the local gateway's MAC address which then finds the MAC address of Y and sends to X
- (C) X sends an ARP request packet with broadcast MAC address in its local subnet
- (D) X sends an ARP request packet with broadcast IP address in its local subnet

Q.30 Consider three 4-variable functions f_1 , f_2 , and f_3 , which are expressed in sum-of-minterms as

$$f_1 = \Sigma(0, 2, 5, 8, 14), \quad f_2 = \Sigma(2, 3, 6, 8, 14, 15), \quad f_3 = \Sigma(2, 7, 11, 14)$$

For the following circuit with one AND gate and one XOR gate, the output function f can be expressed as:



- (A) $\Sigma(7, 8, 11)$
- (B) $\Sigma(2, 7, 8, 11, 14)$
- (C) $\Sigma(2, 14)$
- (D) $\Sigma(0, 2, 3, 5, 6, 7, 8, 11, 14, 15)$

Q.31 Which one of the following languages over $\Sigma = \{a, b\}$ is **NOT** context-free?

- (A) $\{ww^R \mid w \in \{a, b\}^*\}$
- (B) $\{wa^n b^n w^R \mid w \in \{a, b\}^*, n \geq 0\}$
- (C) $\{wa^n w^R b^n \mid w \in \{a, b\}^*, n \geq 0\}$
- (D) $\{a^n b^i \mid i \in \{n, 3n, 5n\}, n \geq 0\}$

Q.32 Let the set of functional dependencies $F = \{QR \rightarrow S, R \rightarrow P, S \rightarrow Q\}$ hold on a relation schema $X = \{PQRS\}$. X is not in BCNF. Suppose X is decomposed into two schemas Y and Z , where $Y = \{PR\}$ and $Z = \{QRS\}$.

Consider the two statements given below.

- I. Both Y and Z are in BCNF
- II. Decomposition of X into Y and Z is dependency preserving and lossless

Which of the above statements is/are correct?

- (A) Both I and II
- (B) I only
- (C) II only
- (D) Neither I nor II

Q.33 Assume that in a certain computer, the virtual addresses are 64 bits long and the physical addresses are 48 bits long. The memory is word addressable. The page size is 8 KB and the word size is 4 bytes. The Translation Look-aside Buffer (TLB) in the address translation path has 128 valid entries. At most how many distinct virtual addresses can be translated without any TLB miss?

- (A) $16 \cdot 2^{10}$
- (B) $256 \cdot 2^{10}$
- (C) $4 \cdot 2^{20}$
- (D) $8 \cdot 2^{20}$

Q.34 Consider the following sets:

- S1. Set of all recursively enumerable languages over the alphabet $\{0, 1\}$
- S2. Set of all syntactically valid C programs
- S3. Set of all languages over the alphabet $\{0, 1\}$
- S4. Set of all non-regular languages over the alphabet $\{0, 1\}$

Which of the above sets are uncountable?

- (A) S1 and S2
- (B) S3 and S4
- (C) S2 and S3
- (D) S1 and S3

Q.35 Consider the first order predicate formula φ :

$$\forall x (\forall z x|z \Rightarrow (z = x \vee z = 1)) \Rightarrow \exists w (w > x \wedge (\forall z x|w \Rightarrow (w = z \vee z = 1)))$$

Here $a|b$ denotes 'a divides b', where a and b are integers. Consider the following sets:

- S1. $\{1, 2, 3, \dots, 100\}$
- S2. Set of all positive integers
- S3. Set of all integers

Which of the above sets satisfy φ ?

- (A) S1 and S2
- (B) S1 and S3
- (C) S2 and S3
- (D) S1, S2 and S3

Q.36 Consider the following grammar and the semantic actions to support the inherited type declaration attributes. Let X_1, X_2, X_3, X_4 and X_5 be the placeholders for the non-terminals D, T, L or L_1 in the following table:

Production rule	Semantic action
$D \rightarrow T L$	$X_1.type = X_2.type$
$T \rightarrow \text{int}$	$T.type = \text{int}$
$T \rightarrow \text{float}$	$T.type = \text{float}$
$L \rightarrow L_1, \text{id}$	$X_3.type = X_4.type;$ $\text{addType}(\text{id.entry}, X_5.type)$
$L \rightarrow \text{id}$	$\text{addType}(\text{id.entry}, X_3.type)$

Which one of the following are the appropriate choices for X_1, X_2, X_3 and X_4 ?

- (A) $X_1 = L, X_2 = T, X_3 = L, X_4 = L$
- (B) $X_1 = T, X_2 = L, X_3 = L, X_4 = T$
- (C) $X_1 = L, X_2 = L, X_3 = L, X_4 = T$
- (D) $X_1 = T, X_2 = L, X_3 = T, X_4 = L$

Q.37 There are n unsorted arrays: A_1, A_2, \dots, A_n . Assume that n is odd. Each of A_1, A_2, \dots, A_n contains n distinct elements. There are no common elements between any two arrays. The worst-case time complexity of computing the median of the medians of A_1, A_2, \dots, A_n is

- (A) $O(n)$
- (B) $O(n \log n)$
- (C) $O(n^2)$
- (D) $O(n^2 \log n)$

Q.38 Let G be any connected, weighted, undirected graph.

- I. G has a unique minimum spanning tree, if no two edges of G have the same weight.
- II. G has a unique minimum spanning tree, if for every cut of G , there is a unique minimum-weight edge crossing the cut.

Which of the above two statements is/are TRUE?

- (A) I only
- (B) II only
- (C) Both I and II
- (D) Neither I nor II

Q.39 Consider the following snapshot of a system running in n concurrent processes. Process i is holding X_i instances of a resource R , $1 \leq i \leq n$. Assume that all instances of R are currently in use. Further, for all i , process i can place a request for at most r_i additional instances of R while holding the X_i instances it already has. Of the n processes, there are exactly two processes p and q such that $Y_p = Y_q = 0$. Which one of the following conditions guarantees that no other process apart from p and q can complete execution?

- (A) $X_p + X_q < \min\{Y_k \mid 1 \leq k \leq n, k \neq p, k \neq q\}$
- (B) $X_p + X_q < \max\{Y_k \mid 1 \leq k \leq n, k \neq p, k \neq q\}$
- (C) $\min(X_p, X_q) \geq \min\{Y_k \mid 1 \leq k \leq n, k \neq p, k \neq q\}$
- (D) $\min(X_p, X_q) \leq \max\{Y_k \mid 1 \leq k \leq n, k \neq p, k \neq q\}$

Q.40 Consider the following statements:

- I. The smallest element in a max-heap is always at a leaf node
- II. The second largest element in a max-heap is always a child of the root node
- III. A max-heap can be constructed from a binary search tree in $\mathcal{O}(n)$ time
- IV. A binary search tree can be constructed from a max-heap in $\mathcal{O}(n)$ time

Which of the above statements are TRUE?

- (A) I, II and III
- (B) I and IV
- (C) II, III and IV
- (D) III and IV

Q.41 Consider the following four processes with arrival times (in milliseconds) and their length of CPU bursts (in milliseconds) as shown below:

Process	Arrival time	CPU burst time
P1	0	7
P2	1	3
P3	3	1
P4	4	2

These processes are run on a single processor using preemptive Shortest Remaining Time First scheduling algorithm. If the average waiting time of the processes is 1 millisecond, then the value of Z is _____

Q.42 The index node (inode) of a Unix-like file system has 12 direct, one single-indirect and one double-indirect pointers. The disk block size is 4 kB, and the disk block address is 32-bits long. The maximum possible file size is (rounded off to 1 decimal place) ____ GB.

Q.43 Consider the augmented grammar given below:

$$S' \rightarrow S$$

$$S \rightarrow \langle L \rangle \mid id$$

$$L \rightarrow L, S \mid S$$

Let $I_0 = \text{CLOSURE}(\{[S' \rightarrow \cdot S]\})$. The number of items in the set $\text{GOTO}(I_0, \langle \rangle)$ is ____.

Q.44 Consider the following matrix:

$$R = \begin{bmatrix} 1 & 2 & 4 & 8 \\ 1 & 3 & 9 & 27 \\ 1 & 4 & 16 & 64 \\ 1 & 5 & 25 & 125 \end{bmatrix}$$

The absolute value of the product of Eigen values of R is ____.

Q.45 A certain processor deploys a single-level cache. The cache block size is 8 words and the word size is 4 bytes. The memory system uses a 60-MHz clock. To service a cache miss, the memory controller first takes 1 cycle to accept the starting address of the block, it then takes 3 cycles to fetch all the eight words of the block, and finally transmits the words of the requested block at the rate of 1 word per cycle. The maximum bandwidth for the memory system when the program running on the processor issues a series of read operations is ____x10⁶ bytes/sec.

Q.46 Let T be a full binary tree with 8 leaves. (A full binary tree has every level full.) Suppose two leaves a and b of T are chosen uniformly and independently at random. The expected value of the distance between a and b in T (i.e., the number of edges in the unique path between a and b) is (rounded off to 2 decimal places) ____.

Q.47 Suppose Y is distributed uniformly in the open interval $(1, 6)$. The probability that the polynomial $3x^2 + 6x^3 + 3Y + 6$ has only real roots is (rounded off to 1 decimal place) ____.

Q.48 Let σ be the set of all bijections from $\{1, \dots, 5\}$ to $\{1, \dots, 5\}$, where id denotes the identity function, i.e., $\text{id}(i) = i, \forall i$. Let \circ denote composition on functions. For a

string $x = x_1x_2 \dots x_n \in \Sigma^n$, let $\pi(x) = x_1 \circ x_2 \circ \dots \circ x_n$.

Consider the language $L = \{x \in \Sigma^* \mid \pi(x) = \text{id}\}$.

The minimum number of states in any DFA accepting L is ____.

Q.49 Consider that 15 machines need to be connected in a LAN using 8-port Ethernet switches. Assume that these switches do not have any separate uplink ports. The minimum number of switches needed is ____.

Q.50 What is the minimum number of 2-input NOR gates required to implement a 4-variable function expressed in sum-of-minterms form as $F = \Sigma(0, 2, 5, 7, 8, 10, 13, 15)$? Assume that all the inputs and their complements are available. Answer: ____.

Q.51 A relational database contains two tables Student and Performance as shown below:

Roll_no	Student_name
1	Amit
2	Priya
3	Vivek
4	Rohan
5	Smith

Roll_no	Subject_code	Marks
1	A	86
1	B	95
1	C	90
2	A	89
2	C	92
3	C	80

The primary key of the Student table is Roll_no. For the Performance table, the columns Roll_no and Subject_code together form the primary key. Consider the SQL query given below:

```
SELECT S.Student_name, sum(P.Marks)
FROM Student S, Performance P
WHERE S.Roll_no = P.Roll_no
GROUP BY S.Student_name;
```

The number of rows returned by the above SQL query is ____.

Q.52 Consider the following C program:

```
#include <stdio.h>
int main()
{
    float sum = 0.0, j = 1.0, i = 2.0;
    while (i/j > 0.0625)
    {
```



```

        sum = sum + i/j;
        j = j + 1;
        printf("%f\n", sum);
    }
    return 0;
}

```

The number of times the variable `sum` will be printed, when the above program is executed, is ____.

Q.53 Consider the following C program:

```

#include <stdio.h>
int main()
{
    int a[] = {2, 4, 6, 8, 10};
    int i, sum = 0, *b = a + 4;
    for (i = 0; i < 5; i++)
    {
        sum = sum + (*b - i) - *(b - i);
        printf("%d\n", sum);
    }
    return 0;
}

```

The output of the above C program is ____.

Q.54 In an RSA cryptosystem, the value of the public modulus parameter n is 3007. If it is also known that $\varphi(n) = 2880$, where $\varphi()$ denotes Euler's Totient Function, then the prime factor of n which is greater than 50 is ____.

Q.55 Consider the following relations $P(X,Y,Z)$, $Q(X,Y,T)$ and $R(Y,V)$:

P		
X	Y	Z
X1	Y1	Z1
X1	Y1	Z2
X2	Y2	Z2
X2	Y4	Z4

Q		
X	Y	T
X2	Y1	2
X1	Y2	5
X1	Y1	6
X3	Y3	1

R	
Y	V
Y1	V1
Y3	V2
Y2	V3
Y2	V2

How many tuples will be returned by the following relational algebra query?

$$\Pi_X ((\sigma_{P.Y=R.Y \wedge R.V=V_2}(P \times R)) - \Pi_X(\sigma_{Q.Y=R.Y \wedge Q.T>2}(Q \times R)))$$

Answer: ____