
Region Segmentation

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I N D E X

What is image segmentation?

Type of region segmentation

Approaches

Clustering



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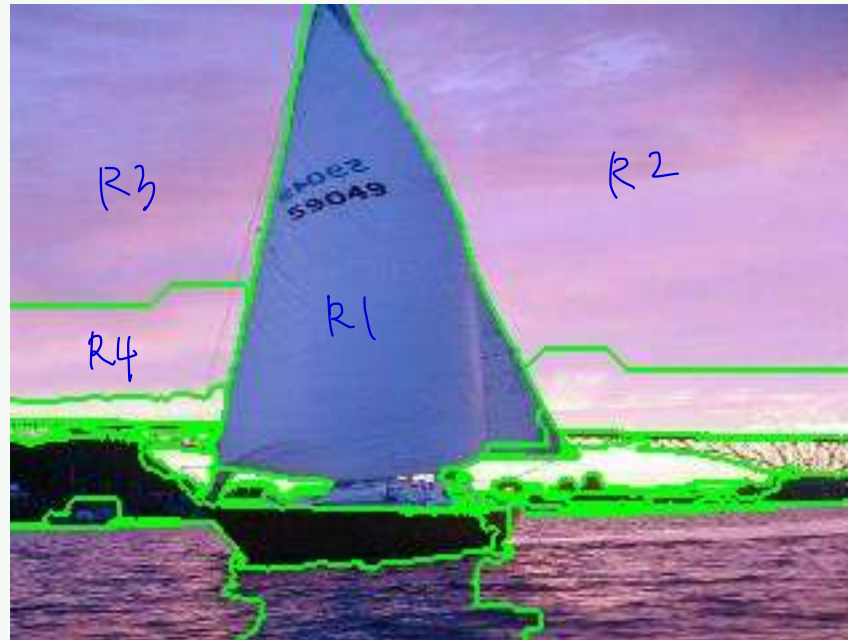


Image Segmentation : 이미지/사진 분할.



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- Image segmentation is the operation of partitioning an image into a collection of connected sets of pixels (regions)



특징을 공유하는 pixel끼리 연결하여
regions으로 나눈다.
feature -
similar property를 갖는
pixel끼리 연결하여
regions으로 나눈다.



Region-based Segmentation



- **Goal:** find coherent (homogeneous) regions in the image
- Coherent regions contain pixel which share some *similar property*
- Advantages: Better for noisy images
- Disadvantages: *Oversegmented (too many regions)*, → similar property를 비슷하게 설정하면.
Undersegmented (too few regions) → " " 너무 많이 설정하면.
⇒ similar를 잘 조정해야 함.
- Can't find objects that span multiple disconnected regions
→ 두 가지 연결하면 Over & Under.



Types of Segmentation



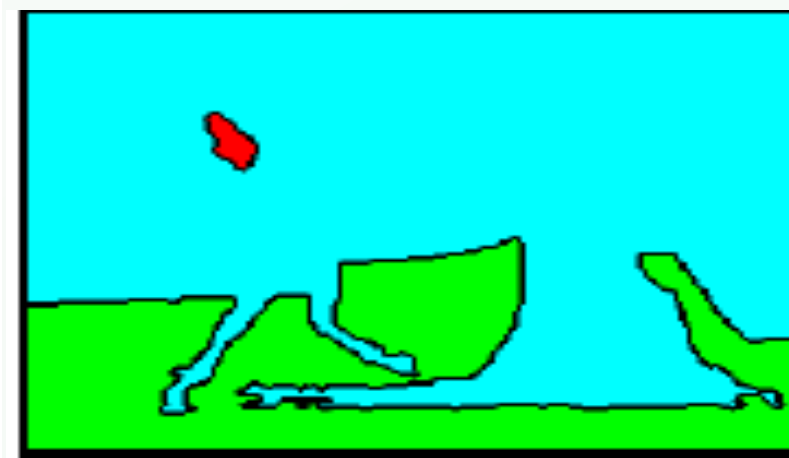
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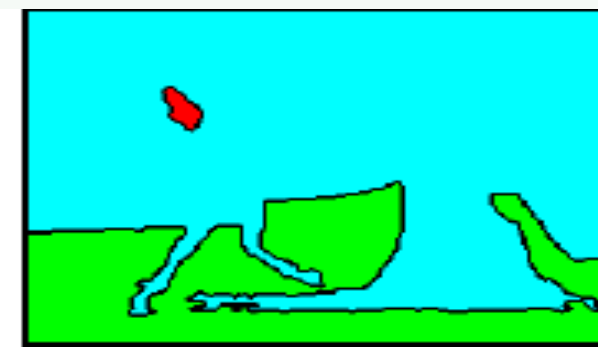
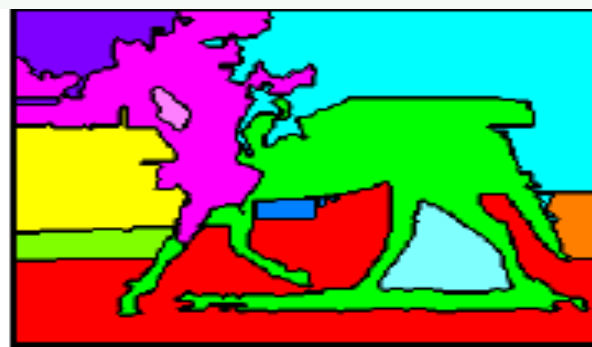
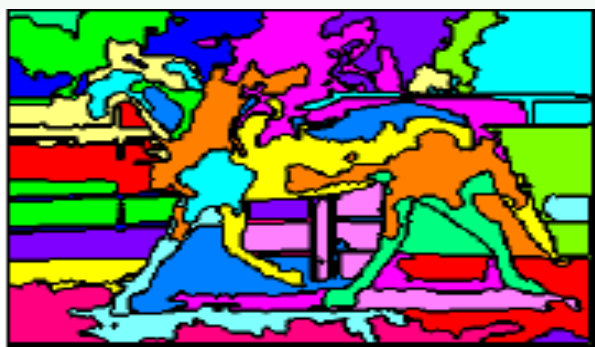
Input



Oversegmentation



Undersegmentation



Multiple Segmentations



Region-based Segmentation: Criteria



A segmentation is a partition of an image I into a set of regions S satisfying:

1. $\cup S_i = S$ Partition covers the whole image.
2. $S_i \cap S_j = \phi, i \neq j$ No regions intersect. \rightarrow *이러한 영역이 2개의 영역이 속하면 X.*
3. $\forall S_i, P(S_i) = \text{true}$ \rightarrow *S_i ni 대항 Property가 similar 해야 함.*
4. $P(S_i \cup S_j) = \text{false}, i \neq j, S_i \text{ adjacent } S_j$ \rightarrow *다른 영역의 Property는 similar 하지 않아야 함.*

Define and implement the **similarity** predicate.



Method of Region Segmentation



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- Region growing
- Split and merge
- ☆ • Clustering

많은 양의 데이터



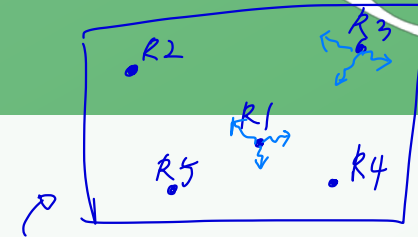
Region Growing

대부분 over segmentation을 하므로
Region Growing을 함



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→ (첫 번째): 처음의 영역 시작점이 될 pixel을 찾는 것
= seed pixel



- It start with one pixel of a potential region → 처음 시작을 한 픽셀을 한 영역이라 다른 가려놓은 시작.
- Try to grow it by adding adjacent pixels till the pixels being compared are too dissimilar
- The first pixel selected can be
 - The first unlabeled pixel in the image
 - A set of seed pixels can be chosen from the image. (region 별로 여러 이점이라)
- Usually a statistical test is used to decide which pixels can be added to a region



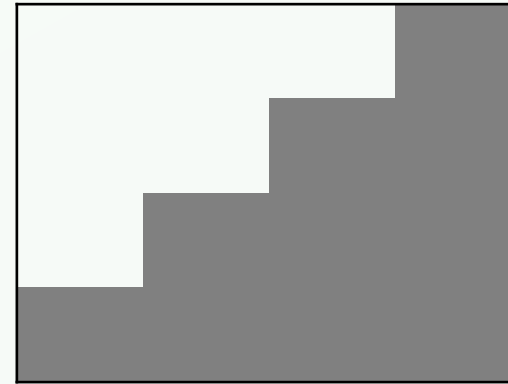
Split and Merge



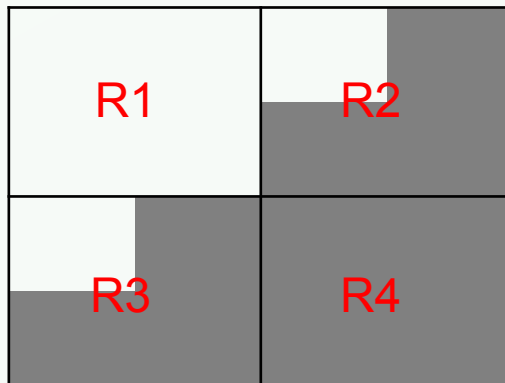
- Split into four disjoint coordinates any region R_i for which $Q(R_i)=\text{false}$
 \Rightarrow 비분할이 불가능한 점에 대해 4개 영역으로 나눔
- When no further splitting is possible, merge **adjacent** region for which $Q(R_i \cup R_j)=\text{true}$
 \Rightarrow 가능한만큼 split하다가, split을 더 이상 못하면 merge.
 가능한만큼 merge하다가, 더 이상 못하면 stop
- Stop when no further merging is possible \leftarrow



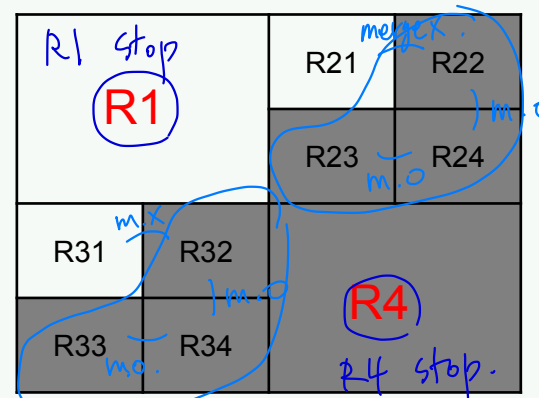
Exercise



Input
image

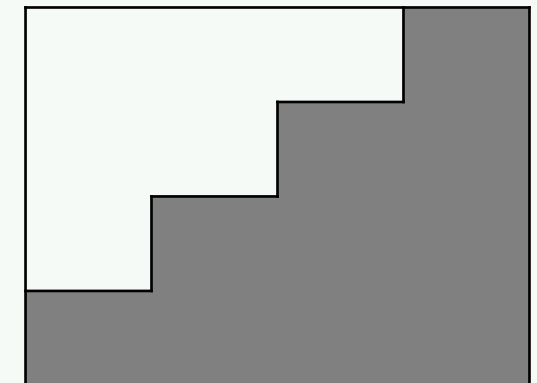


Split



Split

R1, R4는 stop이 라 거기서 split stop.



Merge



☆ 많이 사용 Clustering

(비교) 앞서 두 방식은 image의 spatial information을 기반으로 split, merge 하는 방식.

Clustering은 spatial info를 아예 무시.
pixel들이 가지는 property (feature)만 이용함.
그래서 spatial info를 재형하는 구조에 맞음.

- Task of grouping a set of objects → 이런 정보 이용.
- Objects in the same group (called a **cluster**) are more similar (in some sense or another) to each other
- Object of one cluster is different from an object of the another cluster
- Connectivity model, centroid model, distribution model, density model, graph based model, hard clustering, soft-clustering, ...



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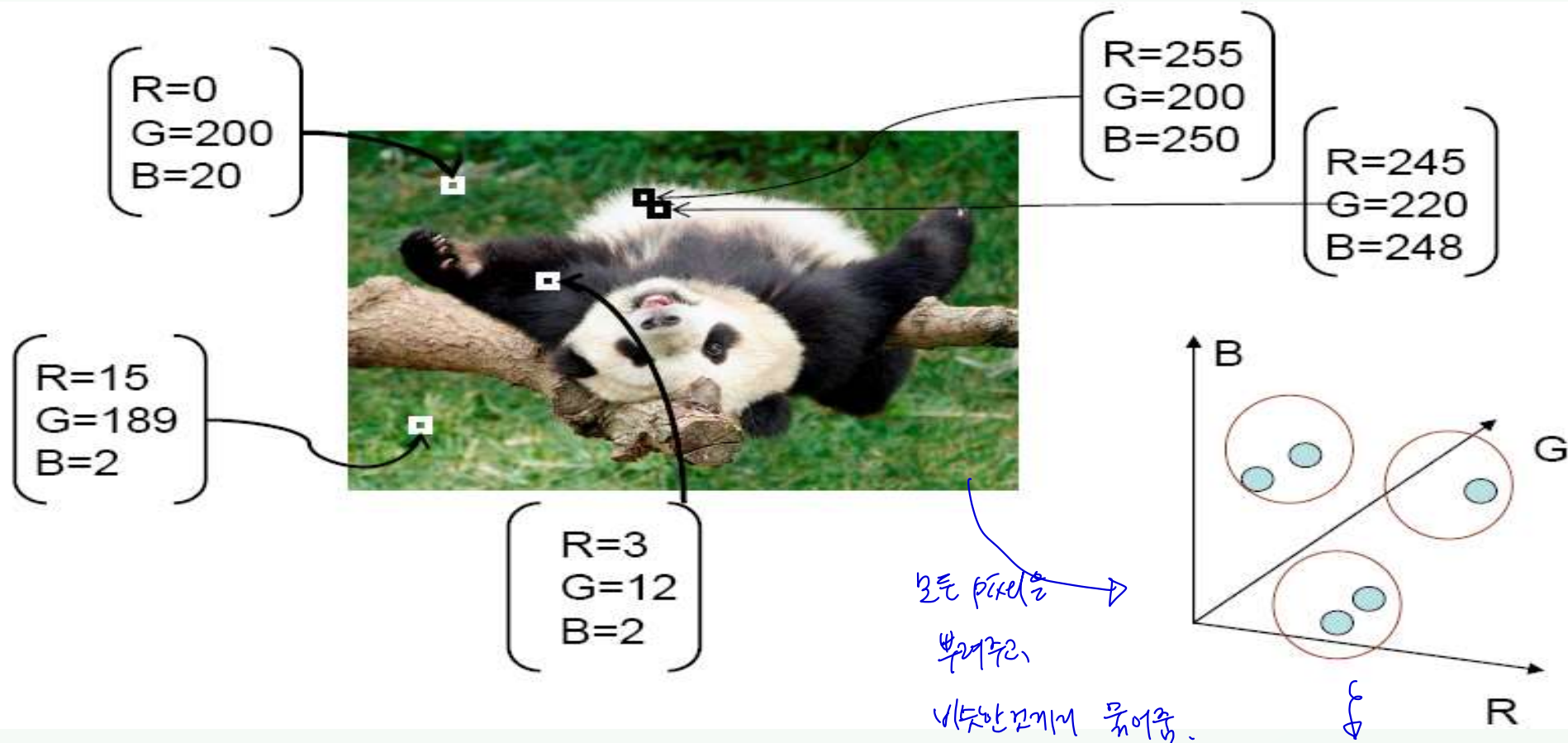


Clustering: feature space



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이러기 용감함.
→ 그림 각각의 pixel을 feature space로 뿌려줌 : plot.



한 cluster라 그 안의 pixel의 색은 다 다르기때, cluster는
cluster는 정의 때문

Centroid Model

Clustering의 가장 Simple 한 모델 -

→ 센터점 이용해서 중심점을 가지는 패턴을 찾음.



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- Computational time is short
- User have to decide the number of clusters before starting classifying data
- The concept of **centroid**
- One of the famous method: **K-means** Method



Clustering



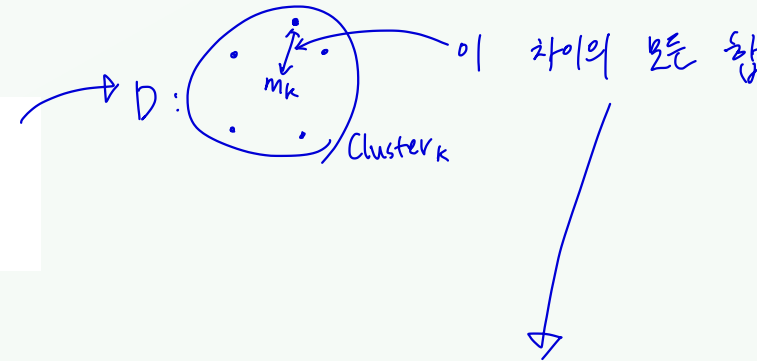
- There are K clusters C_1, \dots, C_K with means m_1, \dots, m_K .

- The least-squares error is defined as

같은 cluster 내의 feature
값을 비교해야 함.

다른
"
다른 cluster와 비교하는 기준

$$D = \sum_{k=1}^K \sum_{x_i \in C_k} \|x_i - m_k\|^2.$$



- Out of all possible partitions into K clusters, choose the one that minimizes D.



K-means Clustering

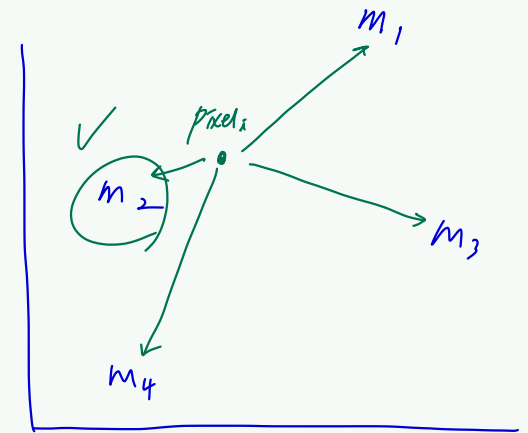


Alg

color space의 dimension은 255

Form K-means clusters from a set of n-dimensional vectors

1. Set ic (iteration count) to 1
2. Choose randomly a set of K means $m_1(1), \dots, m_K(1)$.
3. For each vector x_i compute $D(x_i, m_k(ic))$, $k=1, \dots, K$ and assign x_i to the cluster C_j with nearest mean.
4. Increment ic by 1, update the means to get $m_1(ic), \dots, m_K(ic)$.
→ 모든 pixel 수를 정하면, 모든 mean을 업데이트 함.
5. Repeat steps 3 and 4 until $C_k(ic) = C_k(ic+1)$ for all k.



pixel_i 가 mean과 가장 가까운 cluster에 assign.

47:30



Partitional Clustering

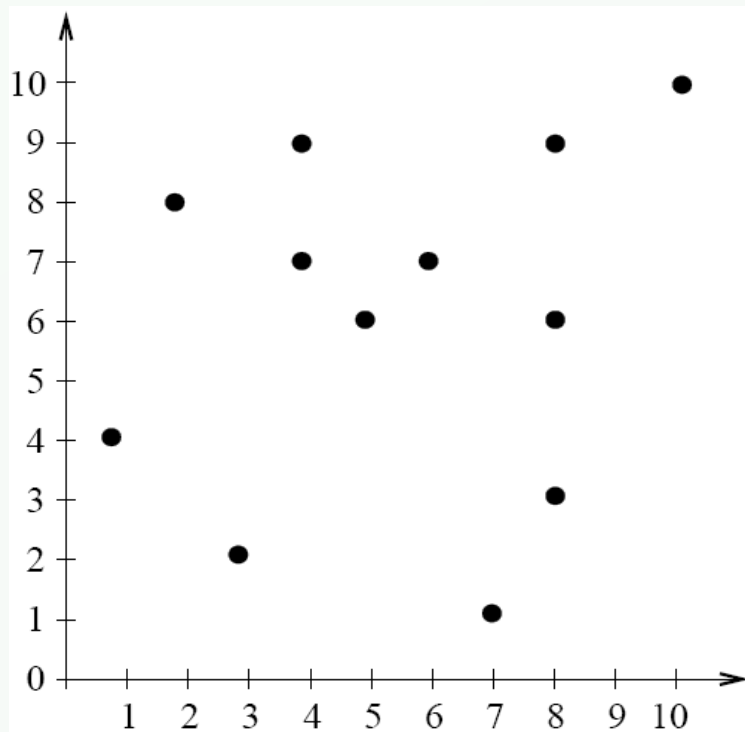
Clustering = k means Clu = Partitional Clu.

2/18/21

Apply the K-means algorithm on the following input: 12/11

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Select an initial clusters (k = 3)



Random
initial
guess

Interaction count

$R_1 = \begin{bmatrix} 1 & 6 \end{bmatrix}$

$R_2 = \begin{bmatrix} 9 & 7 \end{bmatrix}$

$R_3 = \begin{bmatrix} 4 & 3 \end{bmatrix}$



Partitional Clustering

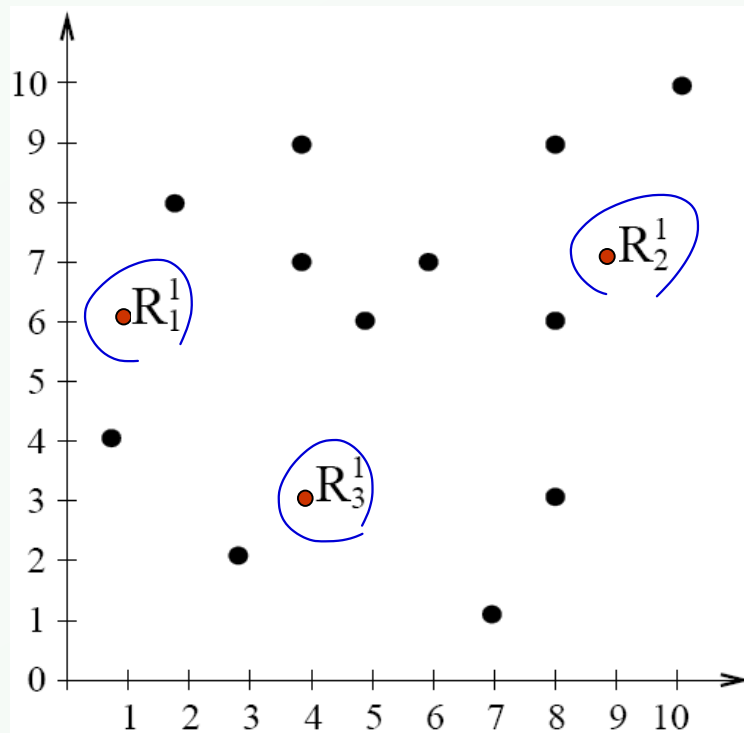


24/02

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Plot these clusters ($k = 3$)



$$R_1^1 = \begin{bmatrix} 1 & 6 \end{bmatrix}$$

$$R_2^1 = \begin{bmatrix} 9 & 7 \end{bmatrix}$$

$$R_3^1 = \begin{bmatrix} 4 & 3 \end{bmatrix}$$



Partitional Clustering

2/28/27

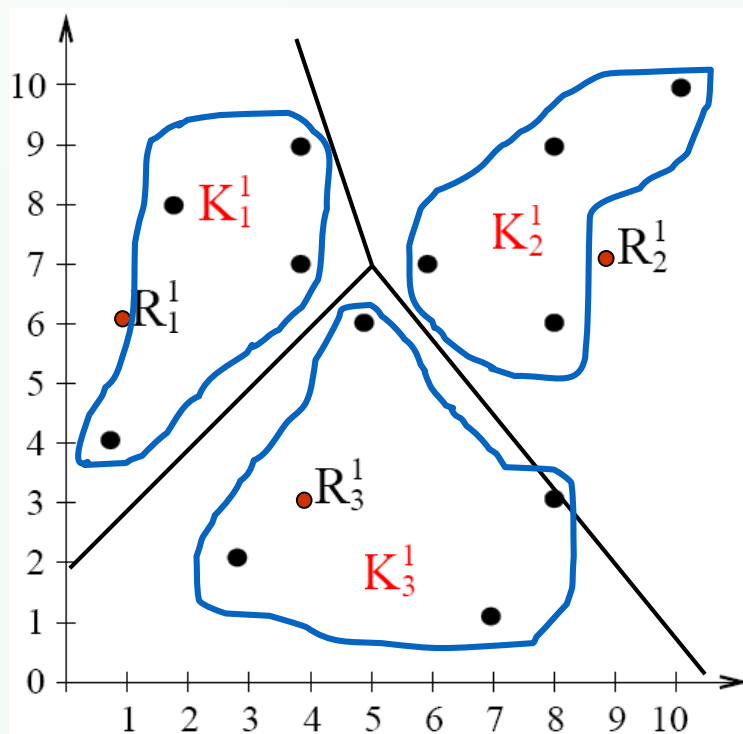


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Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Group vectors around the cluster entries and build clusters



$$R_1^1 = \begin{bmatrix} 1 & 6 \end{bmatrix}$$

$$R_2^1 = \begin{bmatrix} 9 & 7 \end{bmatrix}$$

$$R_3^1 = \begin{bmatrix} 4 & 3 \end{bmatrix}$$

$$K_1^1 = \begin{bmatrix} 4 & 7 & 4 & 9 & 1 & 4 & 2 & 8 \end{bmatrix}$$

$$K_2^1 = \begin{bmatrix} 6 & 7 & 8 & 6 & 8 & 9 & 10 & 10 \end{bmatrix}$$

$$K_3^1 = \begin{bmatrix} 8 & 3 & 7 & 1 & 3 & 2 & 5 & 6 \end{bmatrix}$$



Partitional Clustering

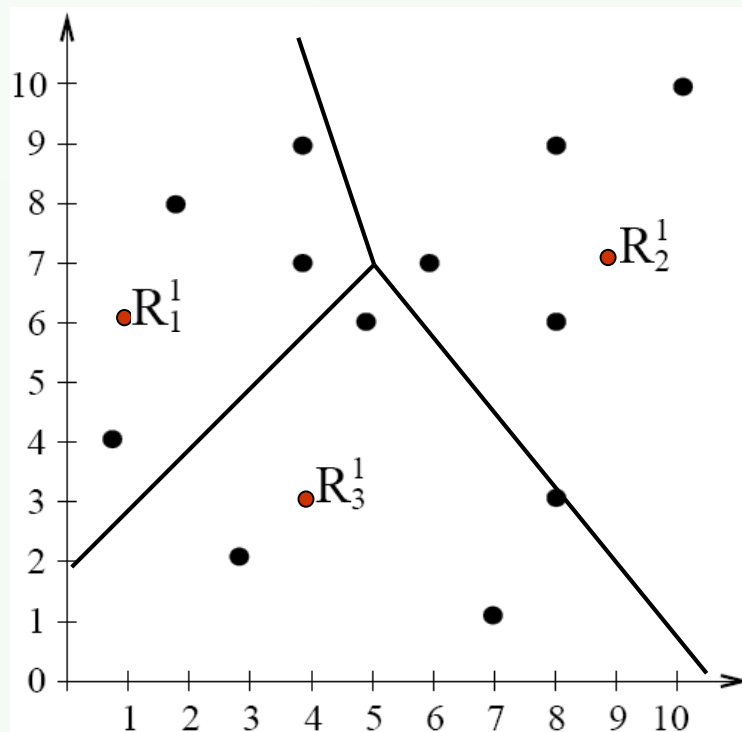


2/27/20

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Calculate centroids for each cluster and
Use these centroids as the new cluster



$$R_1^1 = \begin{bmatrix} 1 & 6 \end{bmatrix}$$

$$R_2^1 = \begin{bmatrix} 9 & 7 \end{bmatrix}$$

$$R_3^1 = \begin{bmatrix} 4 & 3 \end{bmatrix}$$

$$\begin{array}{l} K_1^1 = \begin{bmatrix} 4 & 7 \end{bmatrix} \begin{bmatrix} 4 & 9 \end{bmatrix} \begin{bmatrix} 1 & 4 \end{bmatrix} \begin{bmatrix} 2 & 8 \end{bmatrix} \\ K_2^1 = \begin{bmatrix} 6 & 7 \end{bmatrix} \begin{bmatrix} 8 & 6 \end{bmatrix} \begin{bmatrix} 8 & 9 \end{bmatrix} \begin{bmatrix} 10 & 10 \end{bmatrix} \\ K_3^1 = \begin{bmatrix} 8 & 3 \end{bmatrix} \begin{bmatrix} 7 & 1 \end{bmatrix} \begin{bmatrix} 3 & 2 \end{bmatrix} \begin{bmatrix} 5 & 6 \end{bmatrix} \end{array}$$

Centroids

$$= \begin{bmatrix} 2.75 & 7 \end{bmatrix}$$

$$= \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$= \begin{bmatrix} 5.75 & 3 \end{bmatrix}$$

Distortion = 8.67



Partitional Clustering

9

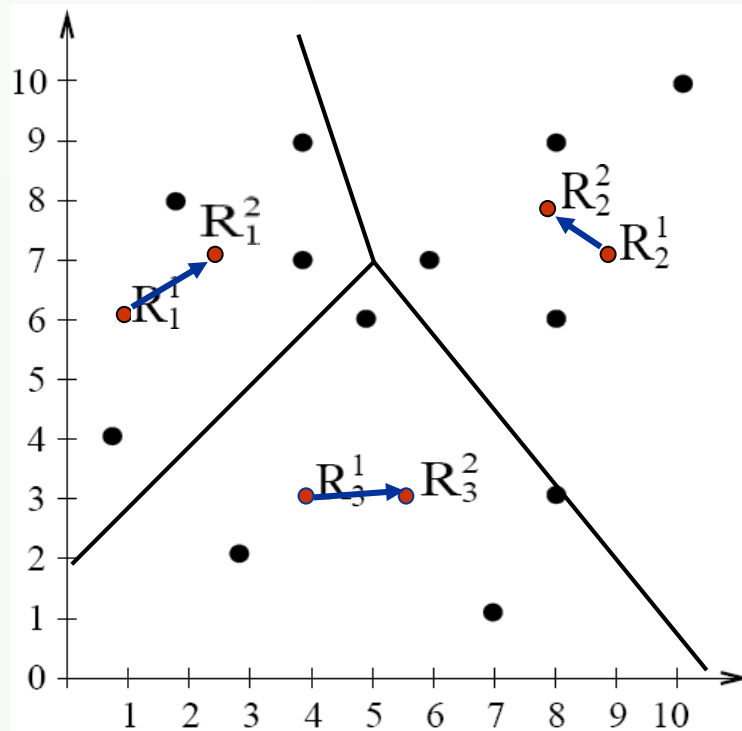


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Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Update the Plot and clustering



$$R_1^2 = \begin{bmatrix} 2.75 & 7 \end{bmatrix}$$

$$R_2^2 = \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$R_3^2 = \begin{bmatrix} 5.75 & 3 \end{bmatrix}$$



Partitional Clustering

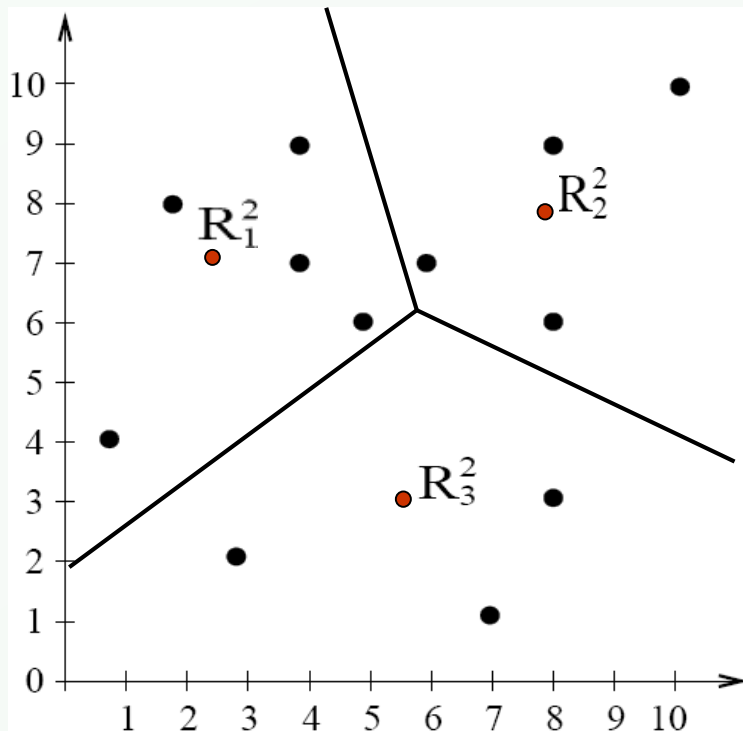


6

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Update the Plot and clustering



$$R_1^2 = \begin{bmatrix} 2.75 & 7 \end{bmatrix}$$

$$R_2^2 = \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$R_3^2 = \begin{bmatrix} 5.75 & 3 \end{bmatrix}$$



Partitional Clustering

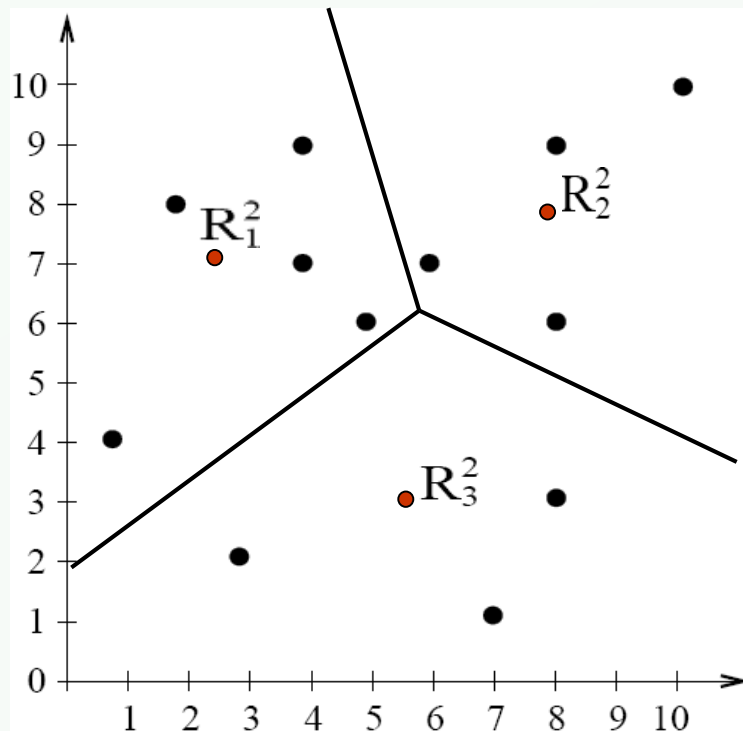


①

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Update the Plot and clustering



$$R_1^2 = \boxed{2.75 \ 7}$$

$$R_2^2 = \boxed{8 \ 8}$$

$$R_3^2 = \boxed{5.75 \ 3}$$

$$K_1^2 = \boxed{4 \ 7} \boxed{4 \ 9} \boxed{1 \ 4} \boxed{2 \ 8} \boxed{5 \ 6}$$

$$K_2^2 = \boxed{6 \ 7} \boxed{8 \ 6} \boxed{8 \ 9} \boxed{10 \ 10}$$

$$K_3^2 = \boxed{8 \ 3} \boxed{7 \ 1} \boxed{3 \ 2}$$

$$\underline{\text{Distortion} = 5.34}$$



Partitional Clustering

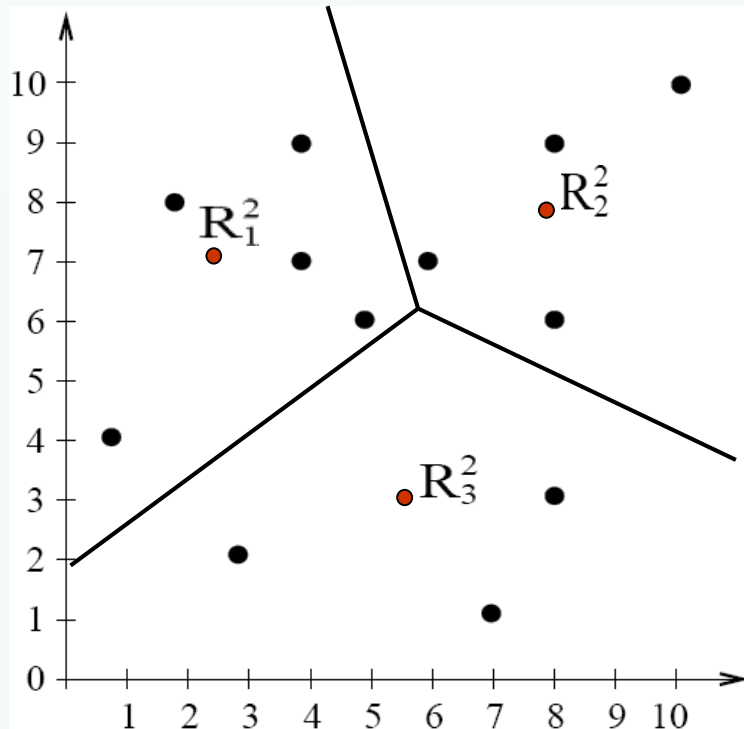


8

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Calculate the new centroids and use as cluster



$$R_1^3 = \begin{bmatrix} 3.2 & 6.8 \end{bmatrix}$$

$$R_2^3 = \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$R_3^3 = \begin{bmatrix} 6 & 2 \end{bmatrix}$$

$$K_1^2 = \begin{bmatrix} 4 & 7 \end{bmatrix} \begin{bmatrix} 4 & 9 \end{bmatrix} \begin{bmatrix} 1 & 4 \end{bmatrix} \begin{bmatrix} 2 & 8 \end{bmatrix} \begin{bmatrix} 5 & 6 \end{bmatrix}$$

$$K_2^2 = \begin{bmatrix} 6 & 7 \end{bmatrix} \begin{bmatrix} 8 & 6 \end{bmatrix} \begin{bmatrix} 8 & 9 \end{bmatrix} \begin{bmatrix} 10 & 10 \end{bmatrix}$$

$$K_3^2 = \begin{bmatrix} 8 & 3 \end{bmatrix} \begin{bmatrix} 7 & 1 \end{bmatrix} \begin{bmatrix} 3 & 2 \end{bmatrix}$$



Partitional Clustering

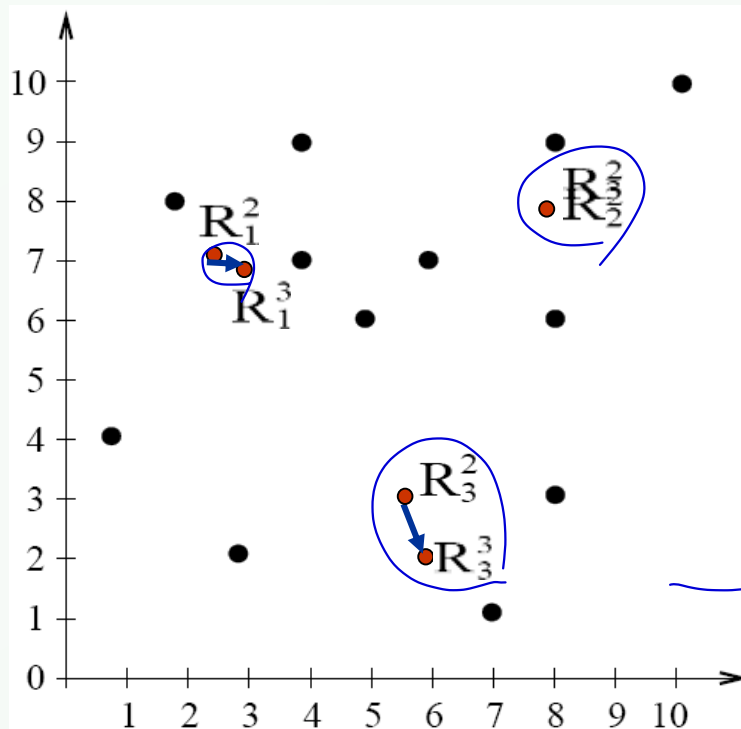


9

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Update the Plot



$$R_1^3 = \begin{bmatrix} 3.2 & 6.8 \end{bmatrix}$$

$$R_2^3 = \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$R_3^3 = \begin{bmatrix} 6 & 2 \end{bmatrix}$$

$$K_1^2 = \begin{bmatrix} 4 & 7 \end{bmatrix} \begin{bmatrix} 4 & 9 \end{bmatrix} \begin{bmatrix} 1 & 4 \end{bmatrix} \begin{bmatrix} 2 & 8 \end{bmatrix} \begin{bmatrix} 5 & 6 \end{bmatrix}$$

$$K_2^2 = \begin{bmatrix} 6 & 7 \end{bmatrix} \begin{bmatrix} 8 & 6 \end{bmatrix} \begin{bmatrix} 8 & 9 \end{bmatrix} \begin{bmatrix} 10 & 10 \end{bmatrix}$$

$$K_3^2 = \begin{bmatrix} 8 & 3 \end{bmatrix} \begin{bmatrix} 7 & 1 \end{bmatrix} \begin{bmatrix} 3 & 2 \end{bmatrix}$$

처음에 비해 움직이는 폭이 줄음
== 수렴했음



Partitional Clustering

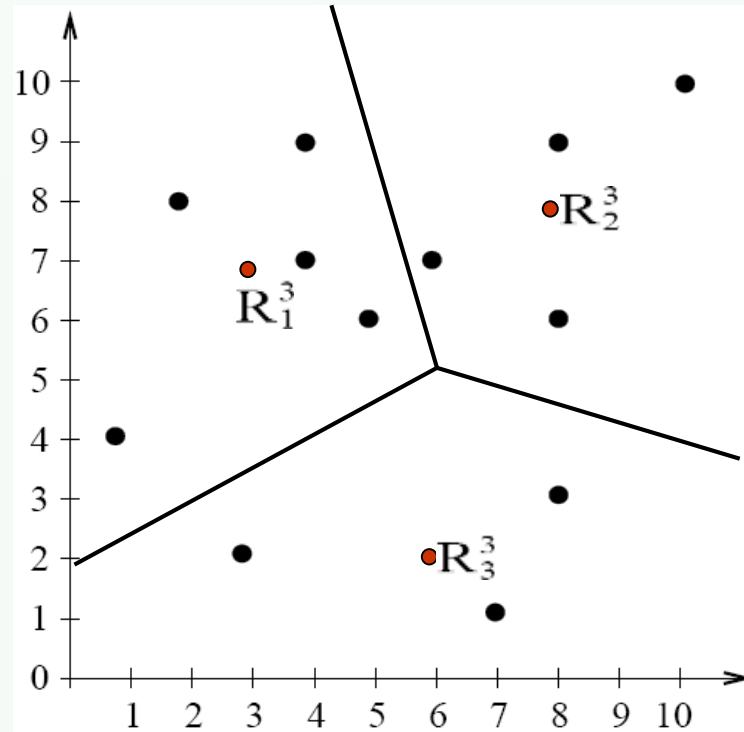


(10)

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Update the Plot



$$R_1^3 = \begin{bmatrix} 3.2 & 6.8 \end{bmatrix}$$

$$R_2^3 = \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$R_3^3 = \begin{bmatrix} 6 & 2 \end{bmatrix}$$

$$K_1^2 = \begin{bmatrix} 4 & 7 \end{bmatrix} \begin{bmatrix} 4 & 9 \end{bmatrix} \begin{bmatrix} 1 & 4 \end{bmatrix} \begin{bmatrix} 2 & 8 \end{bmatrix} \begin{bmatrix} 5 & 6 \end{bmatrix}$$

$$K_2^2 = \begin{bmatrix} 6 & 7 \end{bmatrix} \begin{bmatrix} 8 & 6 \end{bmatrix} \begin{bmatrix} 8 & 9 \end{bmatrix} \begin{bmatrix} 10 & 10 \end{bmatrix}$$

$$K_3^2 = \begin{bmatrix} 8 & 3 \end{bmatrix} \begin{bmatrix} 7 & 1 \end{bmatrix} \begin{bmatrix} 3 & 2 \end{bmatrix}$$



Partitional Clustering

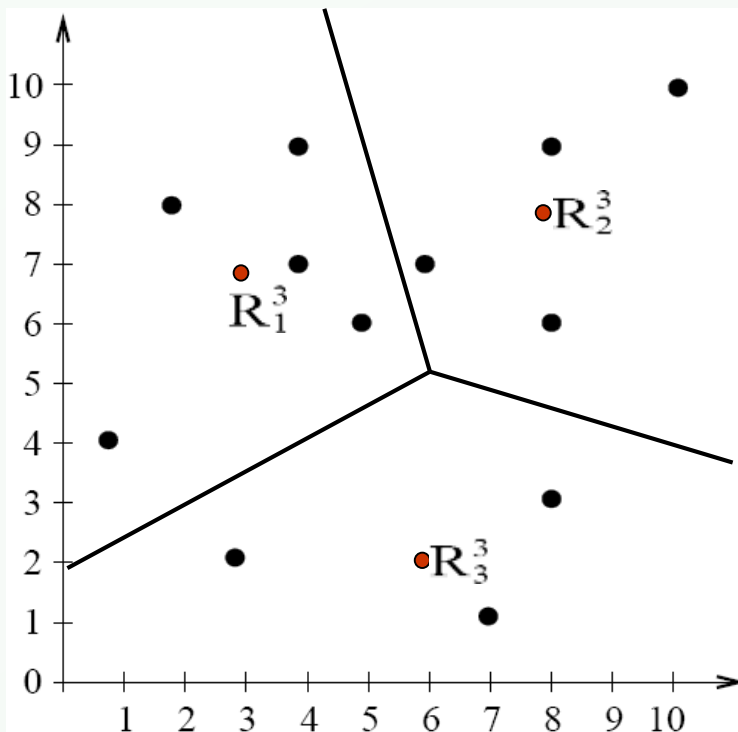


④

Apply the K-means algorithm on the following input:

(4,7), (6,7), (8,6), (8,9), (4,9), (10,10), (1,4), (8,3), (7,1), (3,2), (2,8), (5,6)

Clusters remain the same (and so do the centroids), so we finish



$$R_1^3 = \begin{bmatrix} 3.2 & 6.8 \end{bmatrix}$$

$$R_2^3 = \begin{bmatrix} 8 & 8 \end{bmatrix}$$

$$R_3^3 = \begin{bmatrix} 6 & 2 \end{bmatrix}$$

$$K_1^2 = \begin{bmatrix} 4 & 7 \end{bmatrix} \begin{bmatrix} 4 & 9 \end{bmatrix} \begin{bmatrix} 1 & 4 \end{bmatrix} \begin{bmatrix} 2 & 8 \end{bmatrix} \begin{bmatrix} 5 & 6 \end{bmatrix}$$

$$K_2^2 = \begin{bmatrix} 6 & 7 \end{bmatrix} \begin{bmatrix} 8 & 6 \end{bmatrix} \begin{bmatrix} 8 & 9 \end{bmatrix} \begin{bmatrix} 10 & 10 \end{bmatrix}$$

$$K_3^2 = \begin{bmatrix} 8 & 3 \end{bmatrix} \begin{bmatrix} 7 & 1 \end{bmatrix} \begin{bmatrix} 3 & 2 \end{bmatrix}$$

Distortion = 4.97



Exercise

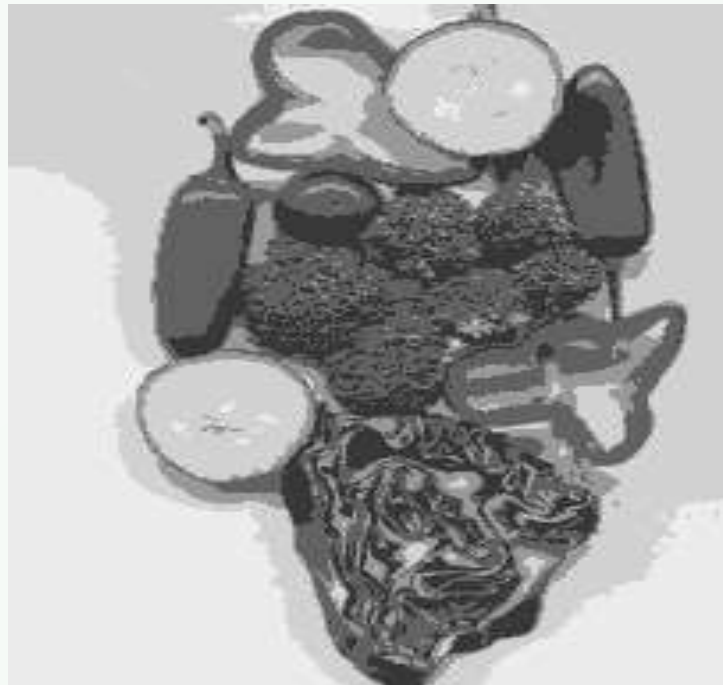


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(origin) Image

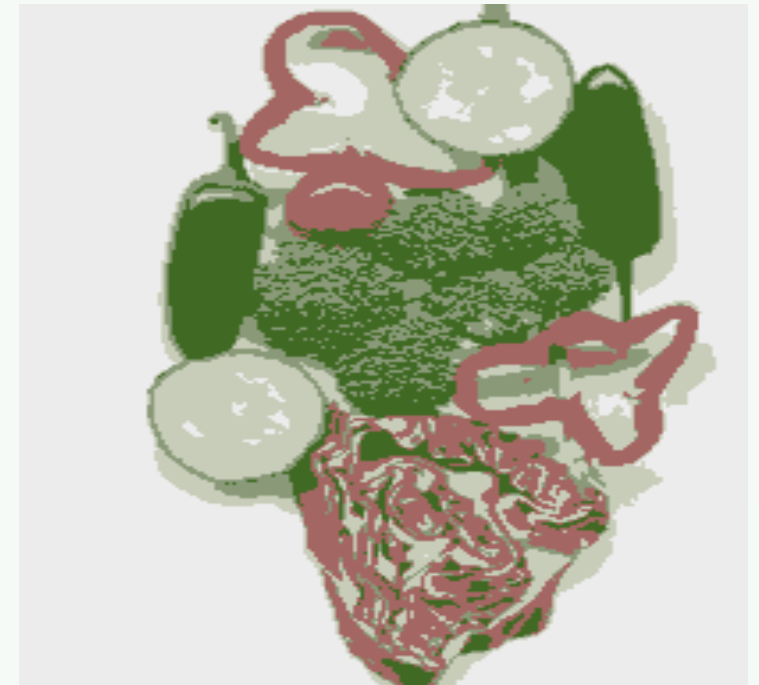


Clusters on intensity



더 잘
←

Clusters on color



CCU

Slides by D.A. Forsyth




K-Means Example 1



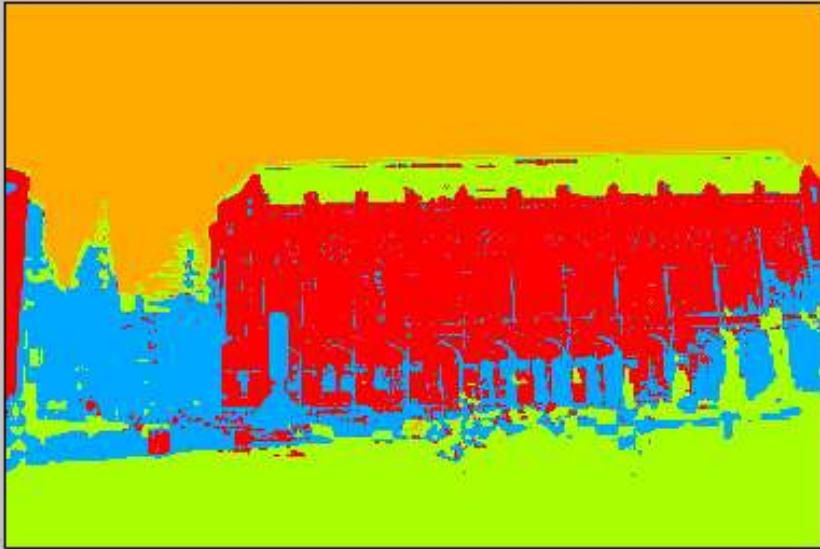
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1. Select an image: 2. Select a processor: 3. Click

Options:
Init Method



640*480 (590,68): RGB(158,206,229)



Process done !

- ◆ Quick help: select an Image and a Processor, click the Process button.
- ◆ Option:



K-Means Example 2



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1. Select an image: 2. Select a processor: 3. Click

Options:
Init Method

Process done !

640*480 (636,95): RGB(102,130,151)

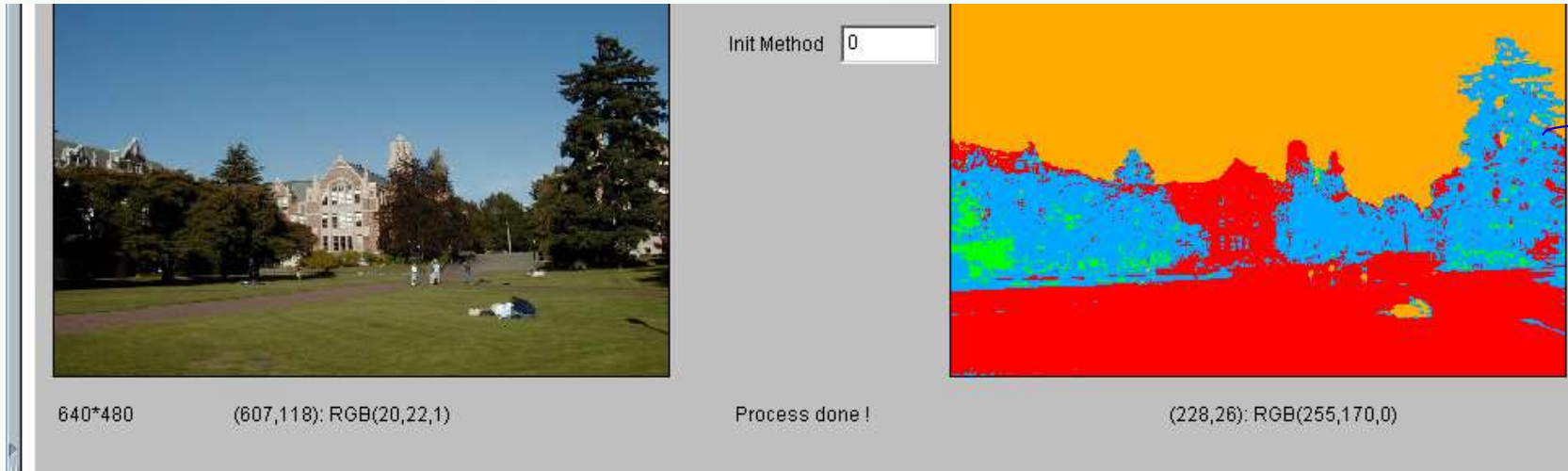
(590,209): RGB(0,46,255)



K-Means Example 3



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- ◆ Quick help: **select an Image and a Processor, click the Process button.**
- ◆ Option:
 - Init Method: 0-Random, 1-Linear, 2-CUBE, 3-Statistics, 4-Possibility
- ◆ Processors:
 - *KMCluster*. Iterative K-Means Cluster

[comments to yi@cs.washington.edu]

Last Modified: January 1, 1970 GMT



K-Means Segmentation



Agglomerative clustering → ^{재미로.} 하루 공부해보기,
↳ 관계를 할 때
이유까지 할 필요 X.

