

$$(1) \quad C_A = \frac{N_A}{V} \quad x_A = \frac{N_A}{N_A + N_B}$$

$$y_A = \frac{C_A}{C_A + C_B} \quad P_A = x_A P = \left( \frac{N_A}{N_A + N_B} \right) P$$

$$\sum x_A = 1 \quad \sum y_A = 1$$

$$P_B = \left( \frac{N_B}{N_A + N_B} \right) P$$

$$(2) \quad v = \frac{\sum c_i u_i}{\sum u_i} \quad u = \frac{\sum f_i u_i}{\sum f_i} \quad \dot{V} = \sum x_A v_A + \sum x_B v_B$$

$$(3) \quad \begin{aligned} N_A &= C_A V_A & J_A &= C_A (V_A - v) & J_A &= C_A (V_A - v) \\ N_B &= C_B V_B & J_B &= C_B (V_B - v) & J_B &= C_B (V_B - v) \end{aligned}$$

$$(4) \quad J_A = C_A (V_A - v) \quad J_B = C_B (V_B - v)$$

$$(5) \quad \begin{aligned} J_A &= C_A (V_A - v) & J_B &= C_B (V_B - v) \\ & & &= C_B \left( V_B - \frac{C_B V_B + C_A V_A}{V_A + V_B} \right) \\ &= C_A \left( V_A - \frac{C_A V_A + C_B V_B}{V_A + V_B} \right) \end{aligned}$$

(If  $v$  is the reference velocity)

$$\begin{aligned} J_A &= C_A V_A - \frac{C_A}{C_A + C_B} (C_A V_A + C_B V_B) \\ &= N_A - \frac{C_A}{C_A + C_B} (N_A + N_B) \end{aligned}$$

$$\text{Similarly, } J_B = N_B - \frac{C_B}{C_A + C_B} (N_A + N_B)$$