

# Natural Language Processing

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# Plan for Today

- Probabilistic Language Models

# Probabilistic Language Modeling

- **Goal:** compute the probability of a sentence or sequence of words.  
**P(words)** is the joint probability that a sequence of **words**= $w_1 w_2 \dots w_n$  is likely for a specified natural language.
- **Related task:** probability of an upcoming word  
 $P(w_5 | w_1, w_2, w_3, w_4)$
- A model that computes either of these:  
**P(W)** or **P( $w_n | w_1, w_2 \dots w_{n-1}$ )**

is called a language model.

- **Probability Function:**

- $P(A)$  means that how likely the event  $A$  happens.
- $P(A)$  is a number between 0 and 1.
- $P(A) = 1$  is a certain event.
- $P(A) = 0$  is an impossible event.

- **Unconditional Probability** or Prior Probability:

- $P(A)$ : the probability of the event  $A$  does not depend on other events.

- **Conditional Probability** – Posterior Probability –

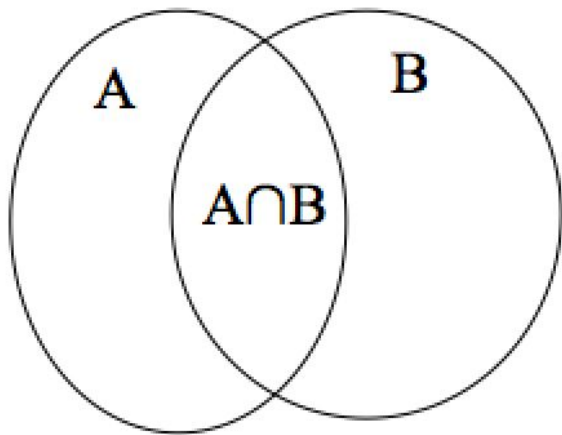
Likelihood:

- $P(A|B)$ : this is read as the probability of  $A$  given that we know  $B$ .

- **Example:**

- $P(\text{put})$  is the probability of to see the word **put** in a text.
- $P(\text{on}|\text{put})$  is the probability of to see the word **on** after seeing the word **put**.

## Unconditional and Conditional Probability



- $P(A|B) = P(A \cap B) / P(B)$
- $P(B|A) = P(A \cap B) / P(A)$

## Bayes' Theorem

- Bayes' theorem is used to calculate  $P(A|B)$  from given  $P(B|A)$ .
- We know that

$$P(A|B) = P(A \cap B) / P(B)$$

$$P(B|A) = P(A \cap B) / P(A)$$

- So, we will have

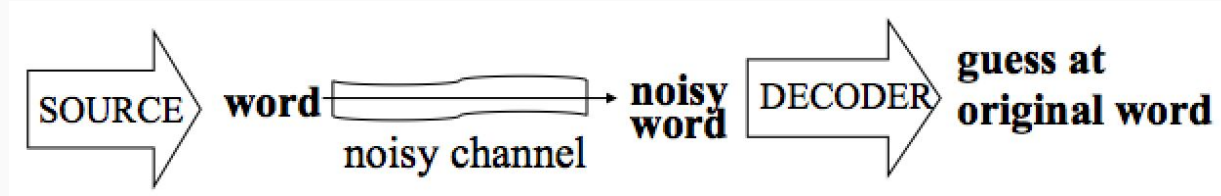
$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

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## **Language Models:**

- The Noisy Channel Model
- N-GRAM models are the language models which are widely used in NLP domain.

## The Noisy Channel Model



Many problems in Natural Language Processing can be viewed as noisy channel model.

- optical character recognition.
- spelling correction.
- speech recognition.



## Chain Rule

- The probability of a word sequence  $w_1, w_2, \dots, w_n$  is:

$$P(w_1, w_2, \dots, w_n)$$

- We can use the chain rule of the probability to decompose this probability:

$$\begin{aligned} P(w_1^n) &= P(w_1)P(w_2|w_1)P(w_3|w_1^2)\dots P(w_n|w_1^{n-1}) \\ &= \prod_{k=1}^n P(w_k|w_1^{k-1}) \end{aligned}$$

- **Example**

$P(\text{the man from jupiter}) = P(\text{the})P(\text{man} | \text{the})P(\text{from} | \text{the man})P(\text{jupiter} | \text{the man from})$

## N Grams

- To collect statistics to compute the functions in the following forms is difficult (sometimes impossible):

$$P(w_n | w_1^{n-1})$$

- Here we are trying to compute the probability of  $w_n$  after seeing  $w_{n-1}$ .
- We may approximate this computation just looking N previous words:

$$P(w_n | w_1^{n-1}) \approx P(w_n | w_{n-N+1}^{n-1})$$

- So, a N-GRAM model:

$$P(w_1^n) \approx \prod_{k=1}^n P(w_k | w_{k-N+1}^{k-1})$$

### N Grams ...

- **Unigrams:**  $P(w_1^n) \approx \prod_{k=1}^n P(w_k)$
- **Bigrams:**  $P(w_1^n) \approx \prod_{k=1}^n P(w_k | w_{k-1})$
- **Trigrams:**  $P(w_1^n) \approx \prod_{k=1}^n P(w_k | w_{k-1} w_{k-2})$
- **Quadgrams:**  $P(w_1^n) \approx \prod_{k=1}^n P(w_k | w_{k-1} w_{k-2} w_{k-3})$

## N Grams Example

- **Unigrams:**  
$$P(\text{the man from jupiter})$$
$$\approx P(\text{the})P(\text{man})P(\text{from})P(\text{jupiter})$$
- **Bigrams:**  
$$P(\text{the man from jupiter})$$
$$\approx P(\text{the} | < s >)P(\text{man} | \text{the})P(\text{from} | \text{man})P(\text{jupiter} | \text{from})$$
- **Trigrams:**  
$$P(\text{the man from jupiter})$$
$$\approx P(\text{the} | < s > < s >)P(\text{man} | < s > \text{the})P(\text{from} | \text{the man})P(\text{jupiter} | \text{man from})$$

## Simple Markov Models

- The assumption that the probability of a word depends only on the previous word is called **Markov assumption**.
- **Markov models** are the class of probabilistic models that assume that we can predict the probability of some future unit without looking too far into the past.
- A **bigram** is called a first-order **Markov model** (because it looks one token into the past);
- A **trigram** is called a second-order **Markov model**;
- In general a **N-Gram** is called a **N-1 order Markov model**.

# Estimating N Gram Probabilities

- Estimating **Bi-Gram Probabilities**

$$\begin{aligned} P(w_n | w_{n-1}) \\ &= \frac{C(w_{n-1} w_n)}{\sum_w C(w_{n-1} w)} \\ &= \frac{C(w_{n-1} w_n)}{C(w_{n-1})} \end{aligned}$$

- Here C is the count of that pattern in the corpus.
- Estimating **N-Gram Probabilities**

$$\begin{aligned} P(w_n | w_{n-N+1}^{n-1}) \\ &= \frac{C(w_{n-N+1}^{n-1} w_n)}{C(w_{n-1}^{n-N+1})} \end{aligned}$$

## Example: Estimating N gram Probabilities

- Consider a mini corpus of three sentences:

<s>I am Sam</s>

<s>Sam I am</s>

<s>i do not like green eggs and ham</s>

- A few **bigram probabilities** from this corpus :

$$\begin{array}{l|l} P(I|<s>) = \frac{2}{3} = 0.67 & P(Sam|<s>) = \frac{1}{3} = 0.33 \\ P(am|I) = \frac{2}{3} = 0.67 & P(<s>|Sam) = \frac{1}{2} = 0.5 \\ P(Sam|am) = \frac{1}{2} = 0.5 & P(do|I) = \frac{1}{3} = 0.33 \end{array}$$

# Which N Gram?

- Which N gram should be used a language Model ?
  - Unigram, Bigram, Trigram, . . .
- Bigger N, the model will be more accurate.
  - But we may not get good estimates for N-Gram probabilities.
- The N-Gram tables will be more sparse.
- Smaller N, the model will be less accurate.
  - But we may get better estimates for N-Gram probabilities.
    - The N-Gram table will be less sparse.
- In reality, we do not use higher than **Trigram (not more than Bigram)**.
- **How big are N-Gram tables with 10,000 words?**
  - Unigram – 10,000
  - Bigram –  $10000 \times 10000 = 100,000,000$
  - Trigram –  $10000 \times 10000 \times 10000 = 1,000,000,000,000$
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# Thank You

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