Recap of the last lecture

Regular Expression (RE)

- A standard notation of characterizing a text sequence
- How can we search for any of the following:
 - woodchuck
 - woodchucks
 - Woodchuck
 - Woodchucks



RE search requires a pattern and a corpus of texts to search through.

Morphology: Definition

The study of words, how they are formed, and their relationship to other words in the same language.

The Porter Stemmer (Porter, 1980)

- A simple rule-based algorithm for stemming
- An example of a HEURISTIC method
- Based on rules like:
 - ATIONAL -> ATE (e.g., relational -> relate)
- The algorithm consists of seven sets of rules, applied in order

The Edit Distance Table

f 5	L	5	6	7	6	5
4	Α	4	5	6	5	6
3	Ι	3	4	5	4	5
2	R	2	3	4	5	6
1	Т	1	2	3	4	5
0	#	0	1	2	3	4
		#	Z	Е	I	L
i	i –	0	1	2	3	4
	J					

$$D(i,j) = \min \begin{cases} D(i-1,j) + 1 \\ D(i,j-1) + 1 \\ D(i-1,j-1) + \begin{cases} 2; & \text{if } S_1(i) \neq S_2(j) \\ 0; & \text{if } S_1(i) = S_2(j) \end{cases}$$

Language Model N-Gram

Assumption: we don't know what is Deep Learning

Word Prediction

- Guess the next word...
 - ... I notice three guys standing on the ???
- There are many sources of knowledge that could be helpful, including world knowledge.
- But we can do pretty well by simply looking at the preceding words and keeping track of simple counts.

Word Prediction

- Formalize this task using N-gram models.
- N-grams are token sequences of length N.
- Given N-grams counts, we can guess likely next words in a sequence.

Probabilistic Language Models

The goal: assign a probability to a sentence

- Machine Translation:
 - P(high winds tonite) > P(large winds tonite)
- Spelling Correction
 - The office is about fifteen **minuets** from my house
 - P(about fifteen minutes from) > P(about fifteen minuets from)
- Speech Recognition
 - P(I saw a van) >> P(eyes awe of an)
- + Summarization, question-answering, etc., etc.!!

Probabilistic Language Modeling

 Goal: compute the probability of a sentence or sequence of words:

$$P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n)$$

Related task: probability of an upcoming word:

```
P(W_5 | W_1, W_2, W_3, W_4)
```

• A model that computes either of these:

```
P(W) or P(W_n|W_1,W_2...W_{n-1}) is called a language model.
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Better: the grammar But language model or LM is standard

How to compute P(W)

How to compute this joint probability:

P(its water is so transparent that <u>the</u>)=

Count(its water is so transparent that the)

Count(its water is so transparent that)

P(its, water, is, so, transparent, that)

• Intuition: let's rely on the Chain Rule of Probability

The Chain Rule: General

The definition of conditional probabilities

$$P(A | B) = P(A, B) / P(B)$$

Rewriting: $P(A, B) = P(A | B) P(B)$

More variables:

$$P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)$$

The Chain Rule in General

$$P(x_1,x_2,x_3,...,x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1,x_2)...P(x_n|x_1,...,x_{n-1})$$

The Chain Rule: joint probability in sentence

$$P(w_1 w_2 ... w_n) = \prod_{i} P(w_i \mid w_1 w_2 ... w_{i-1})$$

P("its water is so transparent") =
P(its) × P(water|its) × P(is|its water) ×
P(so|its water is) × P(transparent|its water is so)

How to estimate these probabilities

Could we just count and divide?

```
P(the | its water is so transparent that) =
Count(its water is so transparent that the)
Count(its water is so transparent that)
```

- No! Too many possible sentences!
- We'll never see enough data for estimating these

Markov Assumption

Simplifying assumption:



 $P(\text{the} | \text{its water is so transparent that}) \approx P(\text{the} | \text{that})$

or maybe

 $P(\text{the} | \text{its water is so transparent that}) \approx P(\text{the} | \text{transparent that})$

Markov Assumption

$$P(w_1 w_2 ... w_n) \approx \prod_i P(w_i \mid w_{i-k} ... w_{i-1})$$

•In other words, we approximate each component in the product

$$P(w_i \mid w_1 w_2 \dots w_{i-1}) \approx P(w_i \mid w_{i-k} \dots w_{i-1})$$

Simplest case: Unigram model

$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i)$$

Some automatically generated sentences from a unigram model

```
fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass thrift, did, eighty, said, hard, 'm, july, bullish that, or, limited, the
```

Quiz

Which is assigned higher probability by a unigram language model for English?

- P(I like ice cream)
- P(the the the)
- P(Go to class daily)
- P(class daily go to)

Bigram model

Condition on the previous word:

$$P(w_i \mid w_1 w_2 \dots w_{i-1}) \approx P(w_i \mid w_{i-1})$$

texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen

outside, new, car, parking, lot, of, the, agreement, reached

this, would, be, a, record, november

N-gram models

- We can extend to trigrams, 4-grams, 5-grams
- In general this is an insufficient model of language
 - because language has long-distance dependencies:

"The computer which I had just put into the machine room on the fifth floor crashed."

But we can often get away with N-gram models

Evaluations Timeline (Tentative)

Project Release: 18/1/23

Assignment 1: 21/1/23 - 27/1/23

Quiz 1: 2/2/23

Assignment 2: 14/3/23 - 20/3/23

Quiz 2: 20/3/23

Assignment 3: 10/4/23 - 23/4/23

Quiz 3: 24/4/23

Release of test set for project: 11/05/23

Project Evaluation: 12/05/23

Sign up!

Piazza: https://piazza.com/iitd.ac.in/spring2023/ell881

Estimating N-gram Probabilities

Estimating bigram probabilities

The Maximum Likelihood Estimate (MLE)

$$P(w_{i} | w_{i-1}) = \frac{count(w_{i-1}, w_{i})}{count(w_{i-1})}$$

$$P(w_{i} | w_{i-1}) = \frac{c(w_{i-1}, w_{i})}{c(w_{i-1})}$$

An example

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$
 ~~I am Sam~~ ~~Sam I am~~ ~~I do not like green eggs and ham~~

$$P({
m I}|{
m <} {
m >}) = {2\over 3} = .67$$
 $P({
m Sam}|{
m <} {
m >}) = {1\over 3} = .33$ $P({
m am}|{
m I}) = {2\over 3} = .67$ $P({
m <}/ {
m s}{
m >}|{
m Sam}) = {1\over 2} = 0.5$ $P({
m Sam}|{
m am}) = {1\over 2} = .5$ $P({
m do}|{
m I}) = {1\over 3} = .33$

More examples: Berkeley Restaurant Project sentences

- can you tell me about any good cantonese restaurants close by
- mid priced thai food is what i'm looking for
- tell me about chez panisse
- can you give me a listing of the kinds of food that are available
- i'm looking for a good place to eat breakfast
- when is caffe venezia open during the day

Raw bigram counts (absolute measure)

• Out of 9222 sentences

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

Raw bigram probabilities (relative measure)

Normalize by unigrams:

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

• Result:

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Bigram estimates of sentence probabilities

```
P(<s> I want english food </s>) =
 P(1|<s>)
 \times P(want|I)
 × P(english|want)
 × P(food|english)
 \times P(</s>|food)
    = .000031
```

What kinds of knowledge?

- P(english | want) = .0011world
- P(chinese | want) = .0065
- P(to | want) = .66
 P(eat | to) = .28
- P(food | to) = 0
- P(want | spend) = 0
- P (i | $\langle s \rangle$) = .25

grammar (contingent zero)

grammar (structural zero)

The **right to food**, and its non variations, is a human right protecting the right for people to feed themselves in dignity

Practical Issues

- We do everything in log space
 - Avoid underflow: multiplying extremely small numbers
 - Adding is faster than multiplying

$$p_1 \times p_2 \times p_3 \times p_4 \Rightarrow \log p_1 + \log p_2 + \log p_3 + \log p_4$$

Evaluation of a Language Model

Evaluation: How good is our model?

- Does our language model prefer good sentences to bad ones?
 - Assign higher probability to "real" or "frequently observed" sentences
 - Than "ungrammatical" or "rarely observed" sentences?
- We train parameters of our model on a training set.
- We test the model's performance on data we haven't seen.
 - A **test set** is an unseen dataset that is different from our training set, totally unused.
 - An evaluation metric tells us how well our model does on the test set.

Extrinsic evaluation of N-gram models

- Best evaluation for comparing models A and B
 - Put each model in a task
 - spelling corrector, speech recognizer, machine translation system
 - Run the task, get an accuracy for A and for B
 - How many misspelled words corrected properly
 - How many words translated correctly
 - Compare accuracy for A and B

Difficulty of extrinsic (in-vivo) evaluation of N-gram models

- Extrinsic evaluation
 - Time-consuming; can take days or weeks
- So instead
 - Sometimes use intrinsic evaluation: perplexity
 - Bad approximation
 - unless the test data looks just like the training data
 - So generally only useful in pilot experiments
 - But is helpful to think about.

Intuition of Perplexity

How well can we predict the next word?

I always order pizza with cheese and _____

The 33rd President of the US was _____

I saw a ____

- Unigrams are terrible at this game. (Why?)
- A better model
 - is one which assigns a higher probability to the word that actually occurs

mushrooms 0.1

pepperoni 0.1

. . . .

fried rice 0.0001

. . . .

and 1e-100

Perplexity

The best language model is one that best predicts an unseen test set

Gives the highest P(sentence)

Perplexity is the probability of the test set, normalized by the number of words:

Chain rule:

For bigrams:

$$PP(W) = P(w_1 w_2 ... w_N)^{-\frac{1}{N}}$$

$$= \sqrt[N]{\frac{1}{P(w_1 w_2 ... w_N)}}$$

$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_1...w_{i-1})}}$$

$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}}$$

Minimizing perplexity is the same as maximizing probability

Example

- How hard is the task of recognizing digits '0,1,2,3,4,5,6,7,8,9'
 - Perplexity 10
- How hard is recognizing (30,000) names at Microsoft.
 - Perplexity = 30,000
- Perplexity is weighted equivalent branching factor (number of possible children)

Perplexity as branching factor

- Let's suppose a sentence consisting of random digits
- What is the perplexity of this sentence according to a model that assign P=1/10 to each digit?

$$PP(W) = P(w_1 w_2 ... w_N)^{-\frac{1}{N}}$$

$$= (\frac{1}{10}^{N})^{-\frac{1}{N}}$$

$$= \frac{1}{10}^{-1}$$

$$= 10$$

Quiz

A traffic signal has three colors: green, yellow, and red, which appear with the following probabilities. Using a unigram model, what is the perplexity of the sequence (green, yellow, red)?

$$P(green) = 2/5$$

$$P(yellow) = 1/5$$

$$P(red) = 2/5$$

$$PP(green, yellow, red) = \left(\frac{2}{5} \times \frac{1}{5} \times \frac{2}{5}\right)^{-\frac{1}{3}}$$

Quiz

- The number zero is really frequent and occurs 10 times more often than other numbers.
- What is the perplexity?

Lower perplexity = better model

Training 38 million words, test 1.5 million words,
 WSJ

N-gram Order	Unigram	Bigram	Trigram
Perplexity	962	170	109