

[Questions]  
chat

Topics:

- QQ-plot  $\rightarrow$  data ~ disb (visual)

[code]

- confidence intervals  $\rightarrow$
- bootstrapping
- CLT

✓ - hypothesis testing (2-3 classes)

X  
heights

Observed  
 $x_1, x_2, \dots, x_{100}$   $\sim \text{Normal}(\mu = 160; \sigma = 10)$

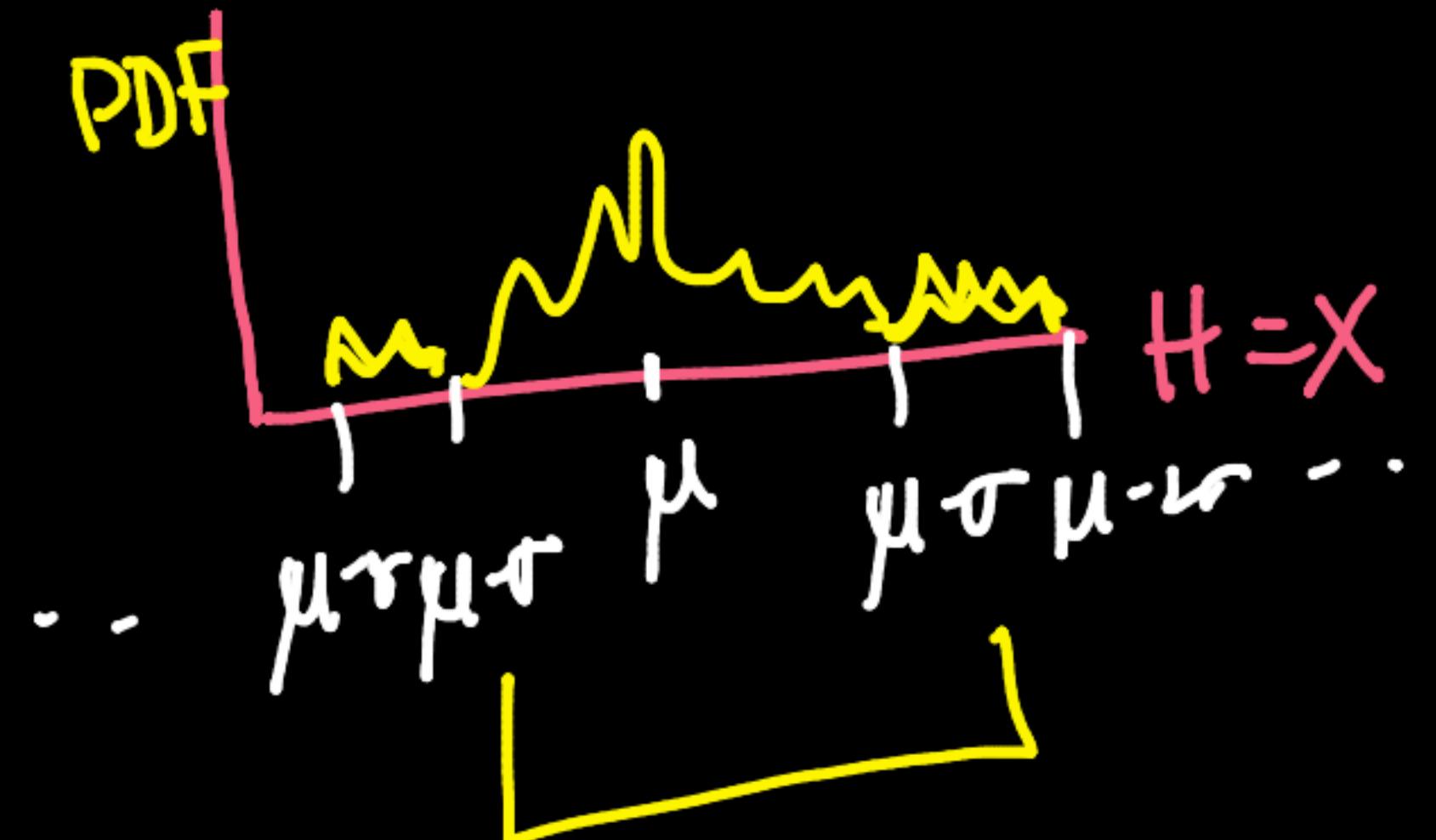
Q

how can you verify that 100 -ds follow  
this dist

QQ-plot

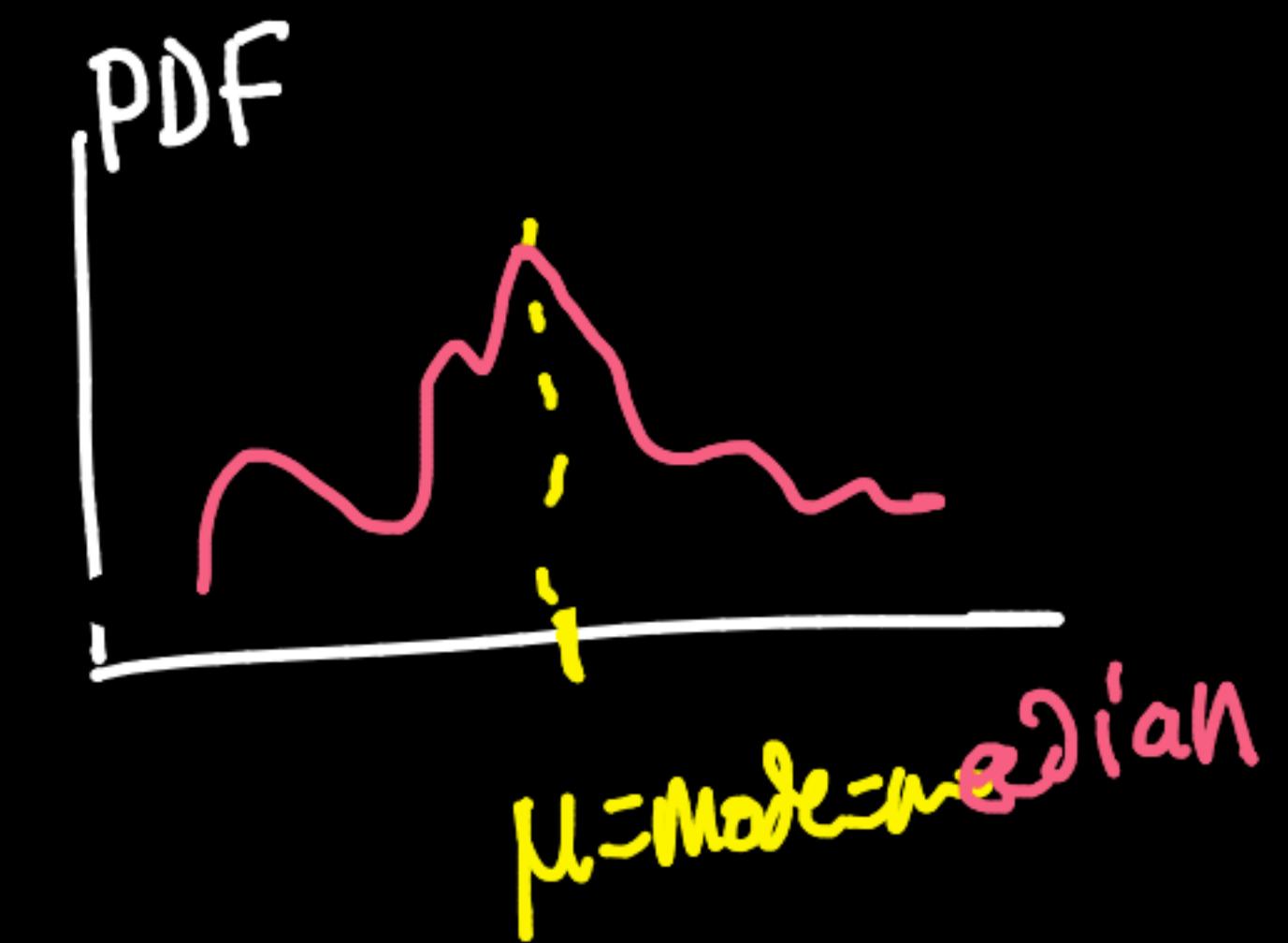
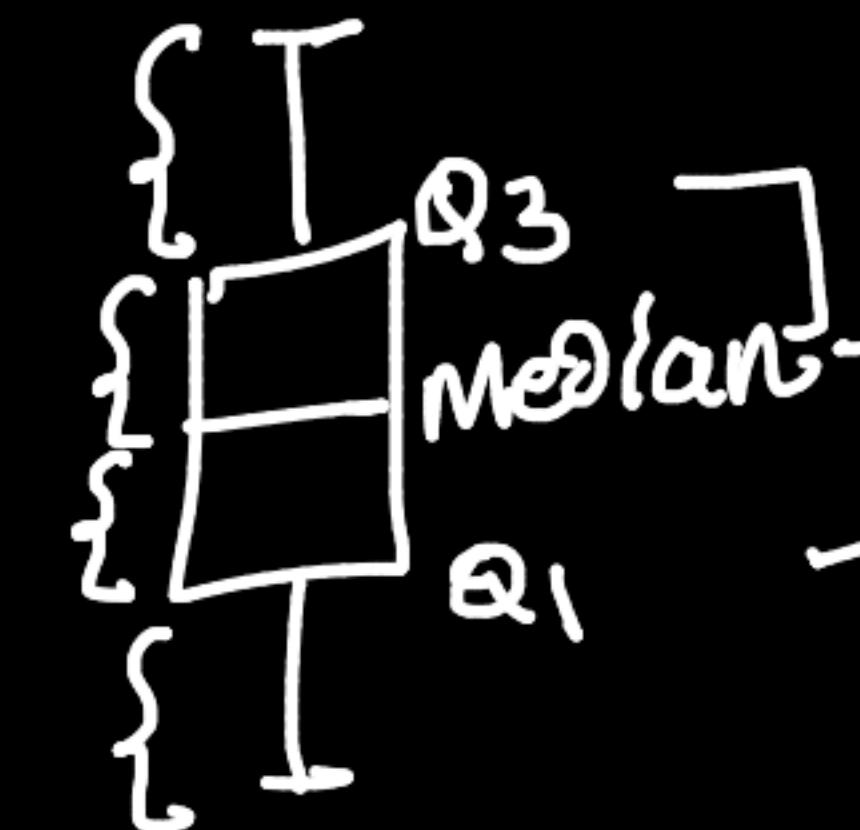
$X \rightarrow \underline{67} - \underline{95} - \underline{99}$  rule

but not gaussian . . .

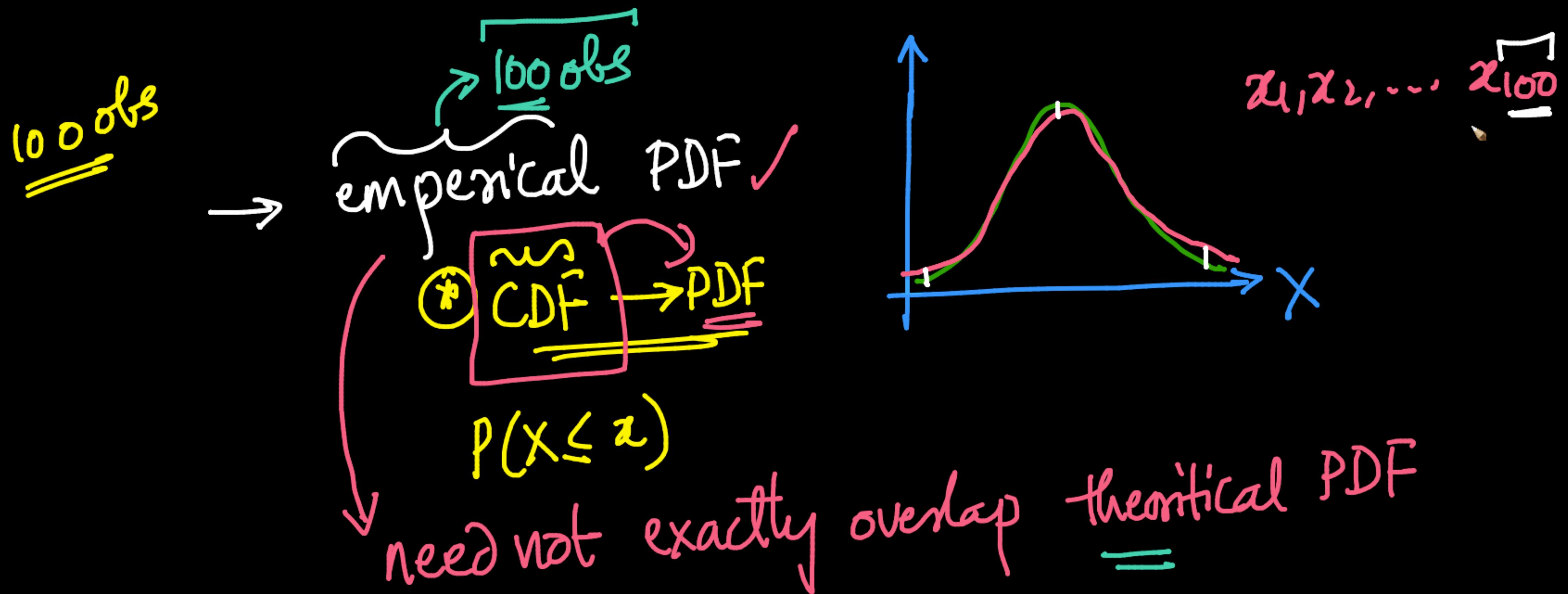


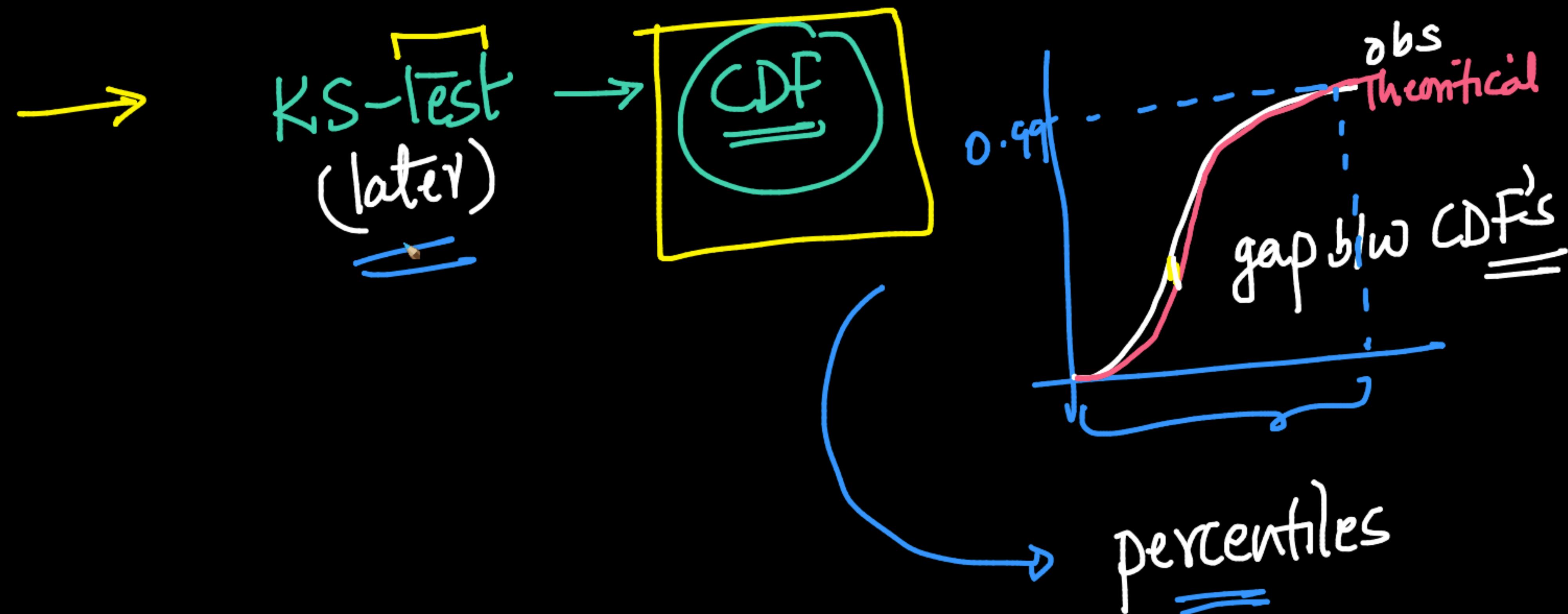
$X \rightarrow \text{Median} = \text{Mode} = \text{Mean}$

→ boxplot



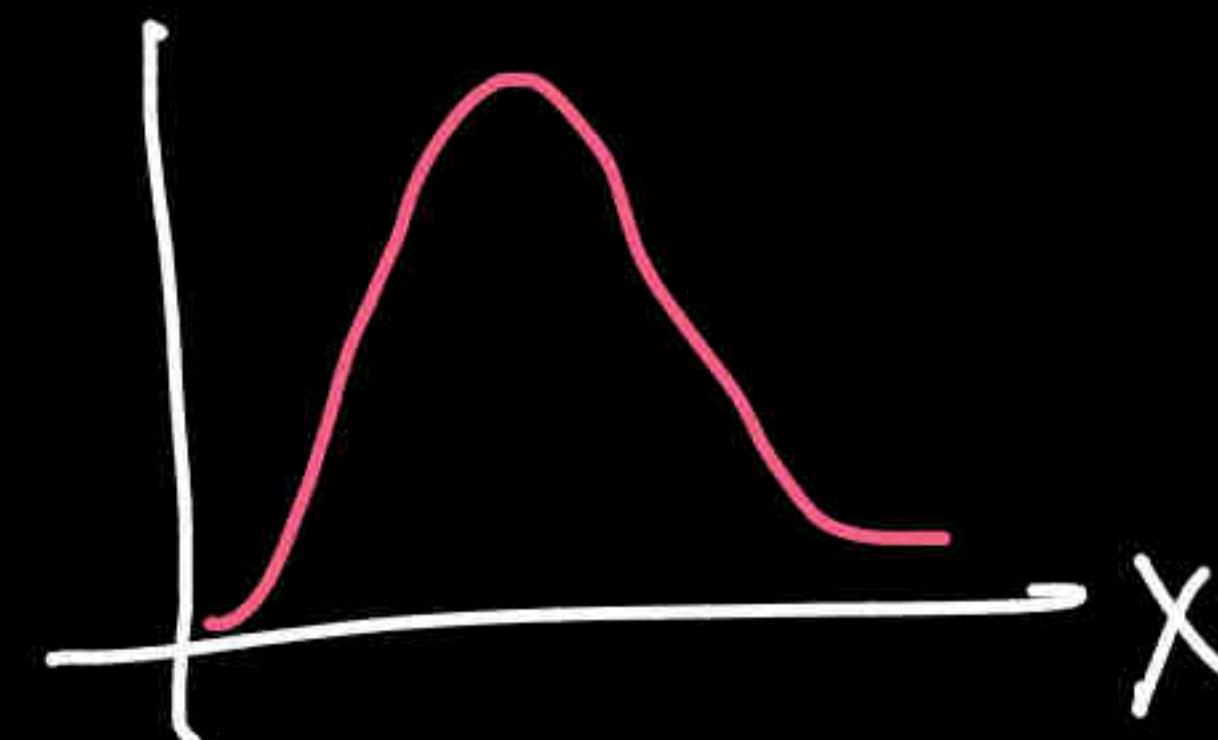
→ bell-shaped curve + 68-95-99  
↳ binomial-distr: bell-shaped  
like a }





$$X \sim N(\mu = 160; \sigma^2 = 10)$$

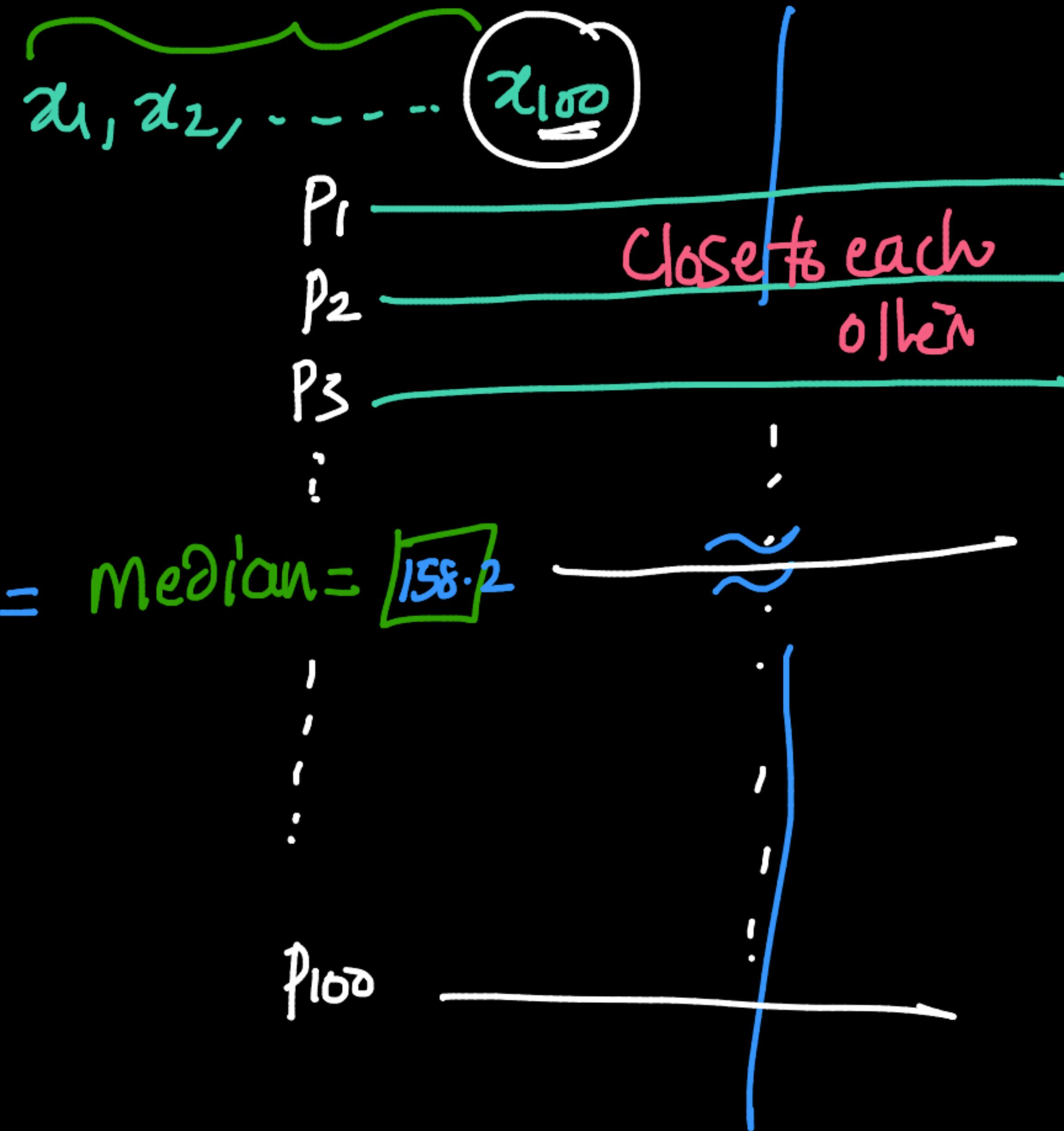
↳  $P(X=x) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left\{-\frac{1}{2}\frac{(x-\mu)^2}{\sigma^2}\right\}$



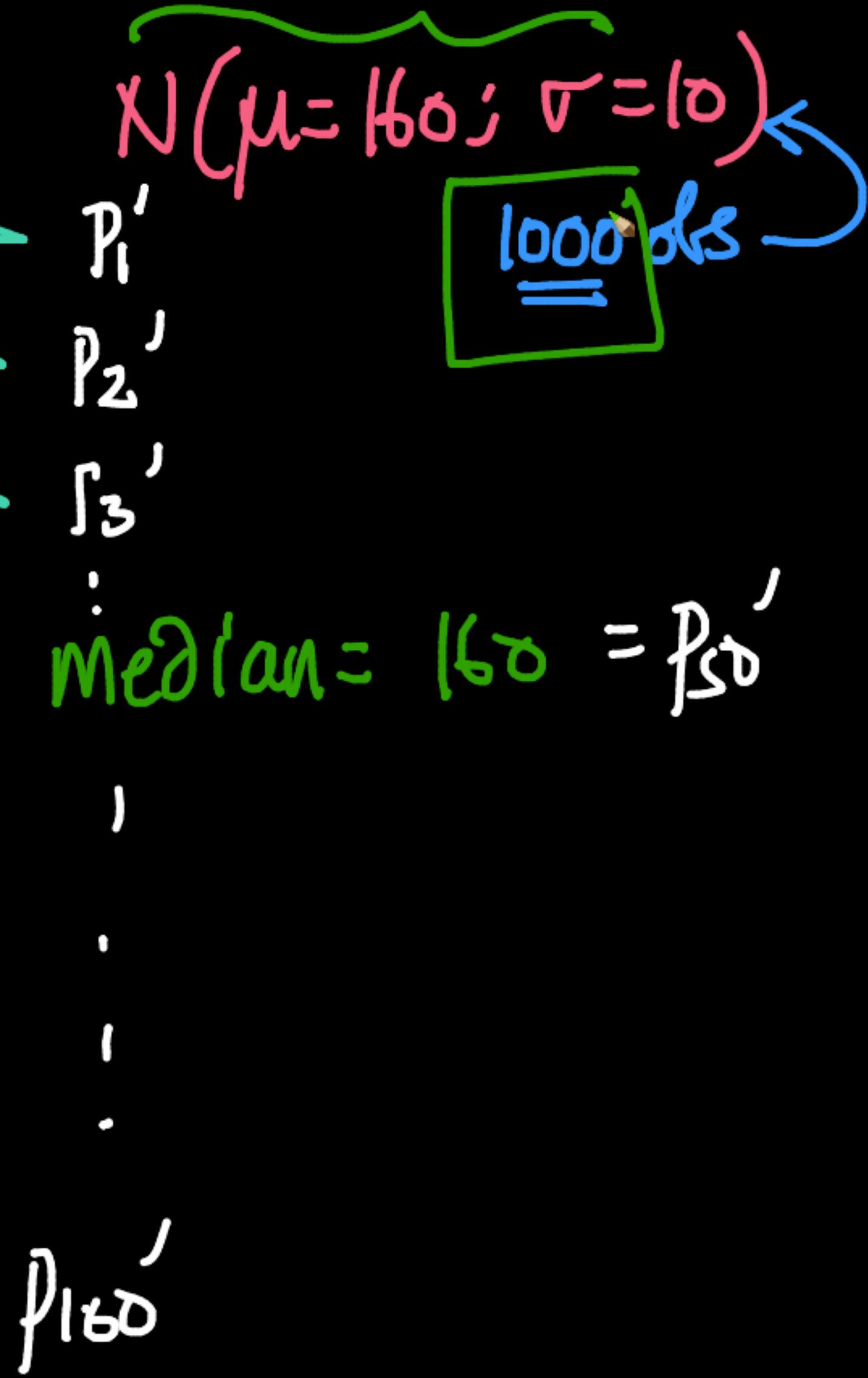
Obs:

not the  
best

slightly  
better  
than  
others

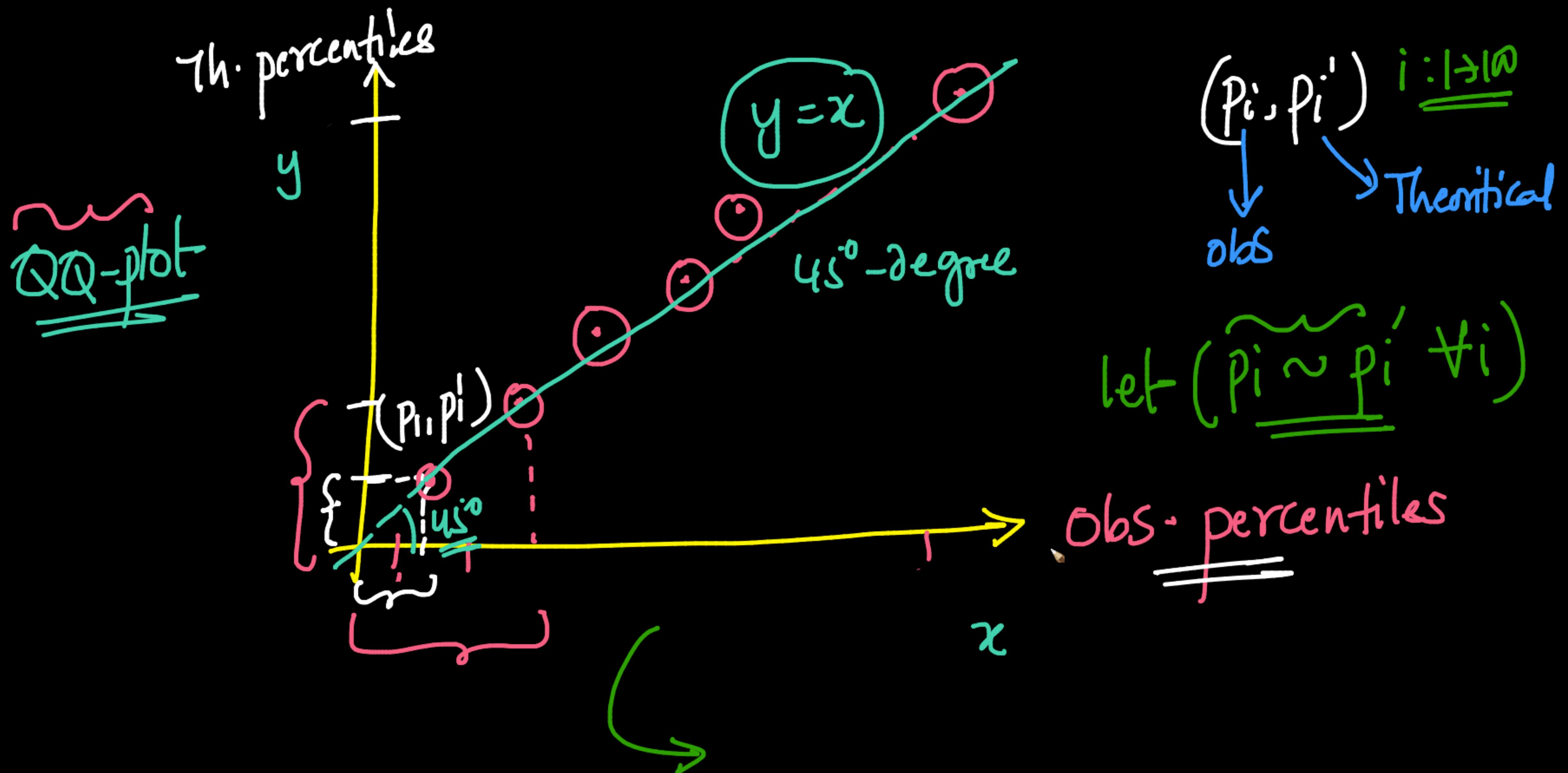


$$P_{50} = \text{Median} = 158.2$$



$$\text{Median} = 160 = P_{50}$$

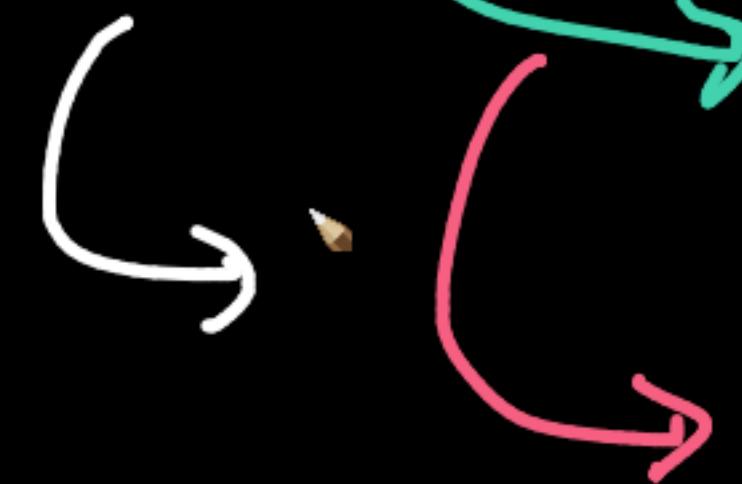
$P_{160}$



Visual

if all  $(\hat{p}_i, p_i)$  lie "close" to the  $y=x$  ( $45^\circ$ )  
line then obs-data follows the th-dish

Drawbacks



how - close?  $\rightarrow$  subjective

Mathematical value on "confident" we are

$x_1, x_2, \dots, x_{100}$  $\sim N(\mu = 160; \sigma^2 = 10)$ 

100 is reasonable size sample

 $m \approx \bar{\mu} \rightarrow \text{for now}$  $s \approx \sigma$   
(later) - bell curve techniques

good enough  
approx

# Rules of thumb

classical stats  
not for  
ML & DL

$\geq 30$  obs

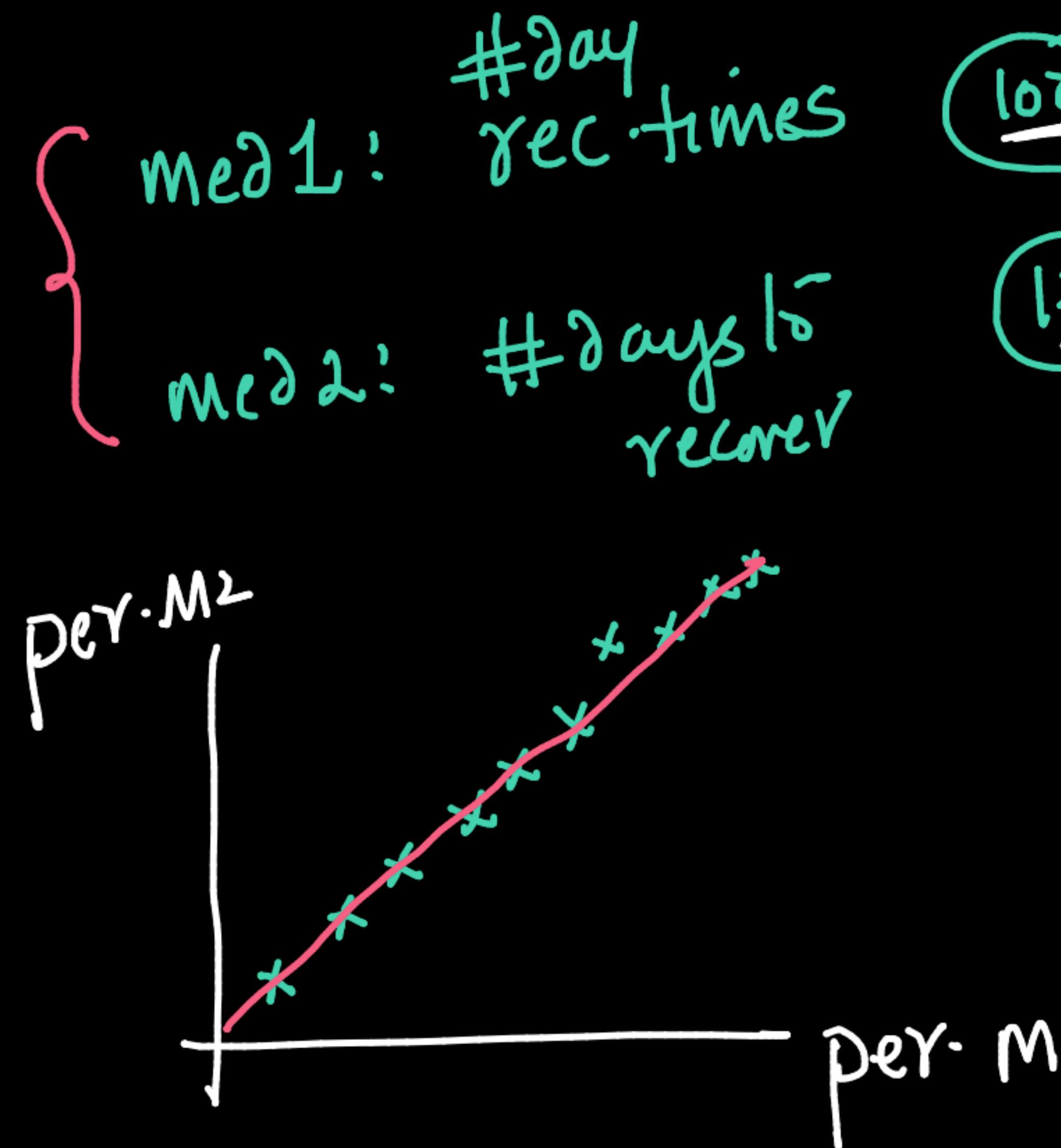
$\sim 100$  obs  $\rightarrow$  v. good

$\sim 1000$  obs  $\rightarrow$  great



comparing

2-d isb



100

120

p<sub>1</sub>, p<sub>2</sub>, ..., p<sub>10</sub>

(p<sub>i</sub>, p<sub>i'</sub>)

↓

Med 1

↓

Med 2

need not  
be gaussian

QQ

$X \sim \text{Normal}(\mu, \sigma)$

$Y \sim \text{Binomial}(n, p)$  ← QQ-plot

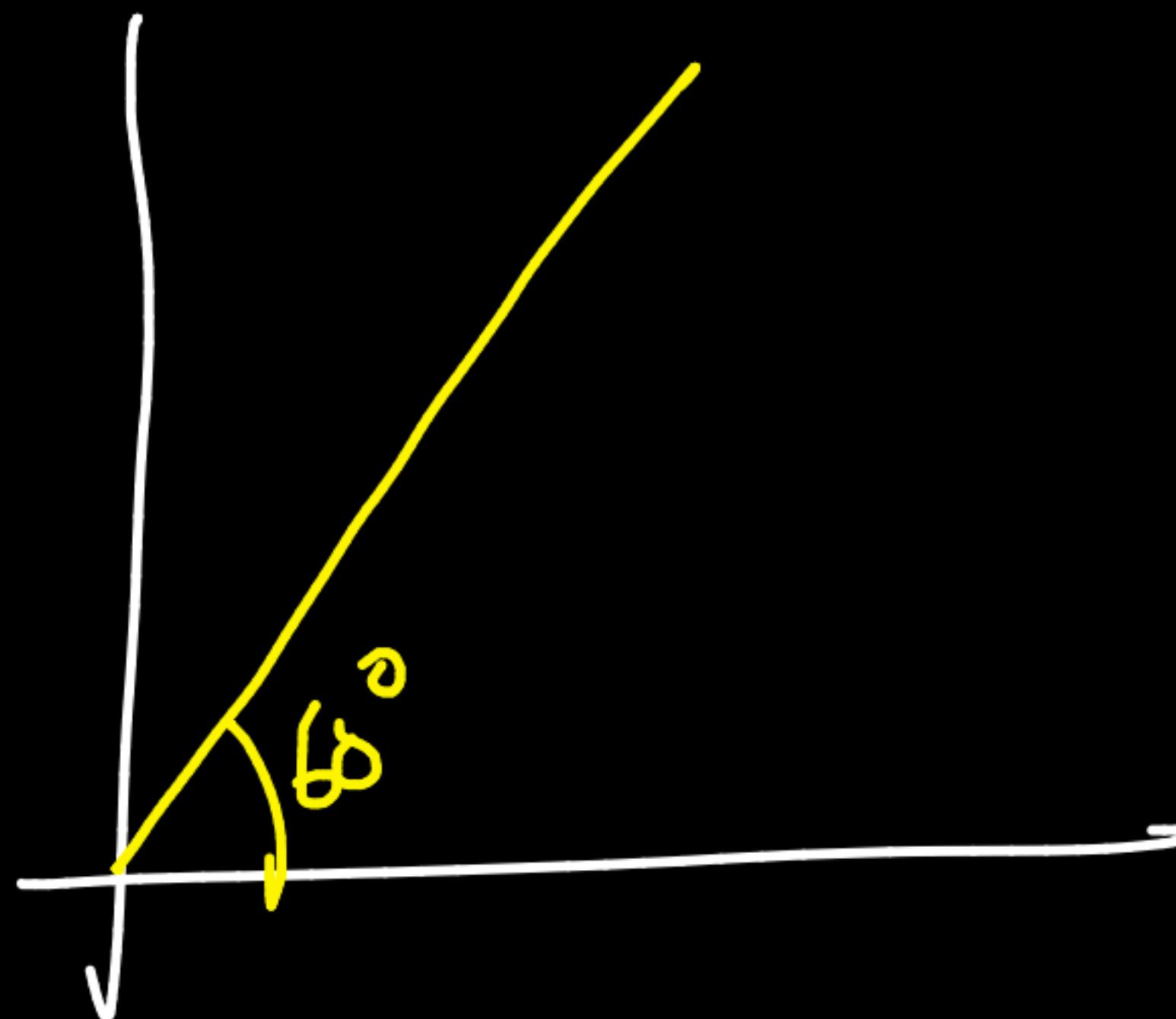
$y_1, \dots, y_{200}$

↓  
percentiles

↓  
percentiles

$x_1, x_2, \dots, x_{100}$

$\sim N(\mu=160, \sigma=10)$



→ distribution  
Shape are similar

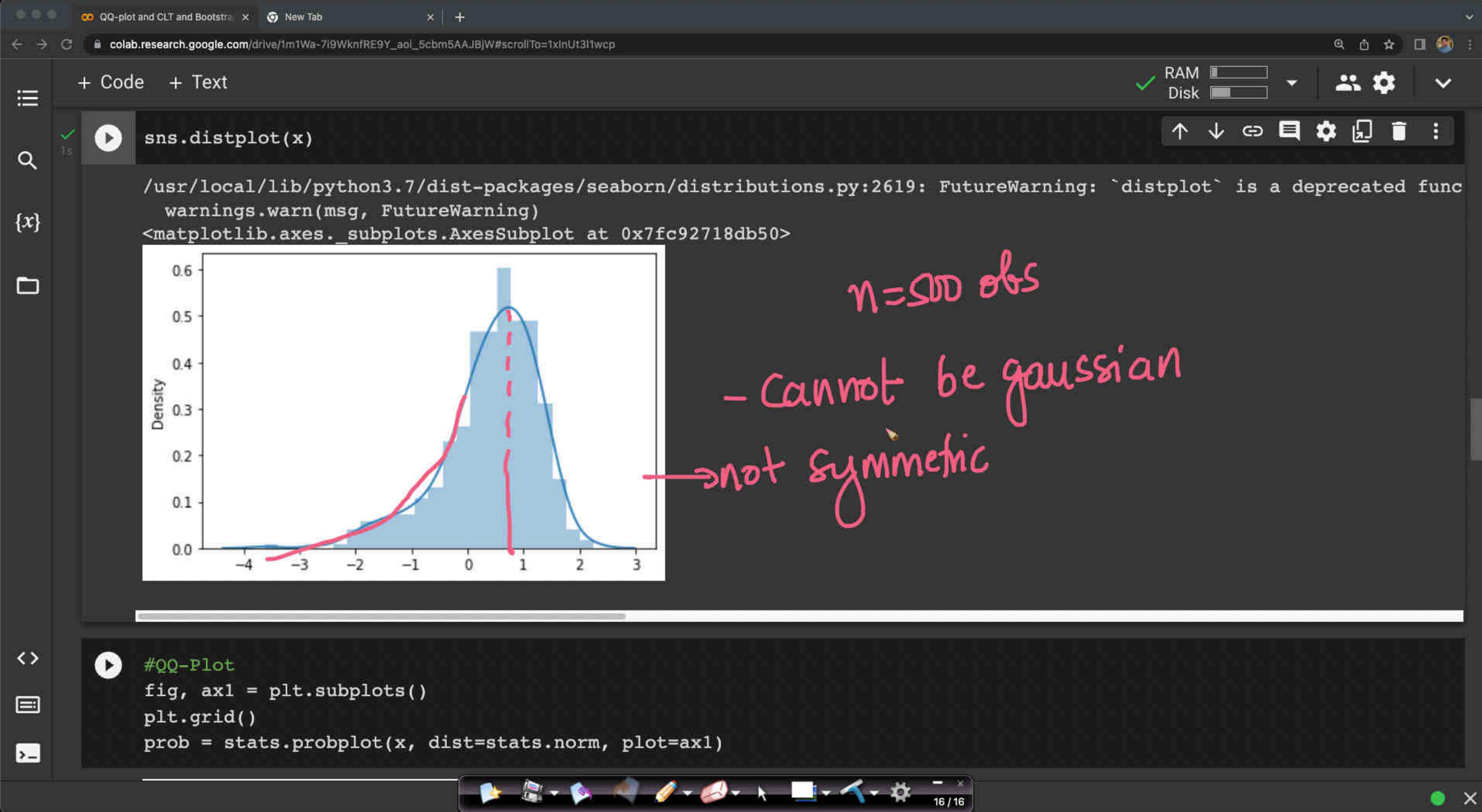
$x_1, \dots, x_{100} \sim$

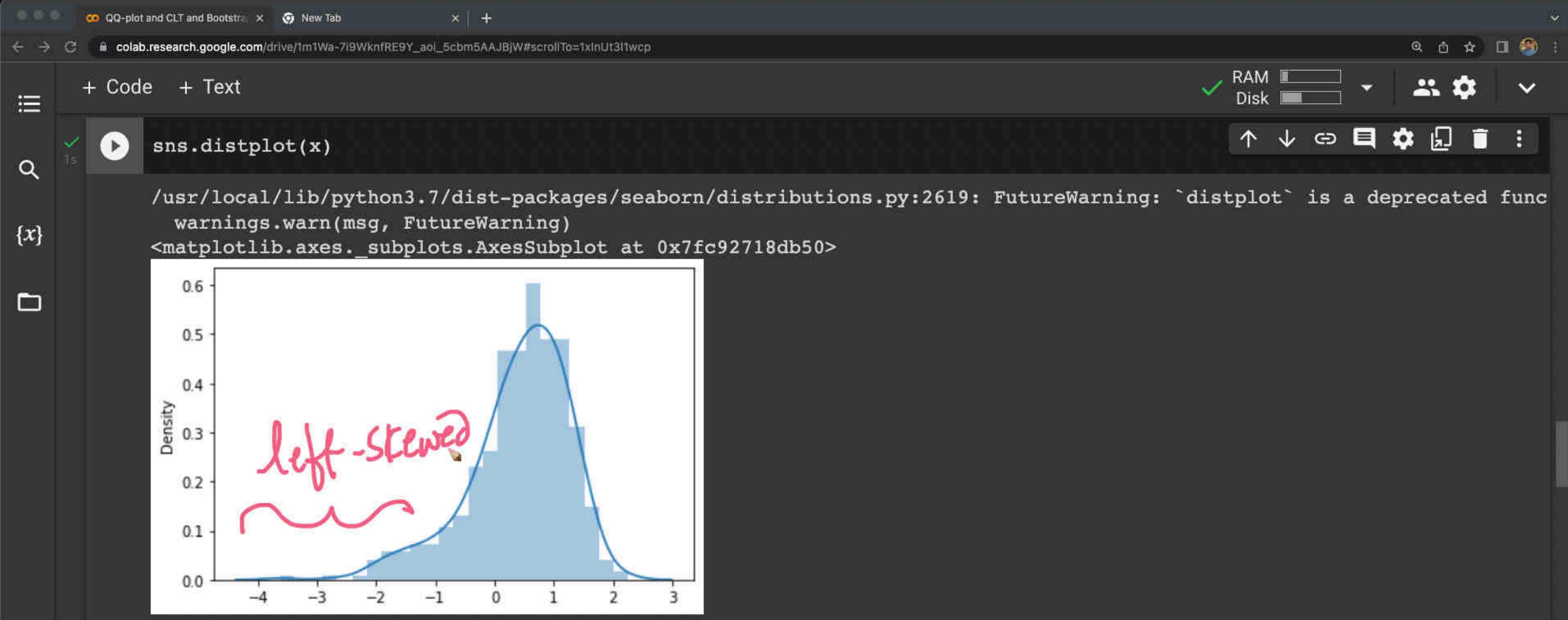
Normal

but not

Normal ( $\mu=160, \sigma=10$ )







#QQ-Plot

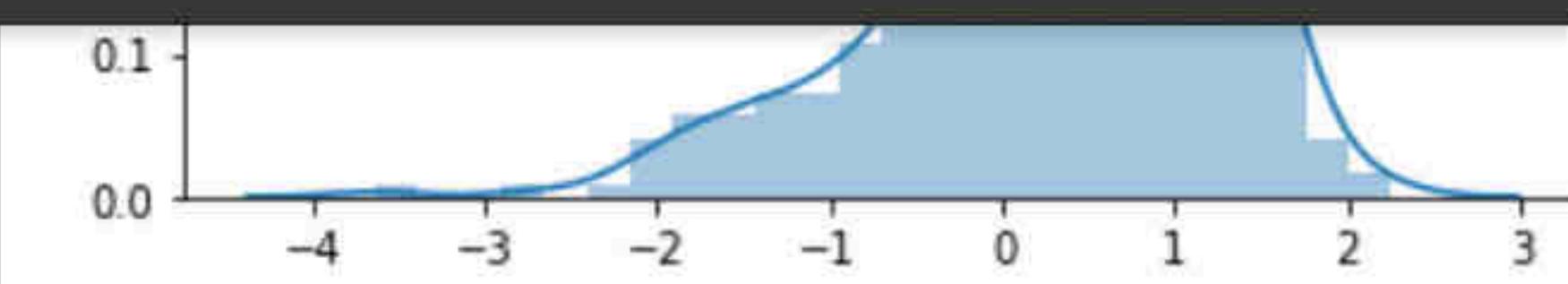
```
fig, ax1 = plt.subplots()
plt.grid()
prob = stats.probplot(x, dist=stats.norm, plot=ax1)
```



QQ-plot and CLT and Bootstrap

New Tab

+ Code + Text

✓ RAM  
Disk

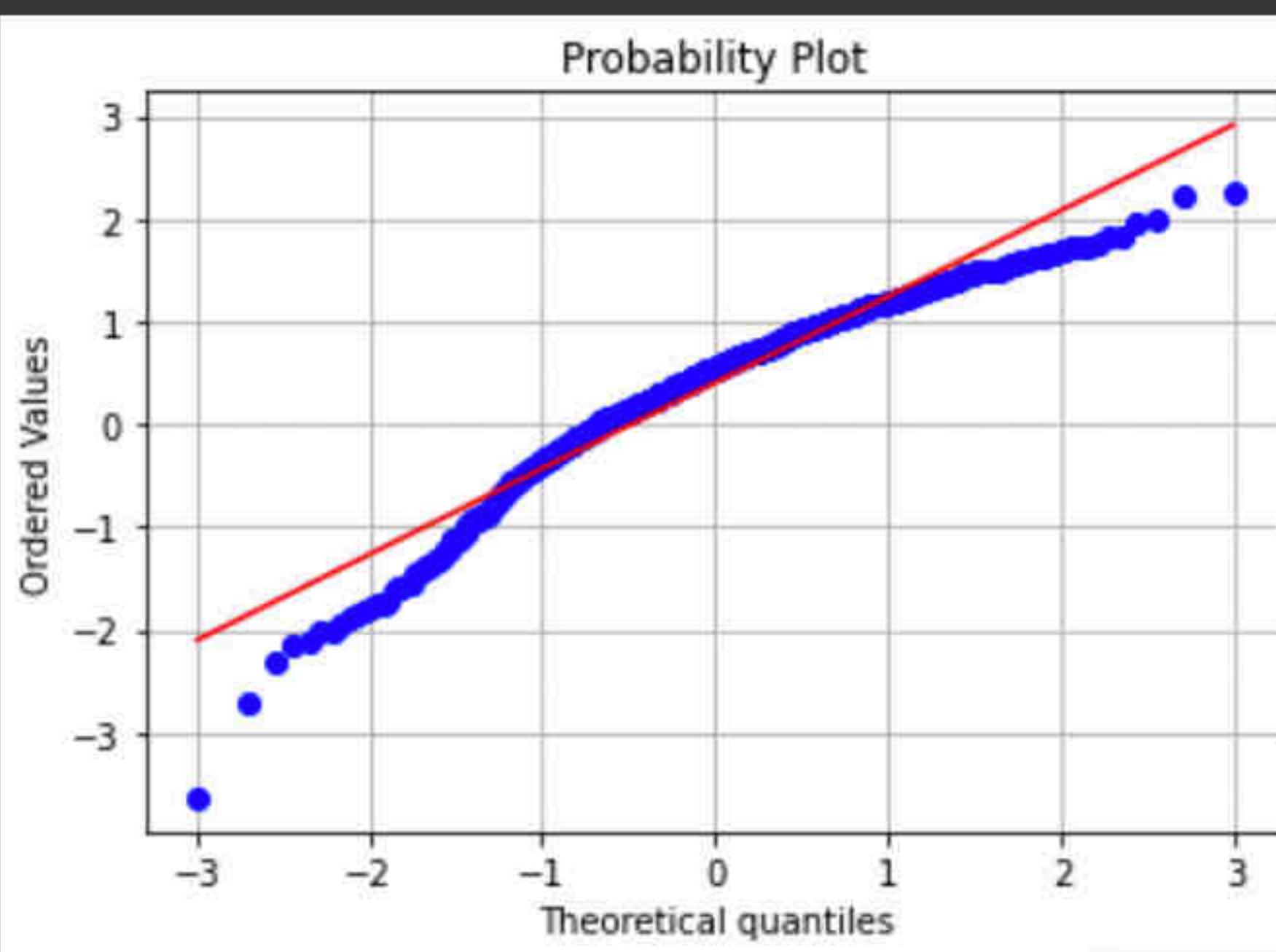
{x}

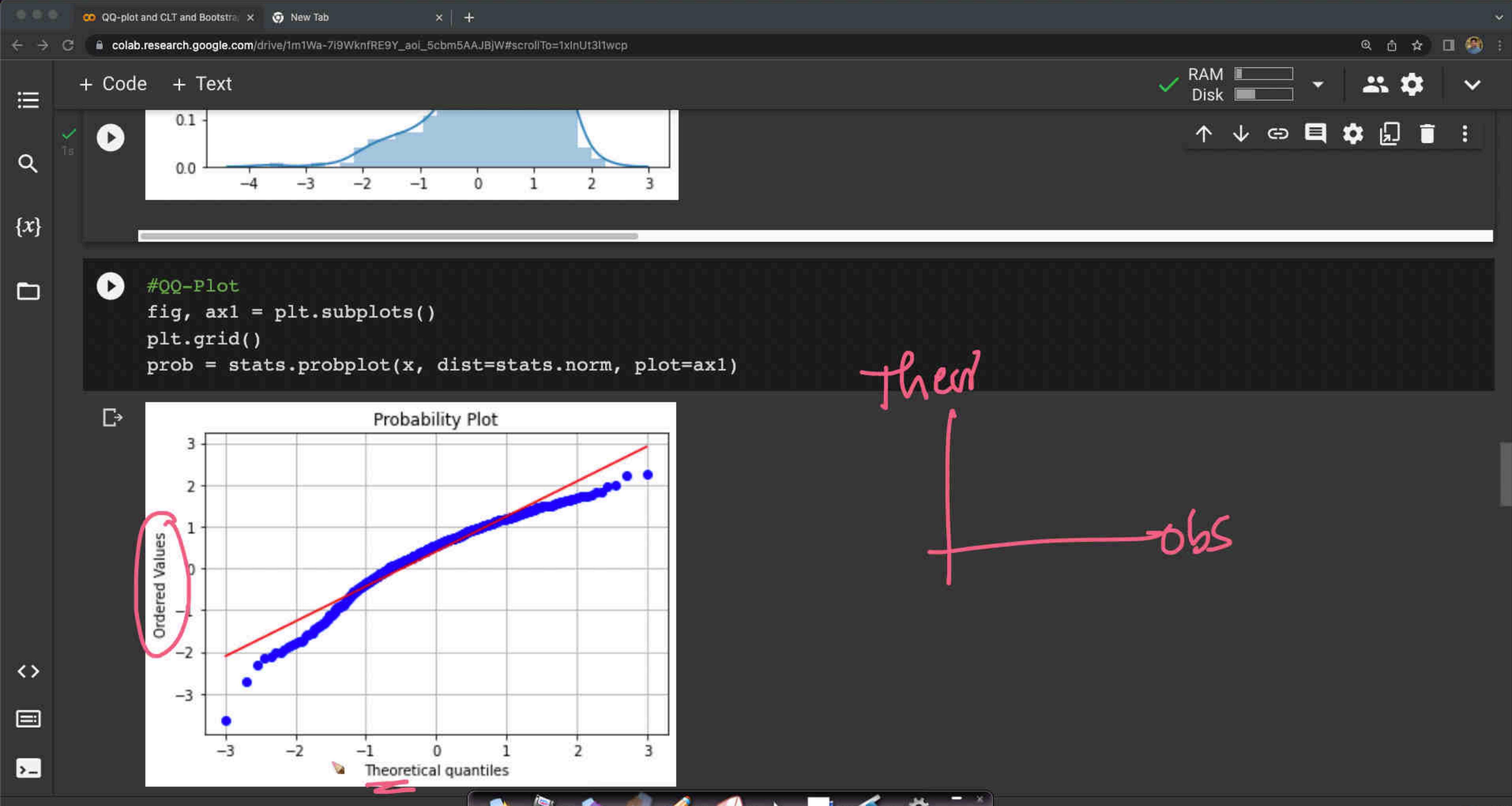
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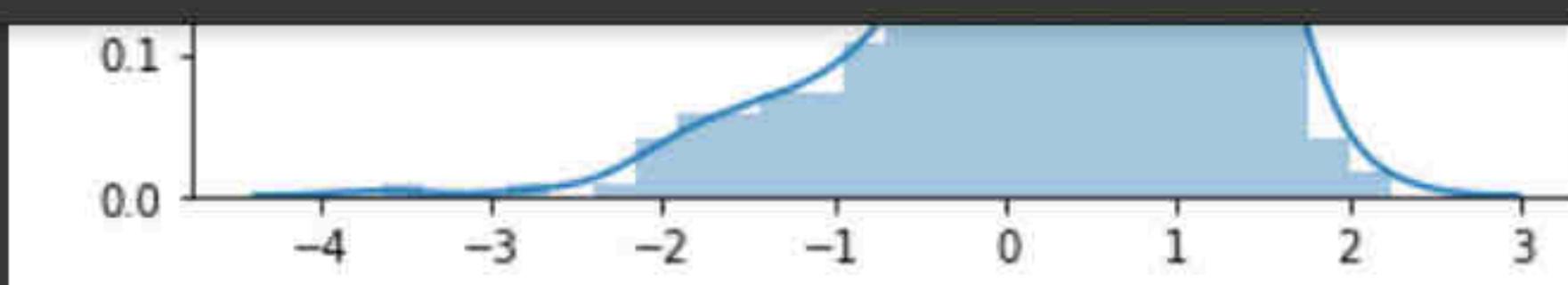
scipy.stats

$x_1, x_2, \dots, x_{50}$

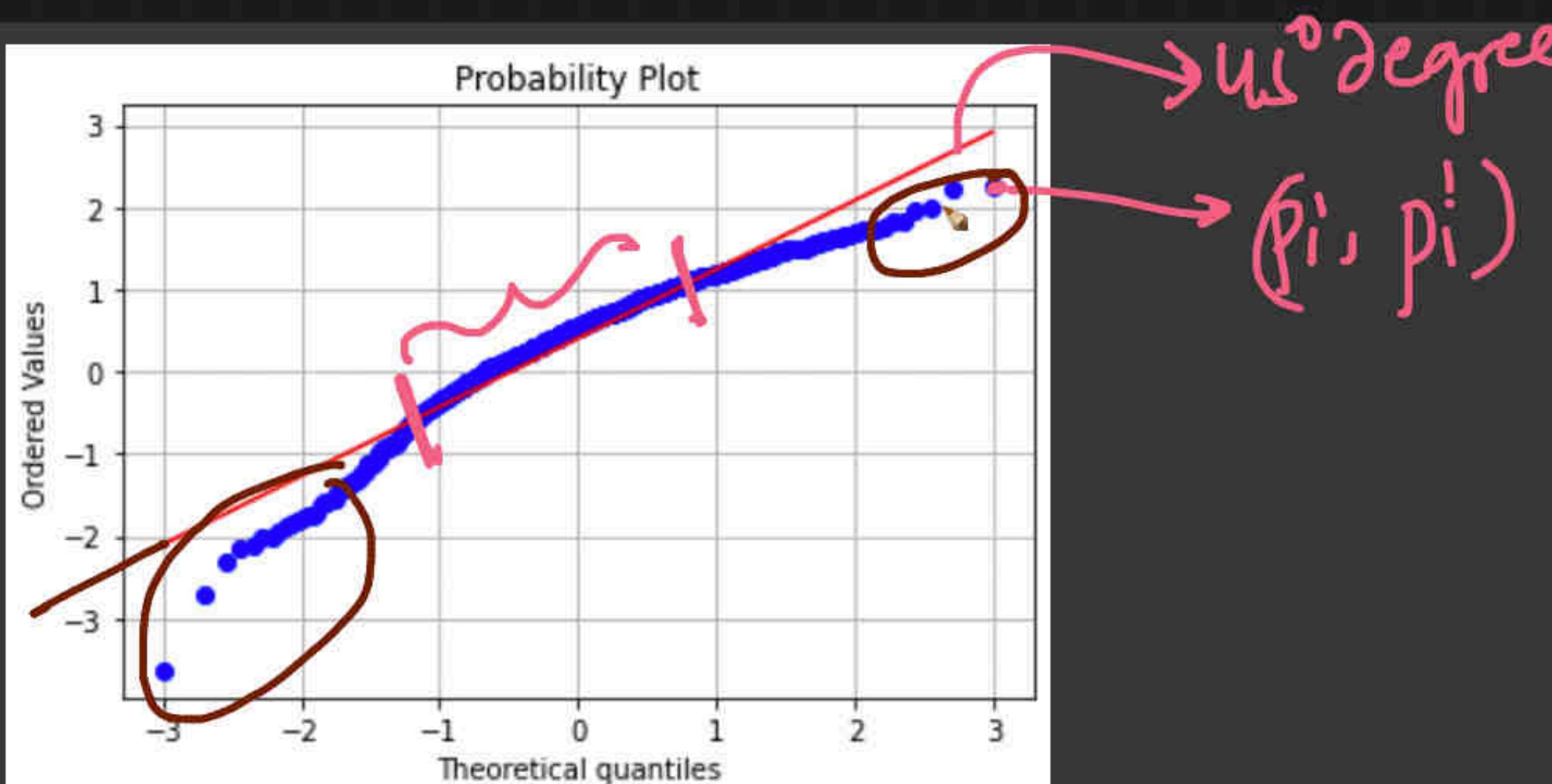
Normal  $(\mu, \sigma^2)$

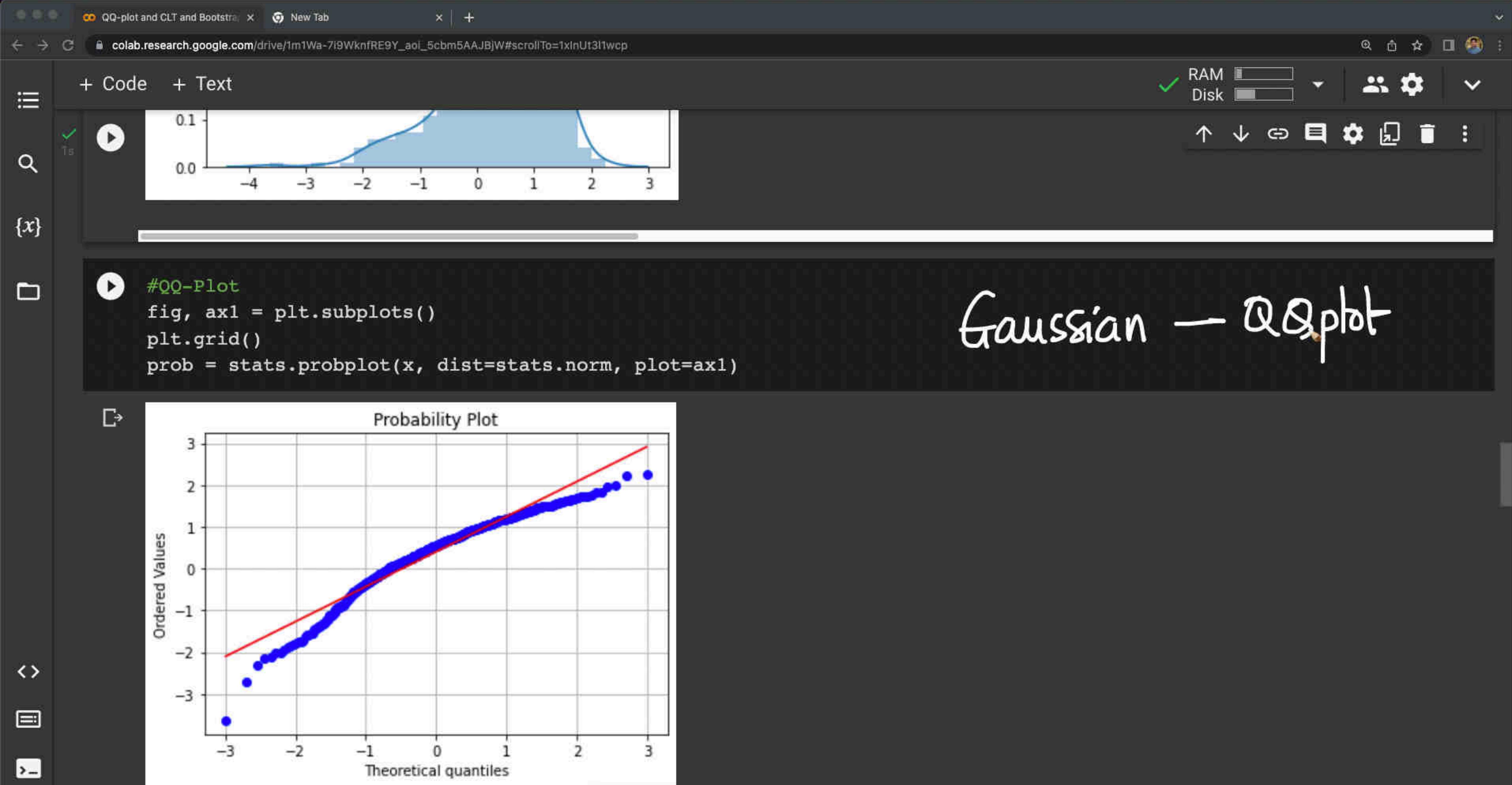


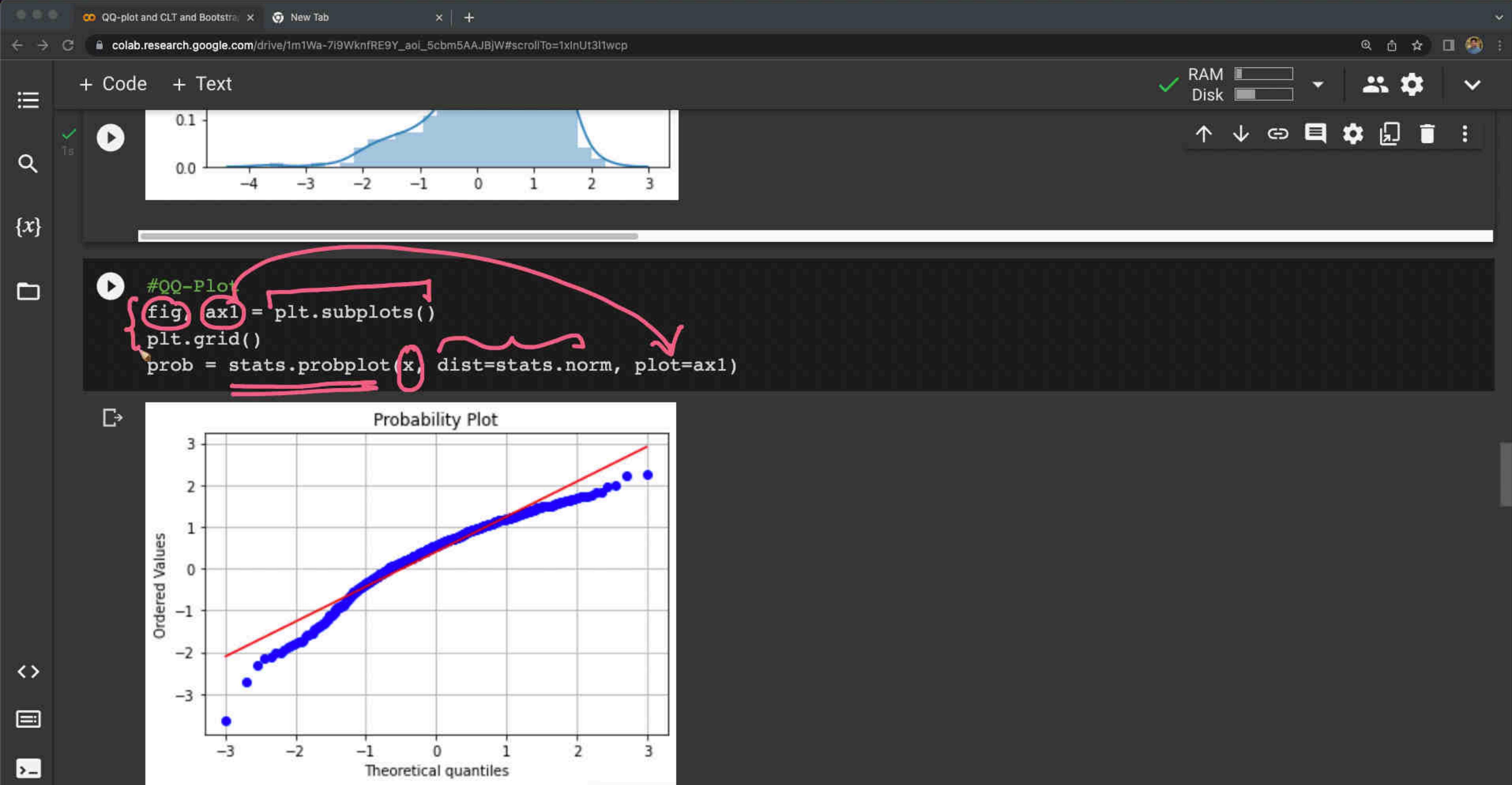


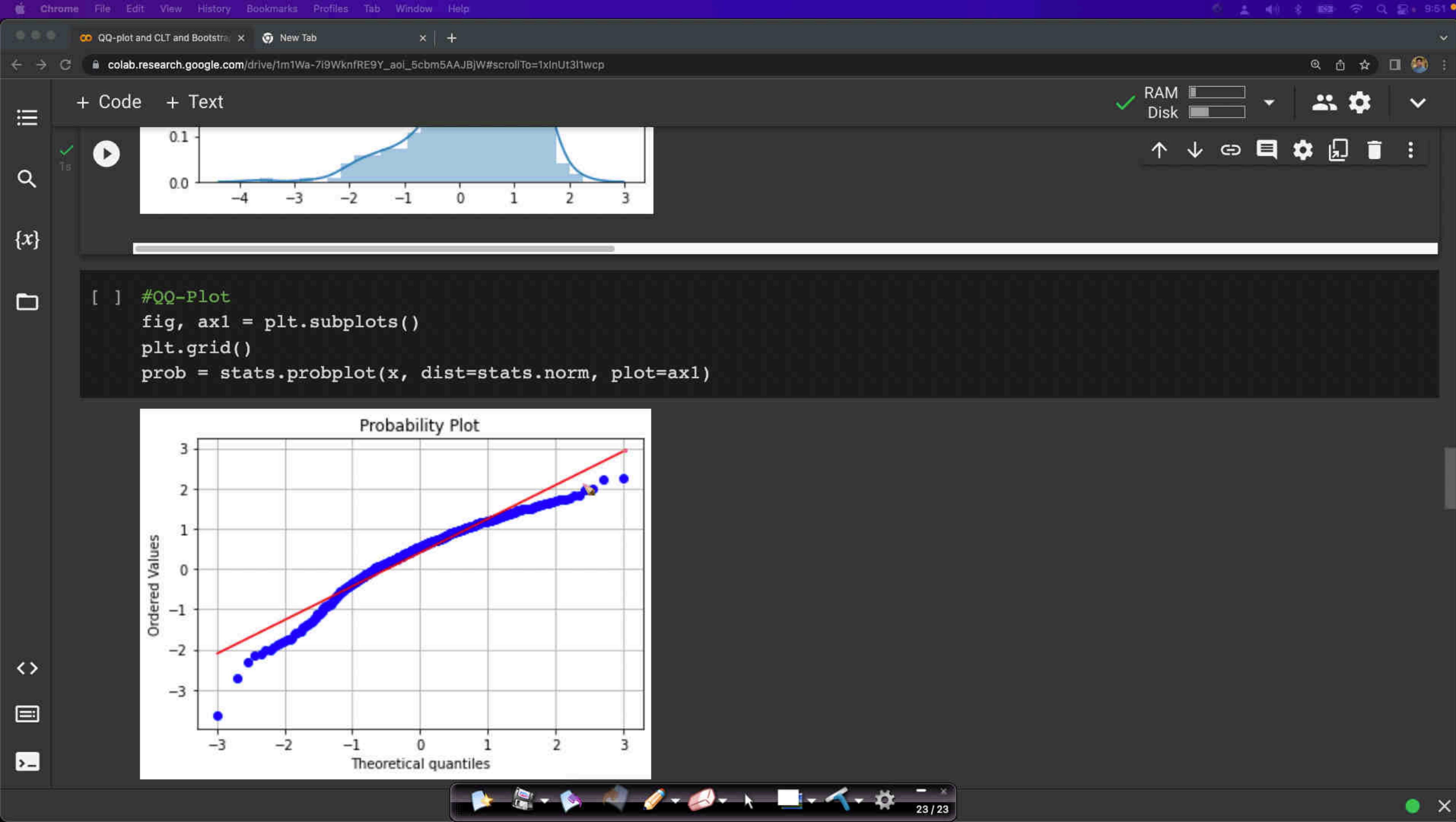


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∞ QQ-plot and CLT and Bootstrap X | New Tab X | [scipy.stats.probplot — SciPy v1.8.0 documentation](#)

docs.scipy.org/doc/scipy/reference/generated/scipy.stats.probplot.html

RELEASE 1.8.0

Getting started User Guide API reference Development Release notes

Search the docs ...

( [scipy.sparse.csgraph](#) )  
Spatial algorithms and data structures  
( [scipy.spatial](#) )  
Distance computations  
( [scipy.spatial.distance](#) )  
Special functions ( [scipy.special](#) )  
**Statistical functions ( [scipy.stats](#) )**  
Result classes  
Contingency table functions  
( [scipy.stats.contingency](#) )  
Statistical functions for masked arrays  
( [scipy.stats.mstats](#) )  
Quasi-Monte Carlo submodule  
( [scipy.stats.qmc](#) )  
Random Number Generators  
( [scipy.stats.sampling](#) )  
Low-level callback functions

squares fit. `plot` is an object that has to have methods `plot` and `text`. The `matplotlib.pyplot` module or a Matplotlib Axes object can be used, or a custom object with the same methods. Default is `None`, which means that no plot is created.

**Returns:** `(osm, osr) : tuple of ndarrays`  
Tuple of theoretical quantiles (`osm`, or order statistic medians) and ordered responses (`osr`). `osr` is simply sorted input `x`. For details on how `osm` is calculated see the Notes section.

`(slope, intercept, r) : tuple of floats, optional`  
Tuple containing the result of the least-squares fit, if that is performed by `probplot`. `r` is the square root of the coefficient of determination. If `fit=False` and `plot=None`, this tuple is not returned.

**Notes**

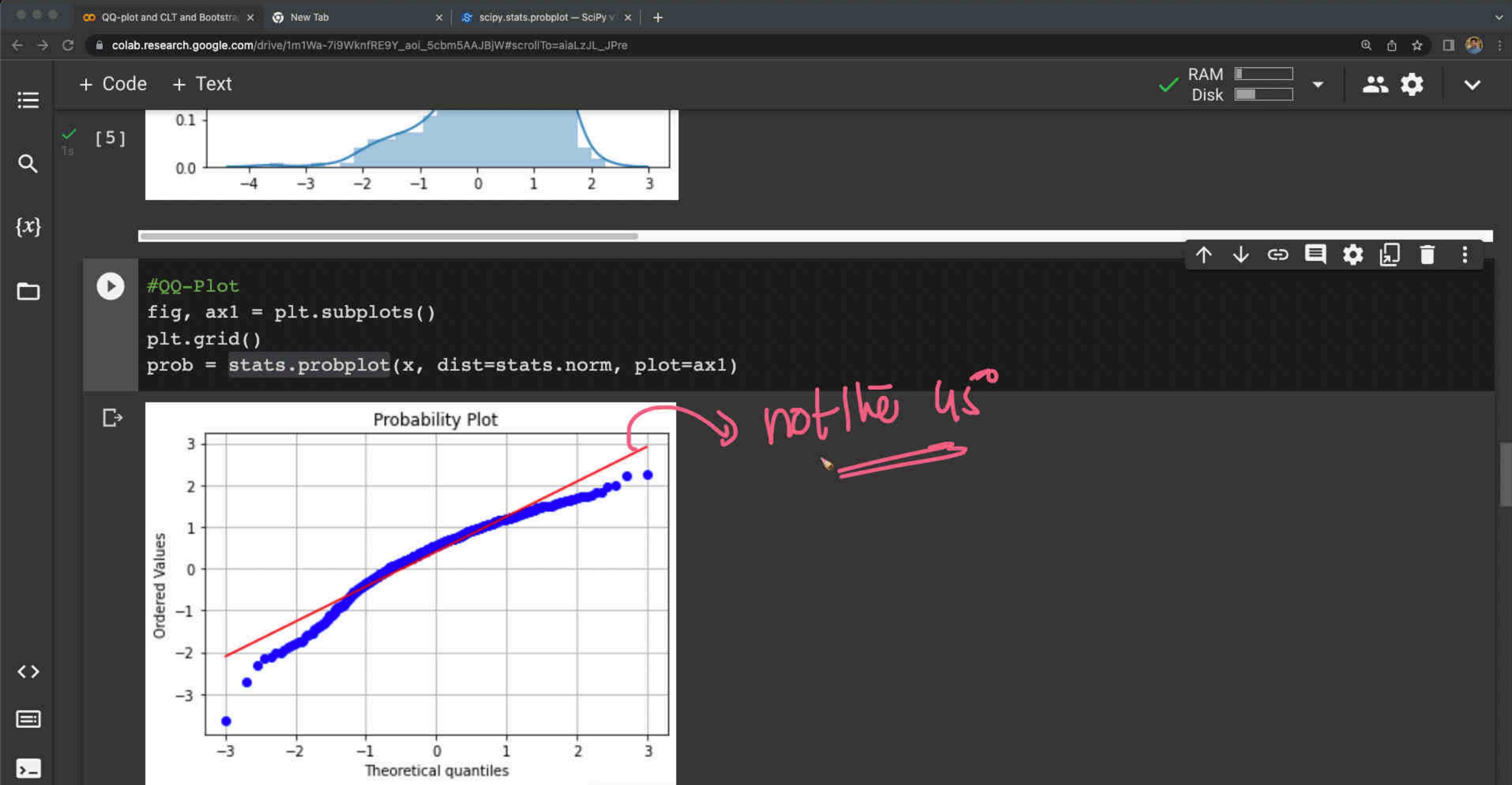
Even if `plot` is given, the figure is not shown or saved by `probplot`; `plt.show()` or `plt.savefig('filename.png')` should be used after calling `probplot`.

`probplot` generates a probability plot, which should not be confused with a Q-Q or a P-P plot. Statsmodels has more extensive functionality of this type, see `statsmodels.api.ProbPlot`.

The formula used for the theoretical quantiles (horizontal axis of the probability plot) is Filliben's



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∞ QQ-plot and CLT and Bootstrap X | New Tab X | [scipy.stats.probplot — SciPy v1.8.0 documentation](#)

docs.scipy.org/doc/scipy/reference/generated/scipy.stats.probplot.html

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Getting started User Guide API reference Development Release notes

Spatial algorithms and data structures

Distance computations

Special functions (scipy.special)

Statistical functions (scipy.stats)

Result classes

Contingency table functions

Statistical functions for masked arrays

Quasi-Monte Carlo submodule

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RELEASE 1.8.0

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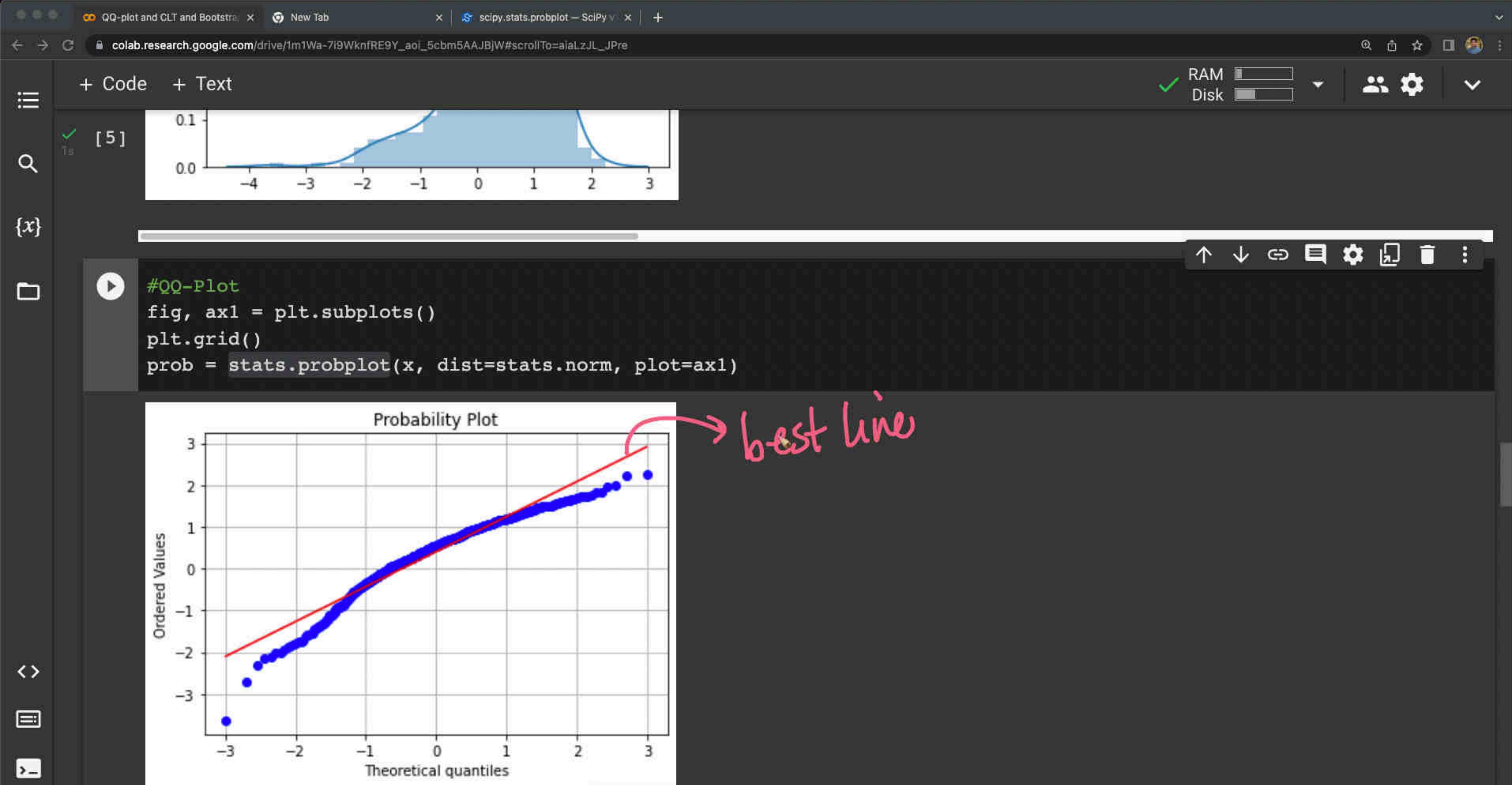
**Notes**

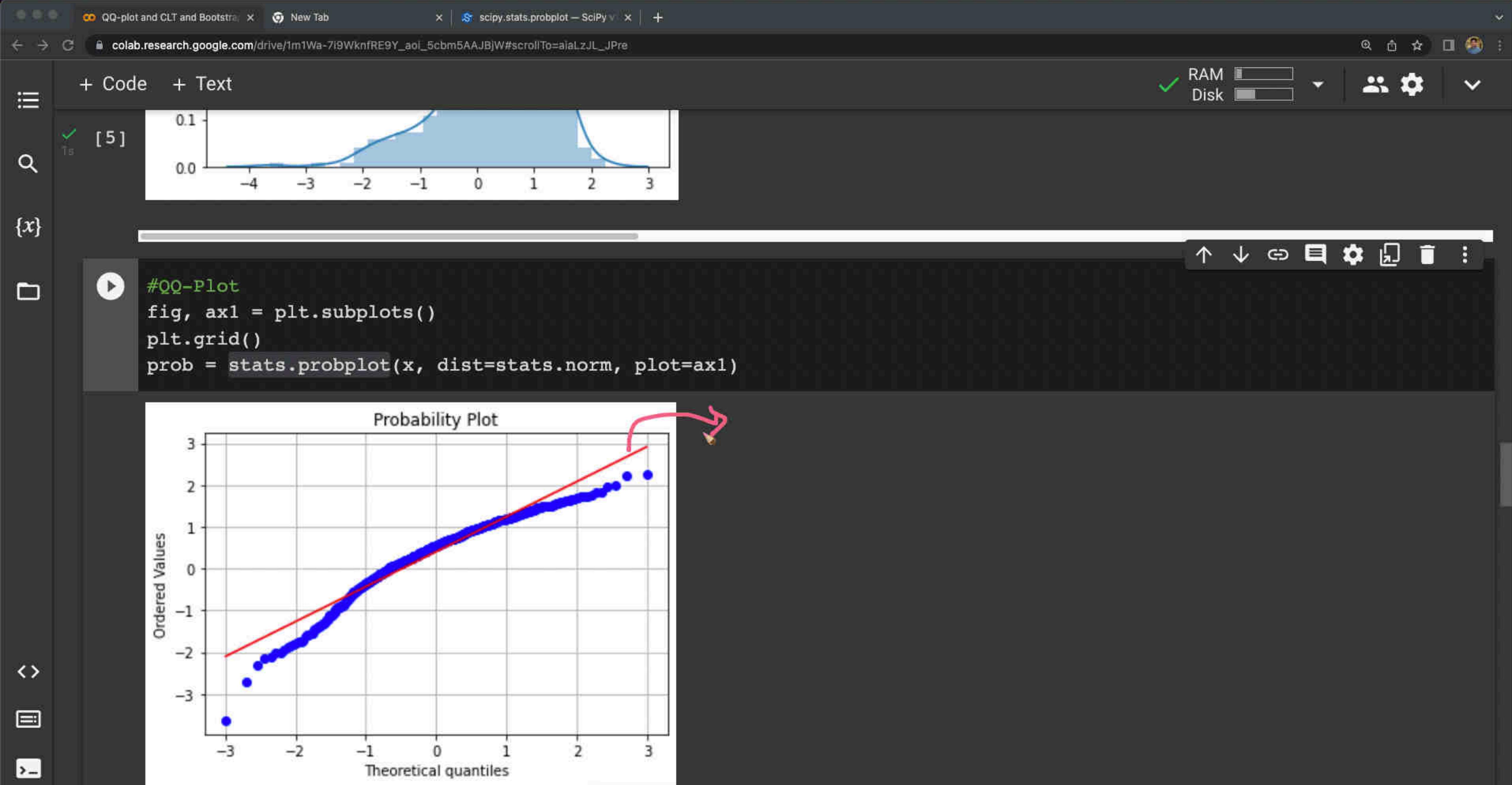
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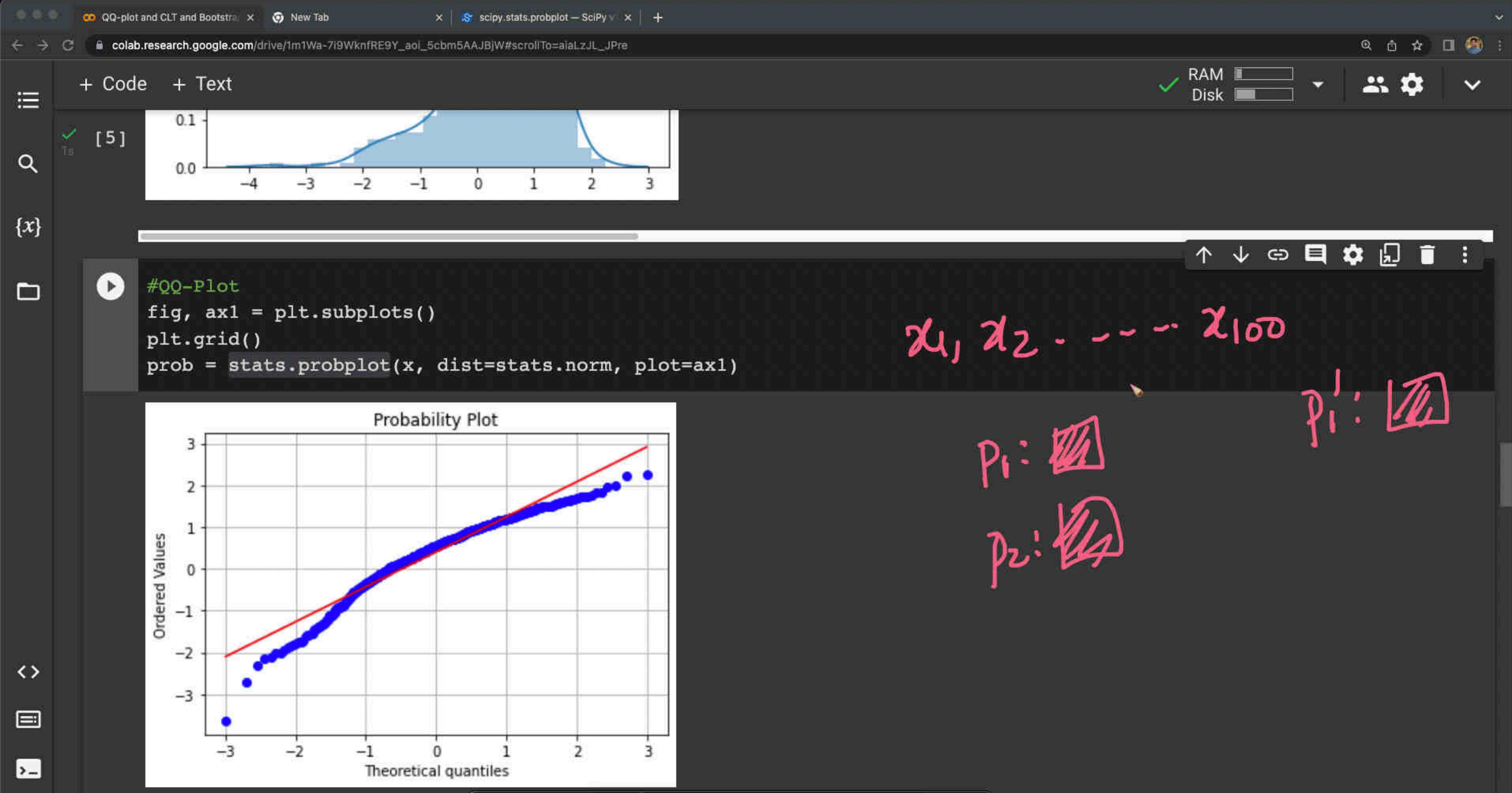
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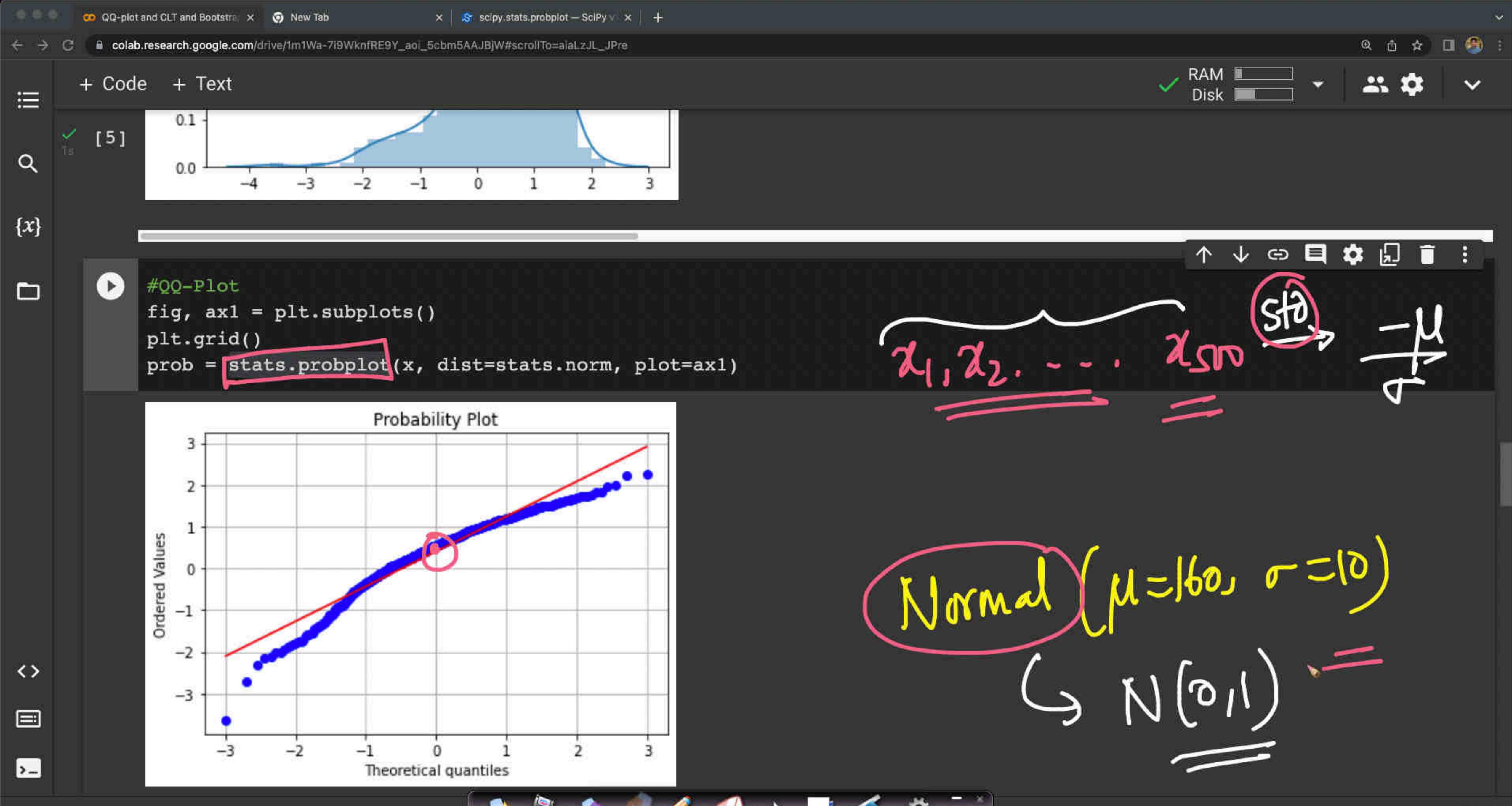
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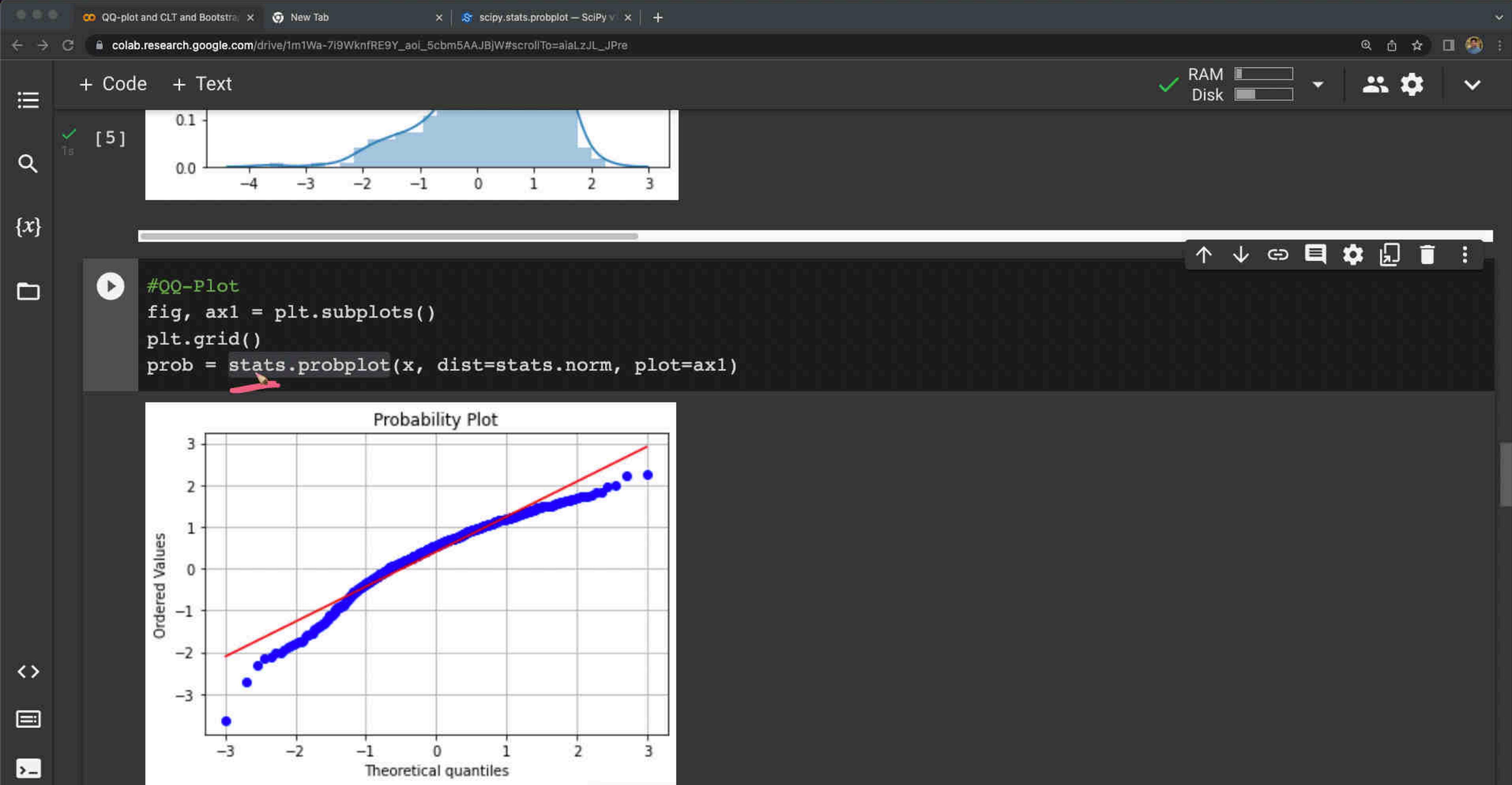
linear-regression(ML)

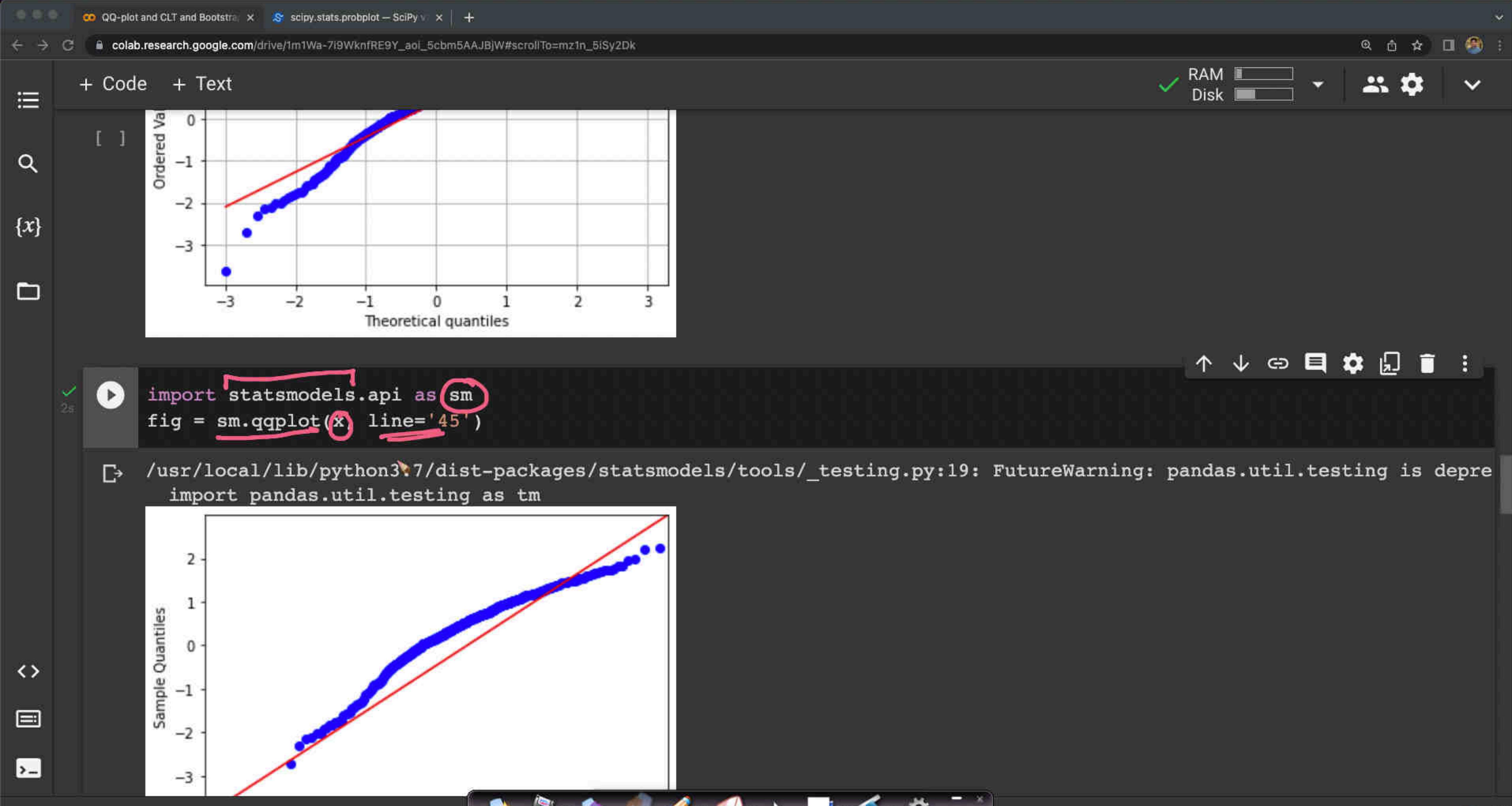












∞ QQ-plot and CLT and Bootstrap x S scipy.stats.probplot — SciPy v1.8.0 statsmodels.graphics.gofplots x +

docs.scipy.org/doc/scipy/reference/generated/scipy.stats.probplot.html

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Low-level callback functions

# scipy.stats.probplot

`scipy.stats.probplot(x, sparams=(), dist='norm', fit=True, plot=None, rvalue=False)`

Calculate quantiles for a probability plot, and optionally show the plot.

Generates a probability plot of sample data against the quantiles of a specified theoretical distribution (the normal distribution by default). **probplot** optionally calculates a best-fit line for the data and plots the results using Matplotlib or a given plot function.

**Parameters:** `x : array_like`  
Sample/response data from which **probplot** creates the plot.

`sparams : tuple, optional`  
Distribution-specific shape parameters (shape parameters plus location and scale).

`dist : str or stats.distributions instance, optional`  
Distribution or distribution function name. The default is 'norm' for a normal probability plot. Objects that look enough like a stats.distributions instance (i.e., they have a `rvs` method) are also accepted.

[source]

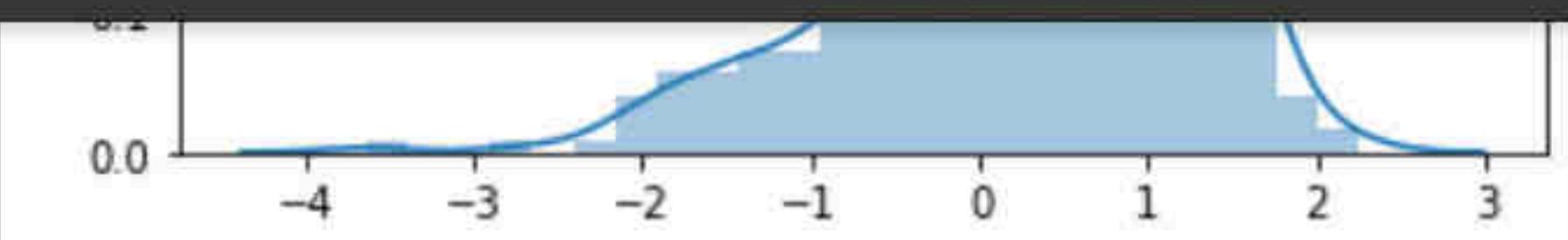
QQ-plot and CLT and Bootstrap x scipy.stats.probplot — SciPy v x statsmodels.graphics.gofplots x +

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RAM Disk

+ Code + Text

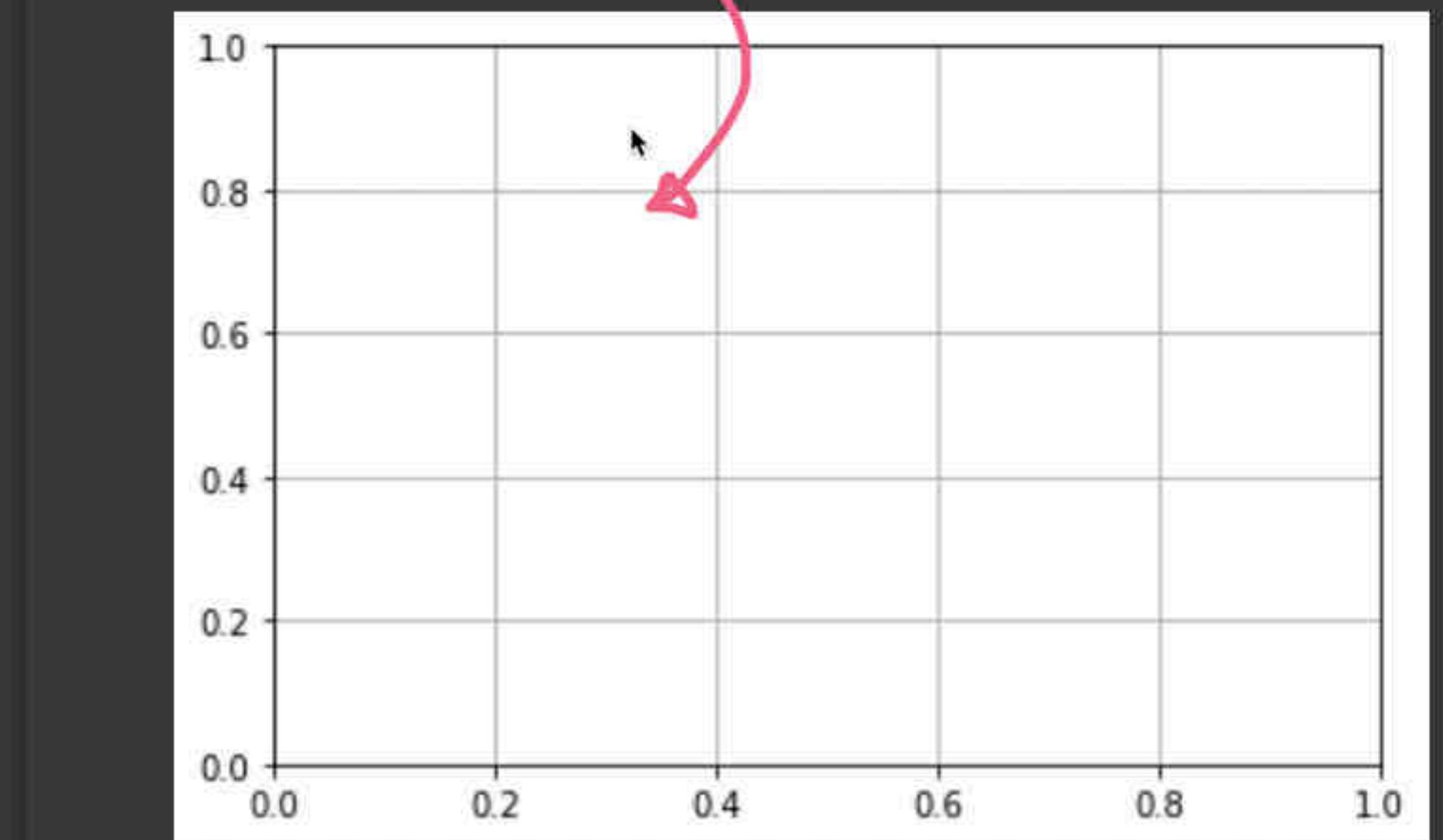
[5]



{x}

[x]

```
#QQ-Plot  
fig, ax1 = plt.subplots()  
plt.grid()  
prob = stats.probplot(x, dist=stats.norm)
```

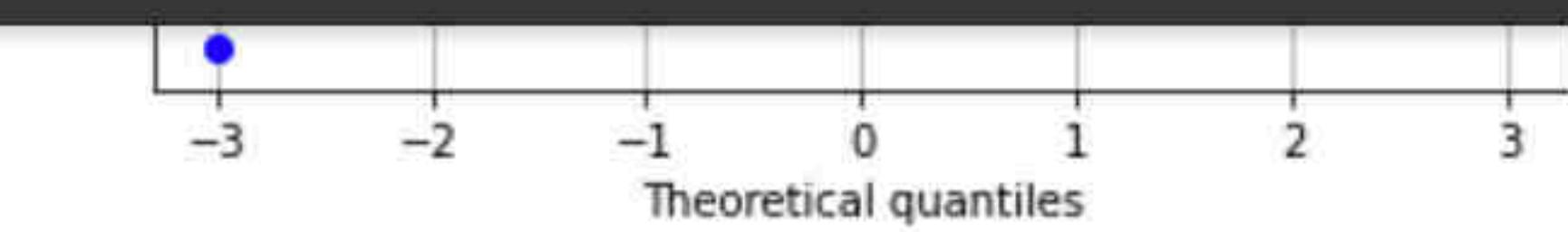


```
161 import statsmodels.api as sm
```



+ Code + Text

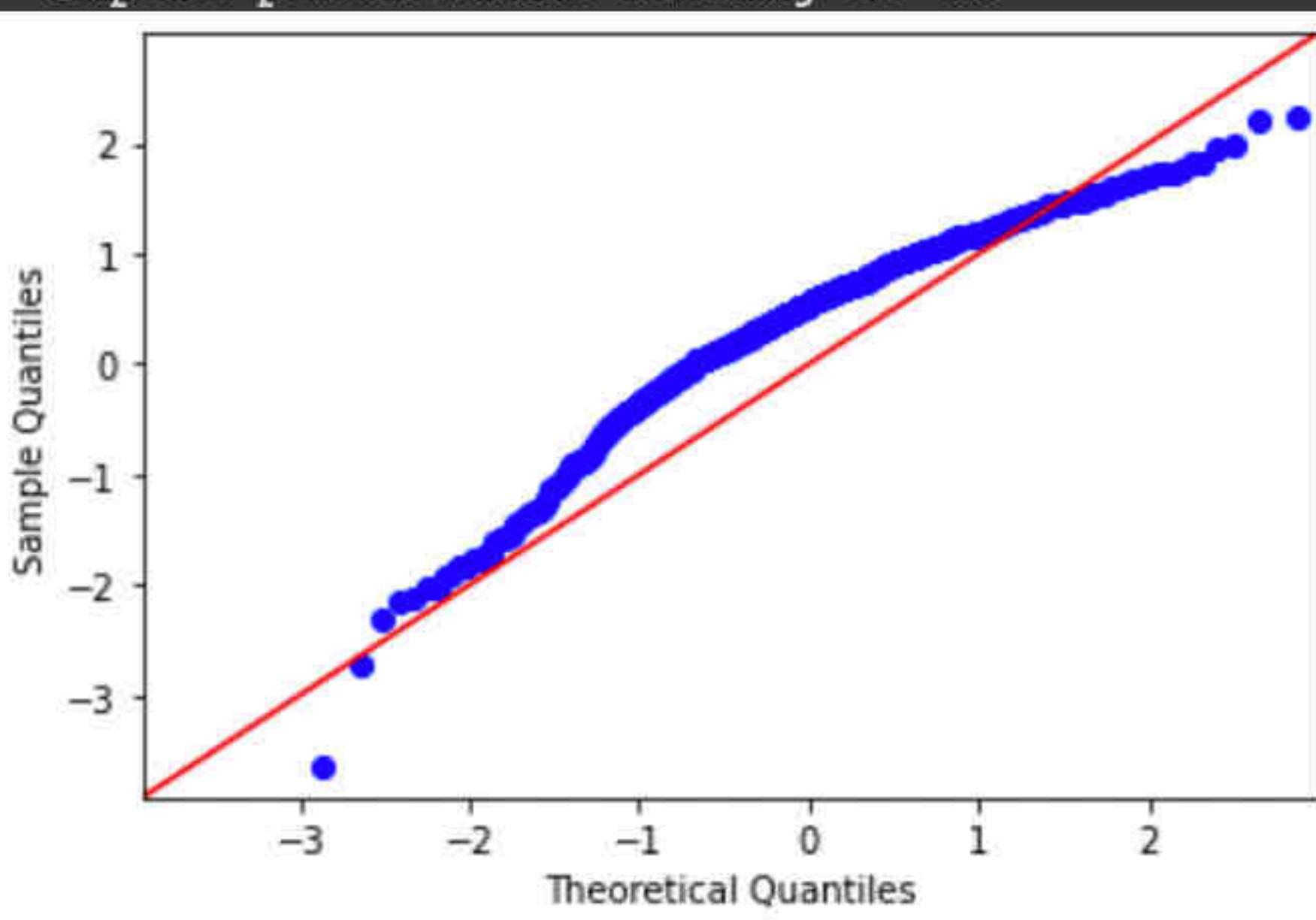
RAM Disk



100

```
[6] import statsmodels.api as sm  
      fig = sm.qqplot(x, line='45')
```

```
/usr/local/lib/python3.7/dist-packages/statsmodels/tools/_testing.py:19: FutureWarning: pandas.util.testing is deprecated
```



$$x_1, \dots, x_m$$

~~Normal~~

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RAM Disk

+ Code + Text

RAM Disk

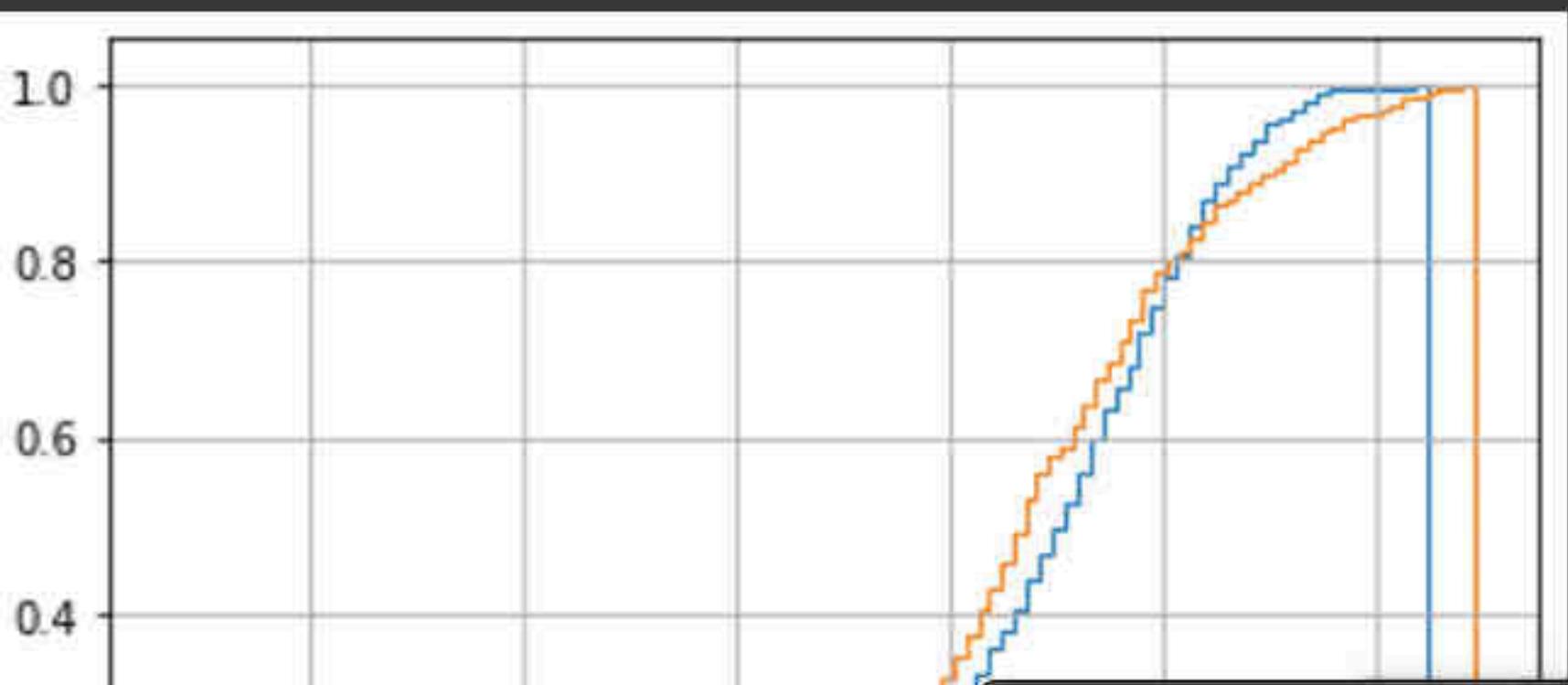
# Let us compare CDFs also  
mu = np.mean(x)  
s = np.std(x)  
print(mu,s)

sample-Mean  $\approx \mu$

0.40812679178 0.8571215209422999

[ ] # normally distributed data with mean=mu, std-dev=s  
y = stats.norm.rvs(loc=mu, scale=s, size=500)

plt.grid()  
a = plt.hist(x, bins=100, cumulative=True, label='CDF', density=True, histtype='step')  
b = plt.hist(y, bins=100, cumulative=True, label='CDF', density=True, histtype='step')  
plt.show()



∞ QQ-plot and CLT and Bootstrap | S scipy.stats.probplot — SciPy v1.6.3.dev0+g3a09d1f6f6 | statsmodels.graphics.gofplots | +

[colab.research.google.com/drive/1m1Wa-7i9WknfRE9Y\\_aol\\_5cbm5AAJBjW#scrollTo=gEeJVDFch9WR](https://colab.research.google.com/drive/1m1Wa-7i9WknfRE9Y_aol_5cbm5AAJBjW#scrollTo=gEeJVDFch9WR)

+ Code + Text

✓ RAM Disk

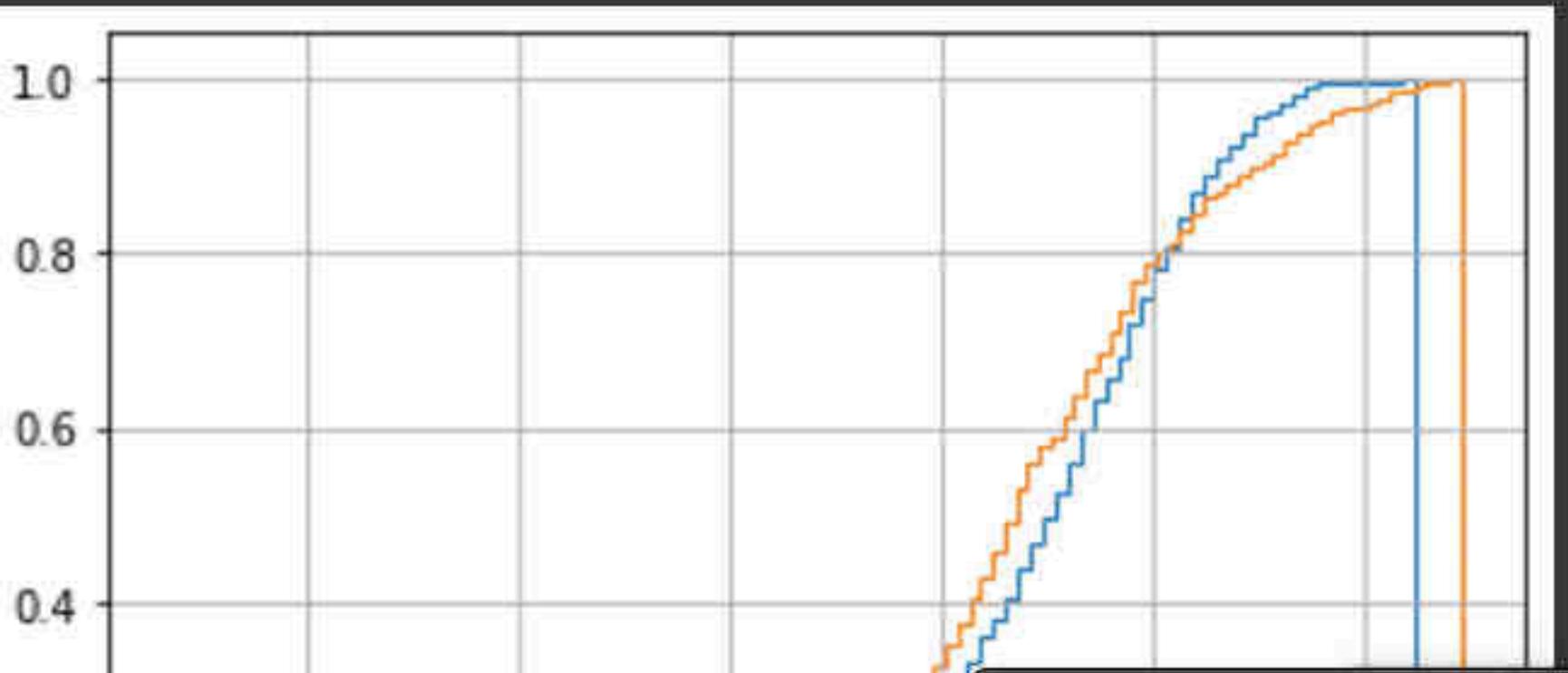
A set of small, light-gray navigation icons located at the bottom right of the slide. From left to right, they include: a downward arrow, a circular arrow, a speech bubble, a gear, a square with a diagonal line, a trash can, and three vertical dots.

```
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+ Code + Text

RAM Disk

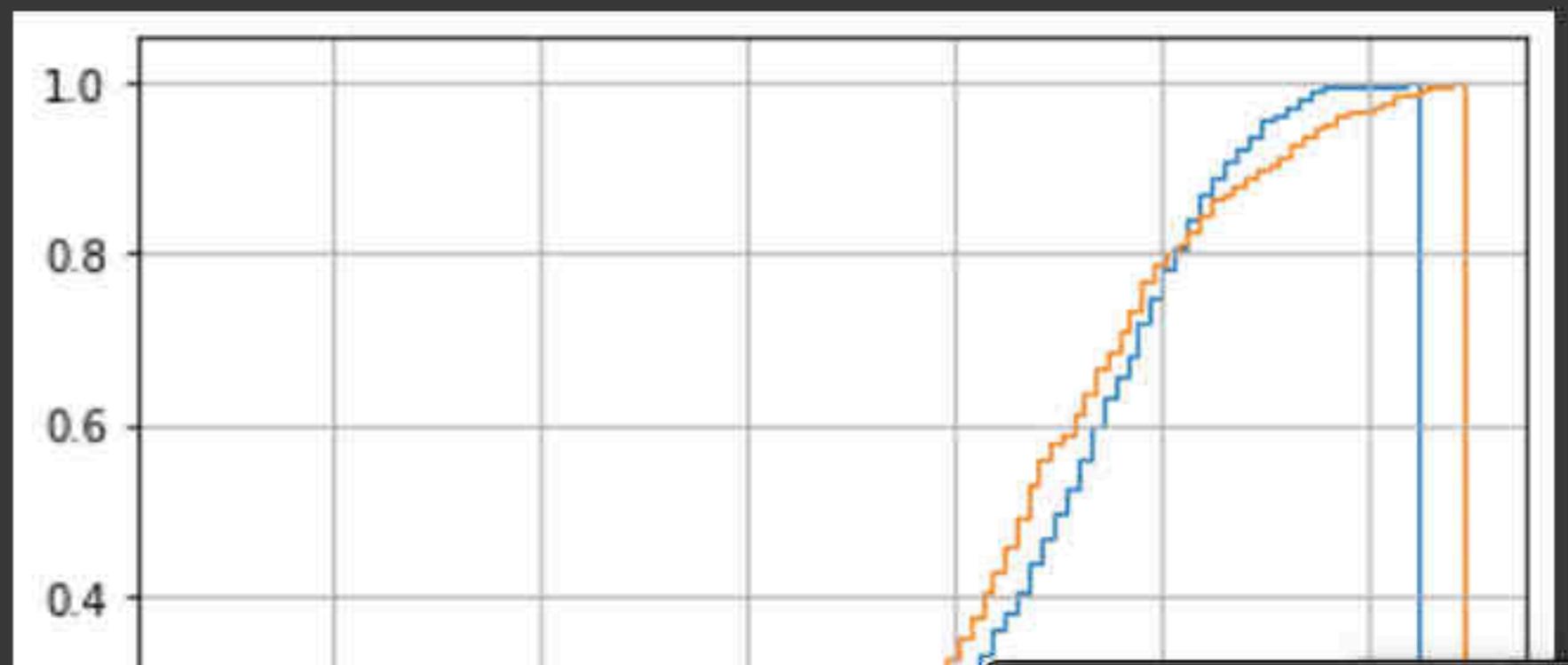
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$x: \underline{\text{obs-data}}$   
 $x_1, \dots, x_{500}$   
 $\mu, \sigma$  : Using SampleData

```
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RAM Disk

+ Code + Text

✓ RAM  
Disk

Users Settings

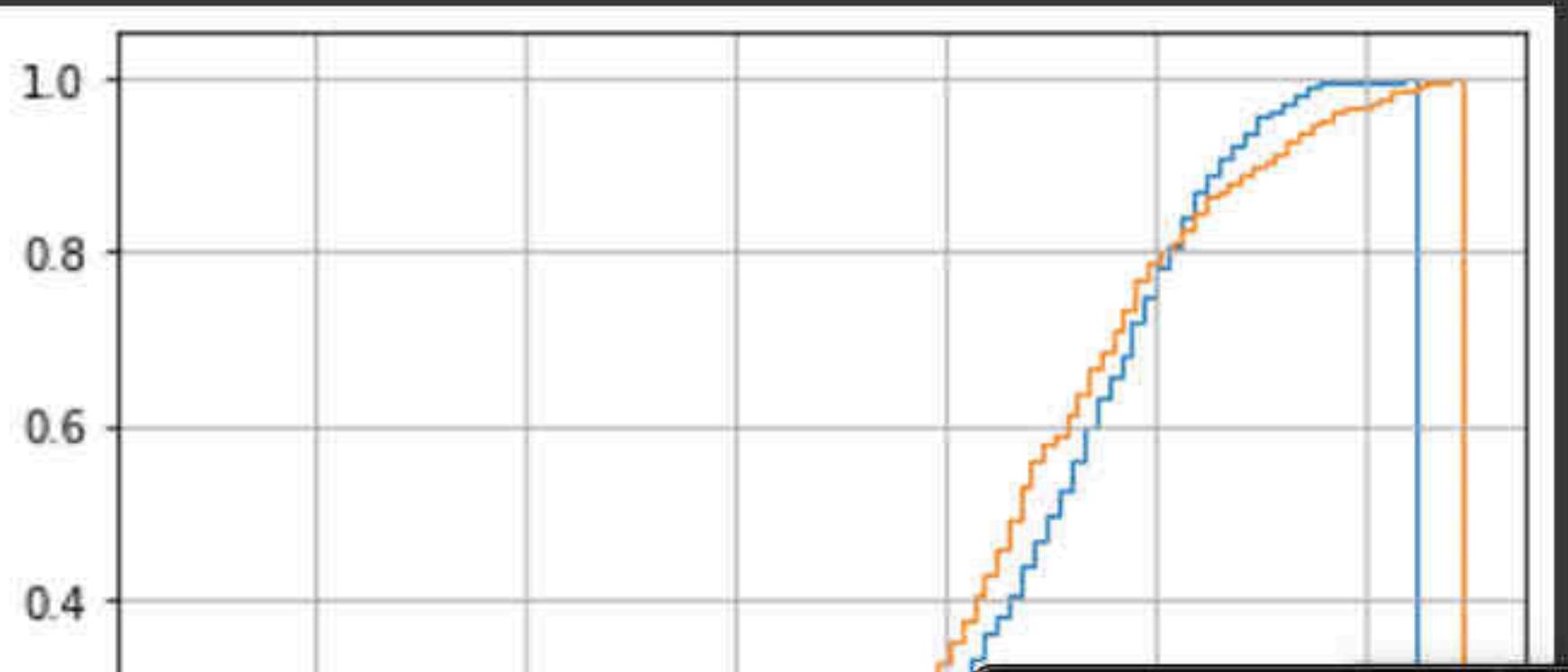
Up Down Reload Settings Copy Clear :>

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RAM Disk

+ Code + Text

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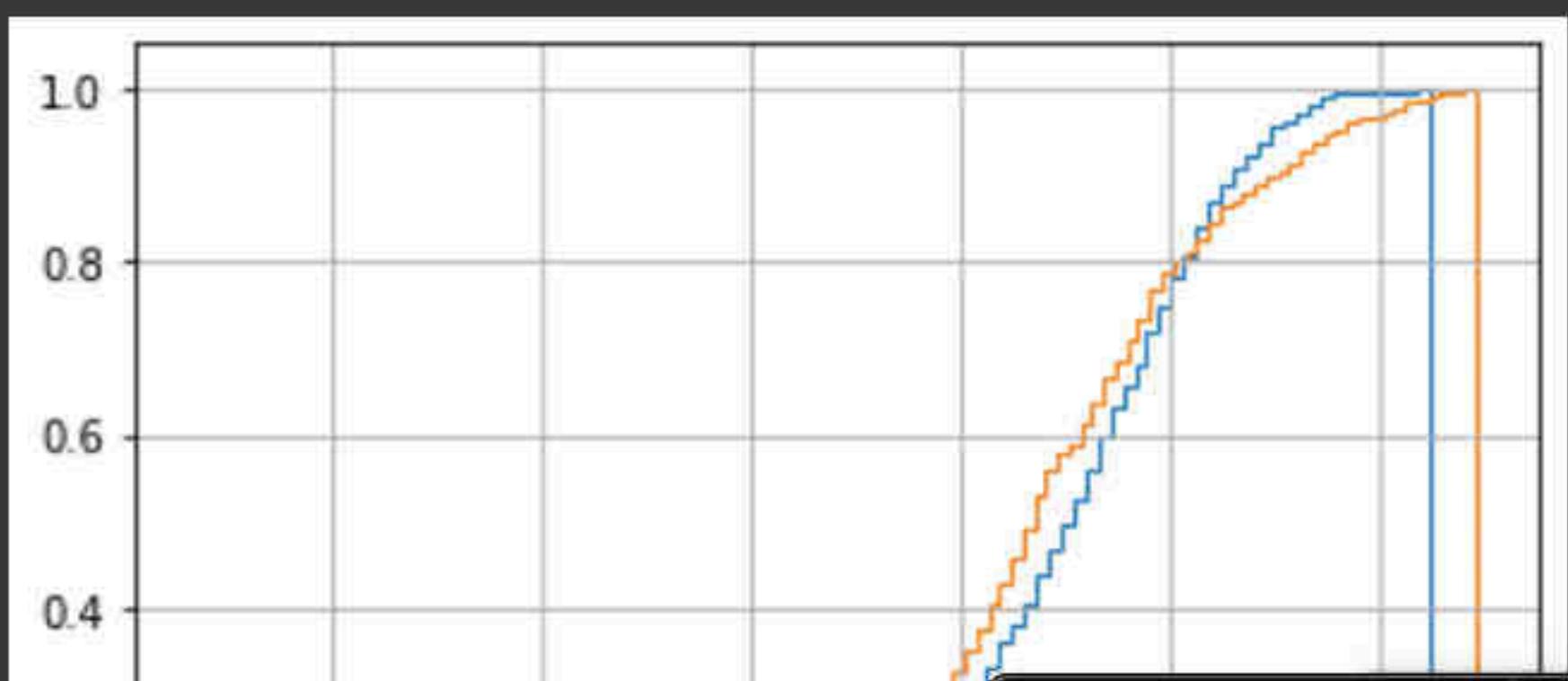
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$y_1 \dots y_m$

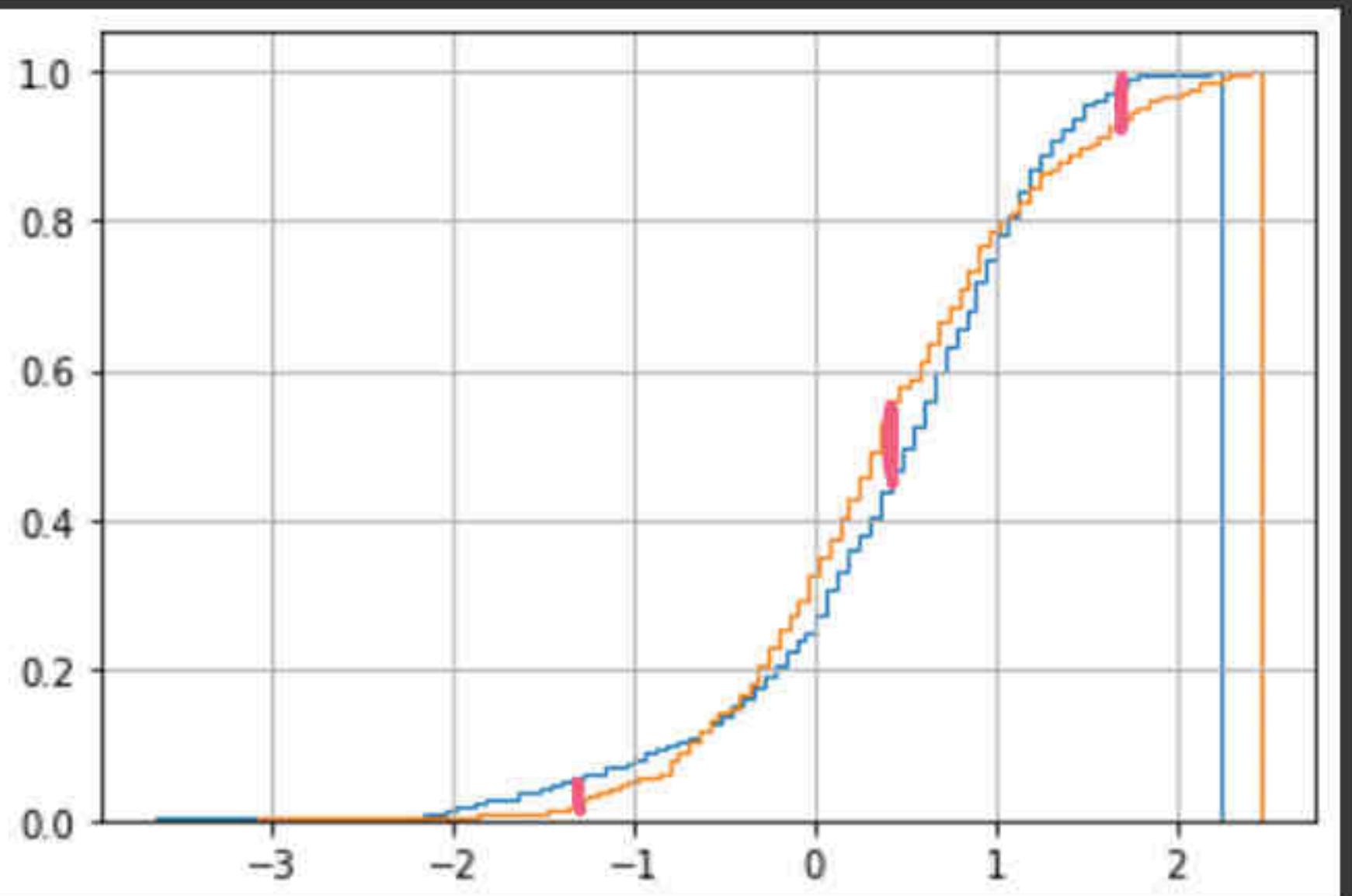
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+ Code + Text  
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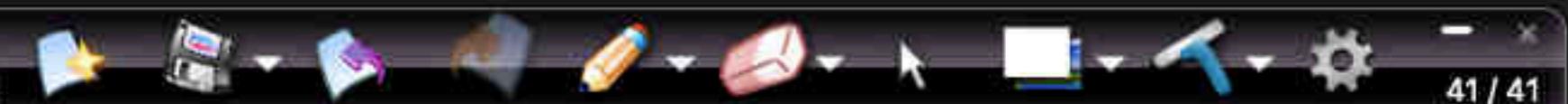
[ ] plt.grid()  
a = plt.hist(x, bins=100, cumulative=True, label='CDF', density=True, histtype='step')  
b = plt.hist(y, bins=100, cumulative=True, label='CDF', density=True, histtype='step')  
plt.show()



more gap → more likely (be)

X Y

[ ] # case 2: QQ Plot for gaussian disb itself  
x = stats.norm.rvs(loc=0, scale=1, size=500) # change 500 to 5000  
sns.distplot(x)

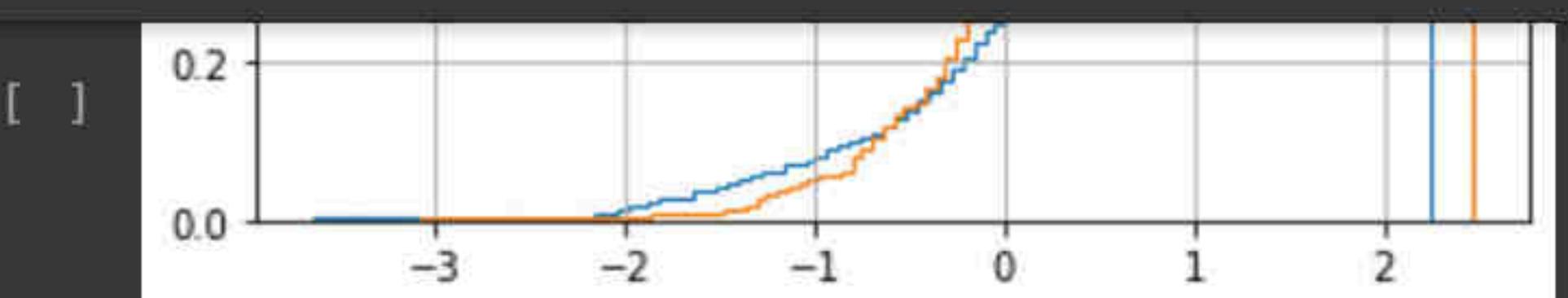


QQ-plot and CLT and Bootstrap x scipy.stats.probplot — SciPy x statsmodels.graphics.gofplots x +

colab.research.google.com/drive/1m1Wa-7i9WknfRE9Y\_aol\_5cbm5AAJBjW#scrollTo=gEeJVOFcH9WR

+ Code + Text

✓ RAM Disk



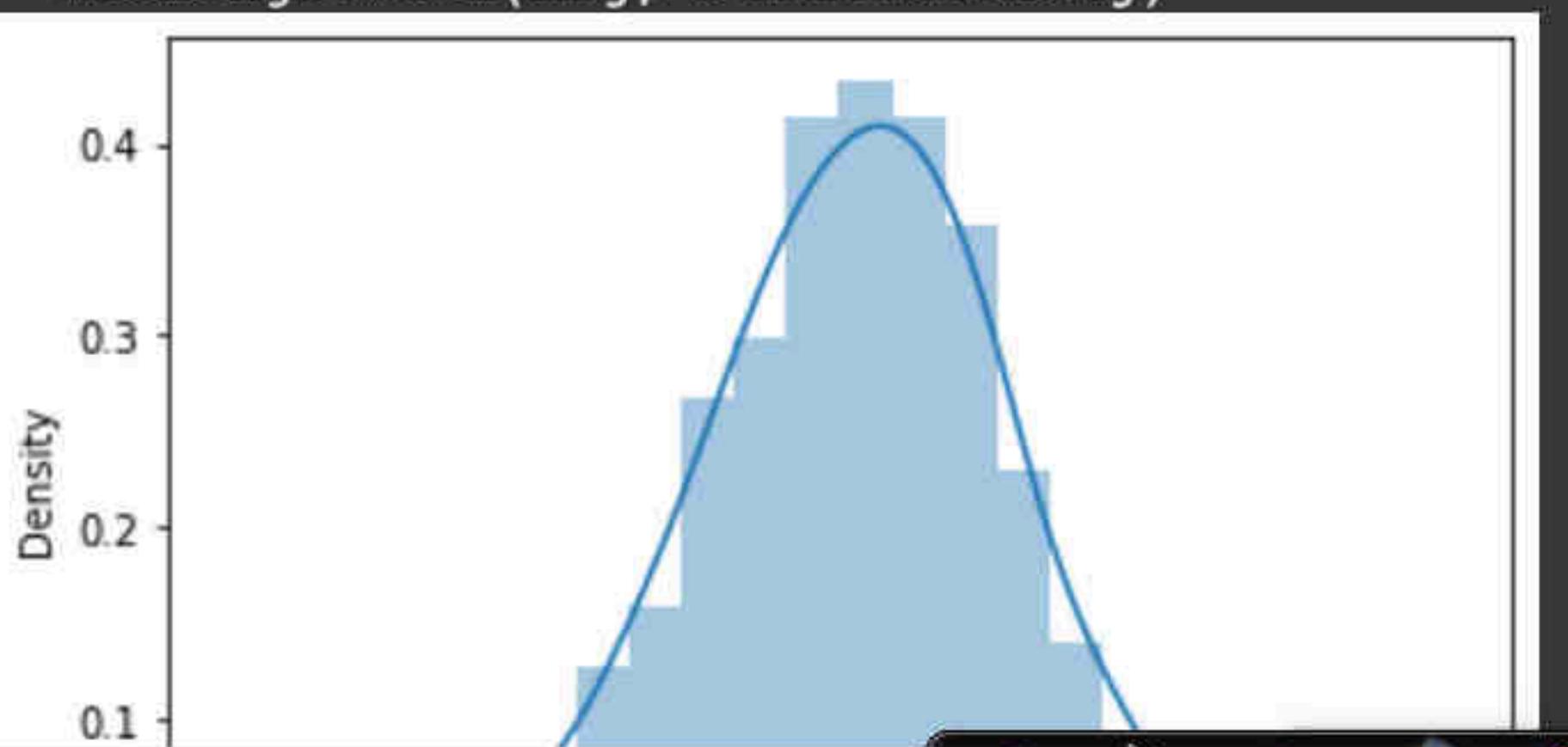
{x}

```
# case 2: QQ Plot for gaussian disb itself
x = stats.norm.rvs(loc=0, scale=1, size=500) # change 500 to 5000
sns.distplot(x)

#QQ-Plot
fig, ax1 = plt.subplots()
plt.grid()
prob = stats.probplot(x, dist=stats.norm, plot=ax1)
```

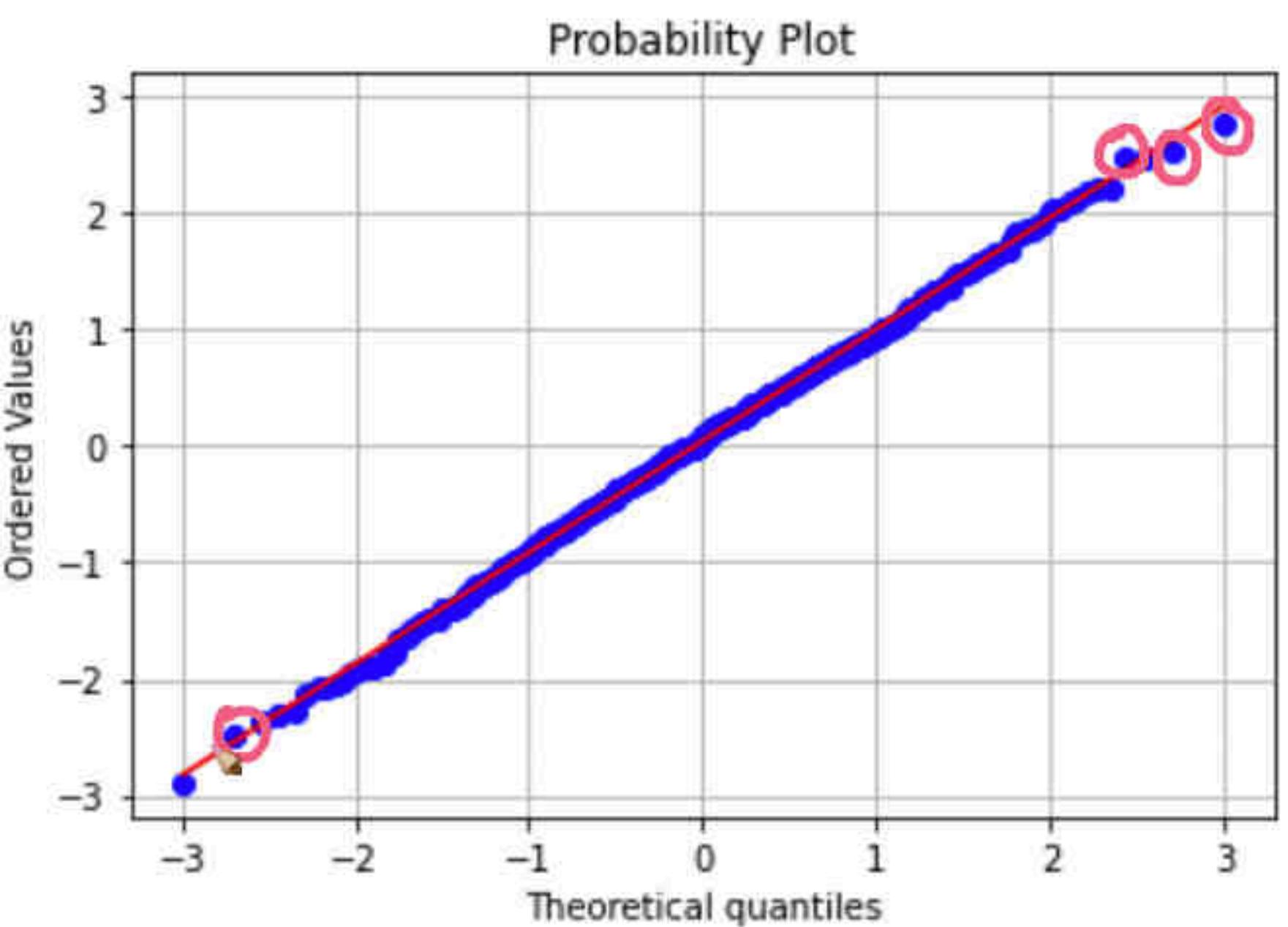
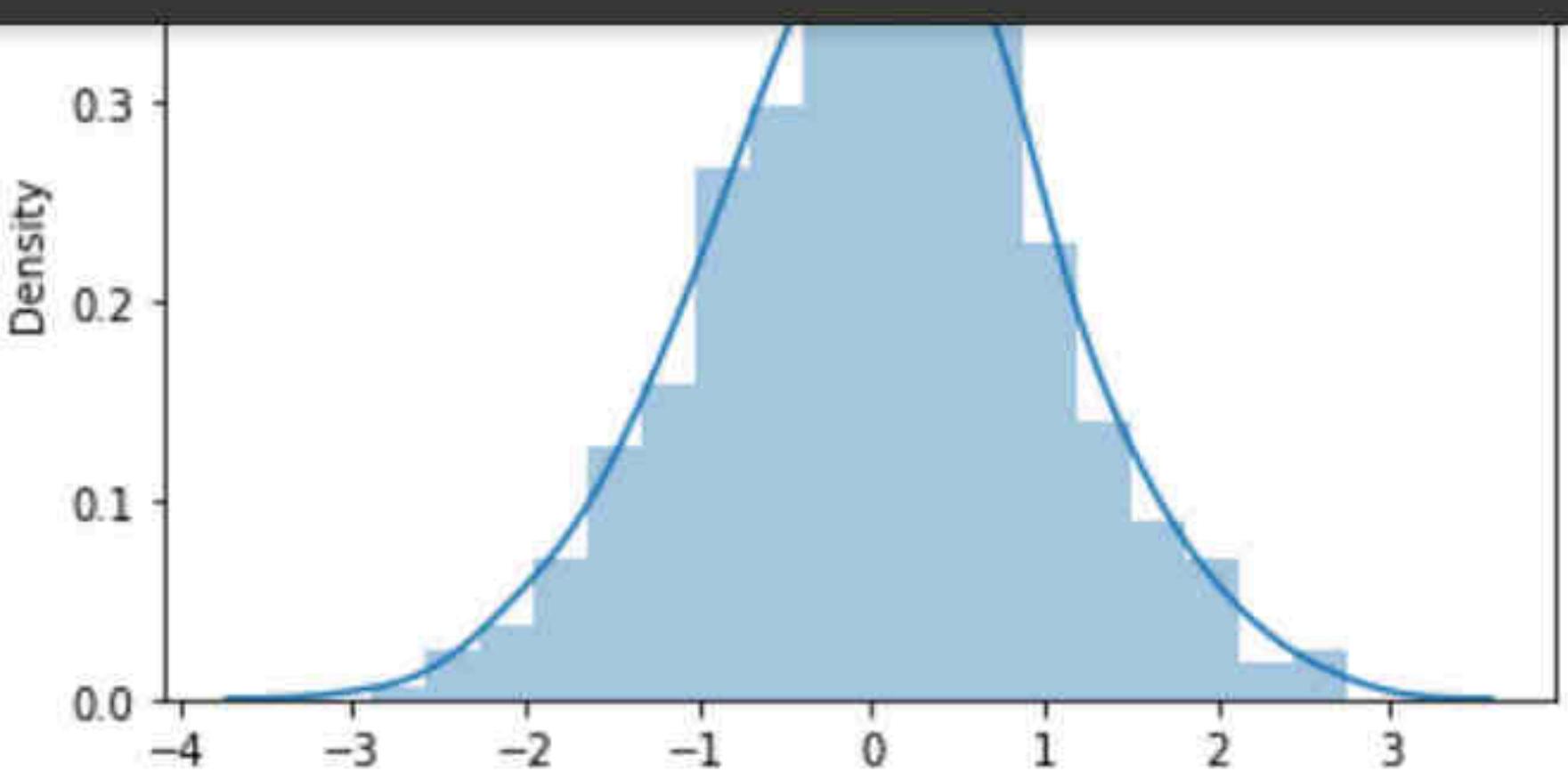
/usr/local/lib/python3.7/dist-packages/seaborn/distributions.py:2619: FutureWarning: `distplot` is a deprecated func  
warnings.warn(msg, FutureWarning)

$x_1, \dots, x_n$

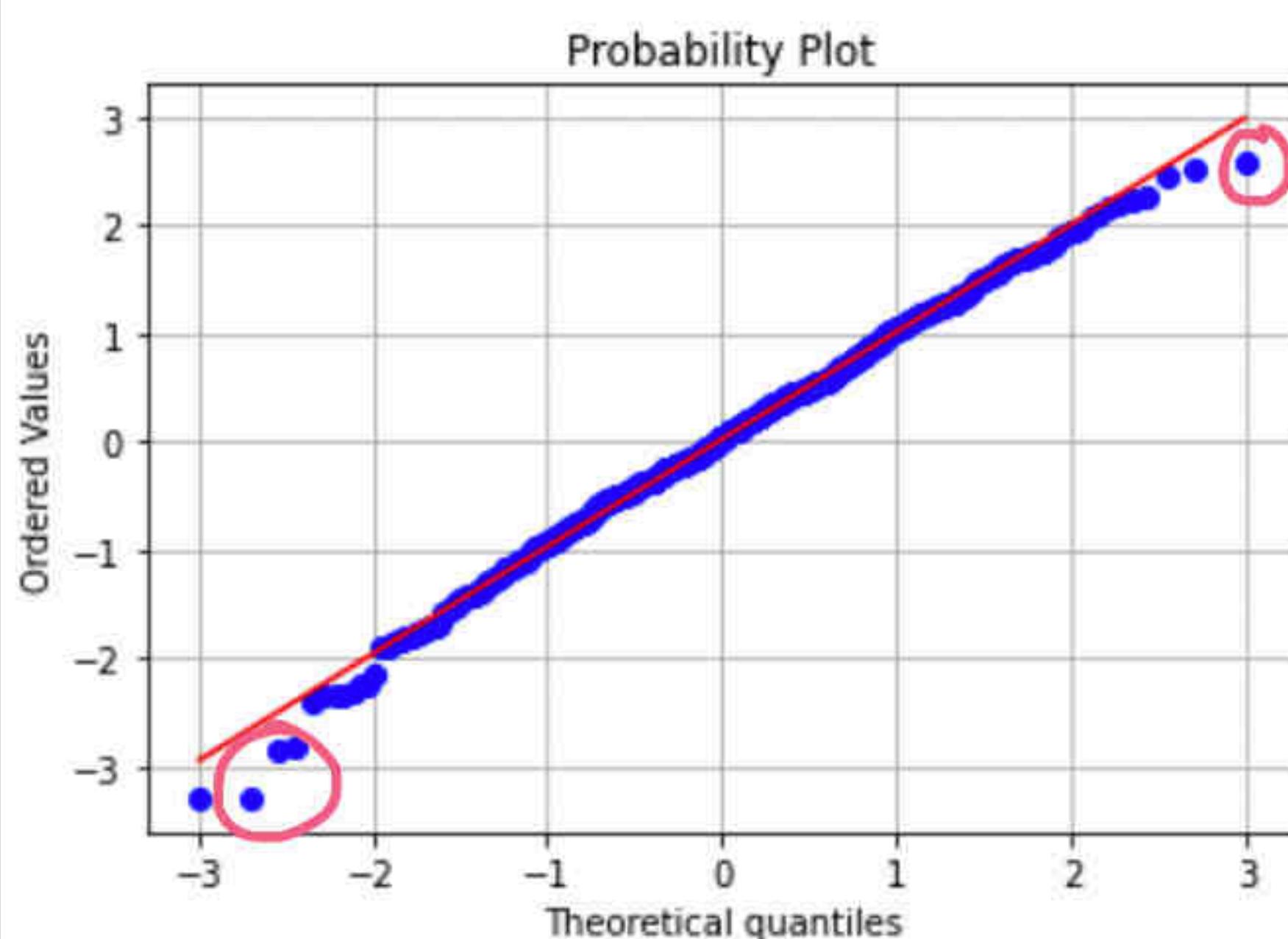
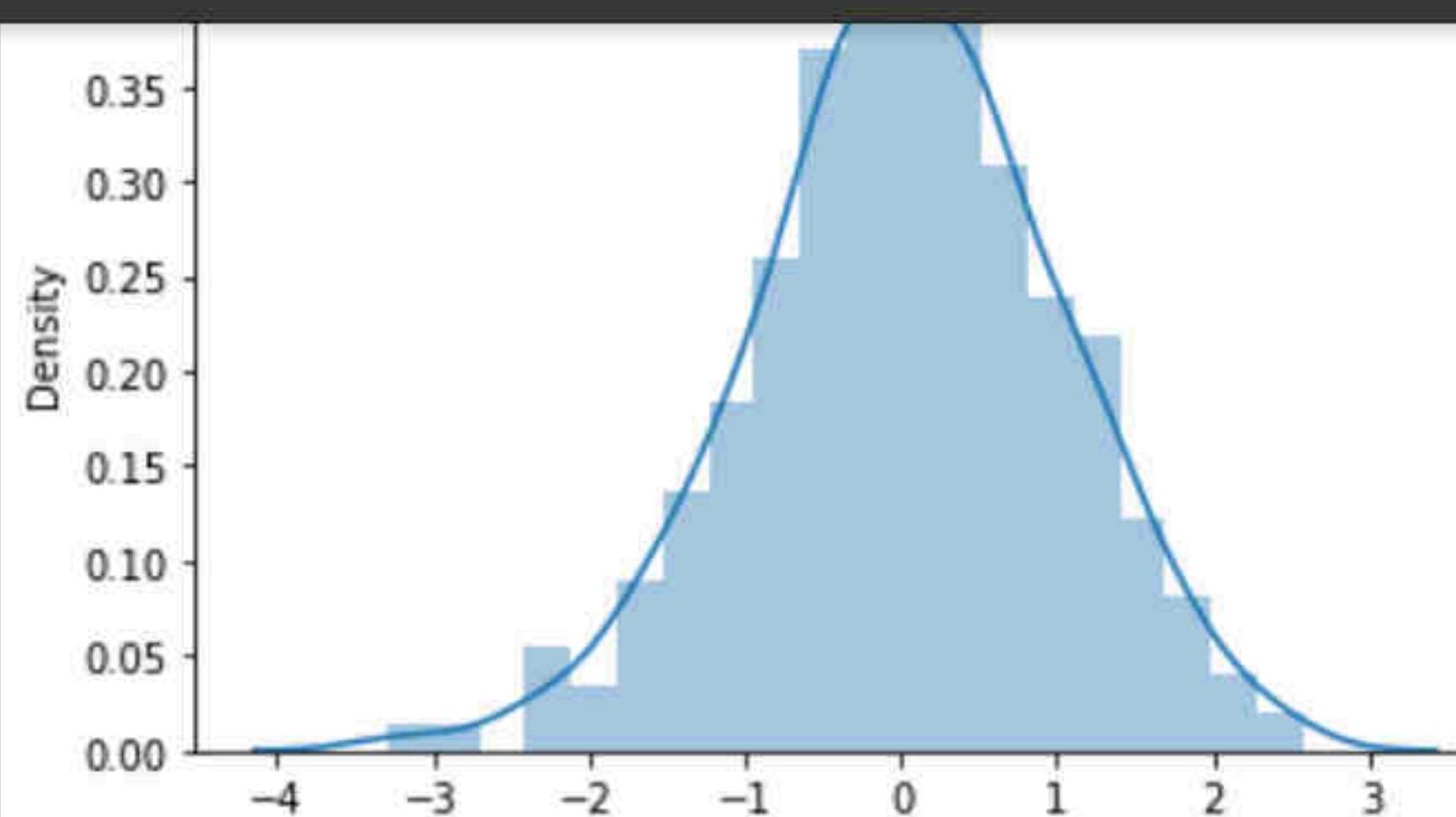


QQplot

+ Code + Text



+ Code + Text



$n \downarrow$  :

$n =$

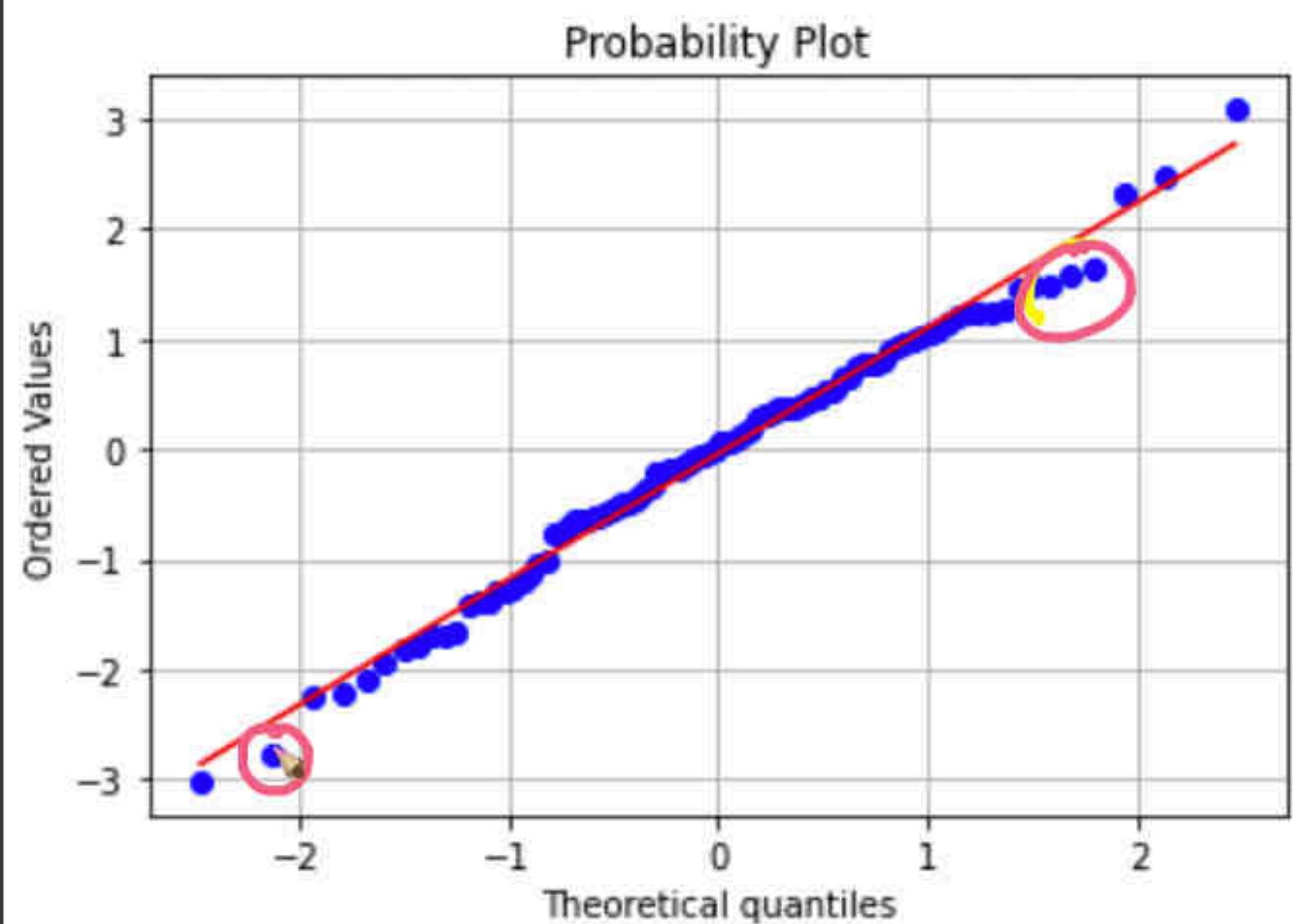
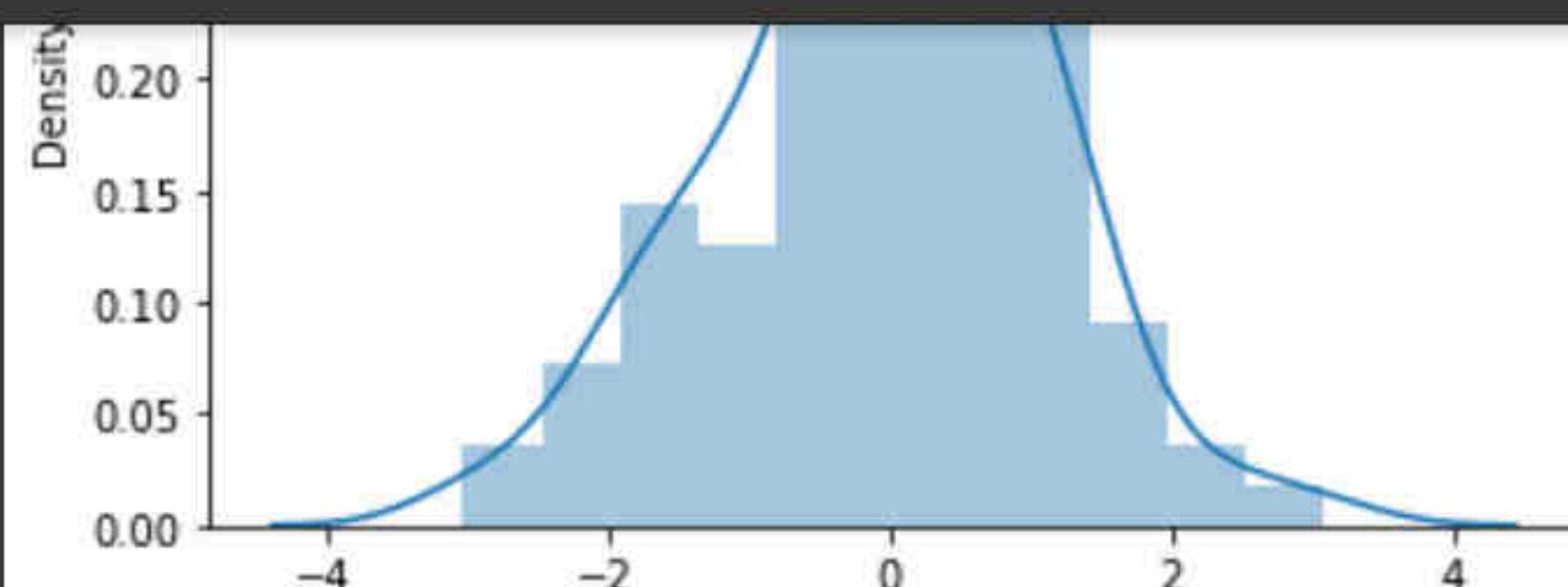
$\sim 500$  obs



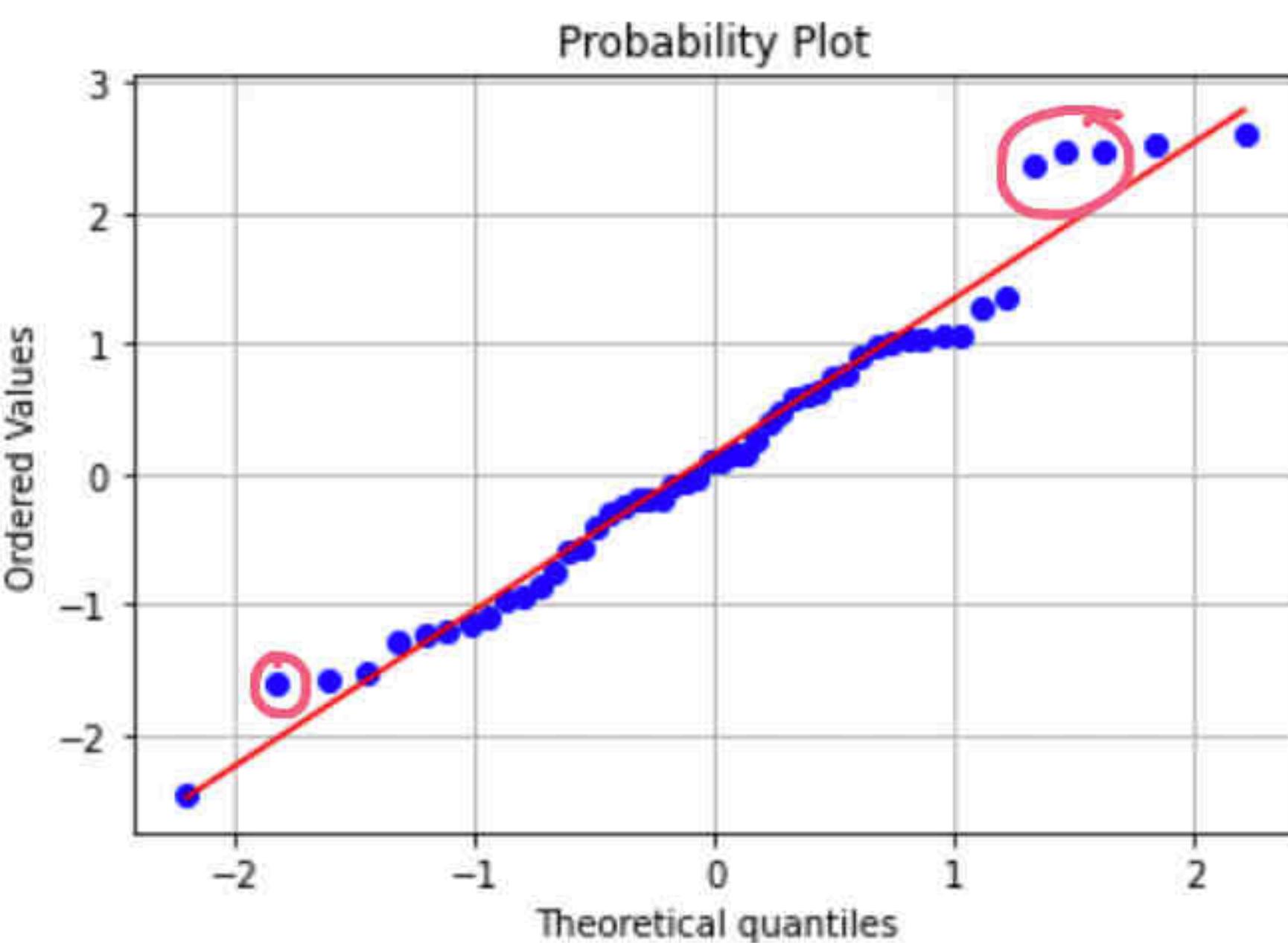
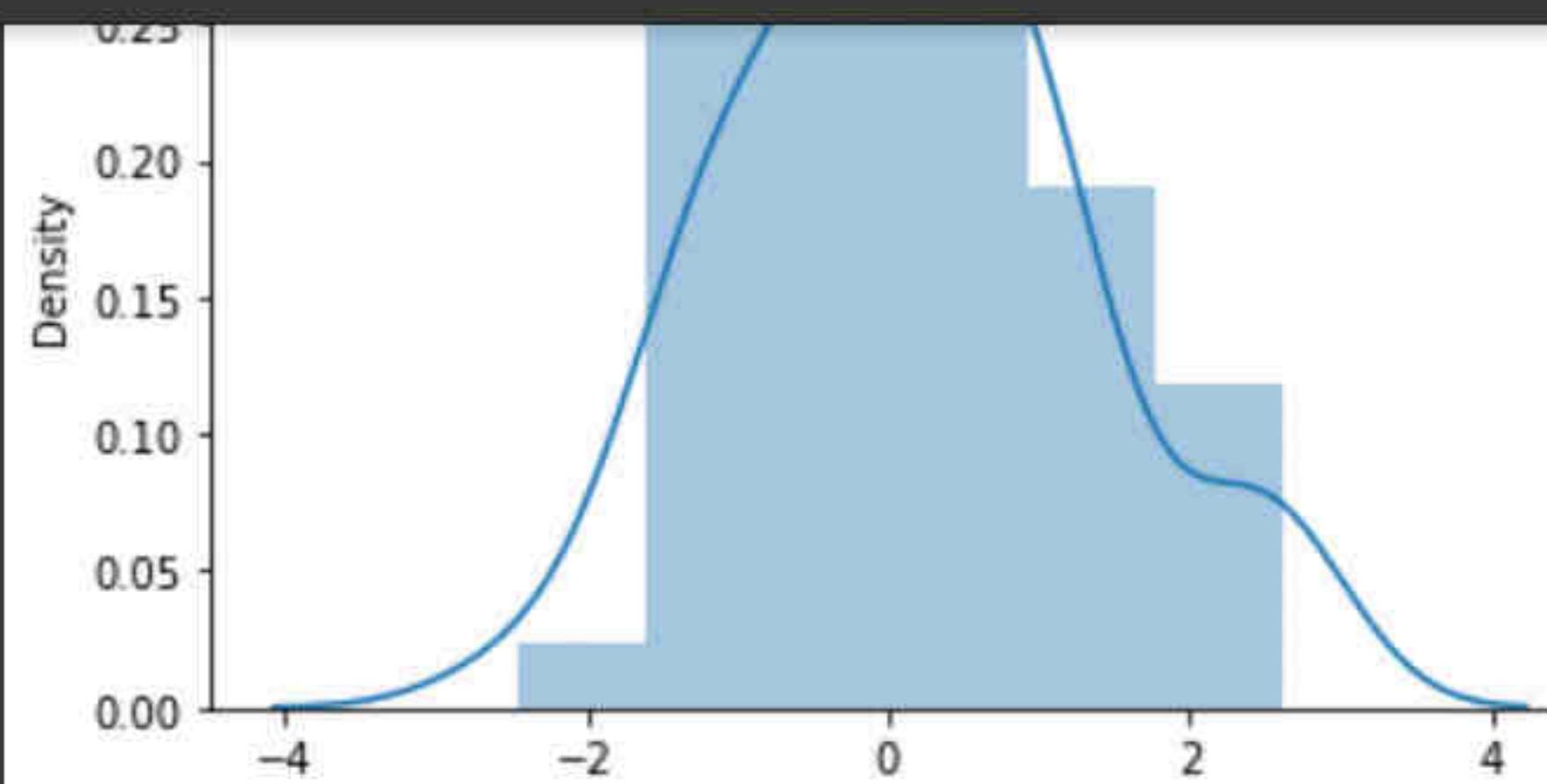
as  $n \rightarrow \infty$



+ Code + Text

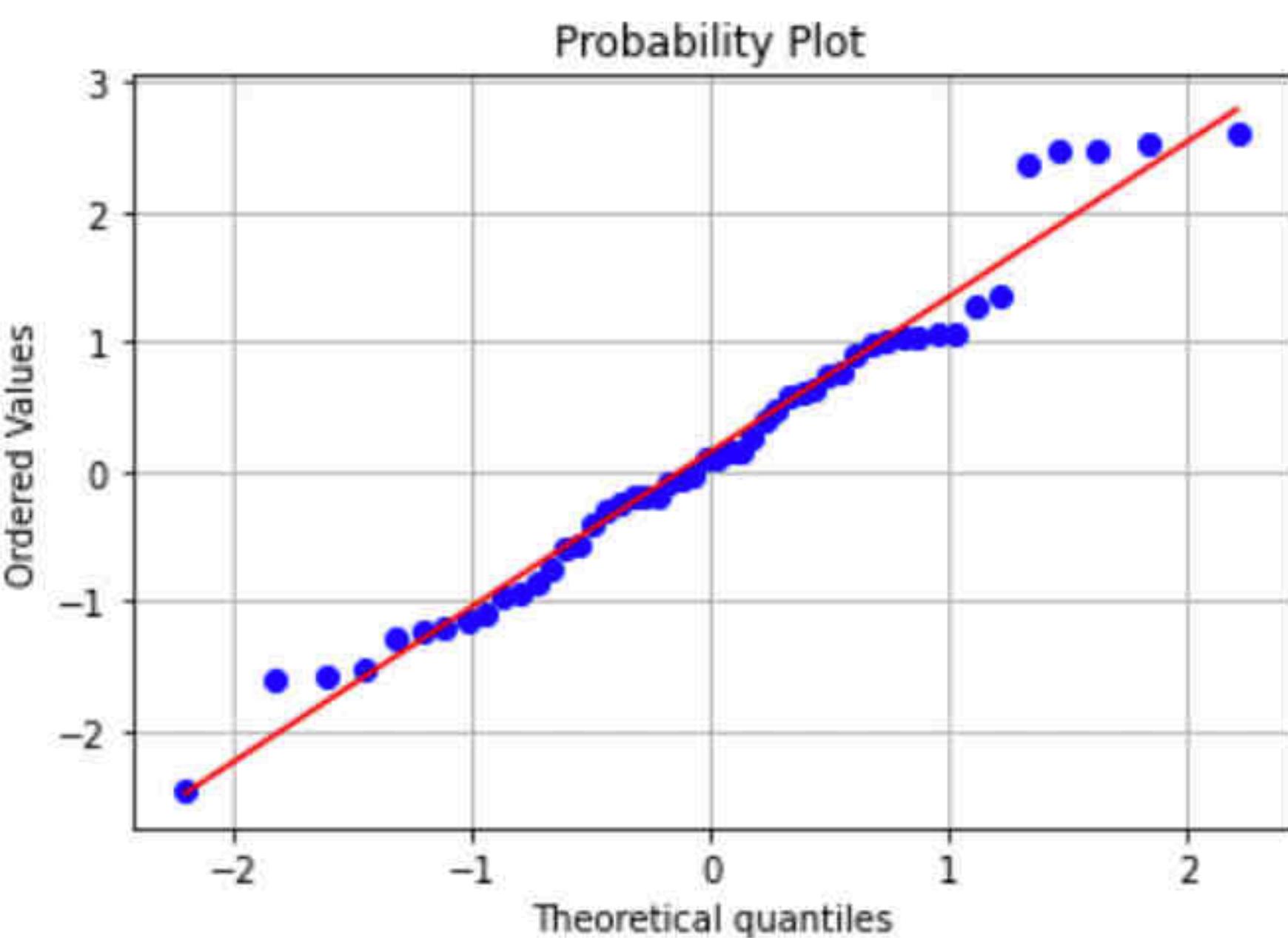
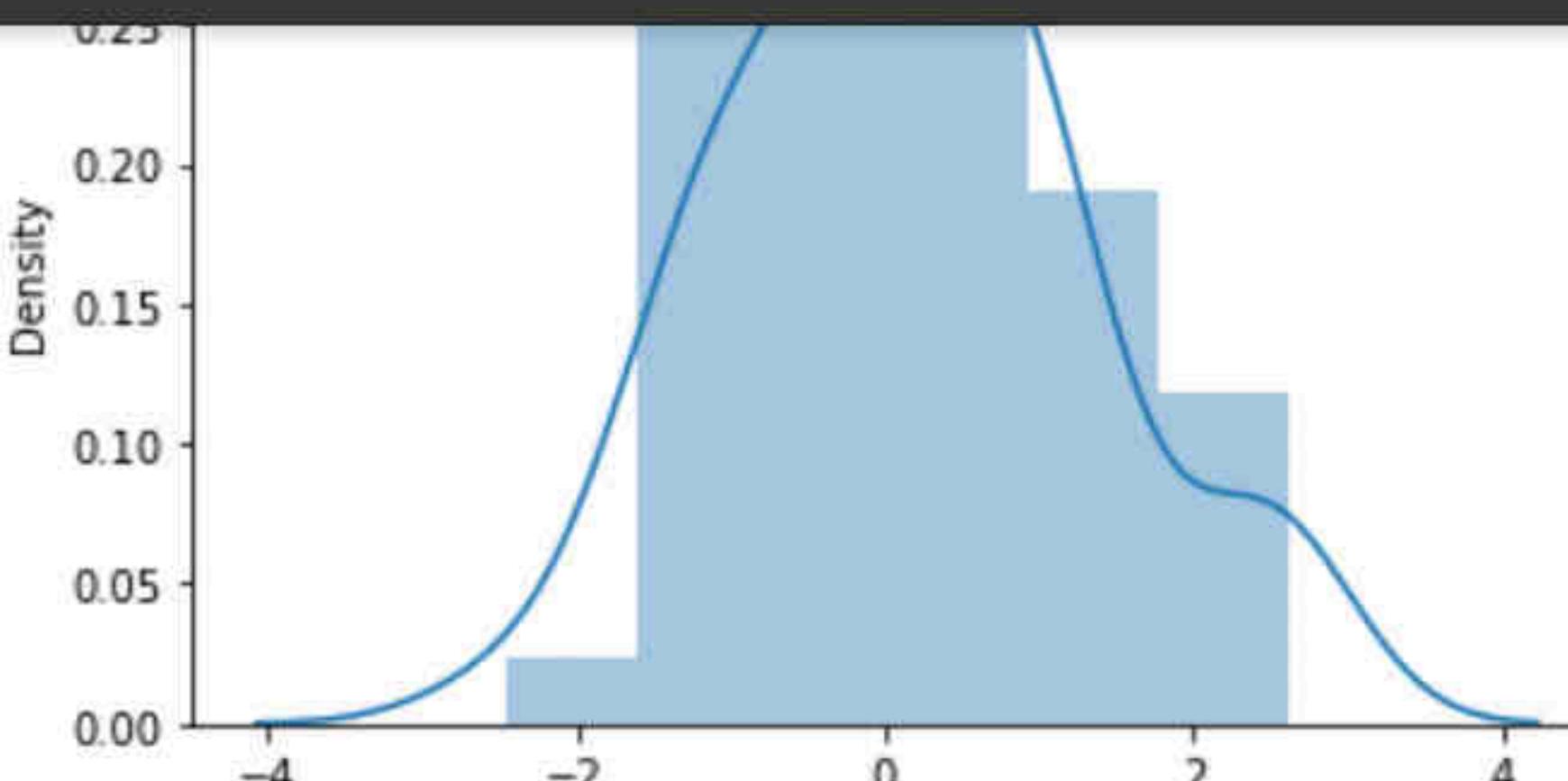


+ Code + Text



QQplot withly ↓

+ Code + Text

as  $n \rightarrow \infty$ 

Q-Qplot will  
work perfectly...

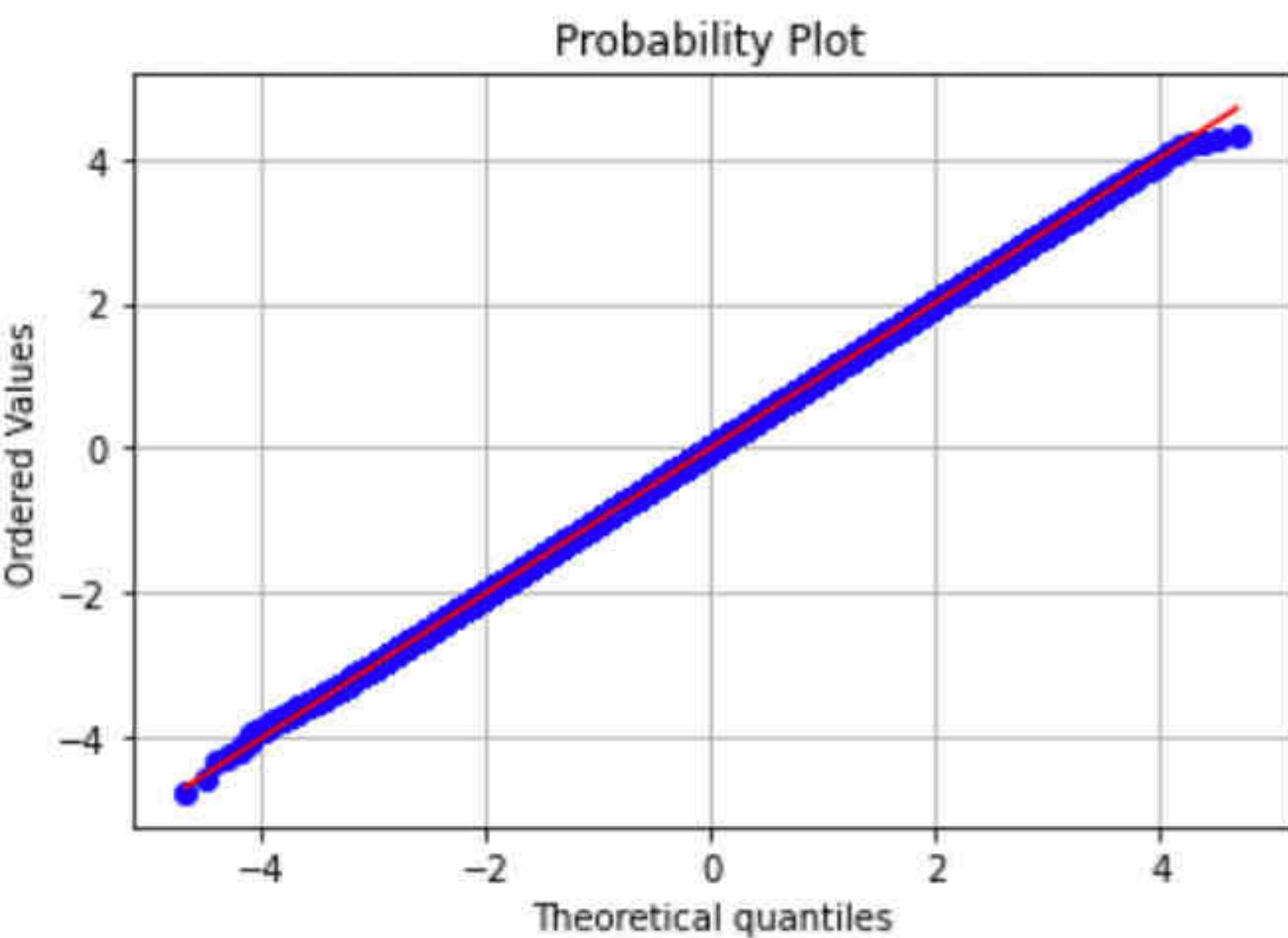
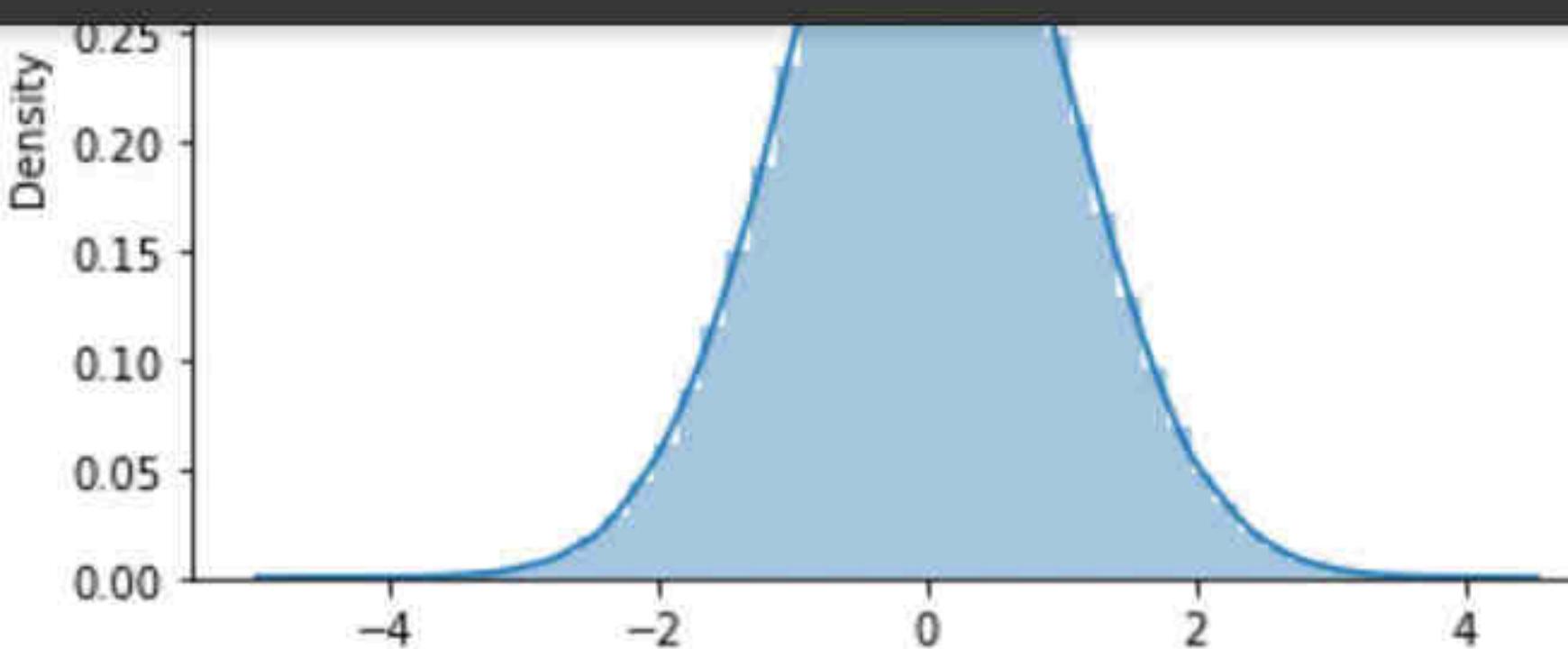
QQ-plot and CLT and Bootstrap

scipy.stats.probplot — SciPy

colab.research.google.com/drive/1m1Wa-7i9WknfRE9Y\_aol\_5cbm5AAJBjW#scrollTo=ZR4zGbf\_I8Sp

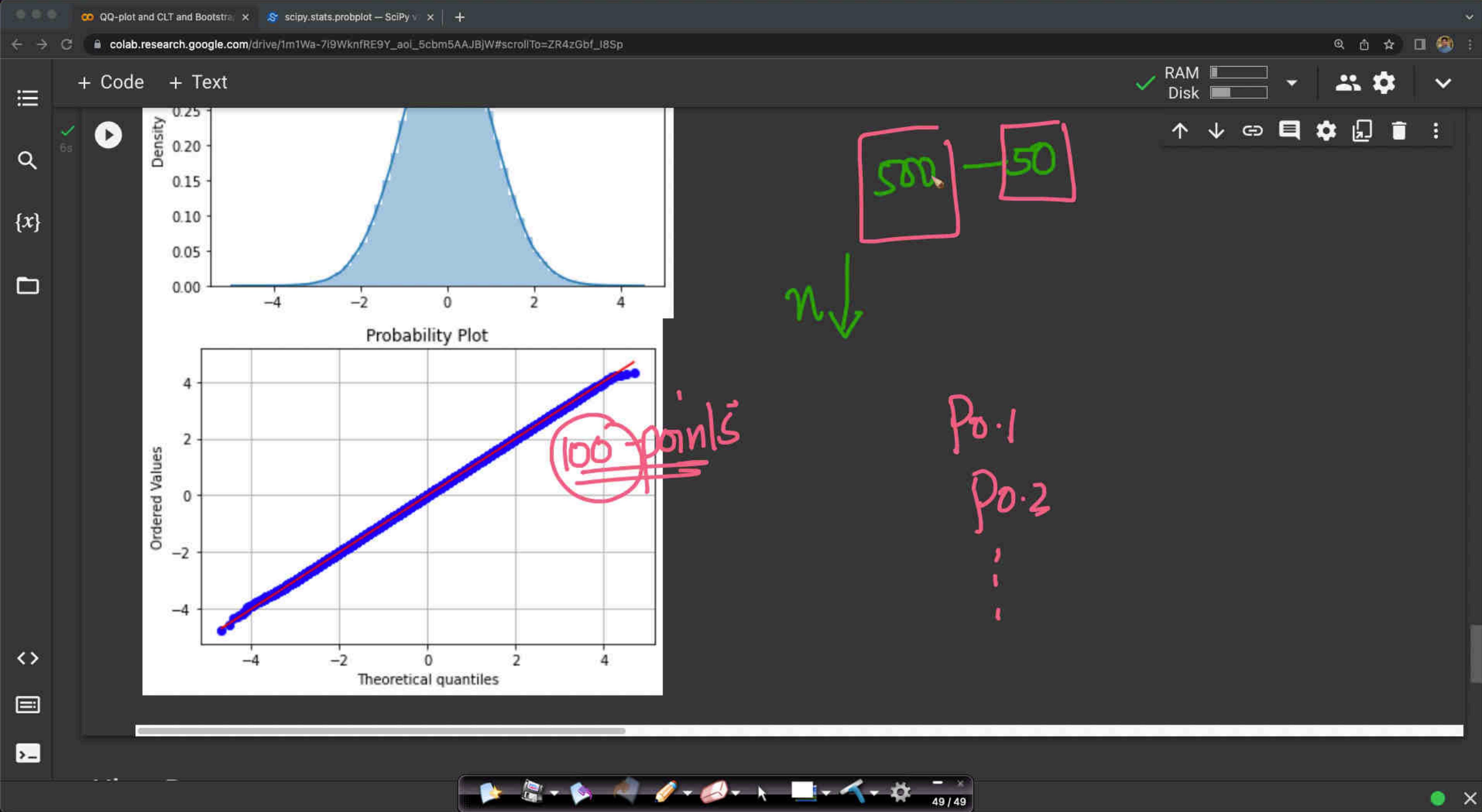
RAM Disk

+ Code + Text

 $n \uparrow$ 

QQ-plot will behave  
perfect

obs data  $\sim N(\cdot)$

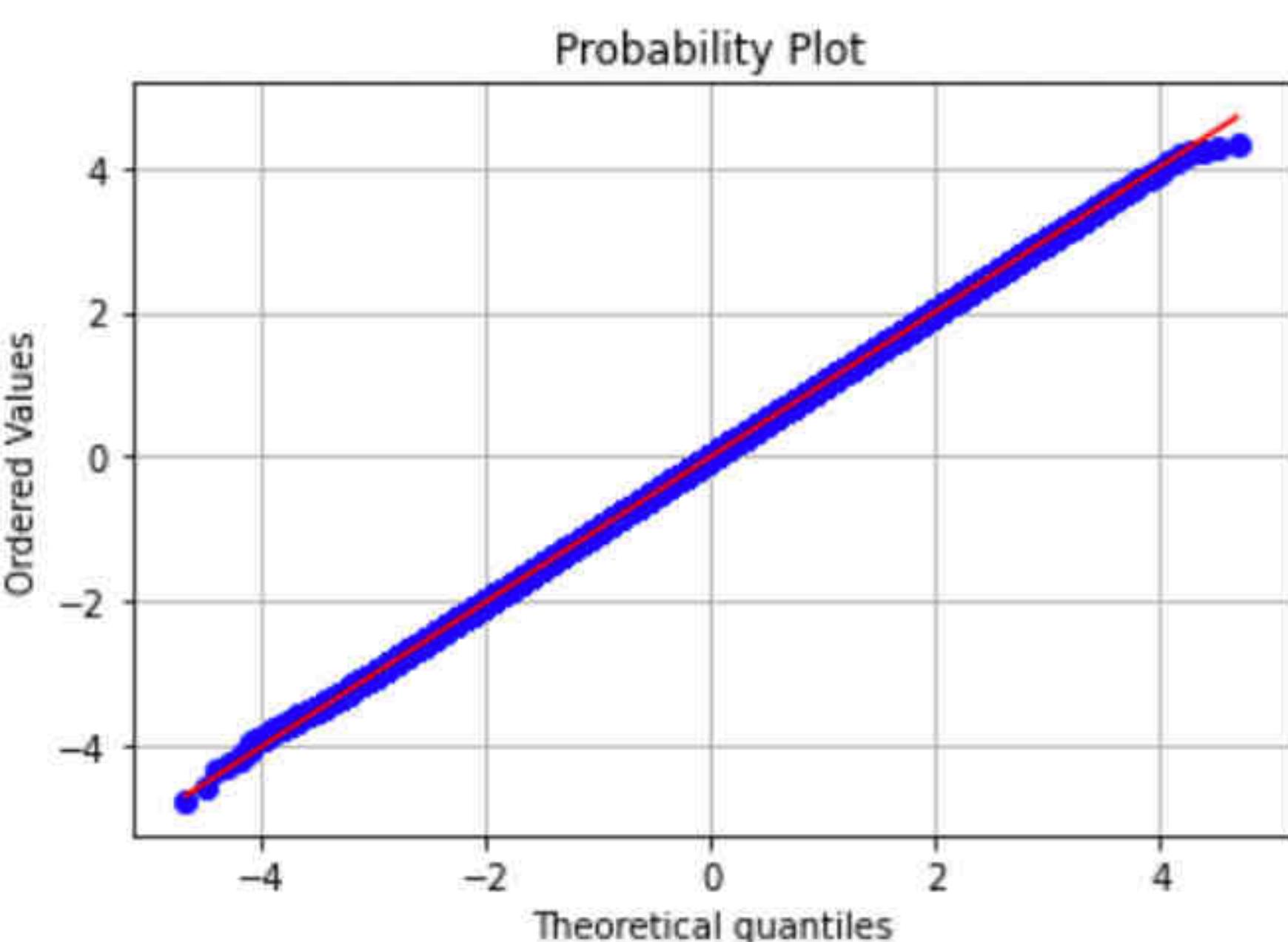


[OO-plot and CLT and Bootstrap](#) × [scipy.stats.probplot – SciPy v1.6.0 documentation](#) ×

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Code + Text

A density plot of a standard normal distribution. The x-axis ranges from -4 to 4 with major ticks at -4, -2, 0, 2, and 4. The y-axis is labeled "Density" and ranges from 0.00 to 0.25 with major ticks at 0.00, 0.05, 0.10, 0.15, 0.20, and 0.25. The distribution is a symmetric bell curve centered at 0, with the highest density (approximately 0.25) occurring near the center. The area under the curve is shaded in light blue.



n is small

→ KS-test

Sw-Test

## AD-test



Programming and

X [stats-scipy  
statsmodels]

WAF to plot QQ-plot using  
scatter plot & line plot

20-25 min

$f(x, \text{dis}, \dots)$

WAF to plot  $\sim$  PDF from scratch

20-Min

✓ [ QQ-plot from scratch on your own ]



implement func or class in popular lib

JOIN pandas --

# Confidence Intervals

Covid

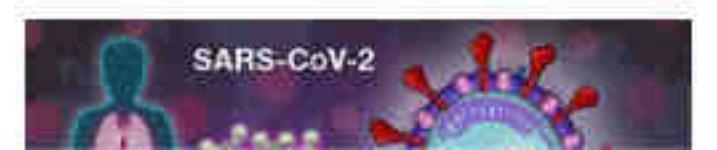
were randomly assigned to receive either remdesivir (200 mg loading dose on day 1, followed by 100 mg daily for up to 9 additional days) or placebo for up to 10 days. The primary outcome was the time to recovery, defined by either discharge from the hospital or hospitalization for infection-control purpose only.

## RESULTS

A total of 1062 patients underwent randomization (with 541 assigned to remdesivir and 521 to placebo). Those who received remdesivir had a median recovery time of 10 days (95% confidence interval [CI], 9 to 11), as compared with 15 days (95% CI, 13 to 18) among those who received placebo (rate ratio for recovery, 1.29; 95% CI, 1.12 to 1.49;  $P < 0.001$ , by a log-rank test). In an analysis that used a proportional odds model with an eight-category ordinal scale, the patients who received remdesivir were found to be more likely than those who received placebo to have clinical improvement at day 15 (odds ratio, 1.5; 95% CI, 1.2 to 1.9, after adjustment for actual disease severity). The Kaplan–Meier estimates of mortality were 6.7% with remdesivir and 11.9% with placebo by day 15 and 11.4% with remdesivir and 15.2% with placebo by day 29 (hazard ratio, 0.73; 95% CI, 0.52 to 1.03). Serious adverse events were reported in 131 of the 532 patients who received remdesivir (24.6%) and in 163 of the 516 patients who received placebo (31.6%).

## CONCLUSIONS

Our data show that remdesivir was superior to placebo in shortening the time to recovery in adults who were hospitalized with Covid-19 and had evidence of lower respiratory tract infection. (Funded by the National Institute of Allergy and Infectious Diseases and others; ACTT-1 ClinicalTrials.gov number, [NCT04280705](#).)



### Related Articles

EDITORIAL NOV 5, 2020

## Remdesivir—An Important First Step

Dolin and M.S. Hirsch

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# Remdesivir for 5 or 10 Days in Patients with Severe Covid-19

J.D. Goldman and Others

CORRESPONDENCE SEP 3, 2020

# Remdesivir for the Treatment of Covid-19 — Preliminary Report

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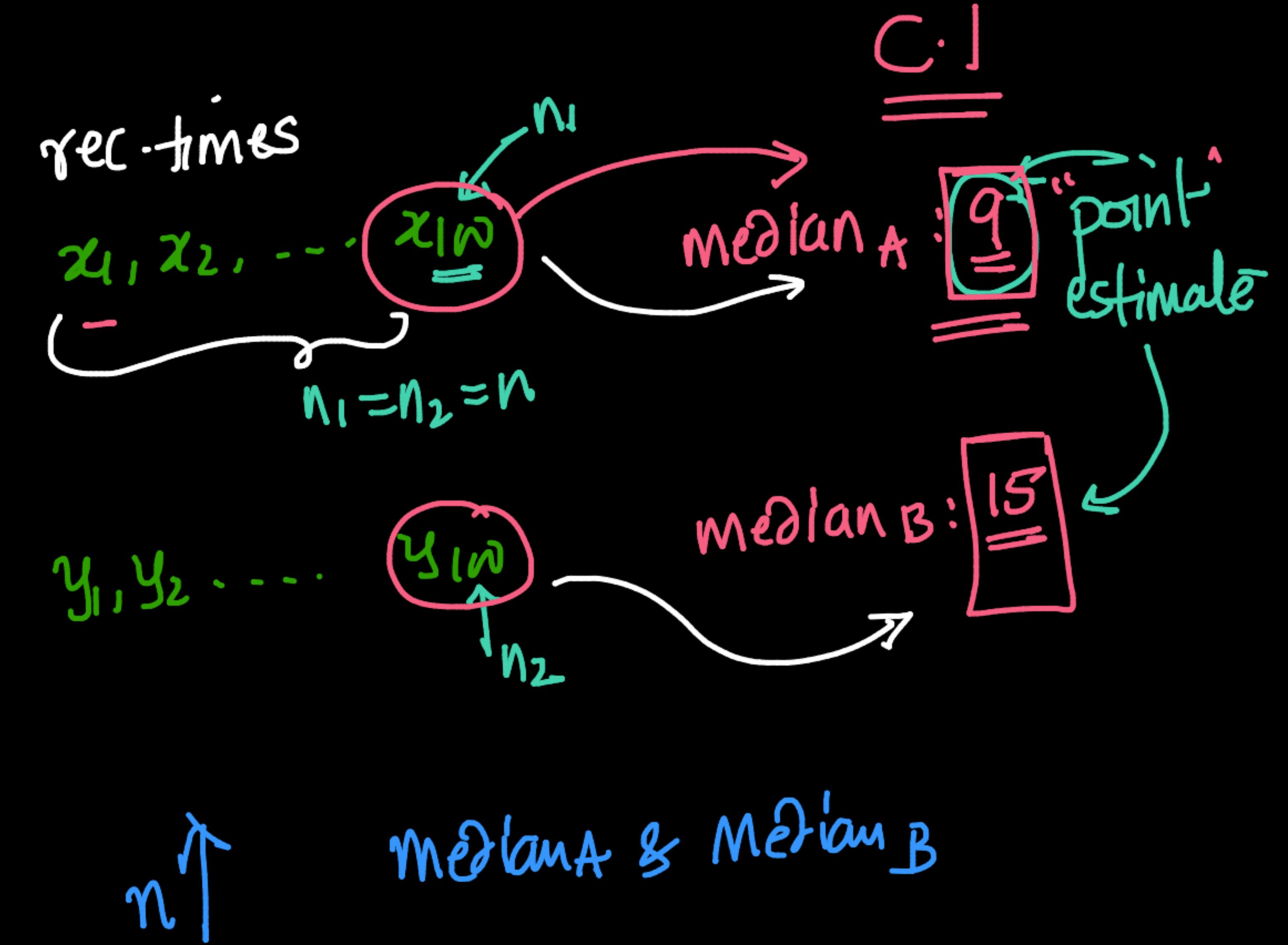
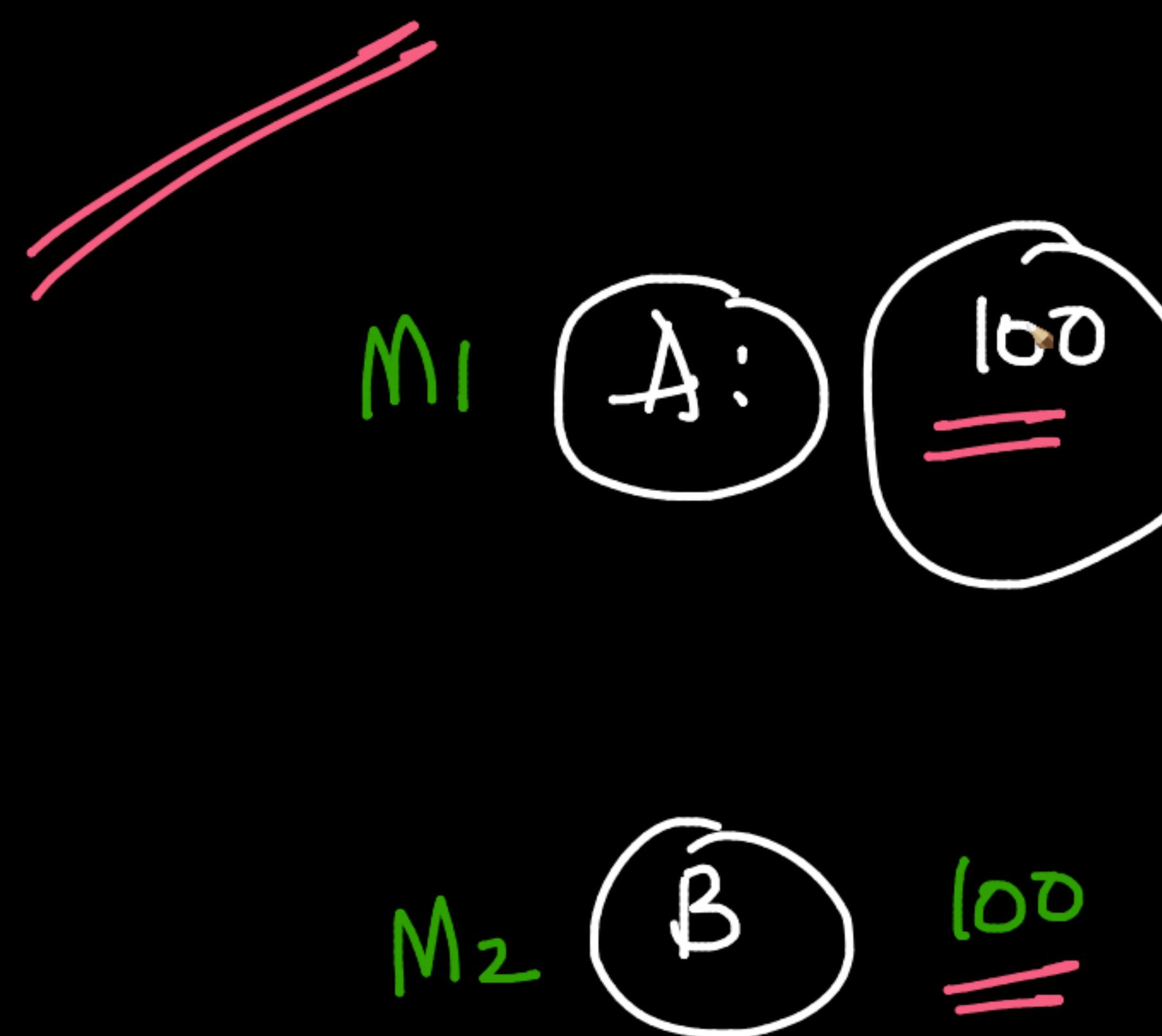
Neurology

Utah

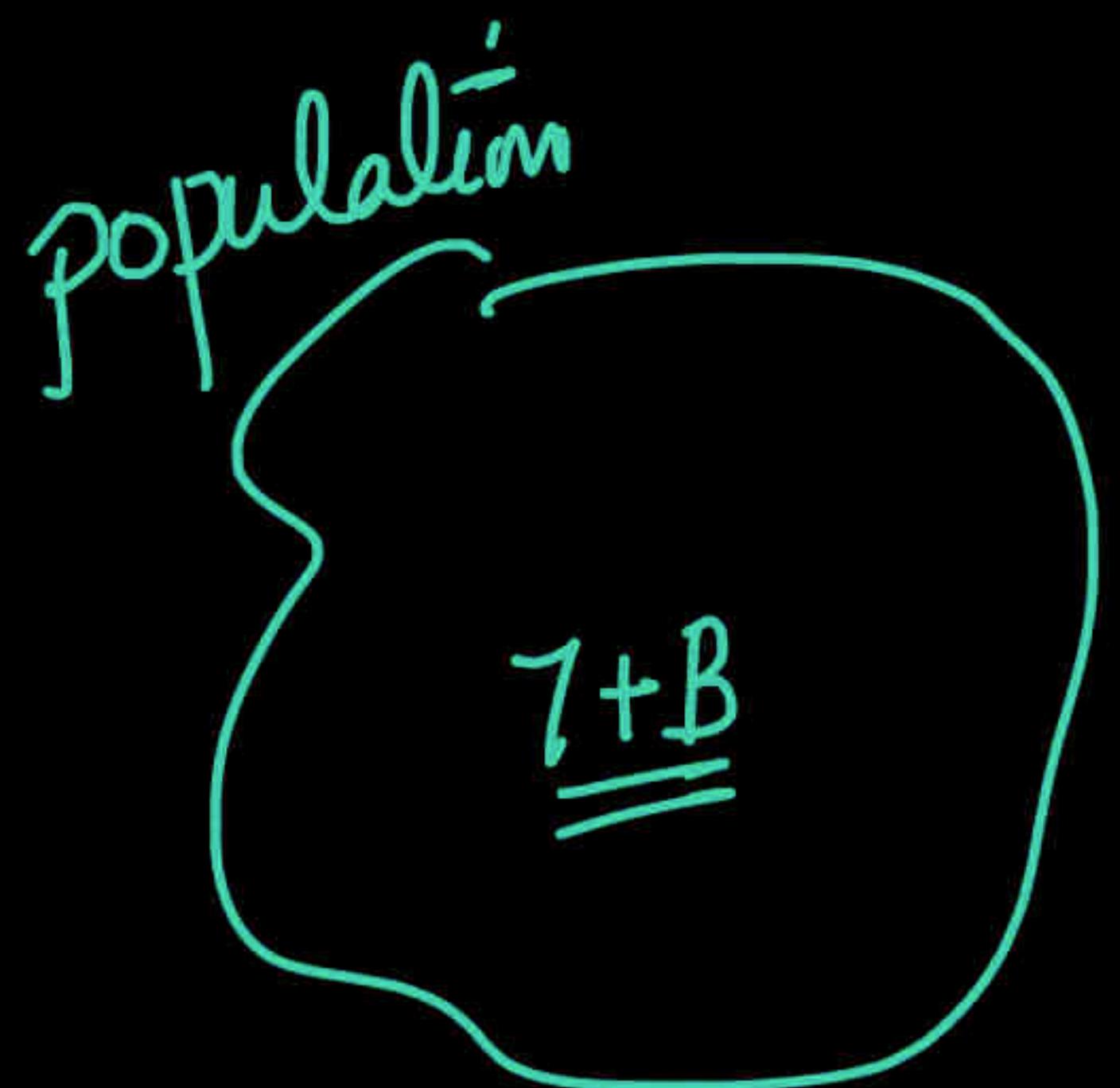
Neurology Intermountain Health Care - Utah - Multiple Locations

## Surgery, Orthopedic

## New York

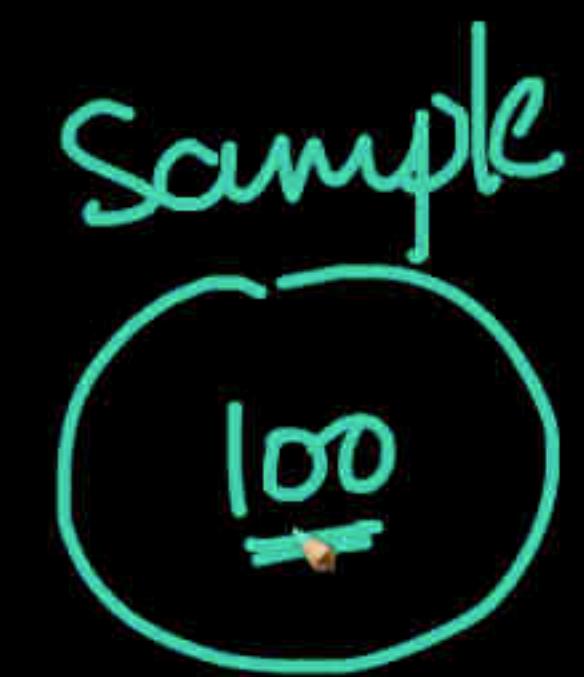


population



7+B

sample



100

A

Sample changes  
=====



slightly diff from 1

B

"

"



"

IS<sup>3</sup>

=====

Code-ideas



95% c. intervals

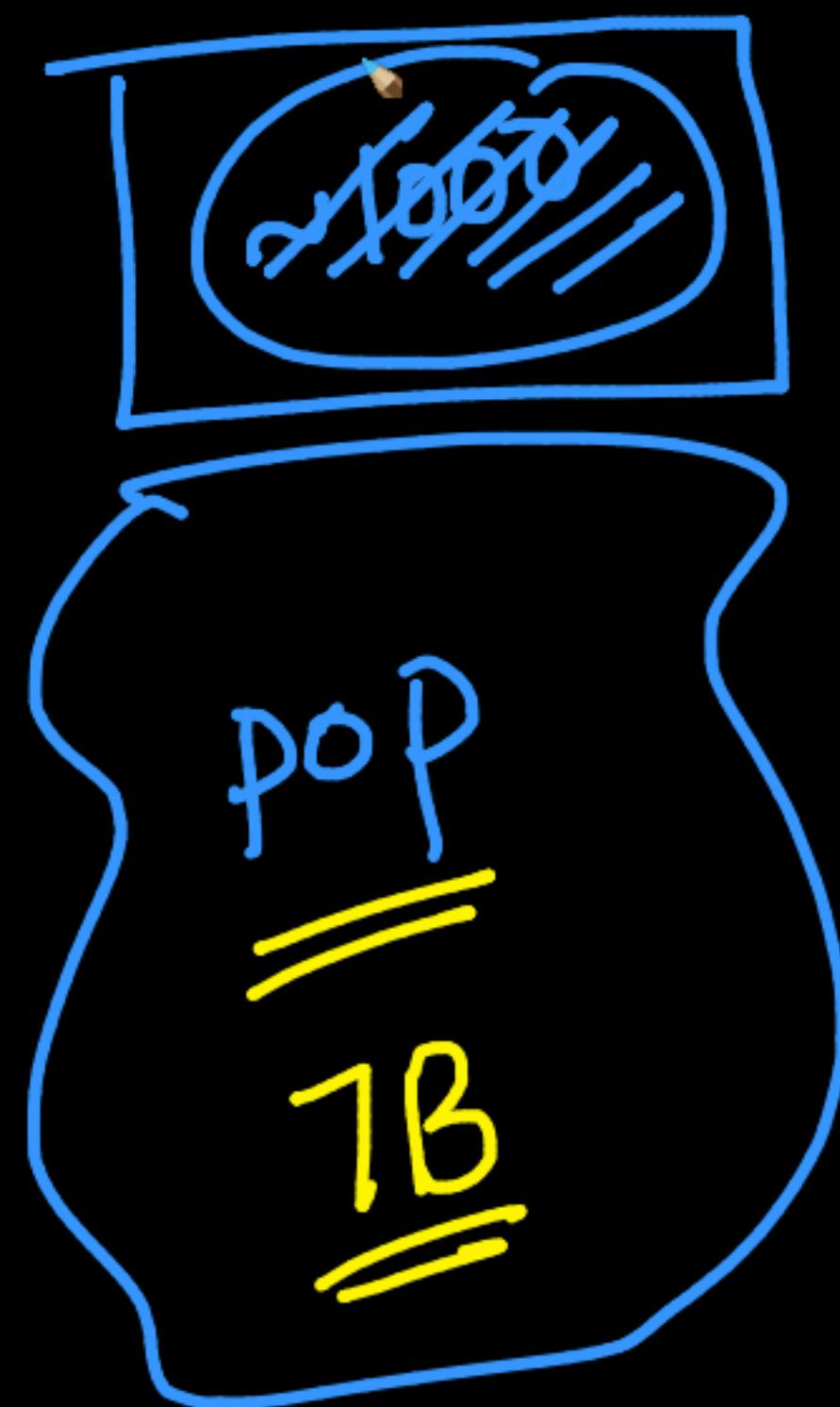
✓ median A:  $[8, 12]$  95% of times

median B: 95%  $[13, 18]$  let

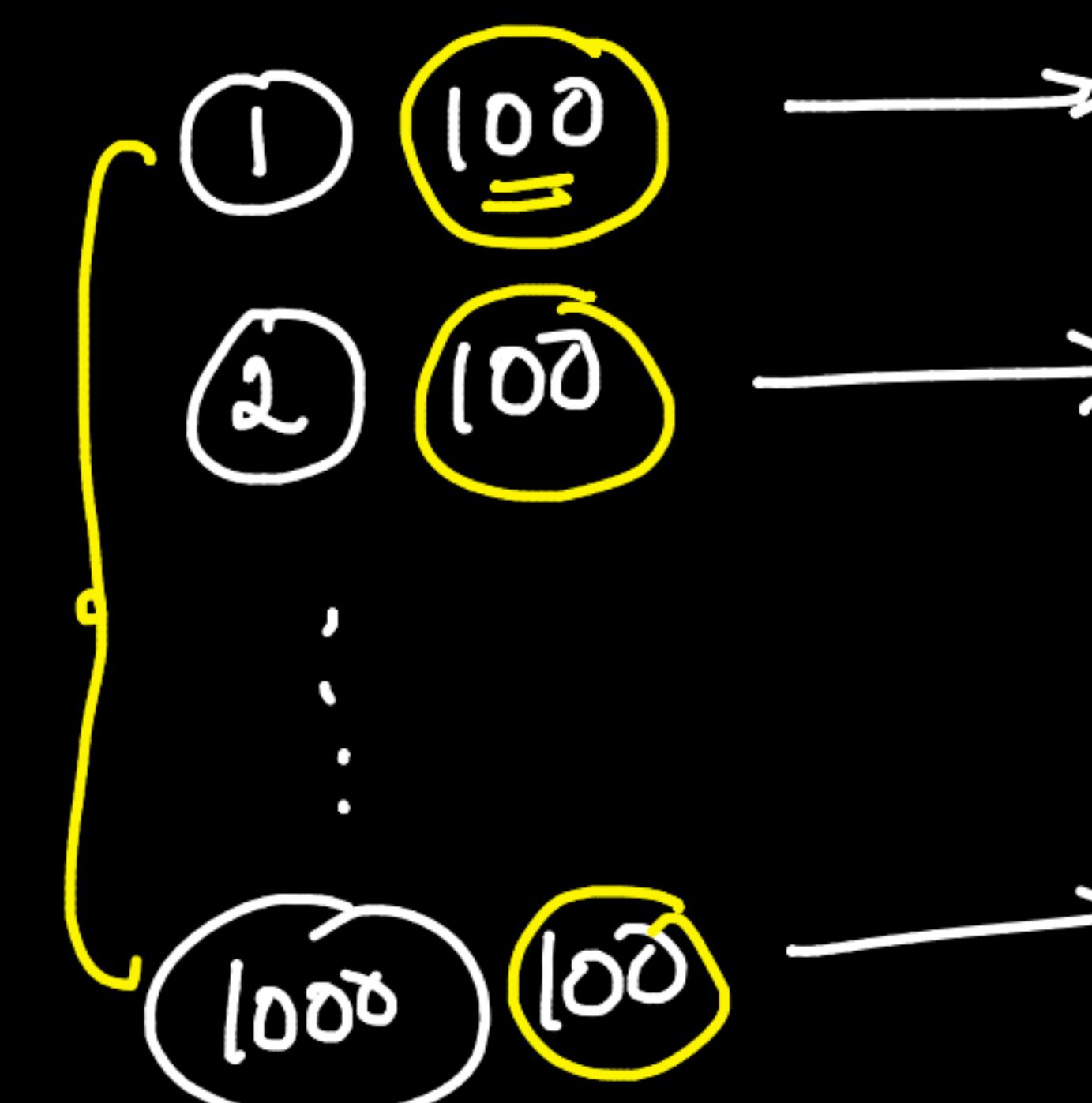
How to compute the C.I  
→ bootstrapping  
→ CLT

95% is commonly used

99% C.I ✓

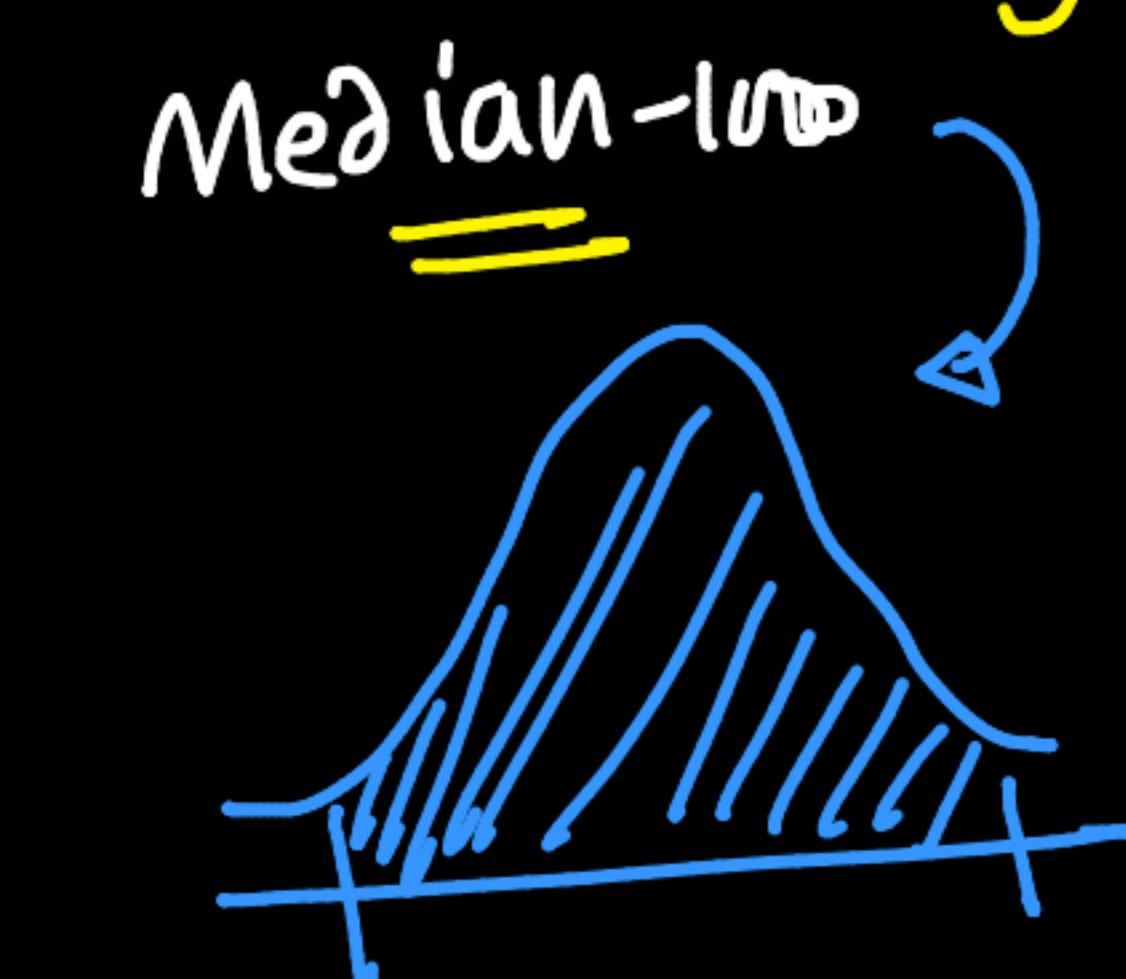


Medicine A



q5% C.I of  
Median A = [8, 12]

q5% of them  
lie in  
[8, 12]



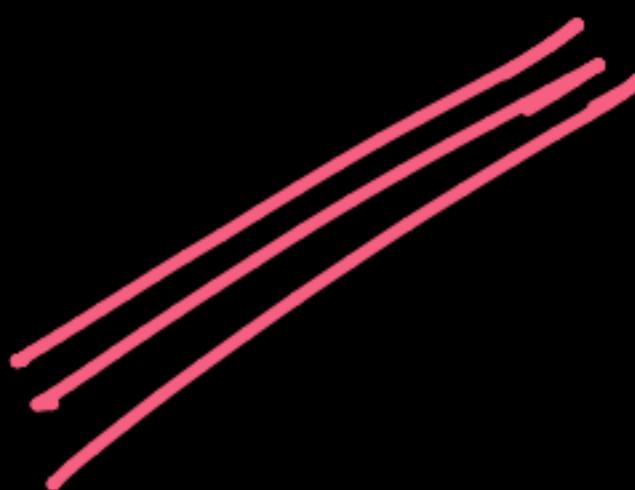
$$\mu - 2\sigma \quad \mu + 2\sigma$$
$$[- \dots \cdot]$$

[ DS @ Amazon → population  
· Gol → bank savings - · · ·

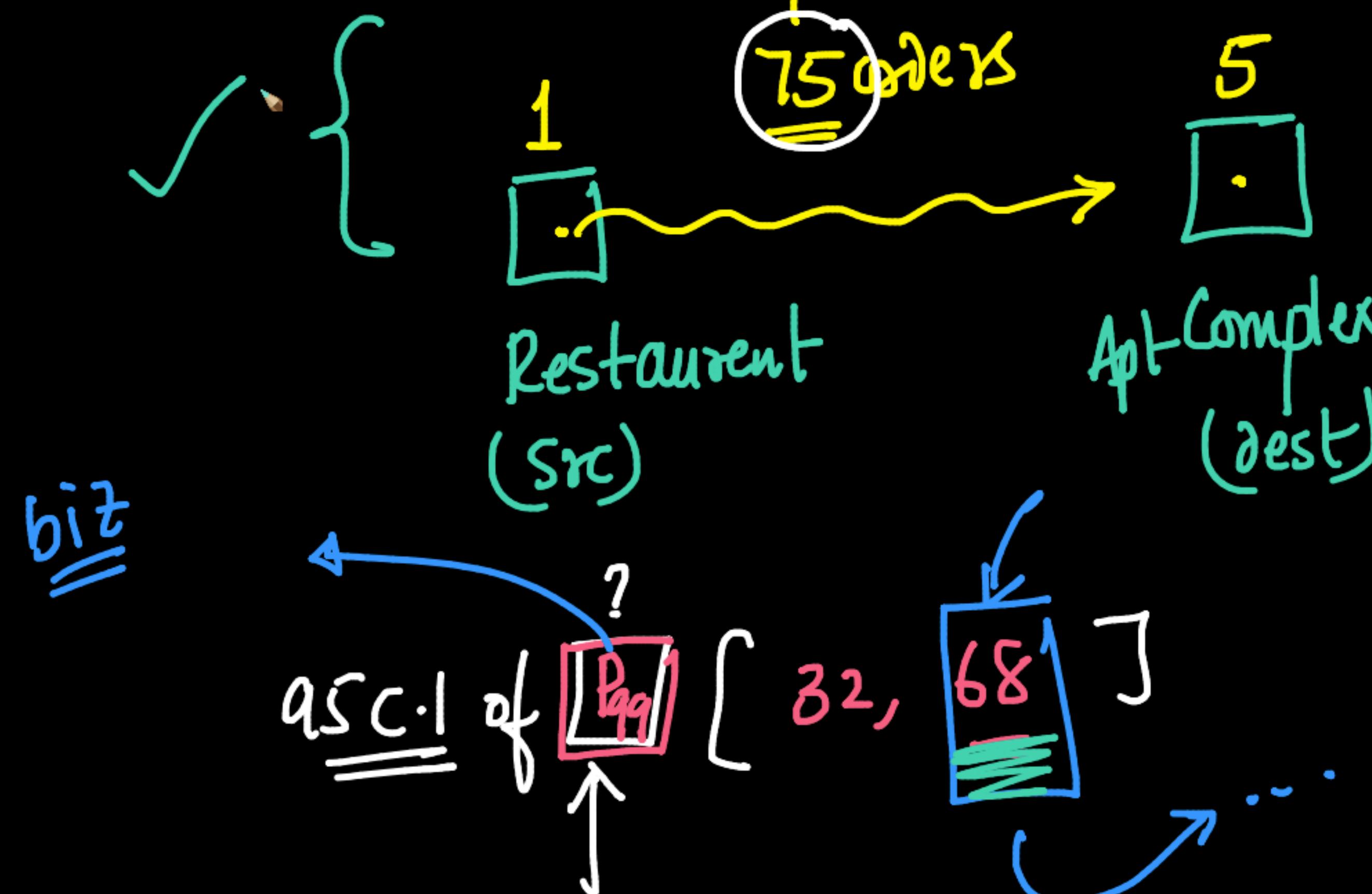
(let)

# mediana

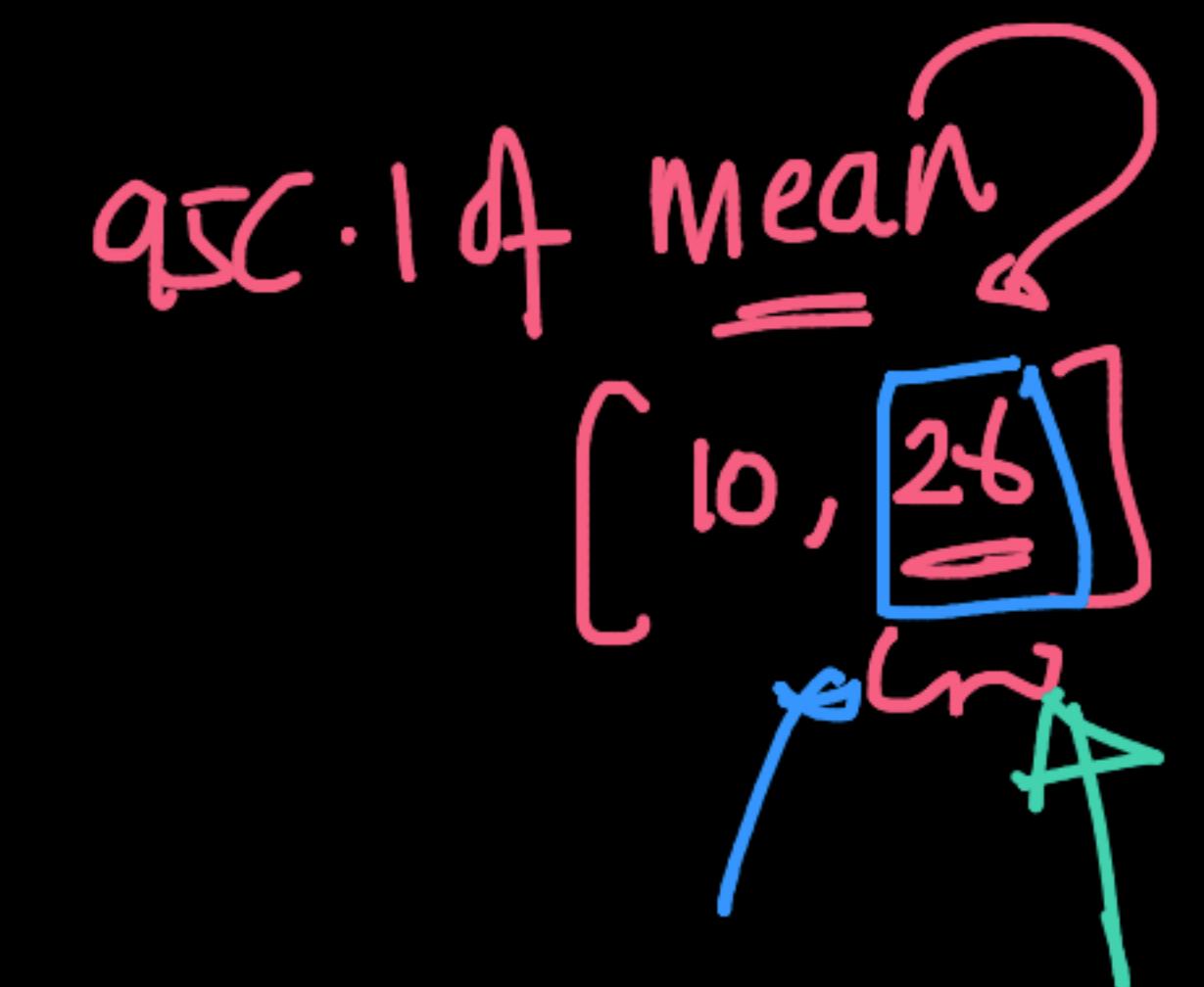
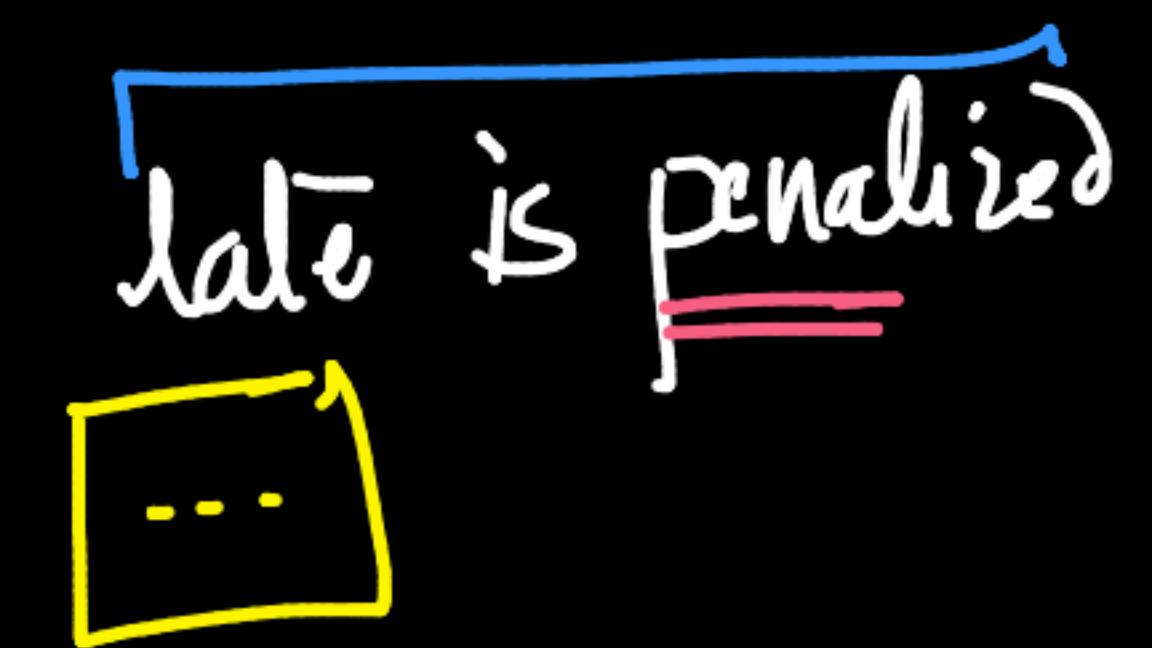
[END] - - - - -  
→ 11:30 PM



delivery times



Uber Eats



asj. C.I. on means  $\rightarrow$  CLT ; bootstrapping

$n$  { medians  
P<sub>qq</sub>  
P<sub>q5</sub>

## Bootstrapping:

rec. times:

$x_1, x_2 \dots$

$x_{100}$ ; sample of  $n=100$  pls

Assumption:

disb of Sample  $\approx$  disb of the  
population

✓  $n \rightarrow \infty$

$\rightarrow$  random-sample &  $n$  is not too small

Pseudo-Code

q-scl of median

medians = [ ]  
 $\gamma = 1000$

for  $i = 1$  to  $\gamma$

{

$\checkmark \gamma = 1000$

- randomly sample  $x_1, \dots, x_{100=n}$  with replacement

$M = n$

$M \leq n = 100$

$m =$

points from

- median of  $m$  points  $\rightarrow$  medians[i]

- Sort 1000 medians

- pick the  $\beta_{2.5} \& \beta_{97.5}$  of 1000 medians

{ with "replacement"

✓ ✓ ✓ ✓ ✓  
1, 6, 8, 12, 3  
=====



bootstrapped samples  
8, 12, 6, 3  
=====

{ without replacement

✗, ✗, 8, ✗, ✗



6, 8, 12, 3, 1

$$m = n = 5$$

n=5



12, 6, 3, 1, 8  
=====

with replacement

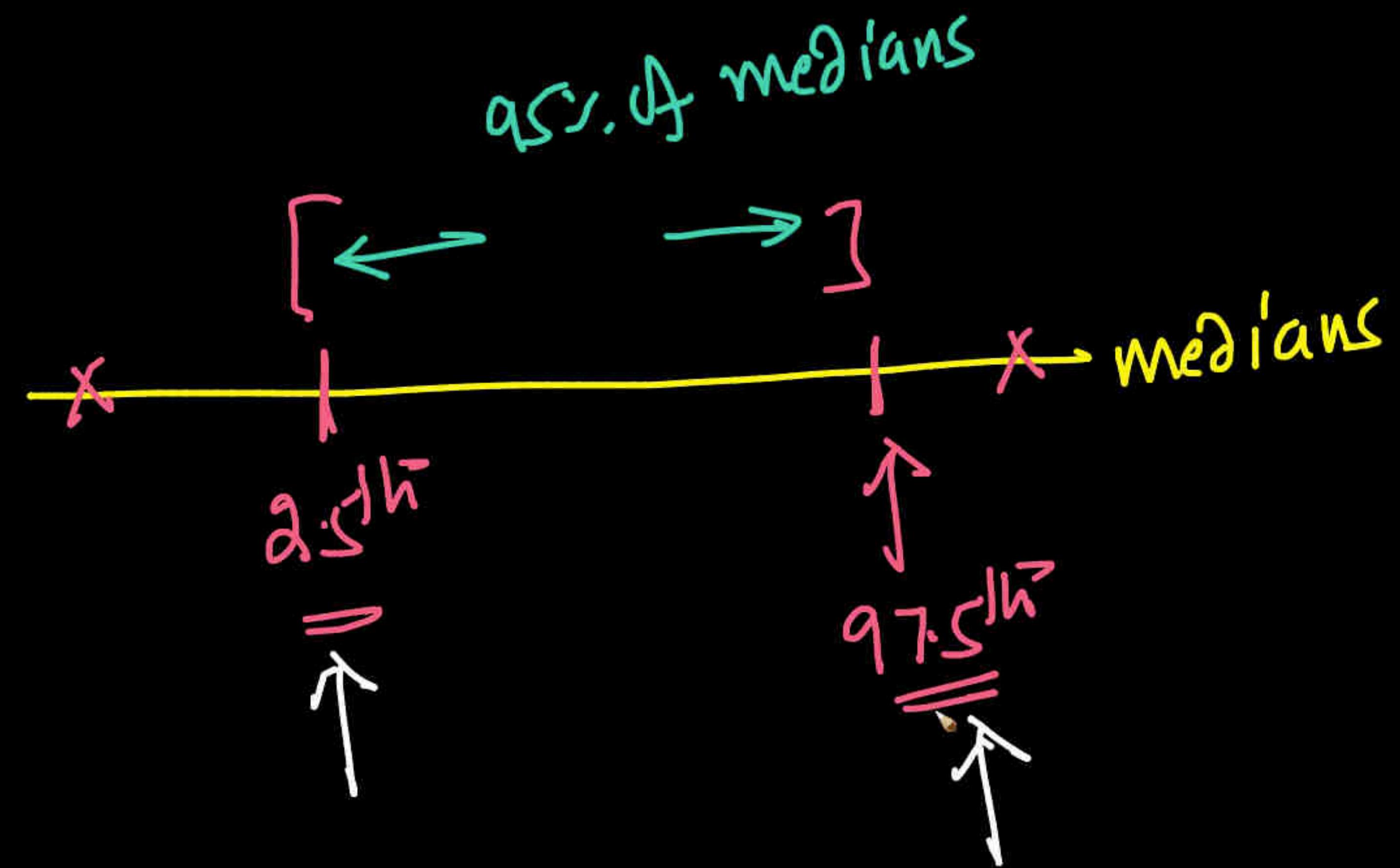
→ can do this

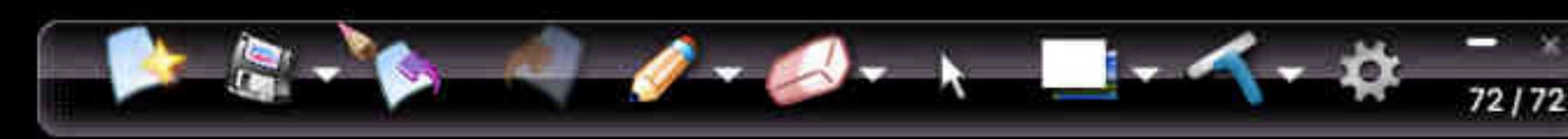
$$m > n$$



$$m < n \quad \alpha$$

$$\boxed{m = n}$$





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QQ-plot and CLT and Bootstrap | scipy.stats.probplot — SciPy v Remdesivir for the Treatment | nejm.org/doi/full/10.1056/nejmoa2007764

Article Figures/Media

recovery, defined by either discharge from the hospital or hospitalization for infection-control purposes only.

**RESULTS**

A total of 1062 patients underwent randomization (with 541 assigned to remdesivir and 521 to placebo). Those who received remdesivir had a median recovery time of 10 days (95% confidence interval [CI], 9 to 11), as compared with 15 days (95% CI, 13 to 18) among those who received placebo (rate ratio for recovery, 1.29; 95% CI, 1.12 to 1.49;  $P<0.001$ , by a log-rank test). In an analysis that used a proportional-odds model with an eight-category ordinal scale, the patients who received remdesivir were found to be more likely than those who received placebo to have clinical improvement at day 15 (odds ratio, 1.5; 95% CI, 1.2 to 1.9, after adjustment for actual disease severity). The Kaplan–Meier estimates of mortality were 6.7% with remdesivir and 11.9% with placebo by day 15 and 11.4% with remdesivir and 15.2% with placebo by day 29 (hazard ratio, 0.73; 95% CI, 0.52 to 1.03). Serious adverse events were reported in 131 of the 532 patients who received remdesivir (24.6%) and in 163 of the 516 patients who received placebo (31.6%).

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**QUICK TAKE**

Remdesivir for the Treatment of Covid-19 — Final Report

01:45

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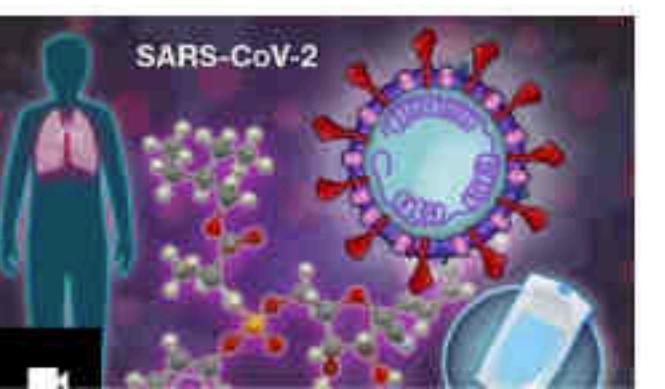
**NEJM CareerCenter**

**PHYSICIAN JOBS** MAY 10, 2022

Neurology Utah  
Neurology Intermountain Health Care - Utah - Multiple Locations

Surgery, Orthopedic New York  
Hand/Upper Extremity Orthopaedic Surgeon - Nassau County

Family Medicine New York City, New York



$\{ n \uparrow$   
 $m \approx n$

$\sim 500$

✓ rem:

median

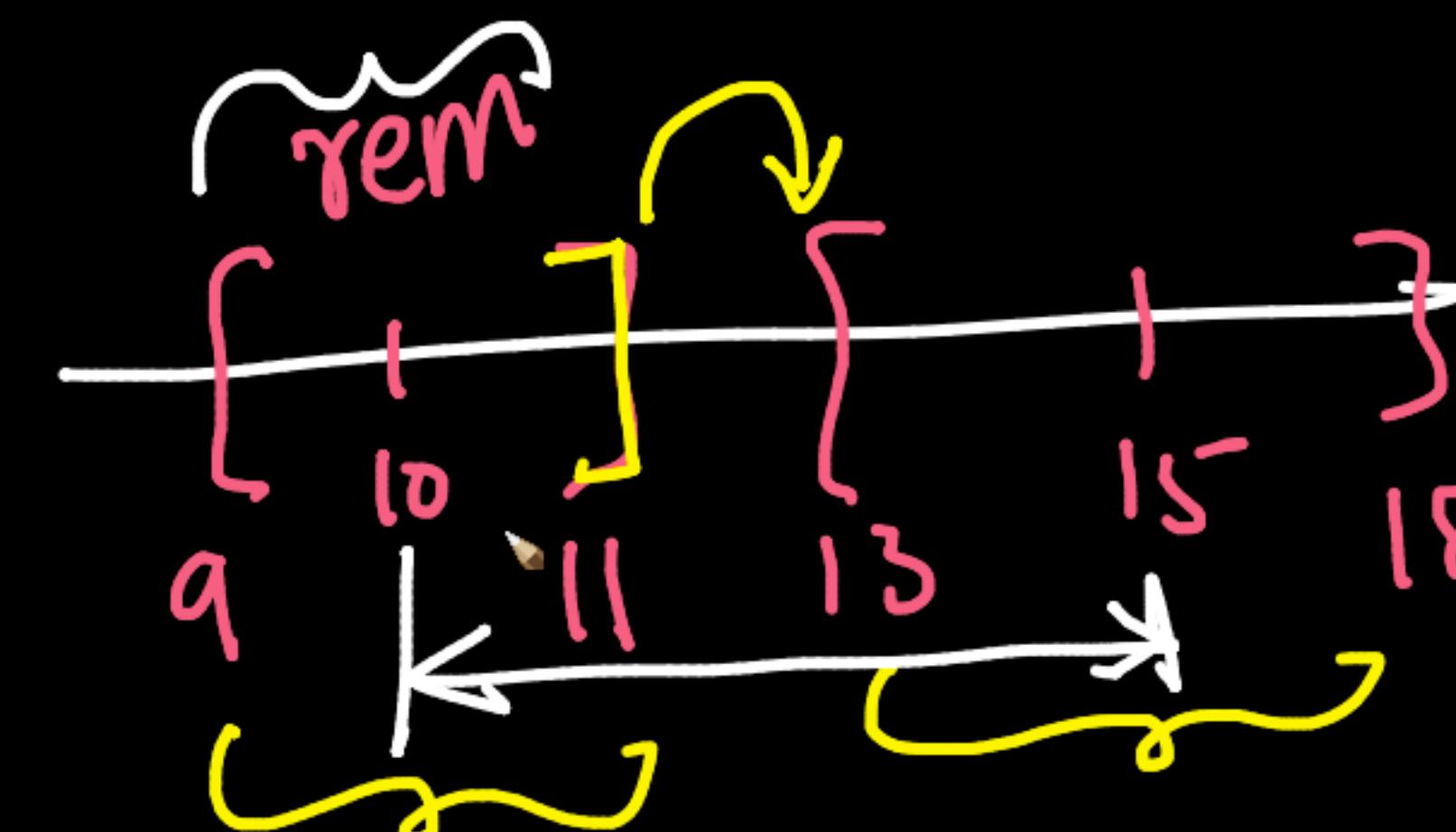
10

[ 9, 11 ]

placebo: [ 13, 18 ]

15

✓ [ ]



gem

$$n = 500 \rightarrow [9 \ 10 \ 11]$$

$M = n$

$$n = \underline{50,000} \rightarrow [9.8 \ 10 \ 10.2]$$

$M = n$

CLT



Samples:

$\{x_1^1, x_2^1, \dots, x_n^1\}$  — Sample 1  $\rightarrow M_1$

$\{x_1^2, x_2^2, \dots, x_n^2\}$  — Sample 2  $\rightarrow M_2$

$\vdots$

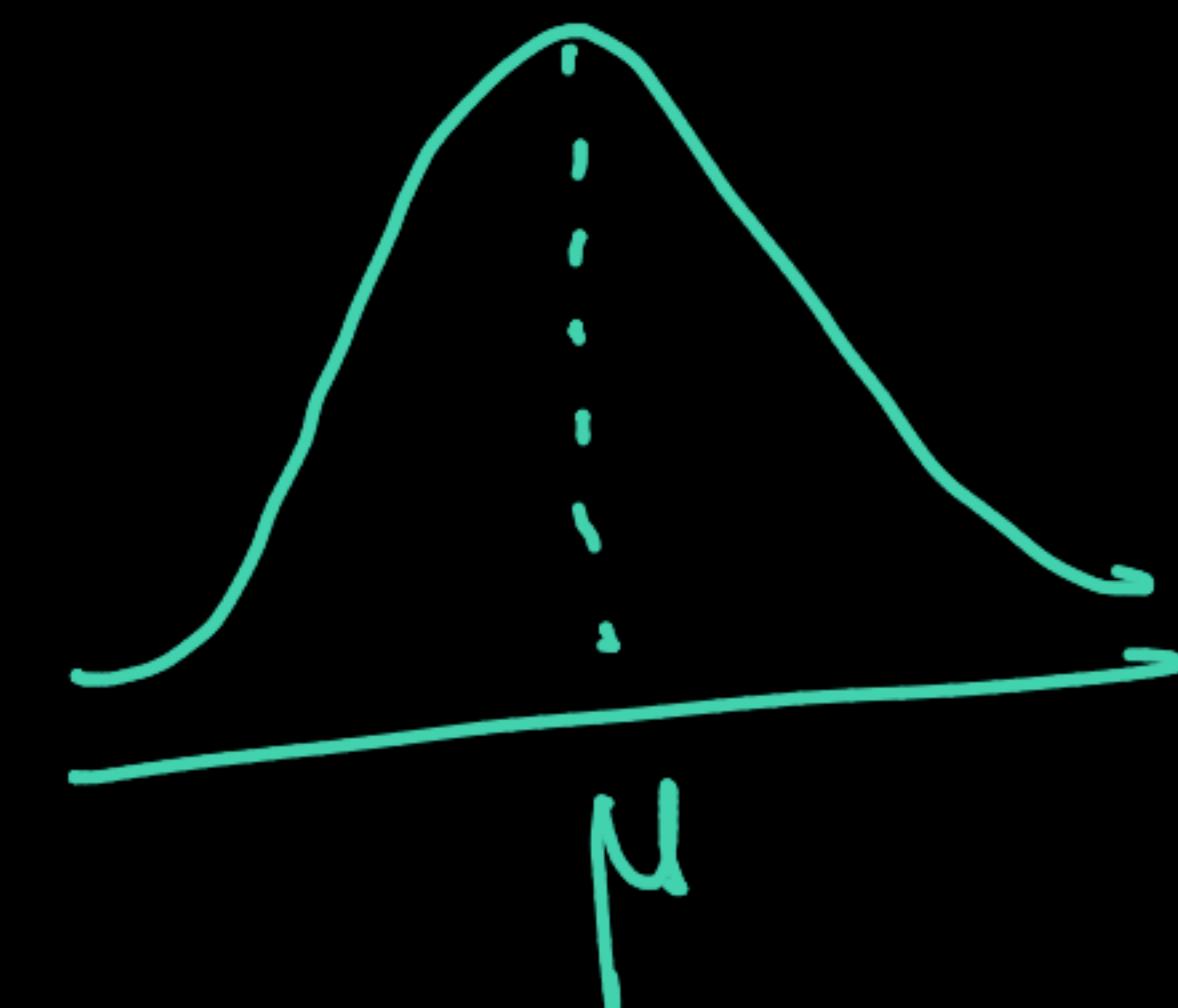
$\{x_1^K, x_2^K, \dots, x_n^K\}$  — Sample K  $\rightarrow M_K$

Sample Means

Sample Size n

sample-means

$\underline{\underline{M_1, M_2, \dots, M_K}} \sim \text{Normal}(\tilde{\mu}, \frac{\sigma}{\sqrt{n}})$



sample size

theoretically  
 $n \rightarrow \infty$



Sample-medians → not guaranteed

$x_1, \dots, x_n$   
rec. times  $\rightarrow$  finite  
pop mean & St Dev

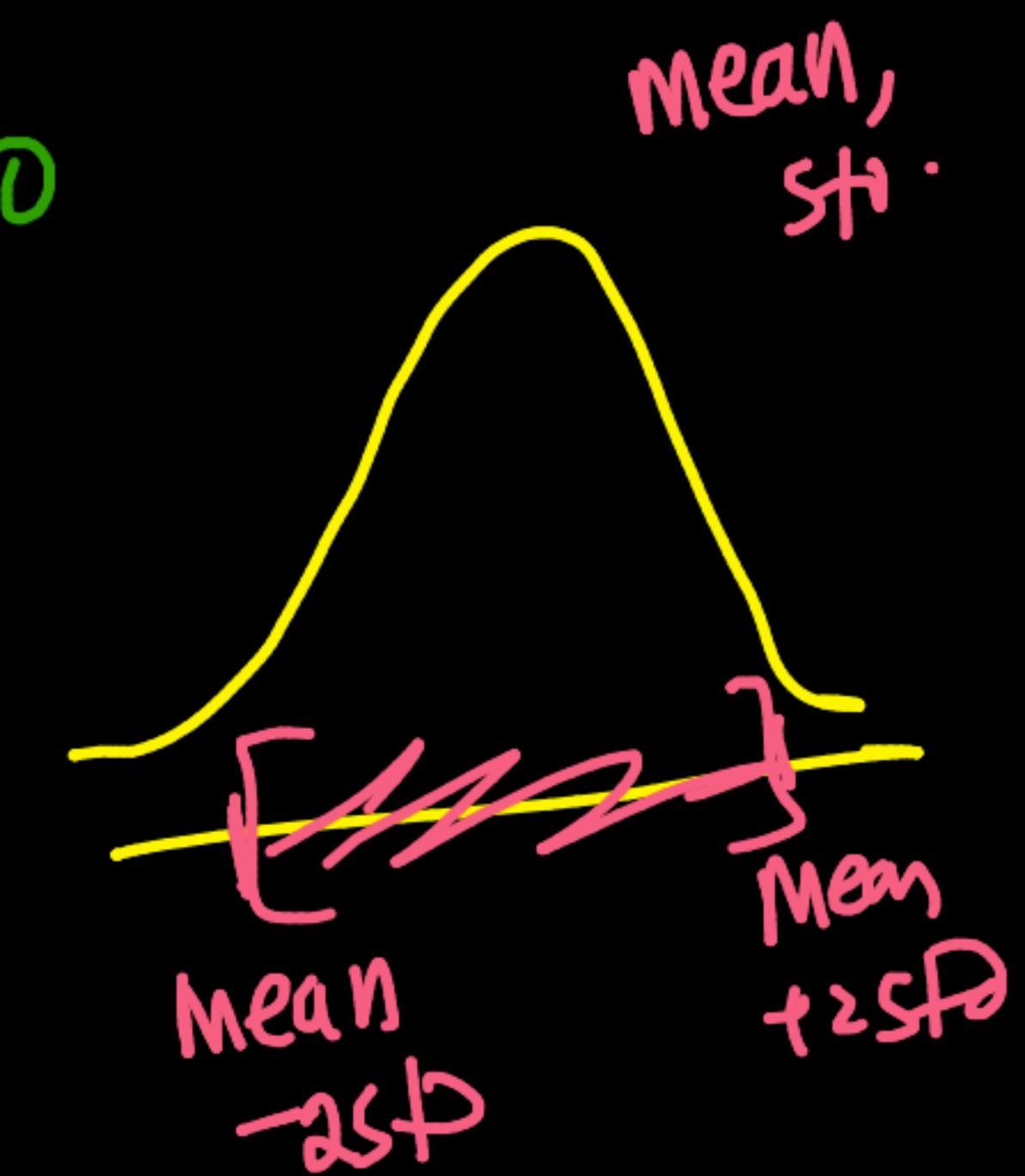


bootstrap samples

$\gamma = 1000$

$S_1 \rightarrow M_1$   
 $S_2 \rightarrow M_2$   
⋮ ⋮

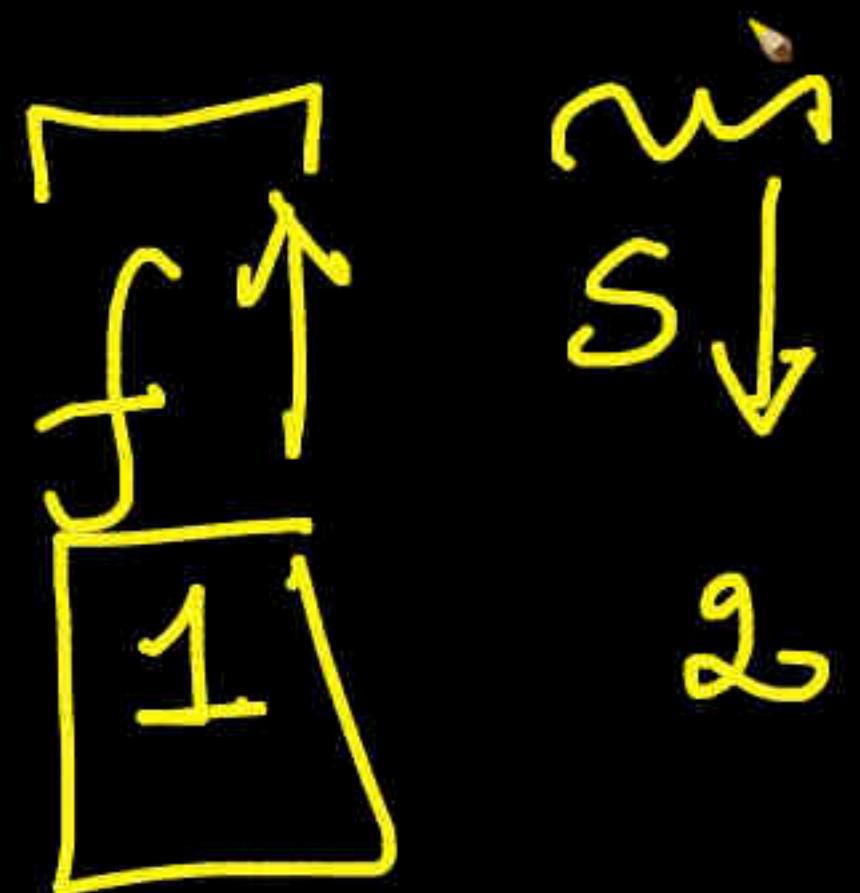
$S_{1000} \rightarrow M_{1000}$



lots of code  
simulation }  
next-class

fast / slow: ↓

(<sup>29</sup>  
good-speed)

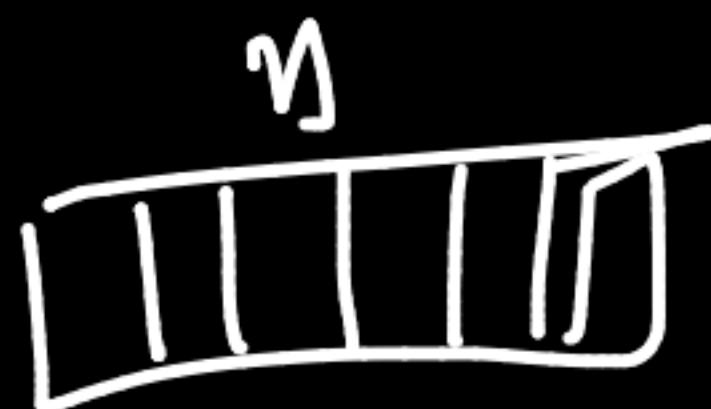


[END.]

QQ-plot

TC:  $\Theta(n \lg n)$  Sort + get percentiles ; plotting  $n$

SC:  $\Theta(1)$



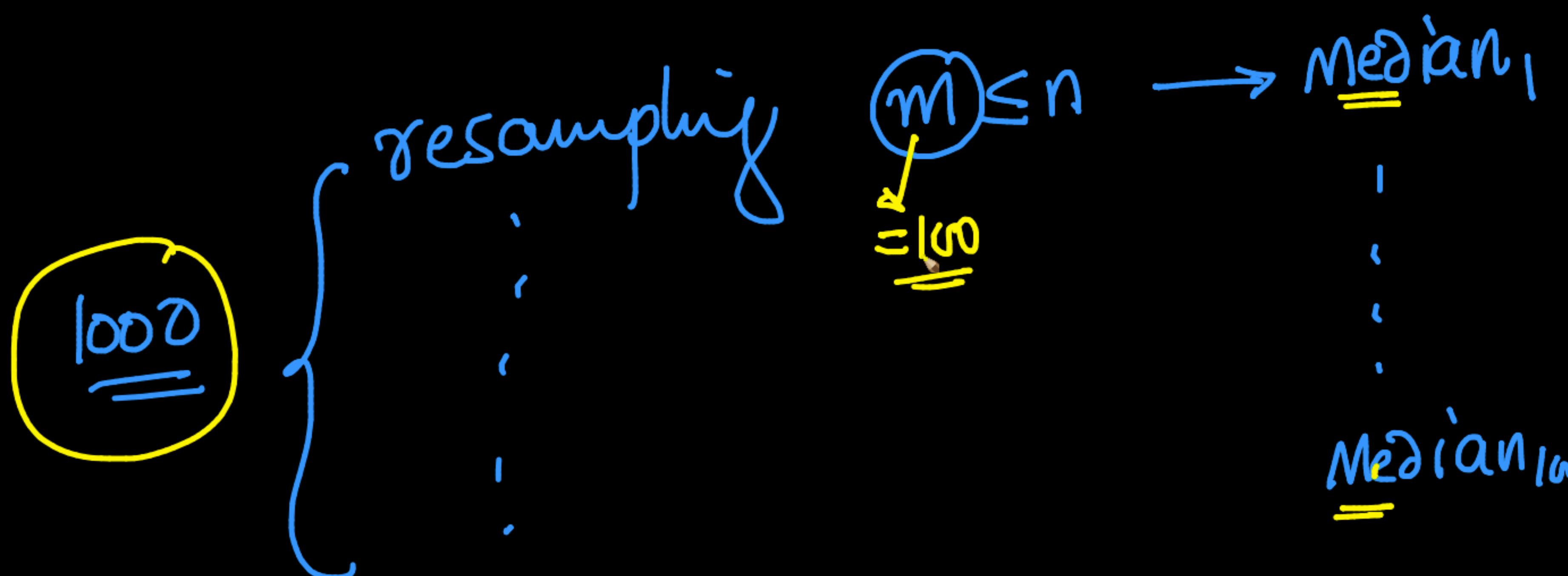
bootstrapping

medicine A

observed sample

$$100 = n$$

dist of sample  
 $\approx$  dist of pop



m, n & r Change → 95 C.I  
[ , ]

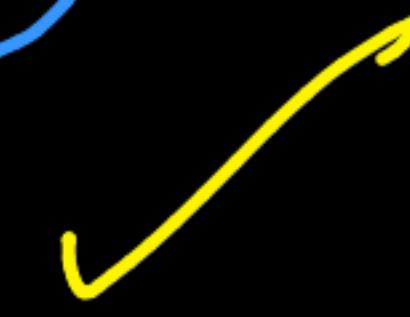
QQ-plot → obs vs Binomial ✓

Bootstrapping → distribution-free method

' $\bar{m}$ ' same  
for all samples

CLT → sample means are Gaussian disb  
( $\gamma_i$  is sample)

CLT  $\rightarrow$  outliers 

$\hookrightarrow$  reasonably well 

sample-1  $\rightarrow$  Small pool of outliers  
  
 $M_1$

mean

CLT

Bootstrap

$\mu \text{ & } \sigma$  are finite ?

parametric

non-parametric

(later)

C.I of mean  $\rightarrow$  CLT ( $\mu$  &  $\sigma$  are finite)  
 $\rightarrow$  sample means ~ Gaussian

C.I of Median  
Pgg  
:  
:  
C.I of Mean  
( $\mu$  &  $\sigma$  are not finite)

→ Bootstrapping

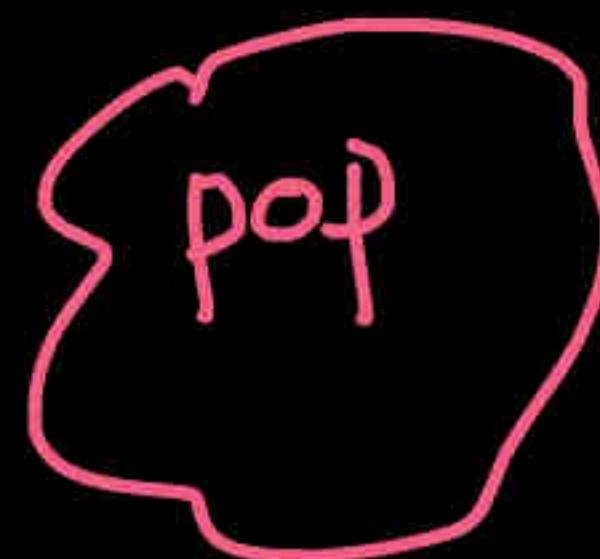
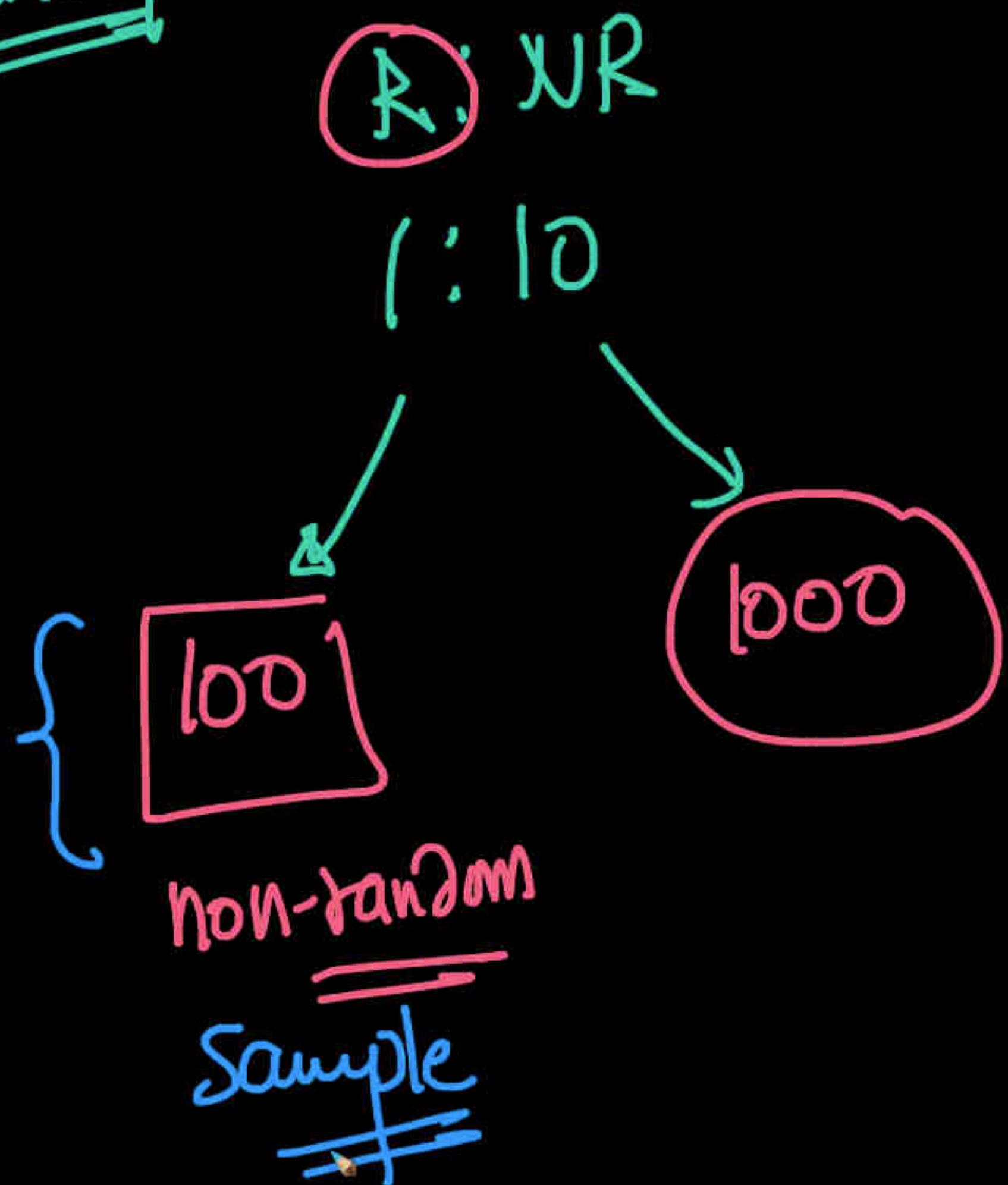
Uber Eats

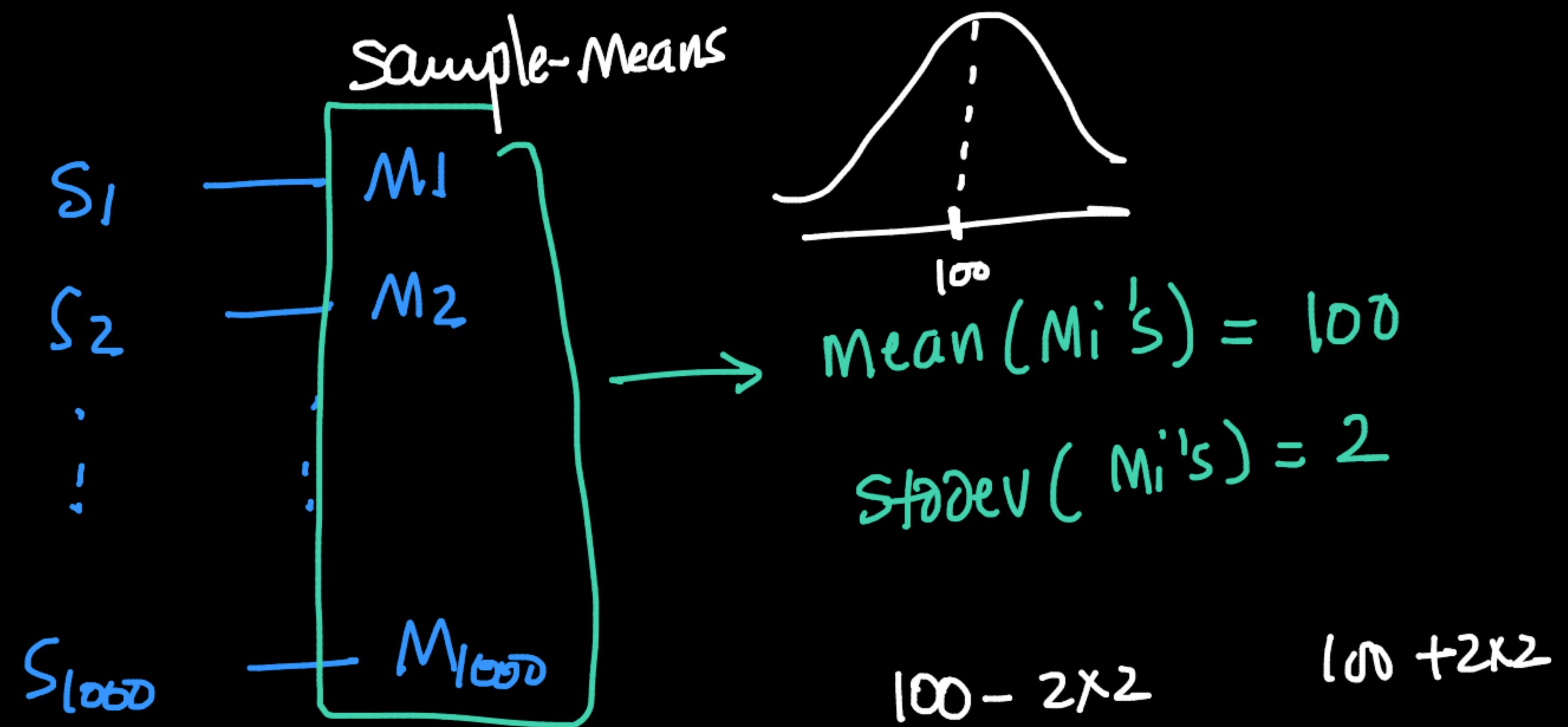
[ , ]  $\xrightarrow{P_{99}} \underline{\underline{}}$

avg  $\rightarrow$  median  $\underline{\underline{}}$

biz-context  $\underline{\underline{}}$

Survey!





asc. of  
mean [96, 104]

CLT:

population

$\mu$  &  $\sigma$  are finite

↳ finance & trading

$y_1, y_2, \dots, y_n$  $y \sim \text{log-normal}$ 

iff  $\log(y) \sim \text{Normal}$

