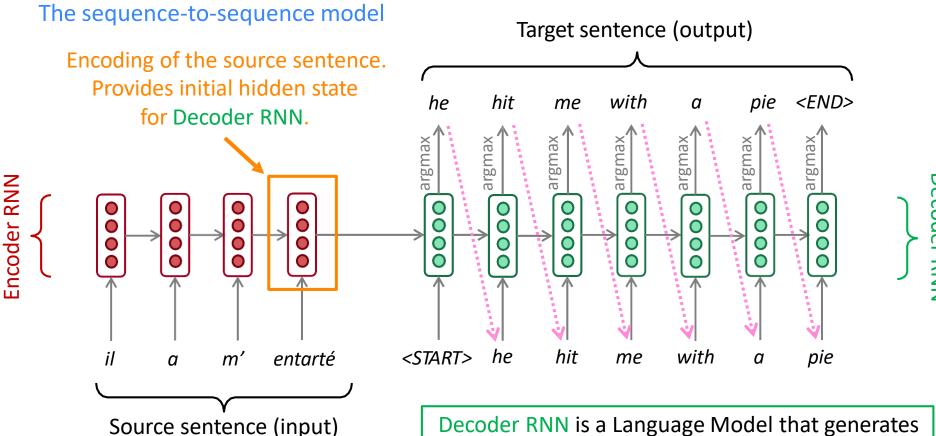
# Sequence to Sequence modeling + Attention

#### **Neural Machine Translation?**

- Neural Machine Translation (NMT) is a way to do Machine Translation with a single neural network
- The neural network architecture is called sequence-to-sequence (aka seq2seq) and it involves two RNNs.

### **Neural Machine Translation (NMT)**



**Encoder RNN produces** an encoding of the source sentence.

Decoder RNN is a Language Model that generates target sentence, conditioned on encoding.

Note: This diagram shows **test time** behavior: decoder output is fed in ...... as next step's input

#### Sequence-to-sequence is versatile!

- Sequence-to-sequence is useful for more than just MT
- Many NLP tasks can be phrased as sequence-to-sequence:
  - Summarization (long text → short text)
  - Dialogue (previous utterances → next utterance)
  - Parsing (input text → output parse as sequence)
  - Code generation (natural language → Python code)

#### **Neural Machine Translation (NMT)**

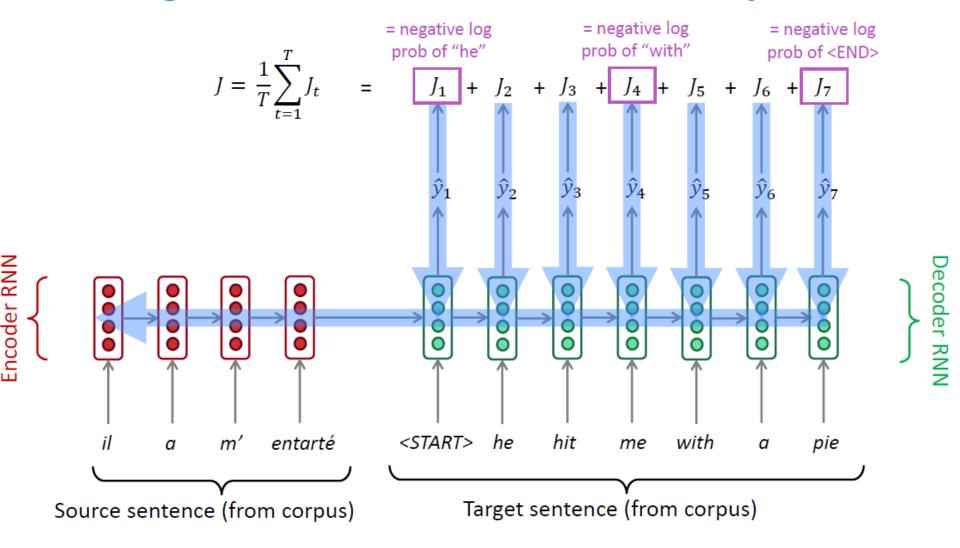
- The sequence-to-sequence model is an example of a Conditional Language Model.
  - Language Model because the decoder is predicting the next word of the target sentence y
  - Conditional because its predictions are also conditioned on the source sentence x
- NMT directly calculates P(y|x):

$$P(y|x) = P(y_1|x) P(y_2|y_1, x) P(y_3|y_1, y_2, x) \dots P(y_T|y_1, \dots, y_{T-1}, x)$$

Probability of next target word, given target words so far and source sentence *x* 

- Question: How to train a NMT system?
- Answer: Get a big parallel corpus...

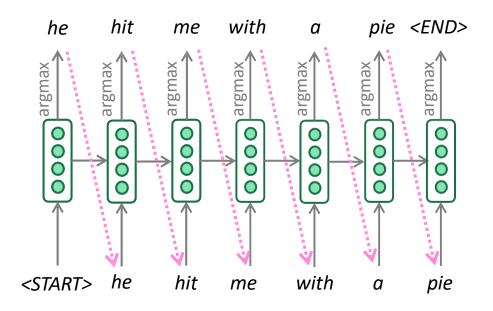
#### **Training a Neural Machine Translation system**



Seq2seq is optimized as a <u>single system</u>. Backpropagation operates "end-to-end".

### **Greedy decoding**

 We saw how to generate (or "decode") the target sentence by taking argmax on each step of the decoder



- This is greedy decoding (take most probable word on each step)
- Problems with this method?

#### Problems with greedy decoding

- Greedy decoding has no way to undo decisions!
  - <u>Input</u>: *il a m'entarté* (he hit me with a pie)
  - → he \_\_\_\_
  - $\rightarrow$  he hit \_\_\_\_
  - $\rightarrow$  he hit a \_\_\_\_\_ (whoops! no going back now...)

How to fix this?

#### **Exhaustive search decoding**

Ideally we want to find a (length T) translation y that maximizes

$$P(y|x) = P(y_1|x) P(y_2|y_1, x) P(y_3|y_1, y_2, x) \dots, P(y_T|y_1, \dots, y_{T-1}, x)$$

$$= \prod_{t=1}^{T} P(y_t|y_1, \dots, y_{t-1}, x)$$

- We could try computing all possible sequences y
  - This means that on each step t of the decoder, we're tracking  $V^t$  possible partial translations, where V is vocab size
  - This O(V<sup>T</sup>) complexity is far too expensive!

#### Beam search decoding

- <u>Core idea:</u> On each step of decoder, keep track of the k most probable partial translations (which we call hypotheses)
  - k is the beam size (in practice around 5 to 10)
- A hypothesis  $y_1, \ldots, y_t$  has a score which is its log probability:

$$score(y_1, ..., y_t) = log P_{LM}(y_1, ..., y_t | x) = \sum_{i=1}^{t} log P_{LM}(y_i | y_1, ..., y_{i-1}, x)$$

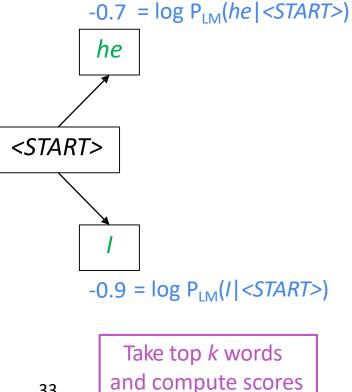
- Scores are all negative, and higher score is better
- We search for high-scoring hypotheses, tracking top k on each step
- Beam search is not guaranteed to find optimal solution
- But much more efficient than exhaustive search!

Beam size = k = 2. Blue numbers = 
$$score(y_1, ..., y_t) = \sum_{i=1}^t log P_{LM}(y_i|y_1, ..., y_{i-1}, x)$$

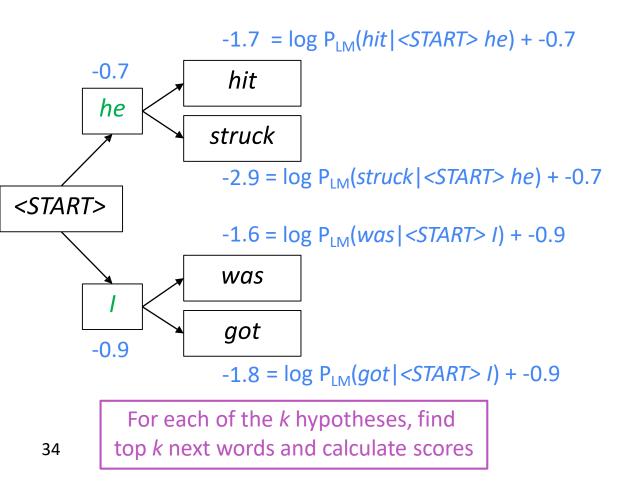
<START>

Calculate prob dist of next word

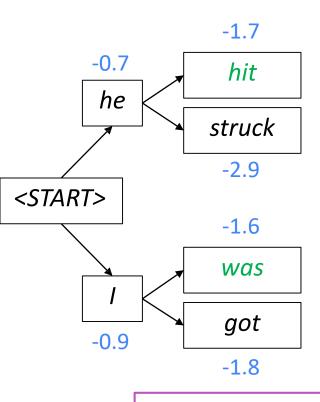
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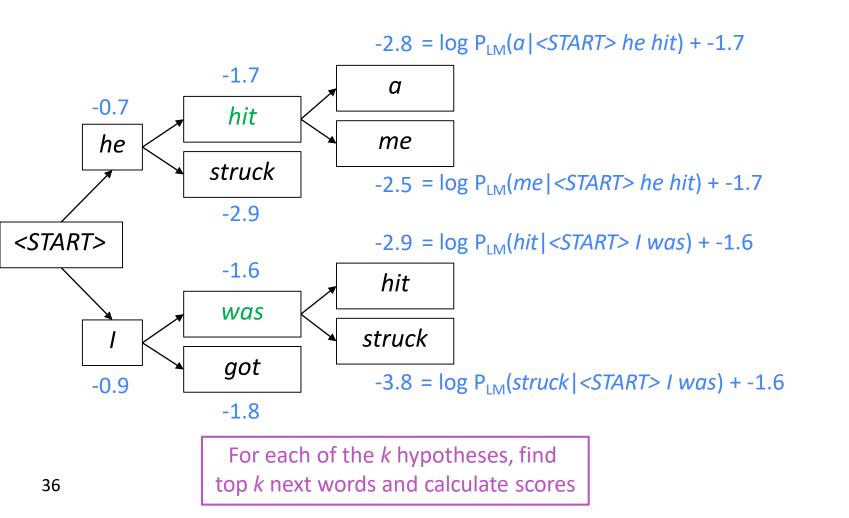


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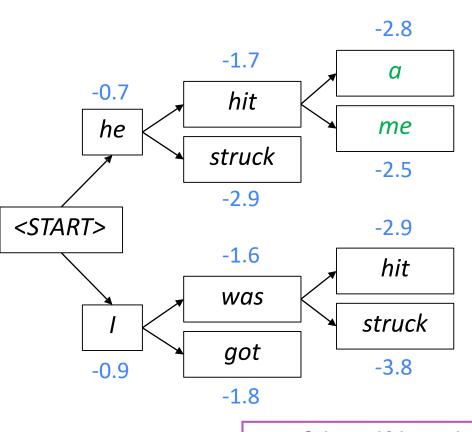


Of these  $k^2$  hypotheses, just keep k with highest scores

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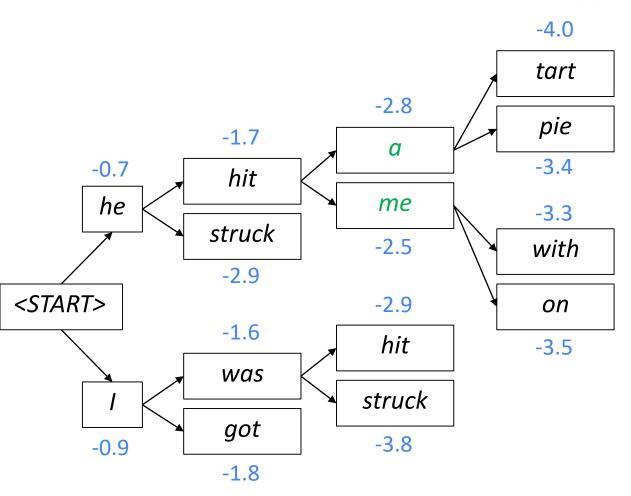


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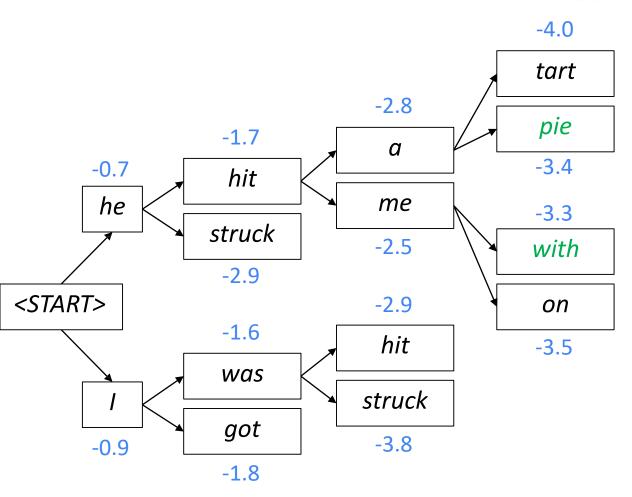
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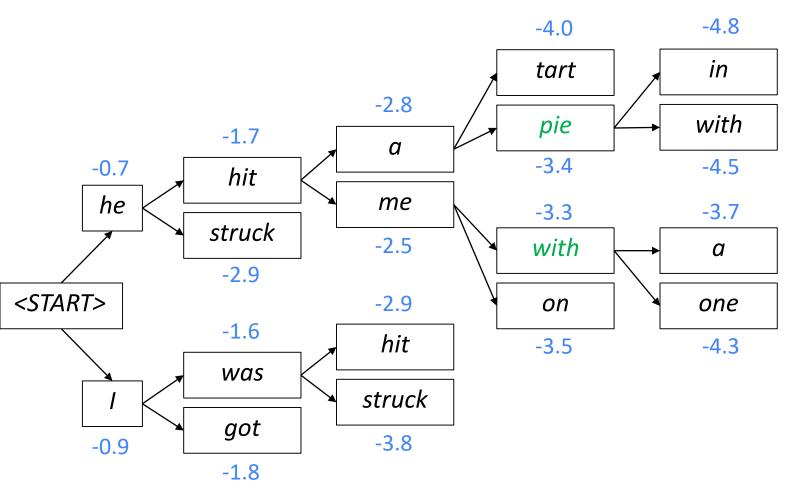
For each of the *k* hypotheses, find top *k* next words and calculate scores

Beam size = k = 2. Blue numbers = 
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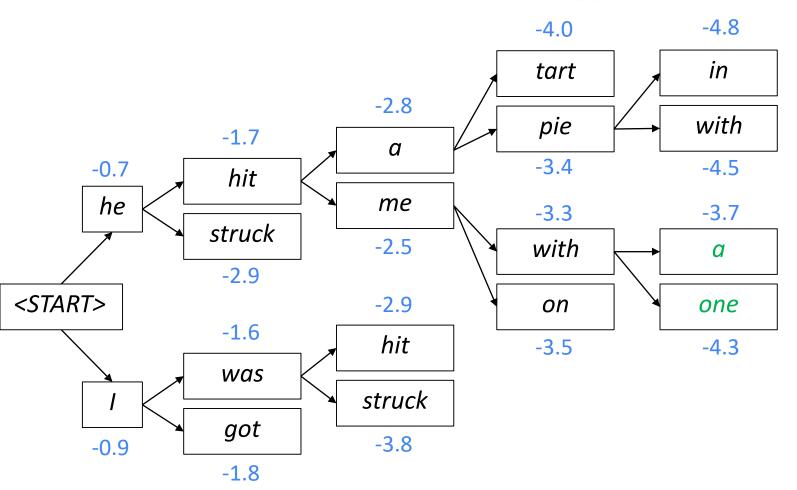
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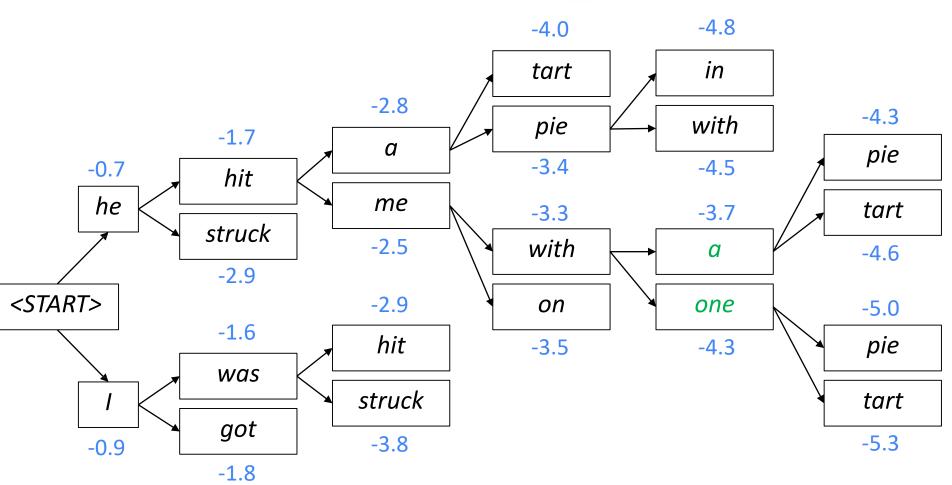
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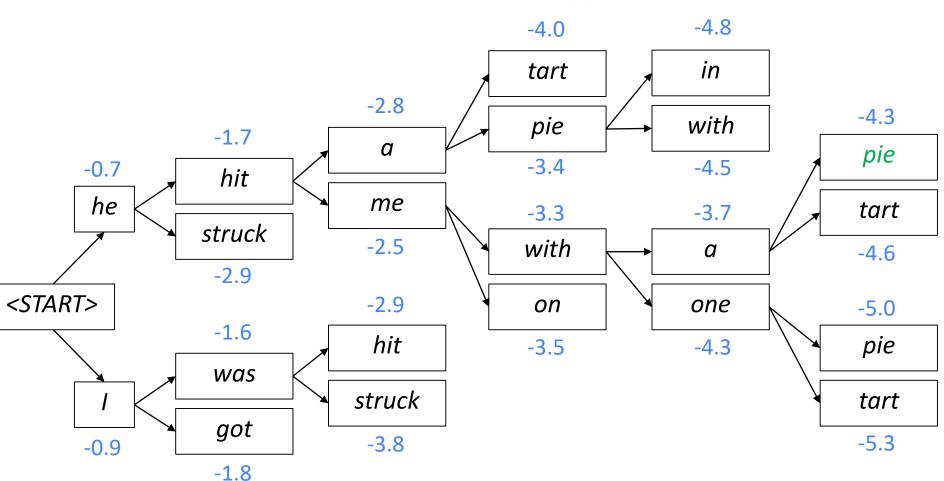
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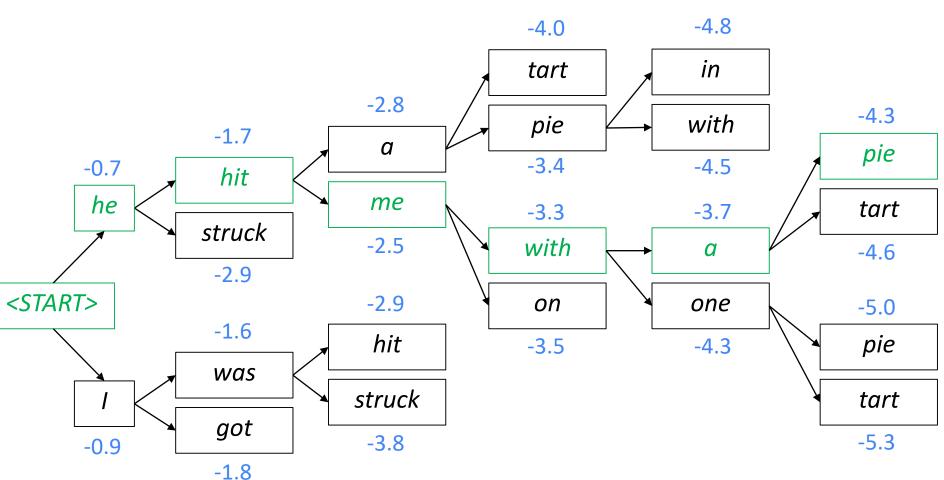


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Beam size = k = 2. Blue numbers =  $score(y_1, ..., y_t) = \sum_{i=1}^t log P_{LM}(y_i|y_1, ..., y_{i-1}, x)$ 



#### Beam search decoding: stopping criterion

- In greedy decoding, usually we decode until the model produces a <END> token
  - For example: <START> he hit me with a pie <END>
- In beam search decoding, different hypotheses may produce <END> tokens on different timesteps
  - When a hypothesis produces <END>, that hypothesis is complete.
  - Place it aside and continue exploring other hypotheses via beam search.
- Usually we continue beam search until:
  - We reach timestep T (where T is some pre-defined cutoff), or
  - We have at least n completed hypotheses (where n is pre-defined cutoff)

#### Beam search decoding: finishing up

- We have our list of completed hypotheses.
- How to select top one with highest score?
- Each hypothesis  $y_1, \ldots, y_t$  on our list has a score

score
$$(y_1, ..., y_t) = \log P_{LM}(y_1, ..., y_t | x) = \sum_{i=1}^t \log P_{LM}(y_i | y_1, ..., y_{i-1}, x)$$

- Problem with this: longer hypotheses have lower scores
- <u>Fix:</u> Normalize by length. Use this to select top one instead:

$$\frac{1}{t} \sum_{i=1}^{t} \log P_{LM}(y_i|y_1, \dots, y_{i-1}, x)$$

#### **NMT** research continues

#### NMT is the **flagship task** for NLP Deep Learning

- NMT research has pioneered many of the recent innovations of NLP Deep Learning
- In 2019: NMT research continues to thrive
  - Researchers have found many, many improvements to the "vanilla" seq2seq NMT system we've presented today
  - But one improvement is so integral that it is the new vanilla...

### **ATTENTION**

#### **Attention**

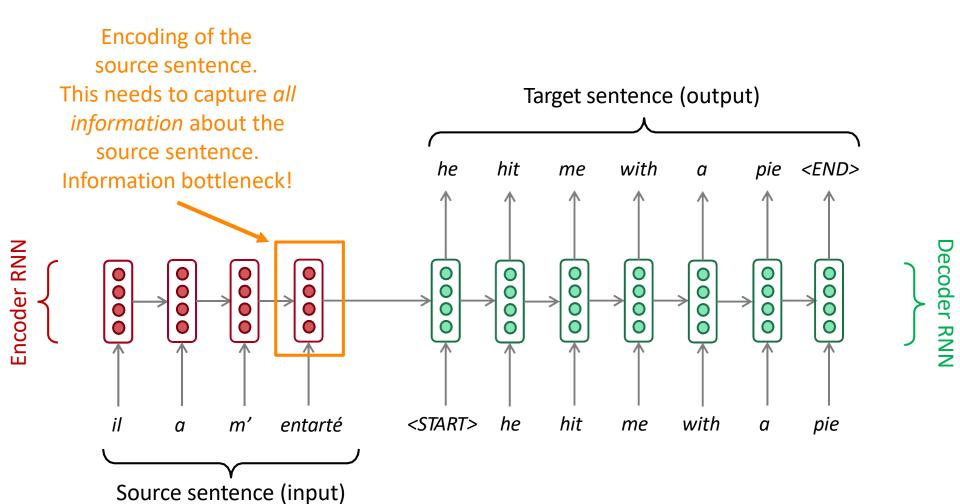
#### Sequence-to-sequence: the bottleneck problem

Encoding of the source sentence. Target sentence (output) hit <END> he with pie me а **Encoder RNN** <START> he hit with m' entarté me pie а а Source sentence (input)

Problems with this architecture?

Decoder RNN

#### Sequence-to-sequence: the bottleneck problem



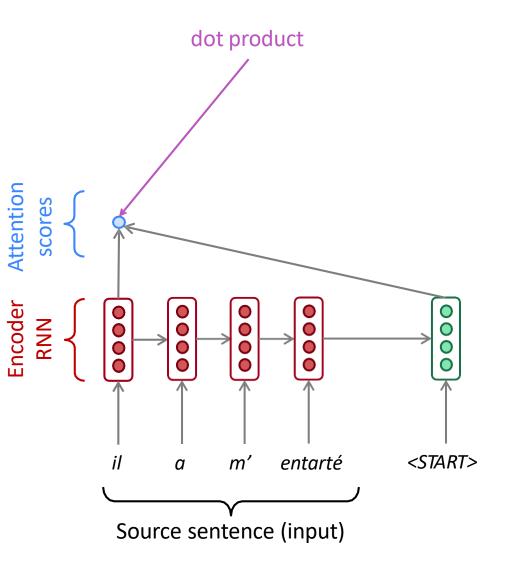
#### **Attention**

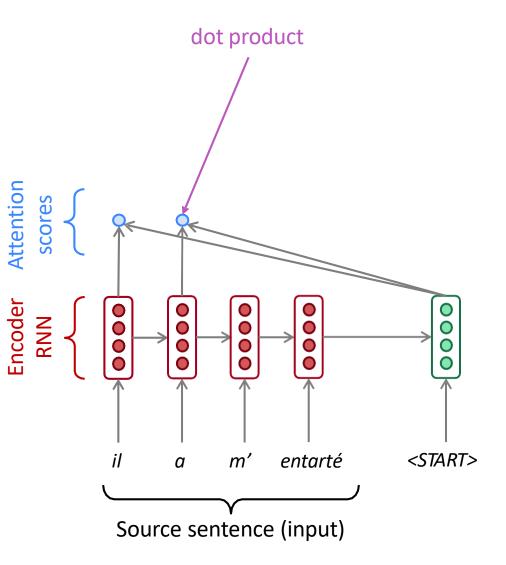
Attention provides a solution to the bottleneck problem.

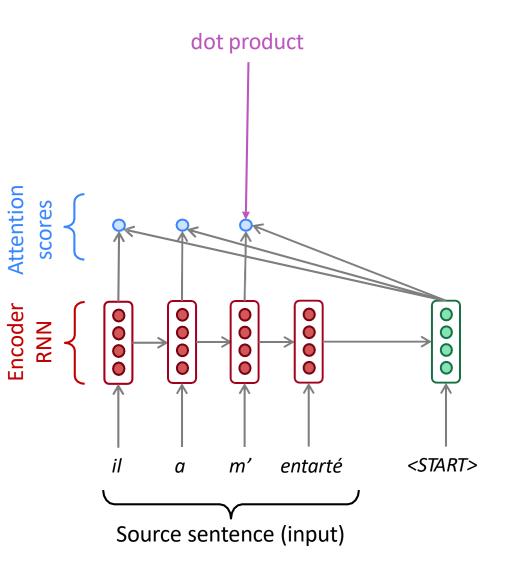
• <u>Core idea</u>: on each step of the decoder, use <u>direct connection to</u> the encoder to focus on a particular part of the source sequence

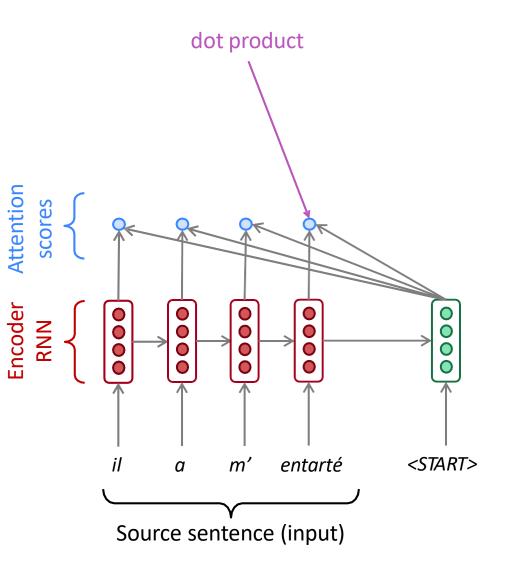


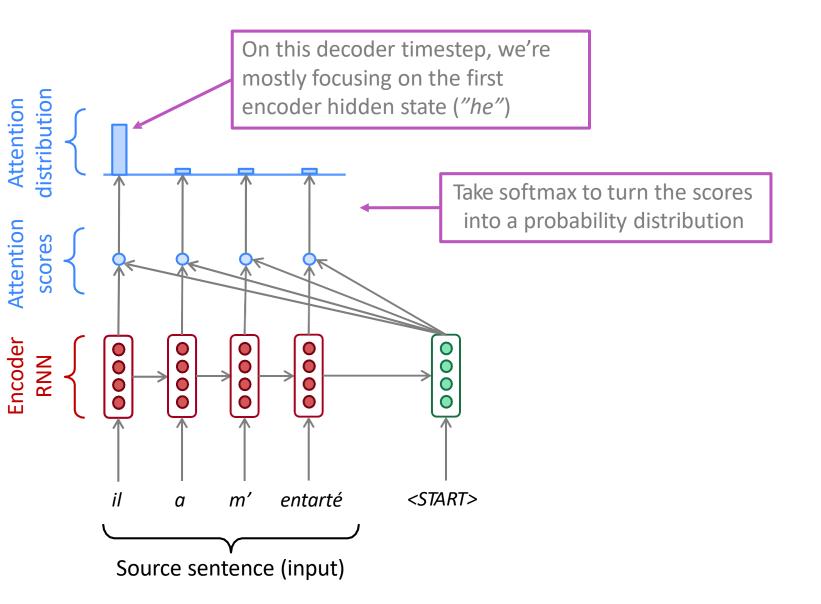
 First we will show via diagram (no equations), then we will show with equations

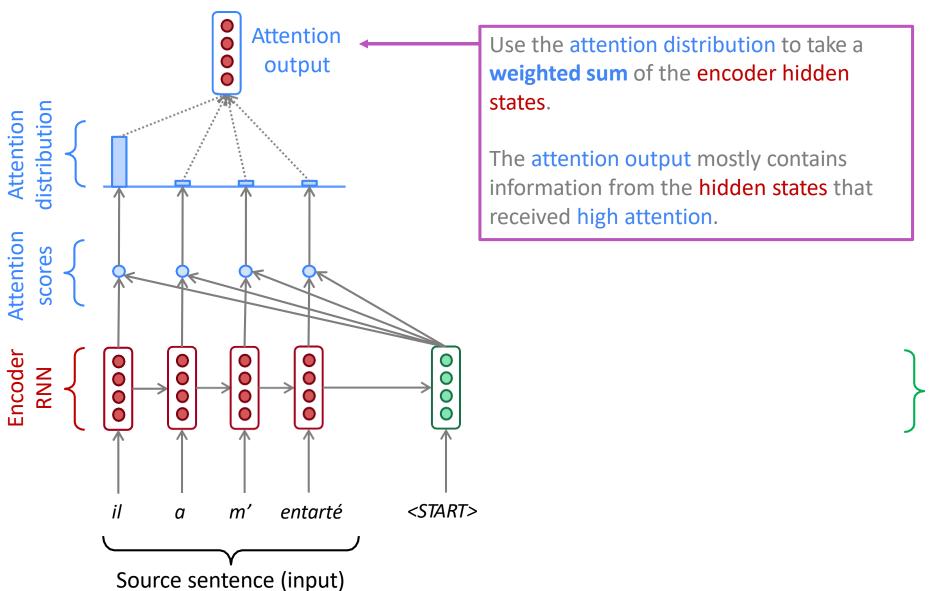




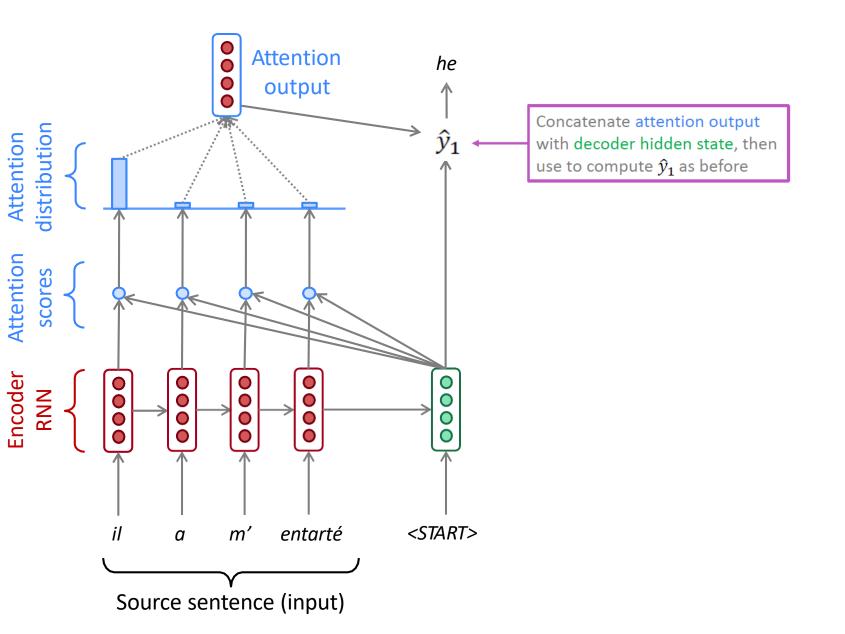






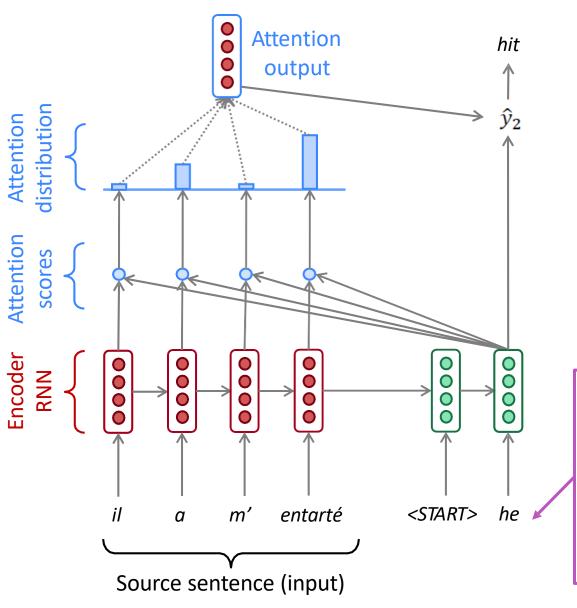


# Decoder RNN

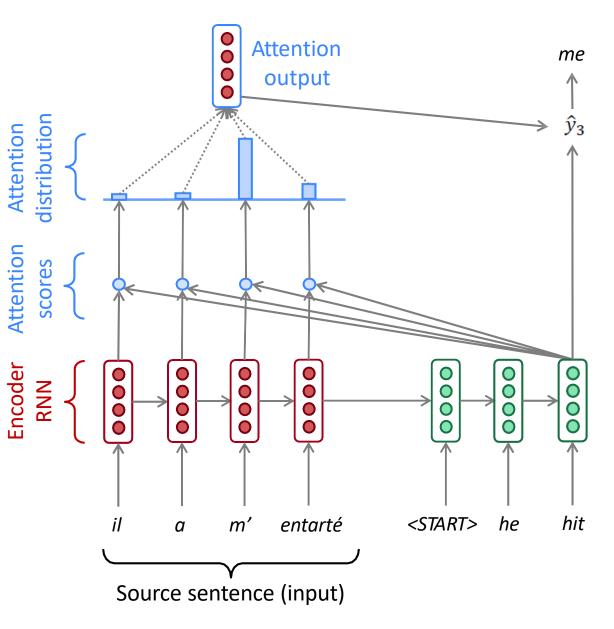


# Decoder RNN

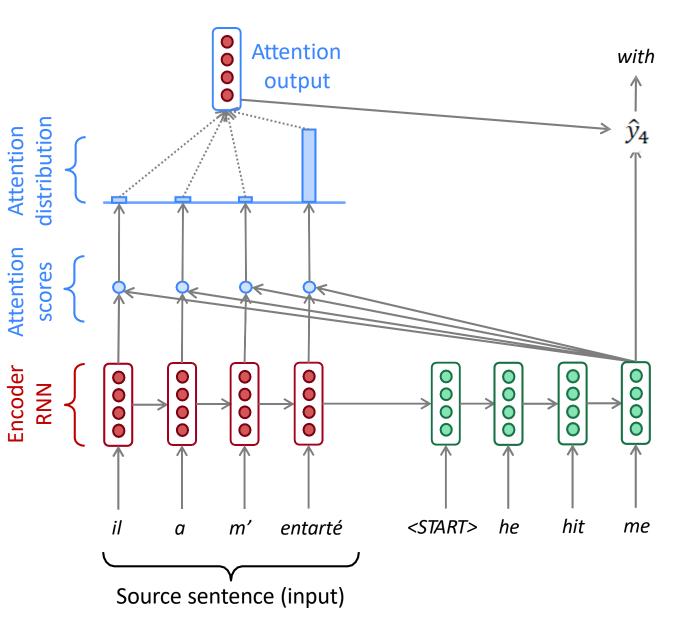
#### Sequence-to-sequence with attention



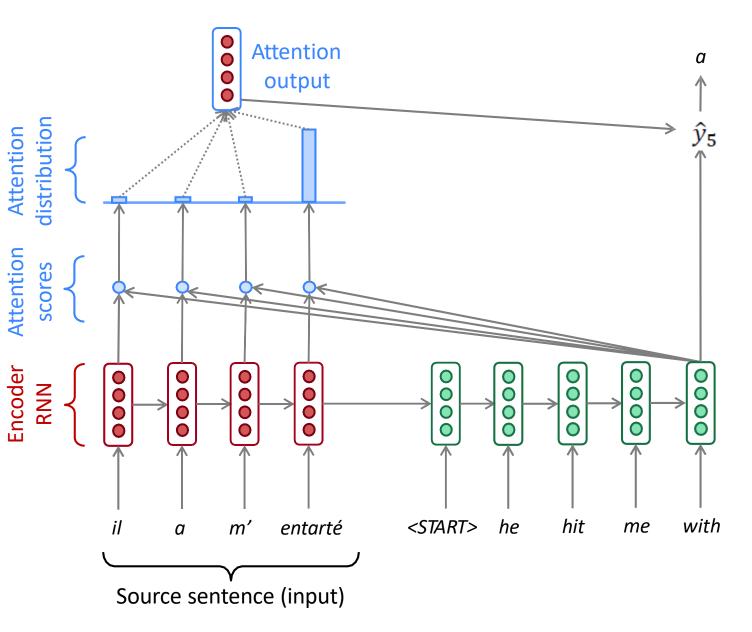
Sometimes we take the attention output from the previous step, and also feed it into the decoder (along with the usual decoder input). We do this in Assignment 4.

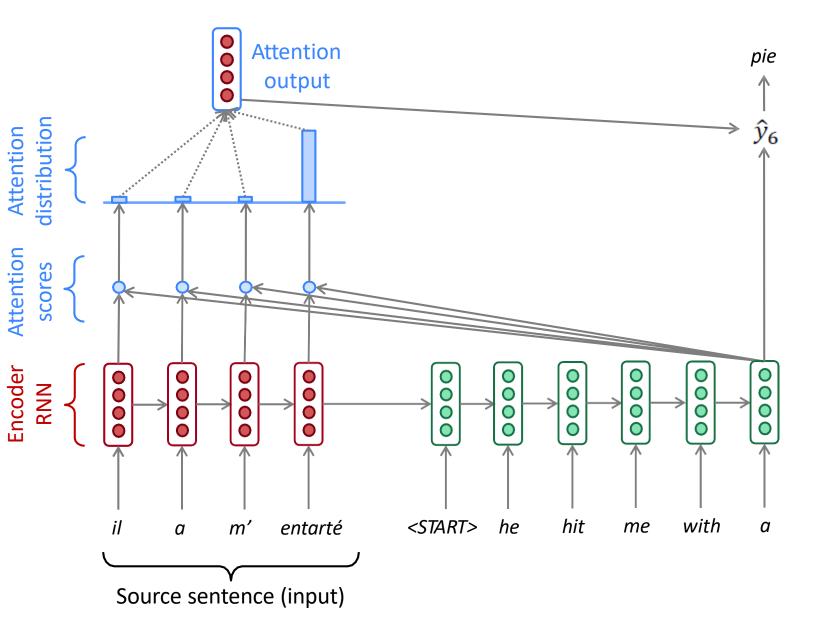












Decoder RNN

#### **Attention: In equations**

- We have encoder hidden states  $h_1, \ldots, h_N \in \mathbb{R}^h$
- On timestep t, we have decoder hidden state  $s_t \in \mathbb{R}^h$
- We get the attention scores  $e^t$  for this step:

$$oldsymbol{e}^t = [oldsymbol{s}_t^Toldsymbol{h}_1, \dots, oldsymbol{s}_t^Toldsymbol{h}_N] \in \mathbb{R}^N$$

• We take softmax to get the attention distribution  $\alpha^t$  for this step (this is a probability distribution and sums to 1)

$$\alpha^t = \operatorname{softmax}(\boldsymbol{e}^t) \in \mathbb{R}^N$$

• We use  $lpha^t$  to take a weighted sum of the encoder hidden states to get the attention output  $m{a}_t$ 

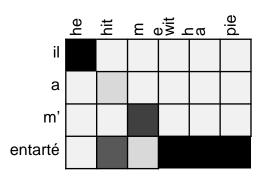
$$m{a}_t = \sum_{i=1}^N lpha_i^t m{h}_i \in \mathbb{R}^h$$

• Finally we concatenate the attention output  $a_t$  with the decoder hidden state  $s_t$  and proceed as in the non-attention seq2seq model

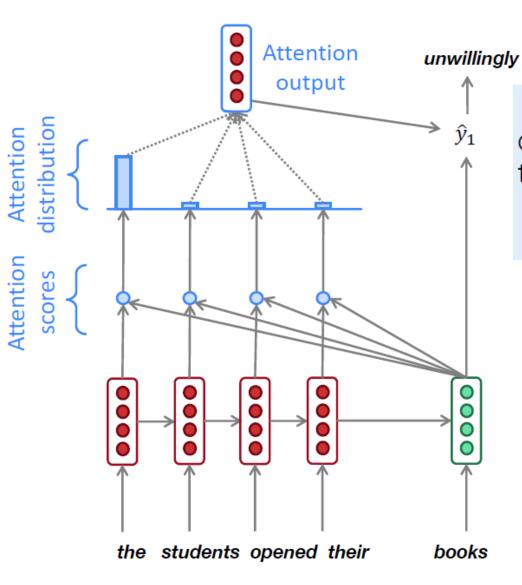
$$[oldsymbol{a}_t;oldsymbol{s}_t]\in\mathbb{R}^{2h}$$

#### **Attention is great**

- Attention significantly improves NMT performance
  - It's very useful to allow decoder to focus on certain parts of the source
- Attention solves the bottleneck problem
  - Attention allows decoder to look directly at source; bypass bottleneck
- Attention helps with vanishing gradient problem
  - Provides shortcut to faraway states
- Attention provides some interpretability
  - By inspecting attention distribution, we can see what the decoder was focusing on
  - We get (soft) alignment for free!
  - This is cool because we never explicitly trained an alignment system
  - The network just learned alignment by itself



#### **Seq2Seq+Attention for LM**



Concatenate (or otherwise compose) the attention output with the current hidden state, then pass through a softmax layer to predict the next word

#### Attention is a *general* Deep Learning technique

- We've seen that attention is a great way to improve the sequence-to-sequence model for Machine Translation.
- However: You can use attention in many architectures (not just seq2seq) and many tasks (not just MT)
- More general definition of attention:
  - Given a set of vector values, and a vector query, attention is a technique to compute a weighted sum of the values, dependent on the query.
- We sometimes say that the query attends to the values.
- For example, in the seq2seq + attention model, each decoder hidden state (query) attends to all the encoder hidden states
   (values).

#### Attention is a general Deep Learning technique

#### **More general definition of attention:**

Given a set of vector *values*, and a vector *query*, <u>attention</u> is a technique to compute a weighted sum of the values, dependent on the query.

#### Intuition:

- The weighted sum is a selective summary of the information contained in the values, where the query determines which values to focus on.
- Attention is a way to obtain a fixed-size representation of an arbitrary set of representations (the values), dependent on some other representation (the query).

### Many variants of attention

- Original formulation:  $a(\mathbf{q}, \mathbf{k}) = w_2^T \tanh(W_1[\mathbf{q}; \mathbf{k}])$
- Bilinear product:  $a(\mathbf{q}, \mathbf{k}) = \mathbf{q}^T W \mathbf{k}$

Luong et al., 2015

• Dot product:  $a(\mathbf{q}, \mathbf{k}) = \mathbf{q}^T \mathbf{k}$ 

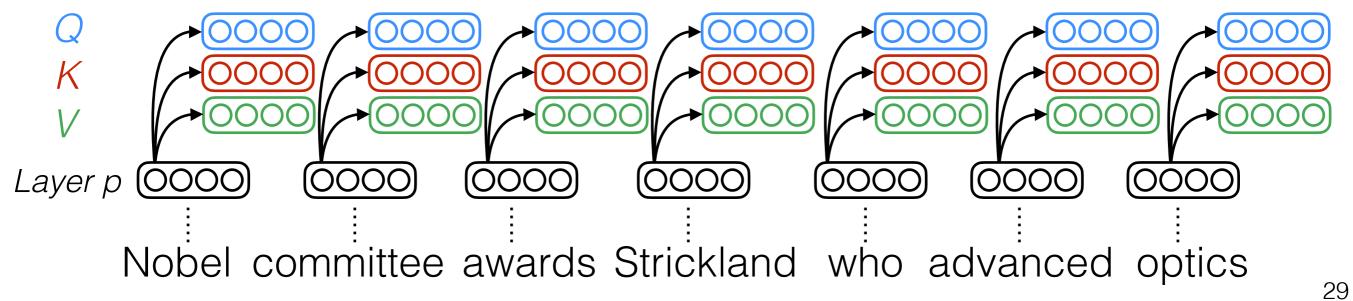
Luong et al., 2015

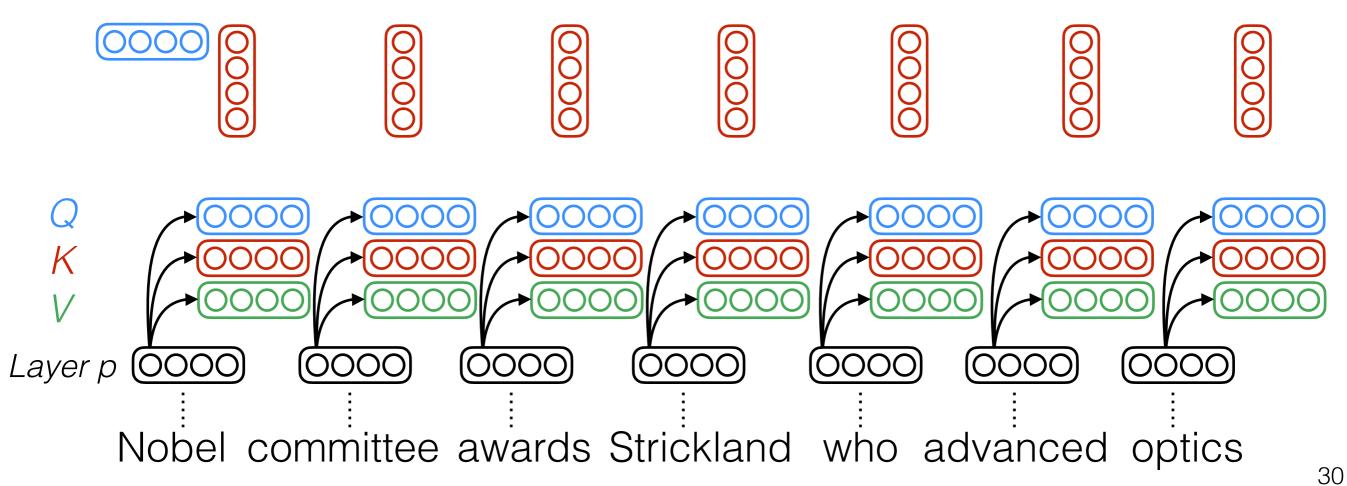
• Scaled dot product:  $a(\mathbf{q}, \mathbf{k}) = \frac{\mathbf{q}^T \mathbf{k}}{\sqrt{|\mathbf{k}|}}$  Vaswani et al., 2017

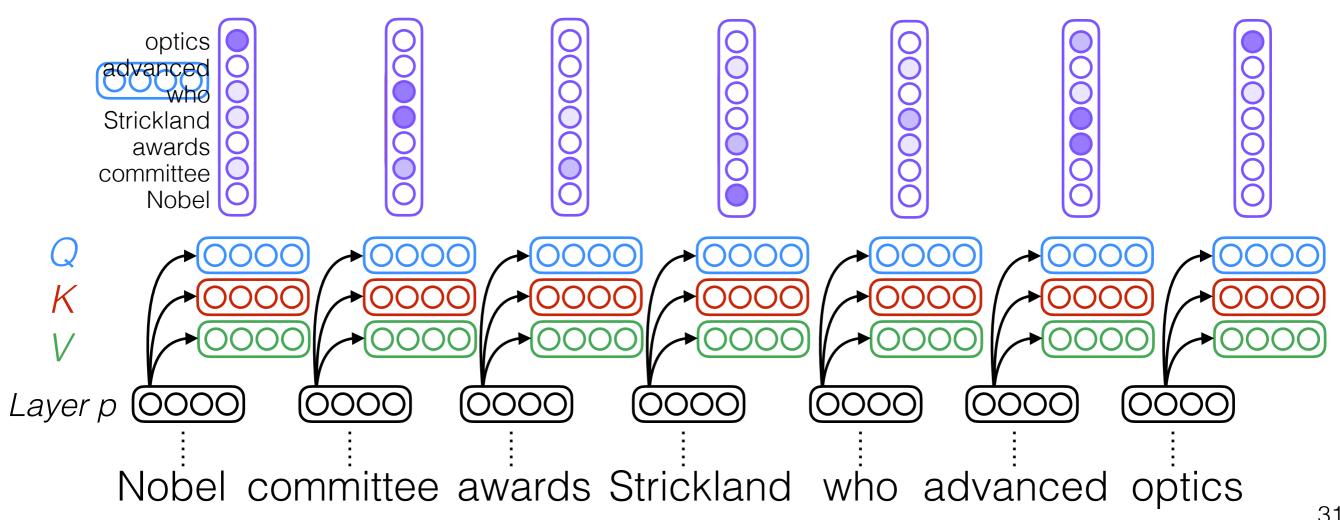
**More information:** 

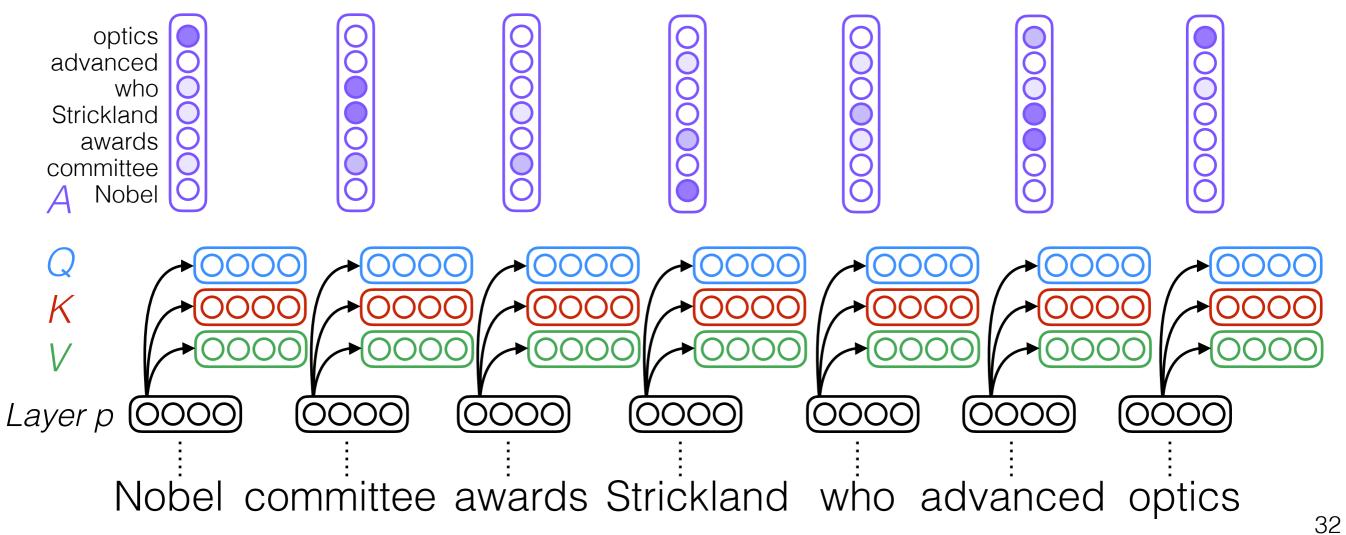
### **Self Attention**

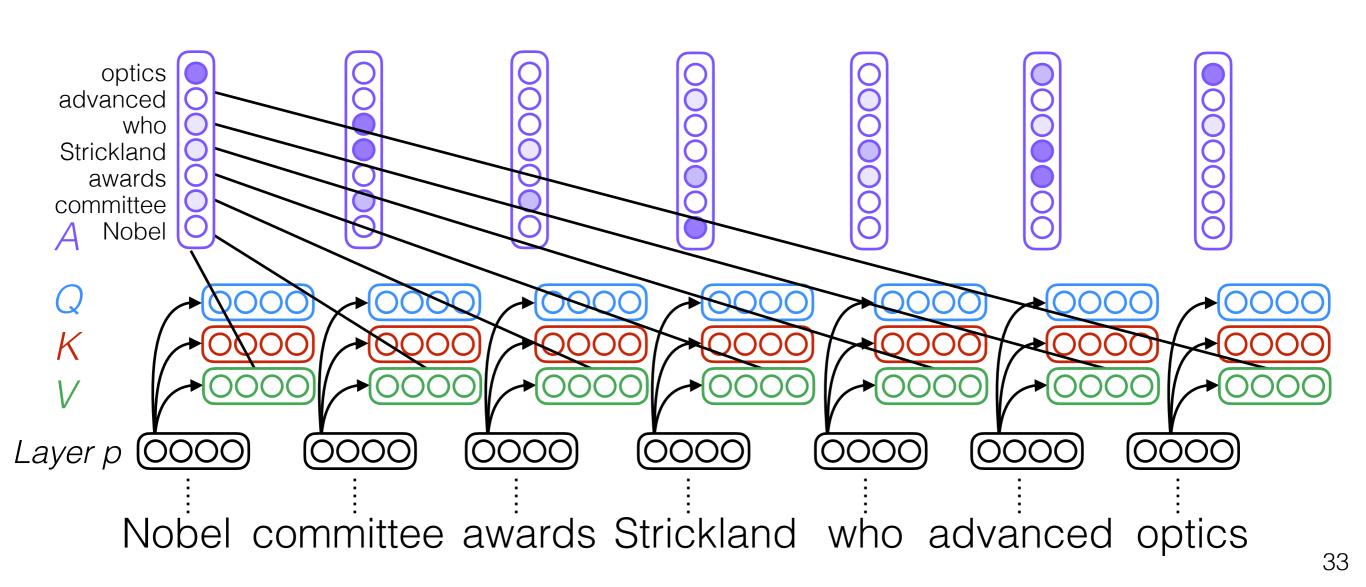
### Whiteboard

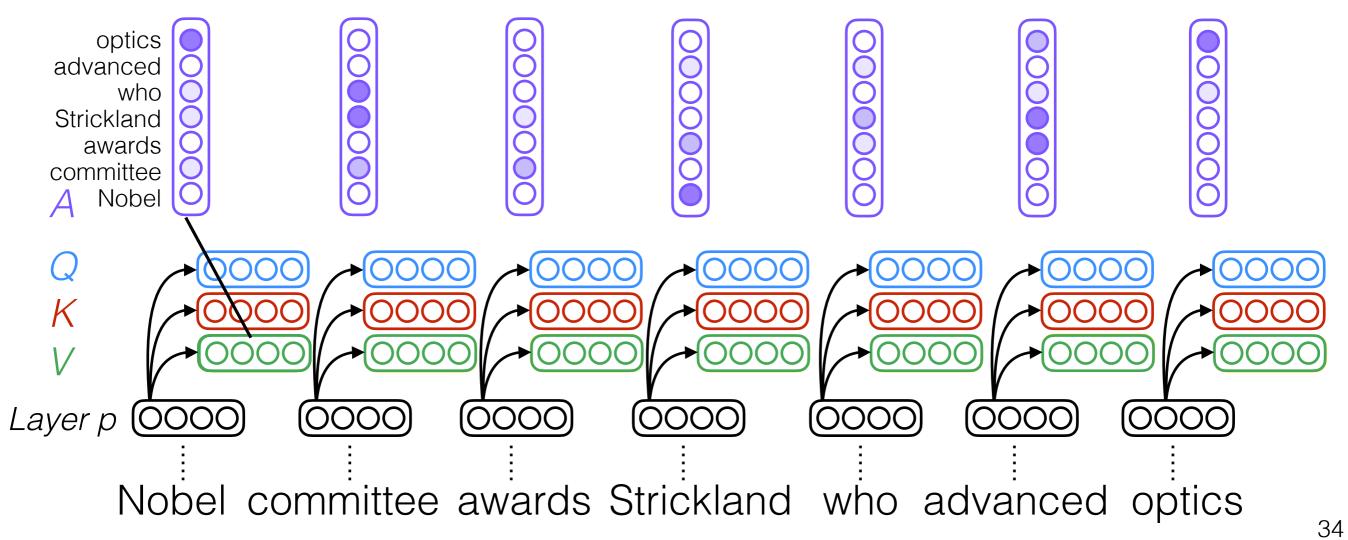


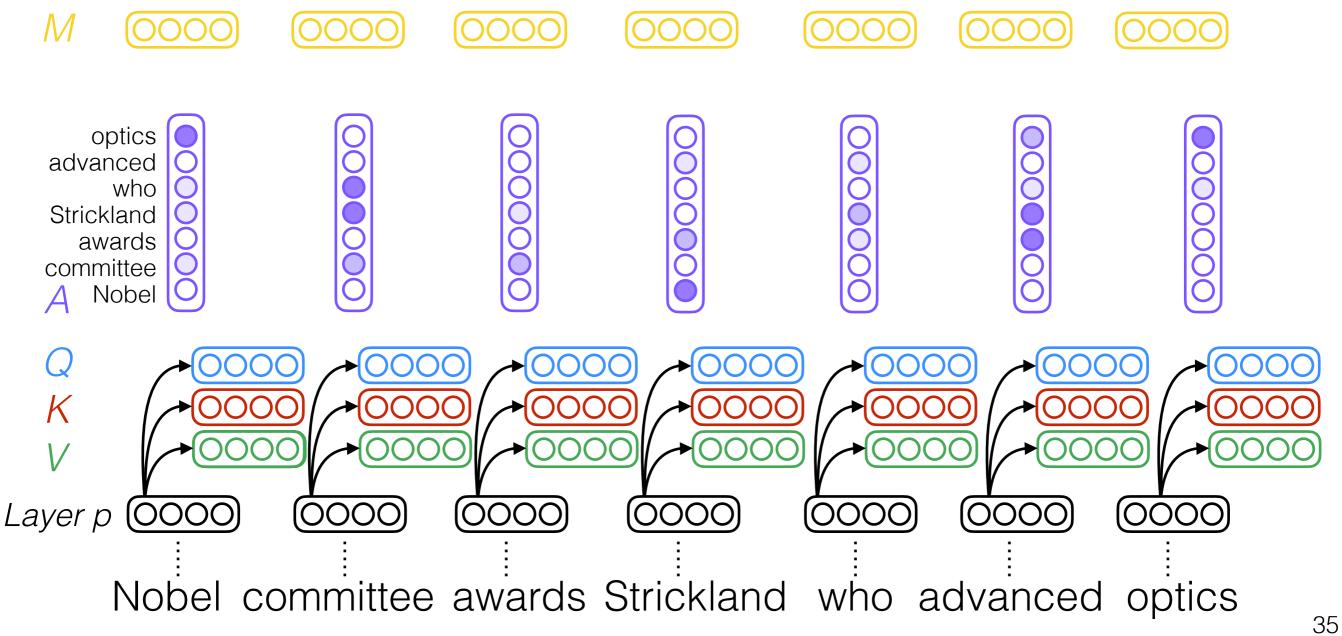


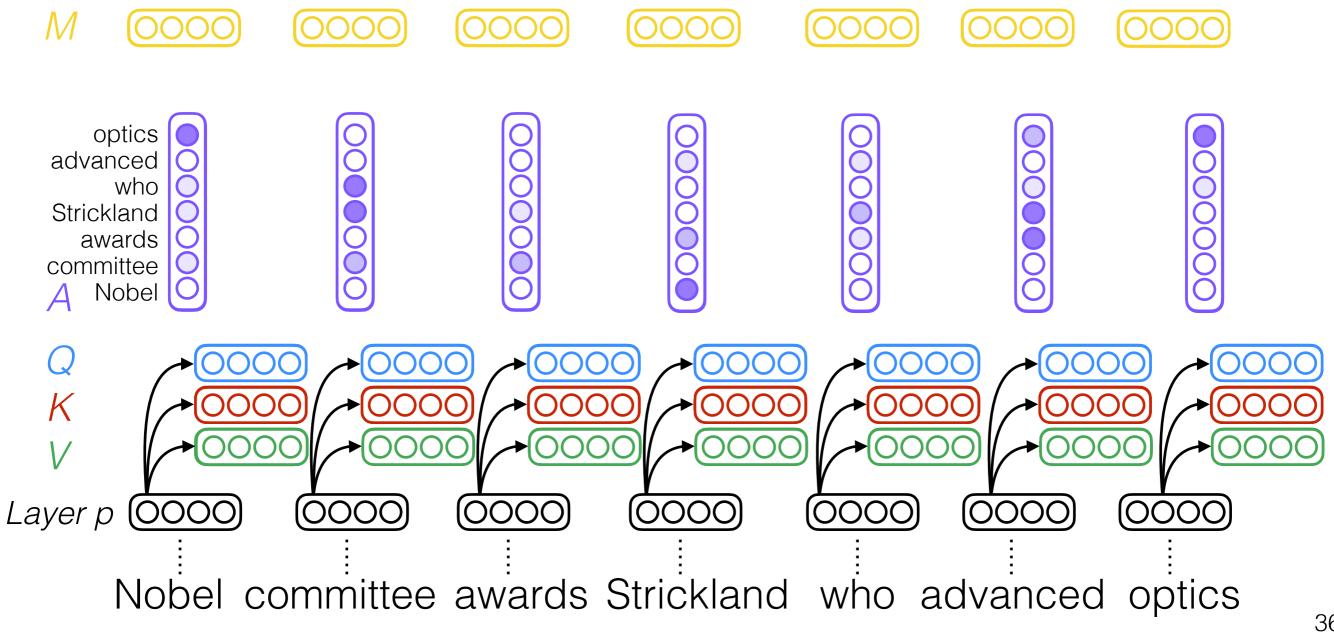




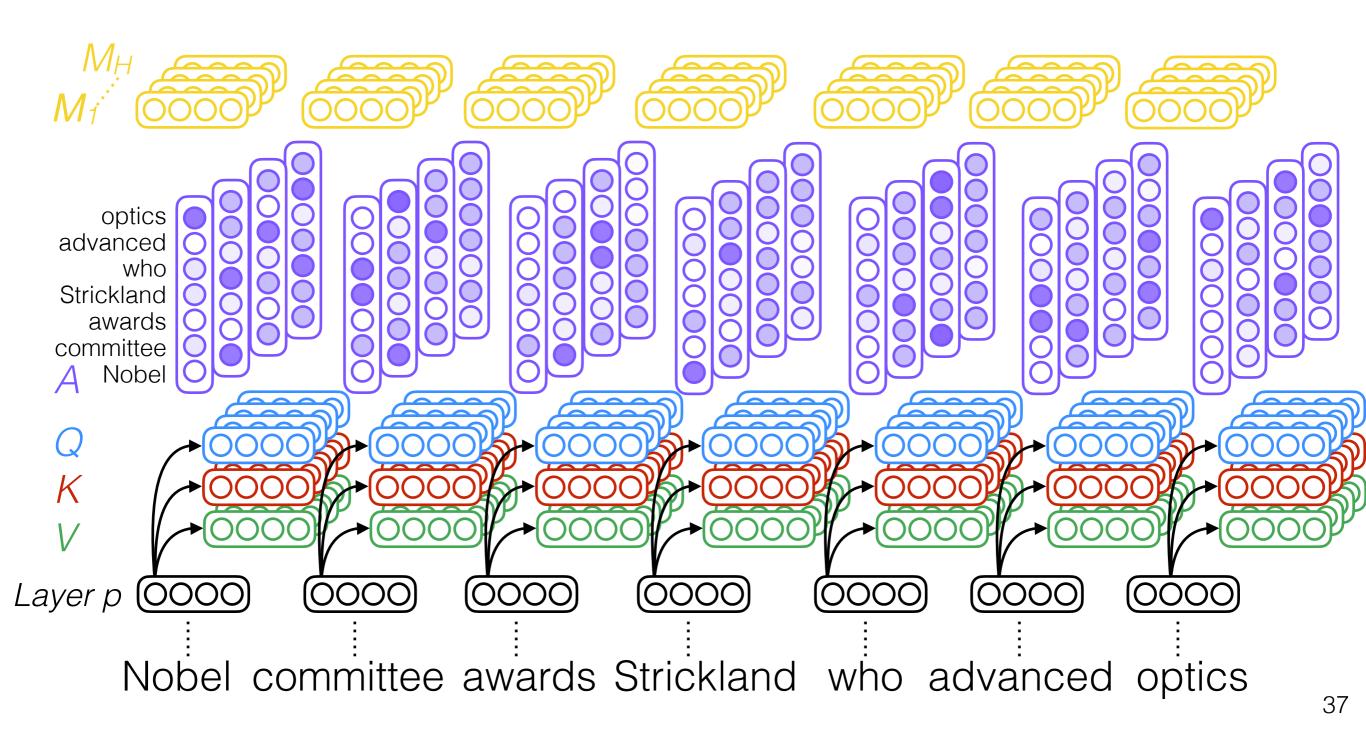




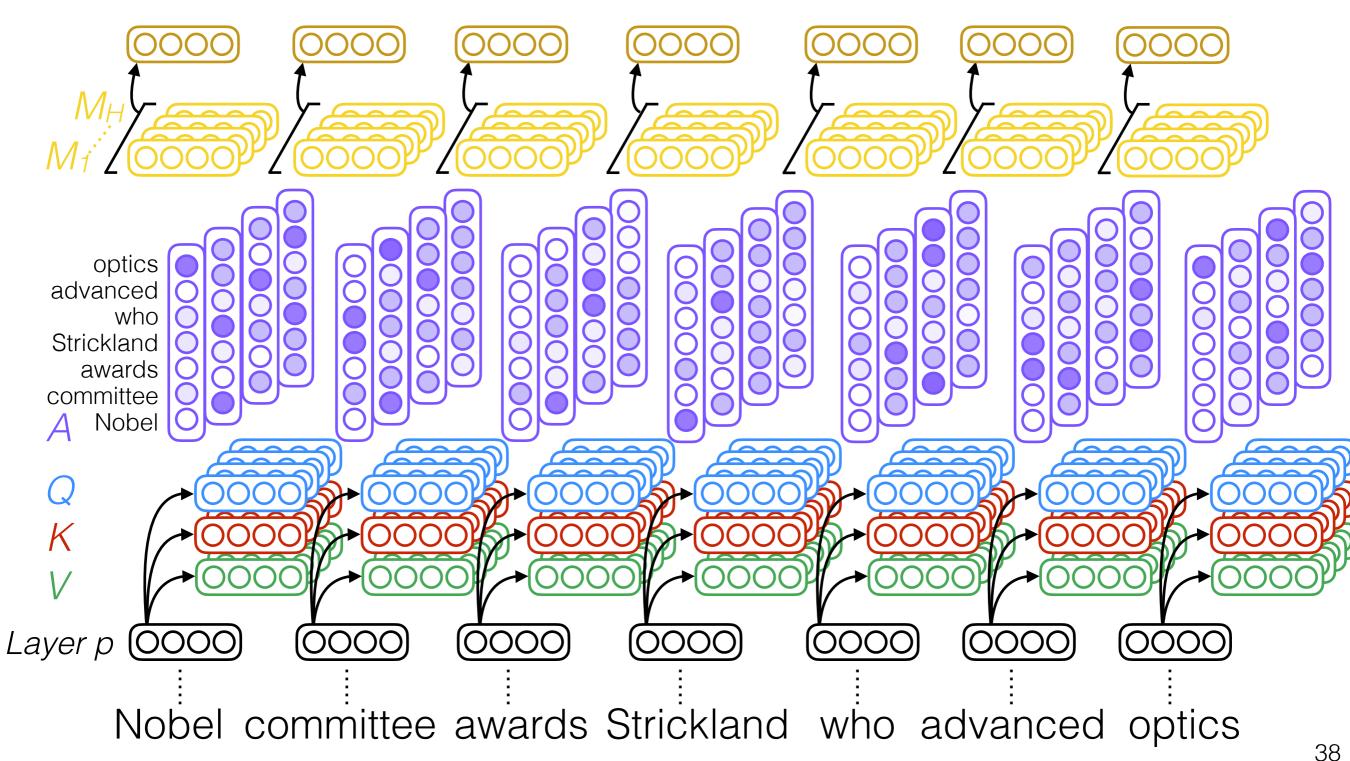


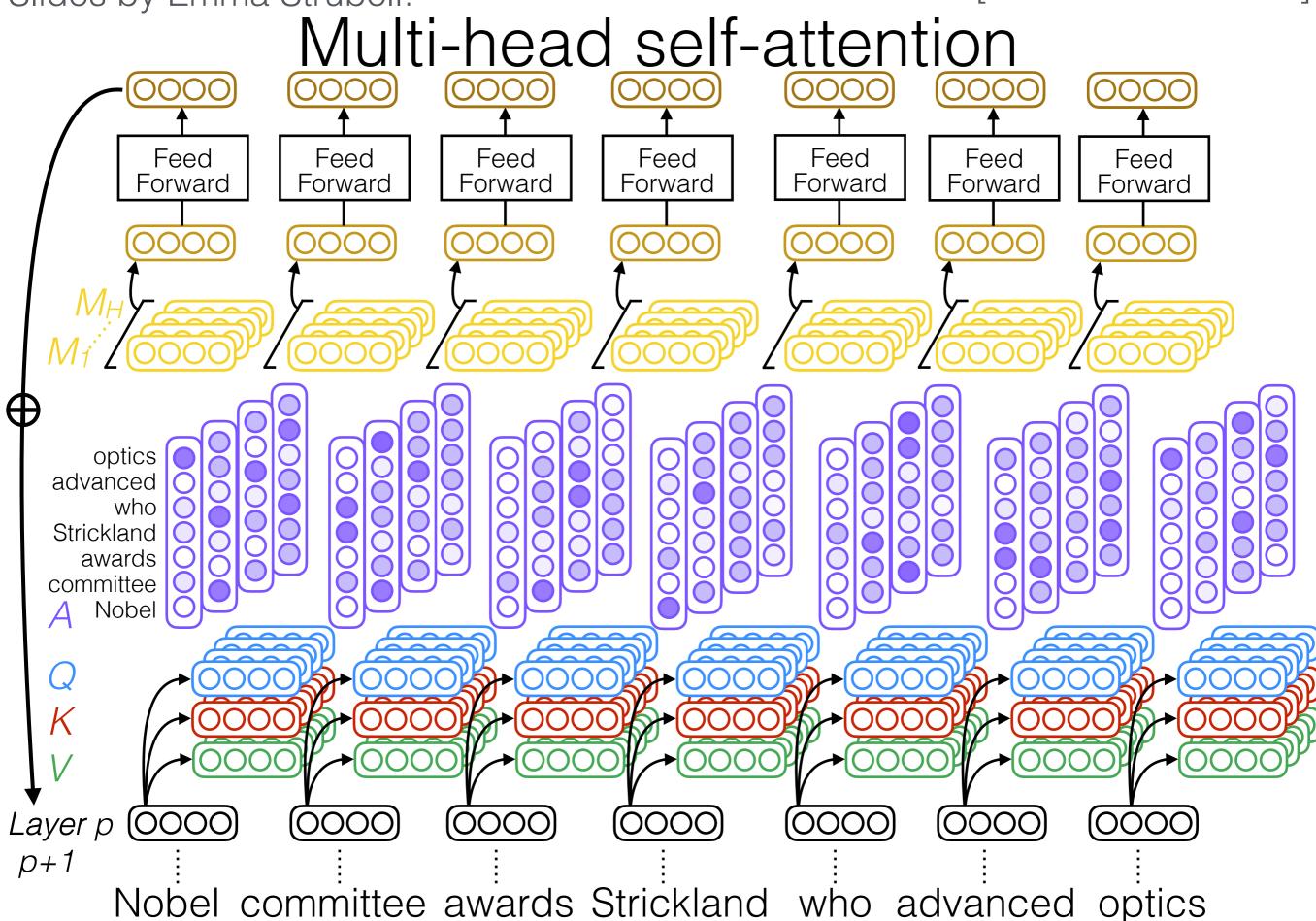


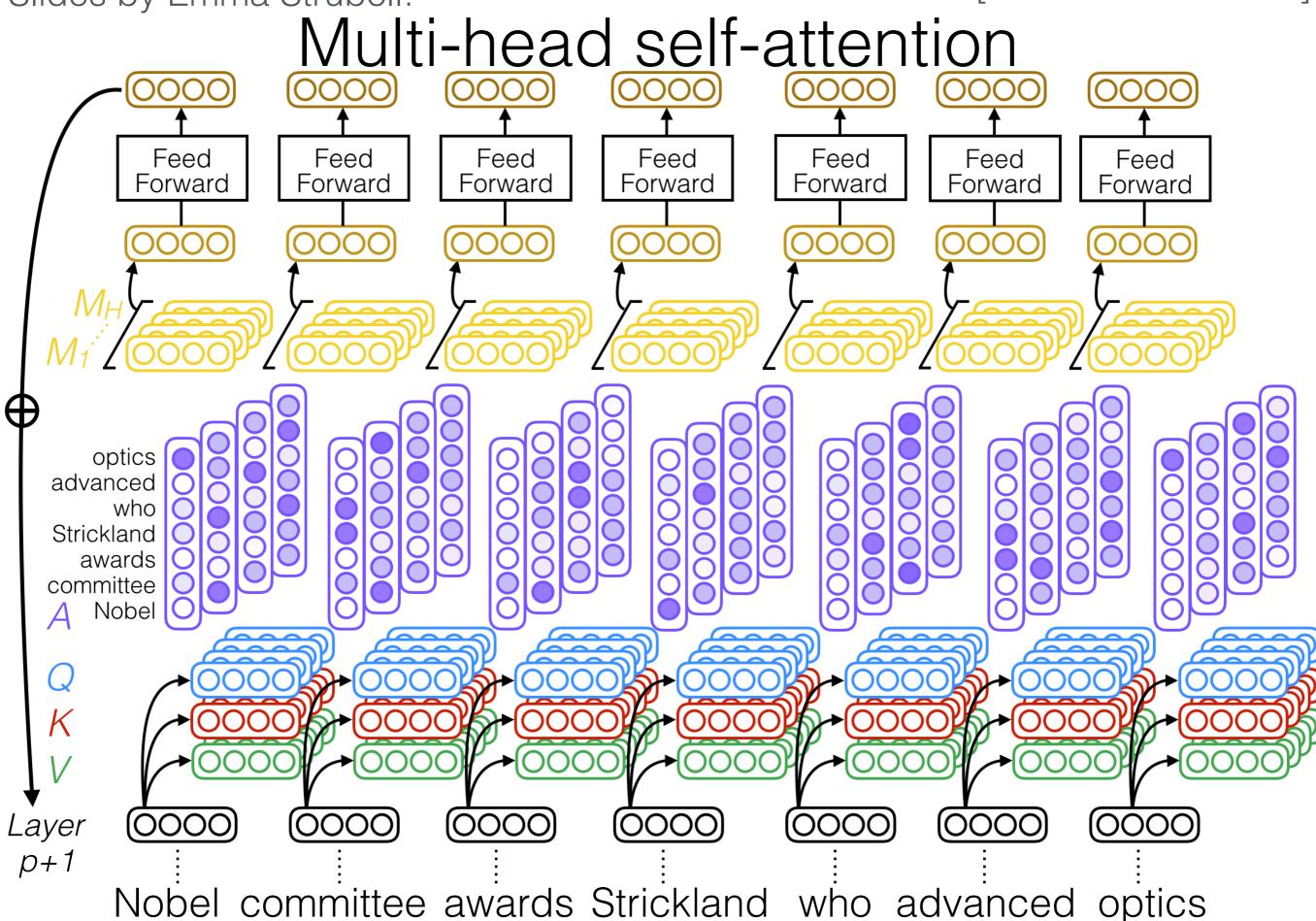
## Multi-head self-attention



## Multi-head self-attention







## Multi-head self-attention

