

Ans 1

$$n(L) = \frac{dN(V)}{dL}$$

$$n_0(L) = \lim_{L \rightarrow 0} \frac{d(N/V)}{dL}$$

Now

\Rightarrow no of crystals with size L in $= 0$

no of crystals with size L out $= F \Delta t n(L) \Delta L$

+ no of crystals grown to size $L = n(L) V \Delta L$

- no of crystals grown to size $L + \Delta L = n(L + \Delta L) V \Delta L$

$$\Rightarrow F n(L) \Delta L = n(L) V \frac{\Delta L}{\Delta t} - n(L + \Delta L) V \frac{\Delta L}{\Delta t}$$

$$\Rightarrow F n(L) \Delta L = n(L) V G - n(L + \Delta L) V G$$

Ans 2 Converting to the differential equation

$$\lim_{\Delta L \rightarrow 0} \frac{n(L) - n(L + \Delta L)}{\Delta L} = \frac{F}{V G} n(L)$$

$$\Rightarrow \frac{-dn(L)}{dL} = \frac{F}{V G} n(L)$$

$$\Rightarrow \frac{dn(L)}{dL} = -\frac{F}{V G} n(L) = -\frac{n(L)}{G \tau}$$

$$\Rightarrow \int_{n_0(L)}^{n(L)} \frac{dn(L)}{dL} = - \int_0^L \frac{1}{G \tau} dL$$

$$\Rightarrow \ln \left(\frac{n(L)}{n_0(L)} \right) = -\frac{L}{G \tau}$$

$$\Rightarrow n(L) = n_0(L) e^{(-L/G \tau)}$$

we know $n_0(L) = \frac{B_0}{G}$

$$\Rightarrow n(L) = \frac{B_0}{G} \exp \left(\frac{-L}{G \tau} \right)$$