



An Extended Behavioral Type System for Memory-Leak Freedom

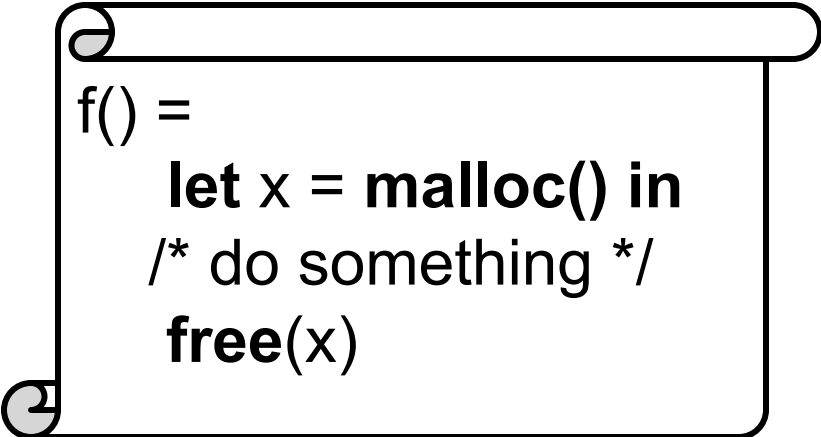
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Introduction

- Memory leak, forgetting to deallocate an allocated memory cell, is a serious problem
 - Decreasing the performance of computer
 - Unexpected termination of an application
 - System crash
- Verification of *memory-leak freedom* is important

Partial memory-leak freedom

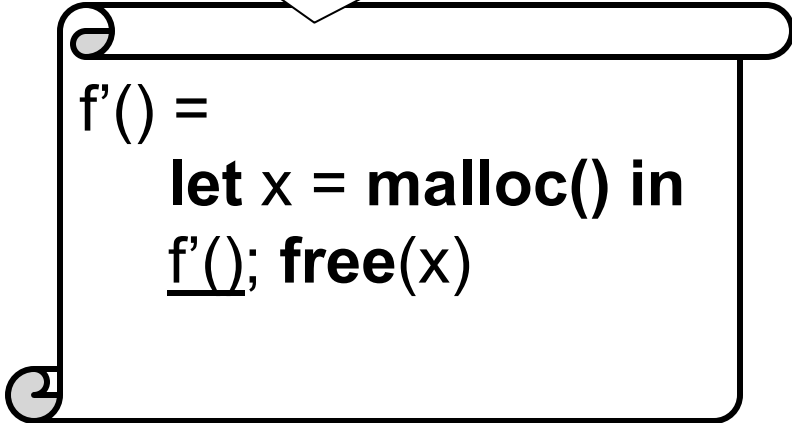
- All the allocated memory cells are eventually deallocated *if a program terminates*



A diagram of a function `f()` represented as a scroll. The scroll has a tab at the top and a handle at the bottom left. The code inside the scroll is:

```
f() =  
  let x = malloc() in  
  /* do something */  
  free(x)
```

Consumes unbounded
number of memory cells

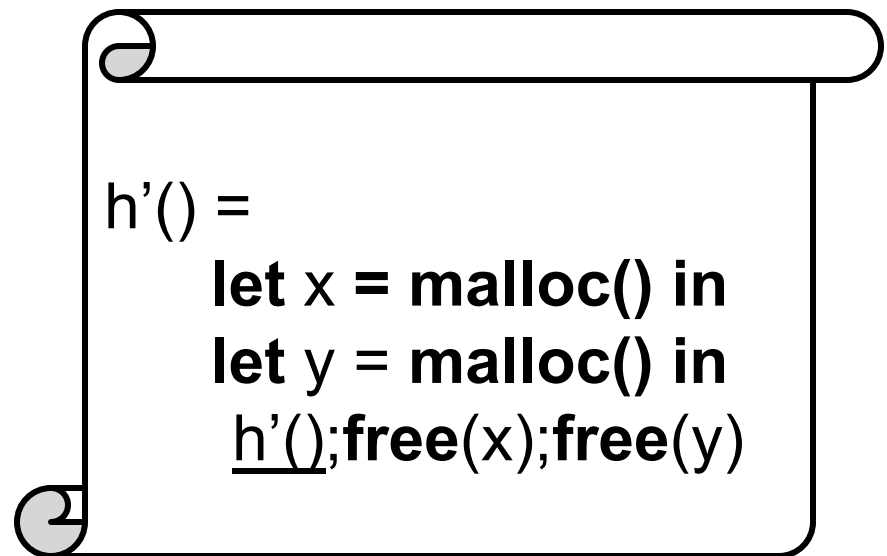
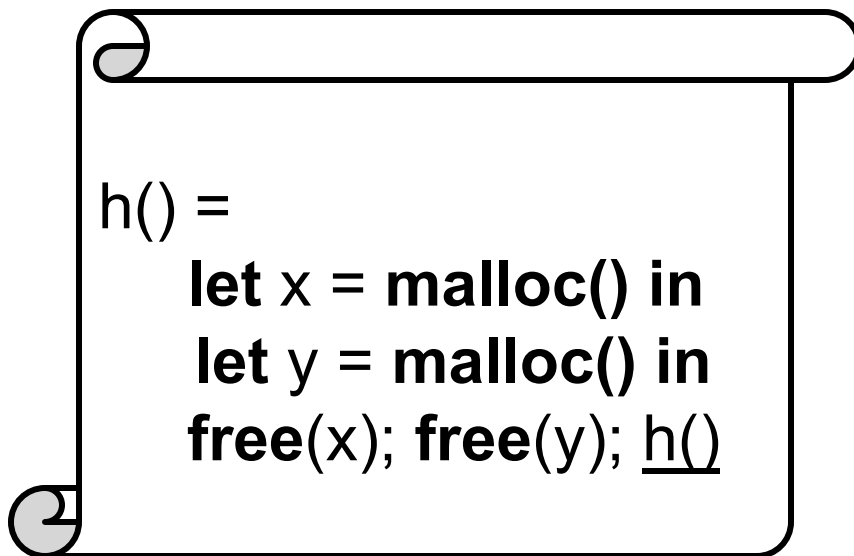


A diagram of a function `f'()` represented as a scroll. The scroll has a tab at the top and a handle at the bottom left. The code inside the scroll is:

```
f'() =  
  let x = malloc() in  
  f'(); free(x)
```

Total memory-leak freedom

- A program consumes bounded number of memory cells *even when it does not terminate*



Both are partially memory-leak free.

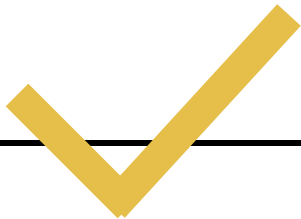
h() is totally memory-leak free, but h'() is not.

Goal

- Verification of total memory-leak freedom
 - Important for nonterminating software such as Web servers and OS

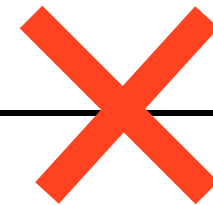
$h() =$

**let $x = \text{malloc}()$ in
let $y = \text{malloc}()$ in
 $\text{free}(x); \text{free}(y); h()$**



$h'() =$

**let $x = \text{malloc}()$ in
let $y = \text{malloc}()$ in
 $h'()$; **$\text{free}(x); \text{free}(y)$****

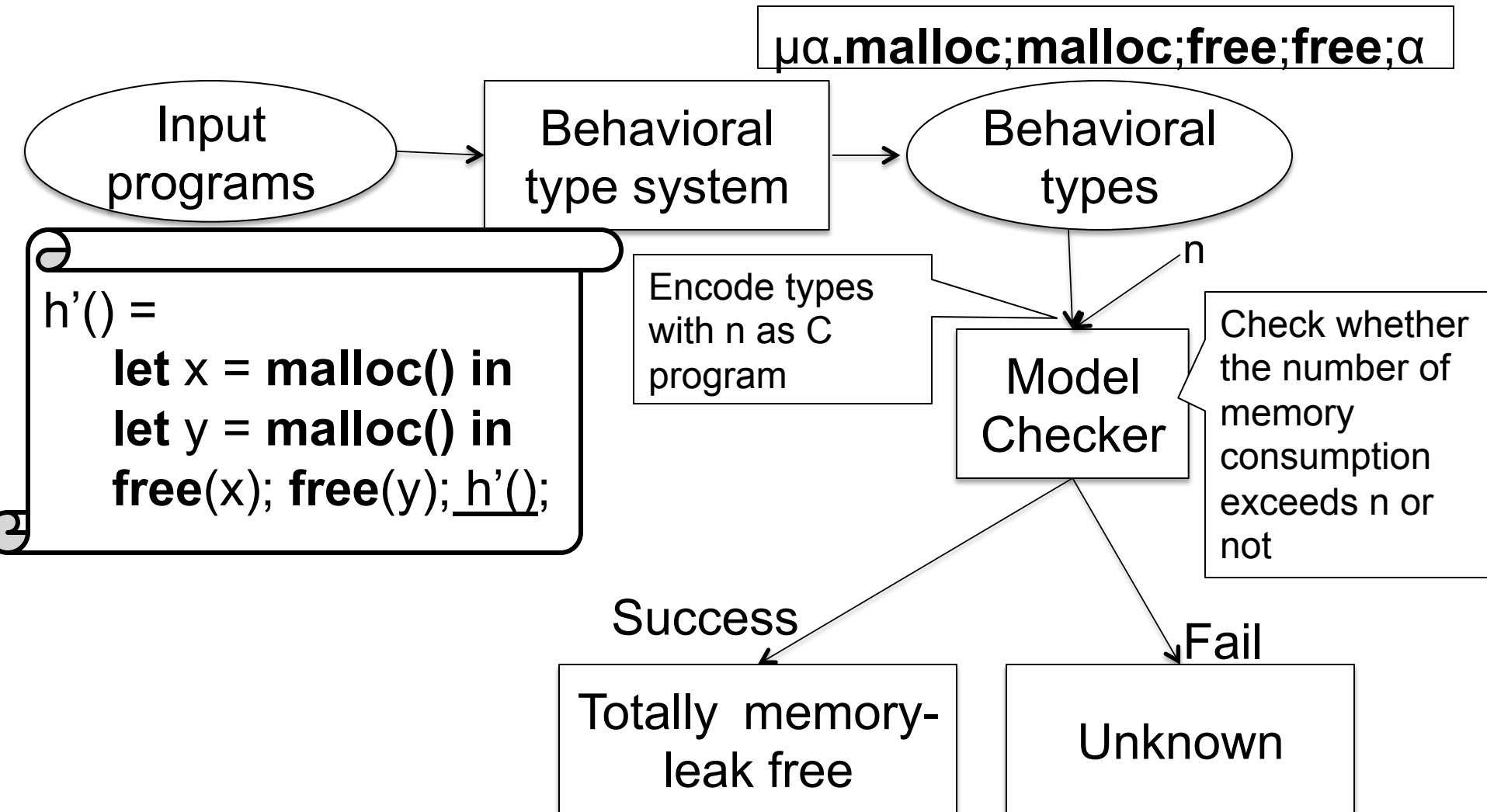


Previous work

[Tan&Suenaga&Igarashi PPL2015]

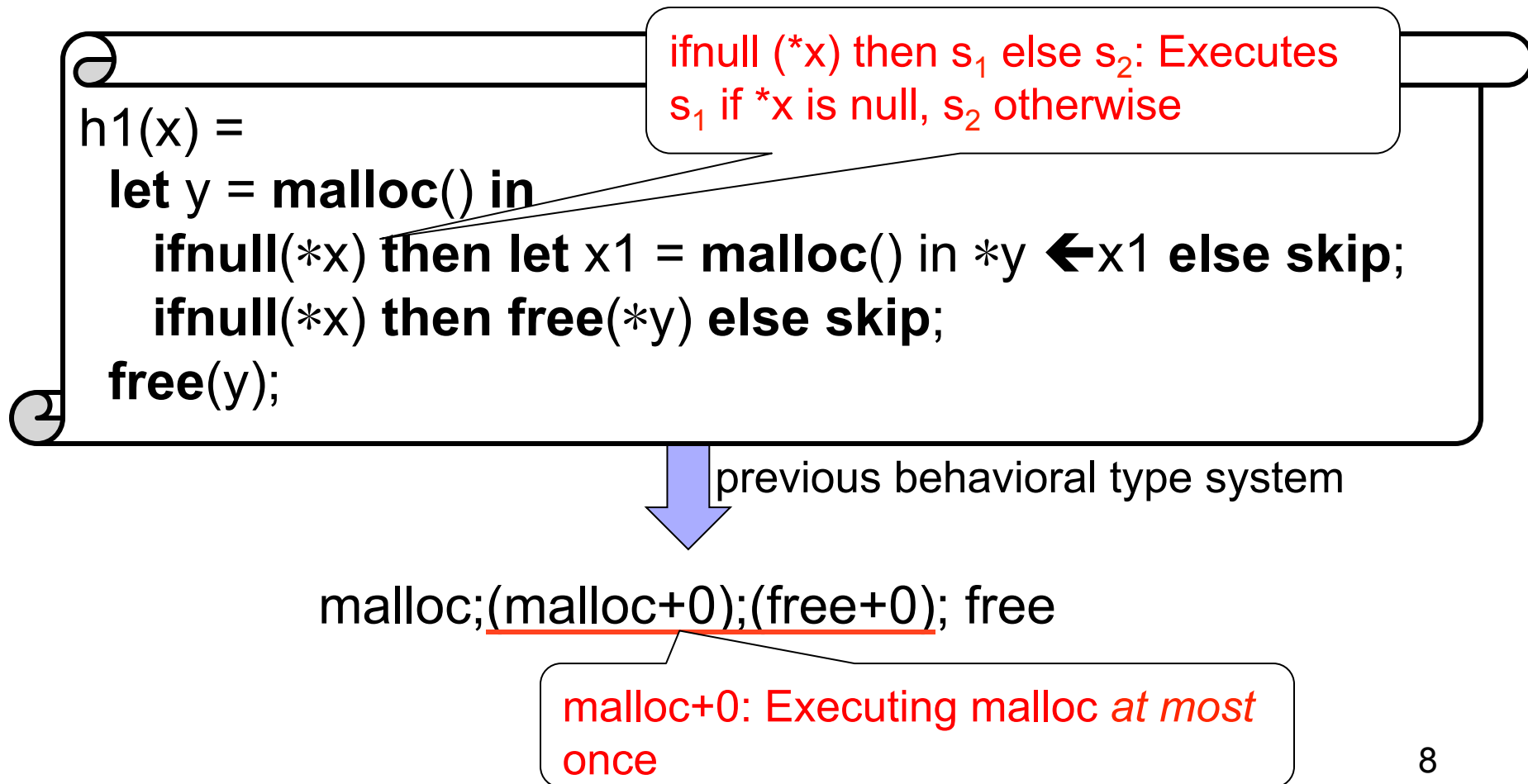
- *Behavioral type system*
 - Type system for abstracting the behavior of a program
 - Sequential processes are used as types
 - Types describe the number and the order of allocations, deallocations, and recursive calls
- Estimating an upper bound of memory cells consumed by a program based on an inferred type

Overview of previous work



Problem in previous work

Imprecise abstraction due to branches



Problem in previous work

Although function h1 is a memory-leak free program, we cannot conclude it from this type

`malloc;malloc;0;free`

`malloc;(malloc+0);(free+0); free`

This type loses information about if-guard part

Our solution

Introducing *path-sensitive behavioral types* to deal with branch statements

- $(*x)(P_1, P_2)$ means execution of P_1 or P_2 depending on $*x$ is null or not

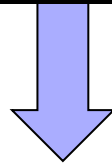
h1(x) =

let y = malloc() in

ifnull(*x) then let x1 = malloc() in *y \leftarrow x1 else skip;

ifnull(*x) then free(*y) else skip;

free(y);



path-sensitive behavioral type system

malloc; $(*x)(\text{malloc}, 0); (*x)(\text{free}, 0)$; free

Our solution

We can conclude h1 is a memory-leak free program from this type

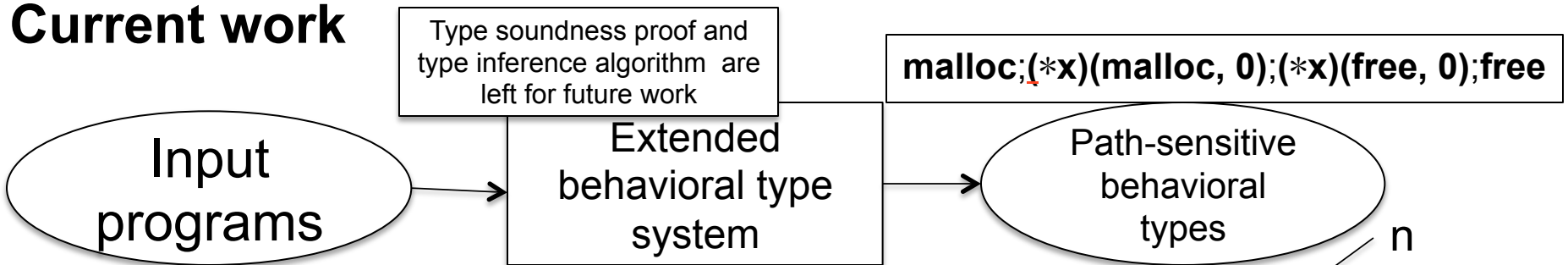
if $*x$ is a null pointer,
behaves like
malloc;malloc;free;free
otherwise like
malloc;0;0;free

malloc;(*x)(malloc, 0**);(*x)(**free, 0**);free**

Requires $*x$ not to change between two branches

Overview of current work

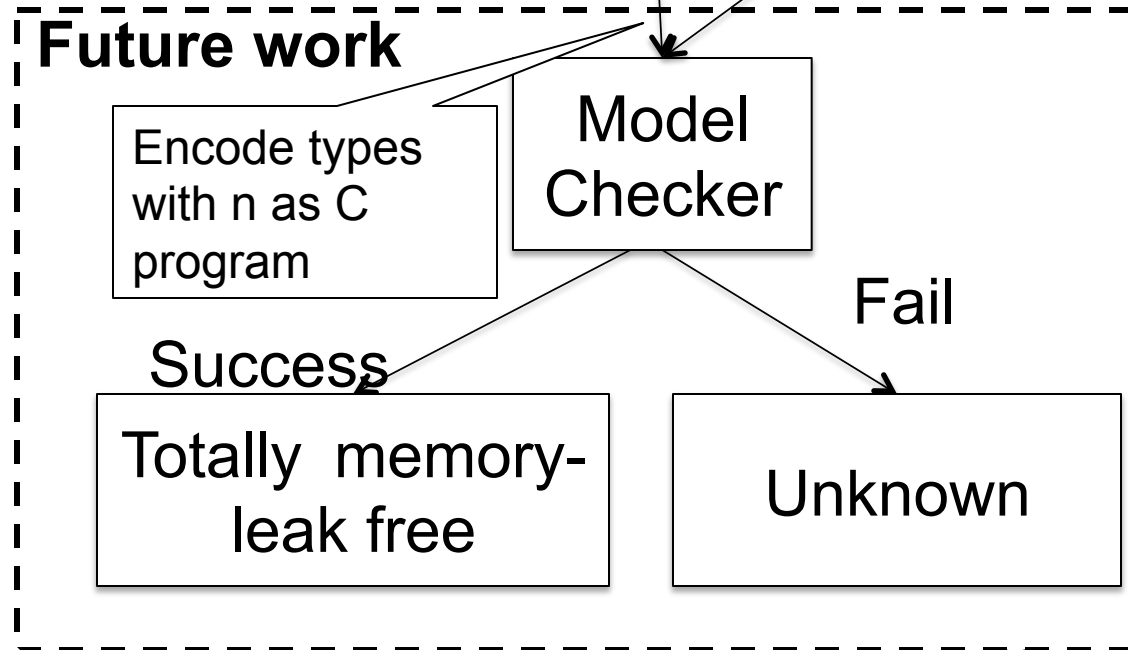
Current work



\mathcal{A}

```
h1(x) =  
let y = malloc() in  
  ifnull(*x) then  
    let x1 = malloc() in *y  $\leftarrow$  x1  
  else skip ;  
  ifnull(*x) then free(*y) else skip;  
free(y);
```

Future work





Outline

- Language
- Extended behavioral type system
- Overview of verification
- Related work
- Conclusion
- Future work

Language

x, y, z, \dots (variables) $\in \mathbf{Var}$

s (statements) $::= \mathbf{skip} \mid s_1; s_2 \mid *x \leftarrow y \mid f(\vec{x})$
| $\mathbf{let } x = y \mathbf{ in } s$
| $\mathbf{let } x = *y \mathbf{ in } s$
| $\mathbf{let } x = \mathbf{null} \mathbf{ in } s$
| $\mathbf{let } x = \mathbf{malloc}() \mathbf{ in } s$
| $\mathbf{free}(x) \mid \mathbf{const}(*x)s$
| $\mathbf{ifnull}(*x) \mathbf{ then } s_1 \mathbf{ else } s_2$

d (proc. defs.) $::= \{ f \rightarrow (x_1, \dots, x_n)s \}$

D (definitions) $::= \langle d_1 \cup \dots \cup d_n \rangle$

P (programs) $::= \langle D, s \rangle$

Outline

- Language
- Extended behavioral type system
 - Syntax of types
 - Type judgment
 - Typing rule for a program
 - $OK_n(P)$
- Overview of verification
- Related Work
- Conclusion
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Syntax of extended behavioral types

- P (behavioral types) ::=
- | **0** do-nothing
- | $P_1;P_2$ sequential execution of P_1 and P_2
- | **malloc** allocation of one memory cell
- | **free** deallocation
- | $(*x)(P_1, P_2)$ execution of P_1 or P_2 depends on $*x$
- | $\text{const}(*x)P$ execution of P under constantness $(*x)$
- | α type variable
- | $\mu\alpha.P$ recursion

Type judgment

$$\Theta; \Gamma \vdash s : P$$

- Under Θ and Γ , the extracted behavior of s is P
 - Θ (function type environment) $::= \{f_1:\psi_1, \dots, f_n:\psi_n\}$
 - Γ (variable type environment) $::= \{x_1, x_2, \dots, x_n\}$
 - ψ (dependent function type) $::= (\vec{x})P$

Example

$$\frac{\Theta; \Gamma, x \vdash s : P}{\Theta; \Gamma \vdash \text{let } x = \text{malloc}() \text{ in } s : \text{malloc}; P} \quad (\text{T-Malloc})$$

$$\frac{\Theta; \Gamma, x \vdash \text{let } x1 = \text{malloc}() \text{ in } *x \leftarrow x1 : \text{malloc}; 0 \quad \Theta; \Gamma \vdash \text{skip} : 0}{\Theta; \Gamma, x, y \vdash \text{ifnull}(*y) \text{ then } \text{let } x1 = \text{malloc}() \text{ in } *x \leftarrow x1 \text{ else skip} : (*y)(\text{malloc}, 0)}$$

$$\frac{\Theta; \Gamma, x \vdash s_1 : P_1 \quad \Theta; \Gamma, x \vdash s_2 : P_2}{\Theta; \Gamma, x \vdash \text{ifnull}(*x) \text{ then } s_1 \text{ else } s_2 : (*x)(P_1, P_2)} \quad (\text{T-IfNull})$$

Typing rule for a program

$$\frac{\vdash D : \Theta \quad \Theta; \emptyset \vdash s : P}{\vdash \langle D, s \rangle : P}$$

- P represents the behavioral type of main statement s
- In order to guarantee $\langle D, s \rangle$ is totally memory-leak free, we use the predicate $OK_n(P)$

$OK_n(P)$

σ represents a sequence of actions such as **malloc**, **free** and other actions

relation \rightarrow means P can perform actions σ and turn into P'

■ Definition:

$OK_n(P)$ holds, if $P \xrightarrow{\sigma} P'$ implies

$\#_{\text{malloc}}(\sigma) - \#_{\text{free}}(\sigma) \leq n$ where $\#_{\rho}(\sigma)$ is the number of ρ in σ .

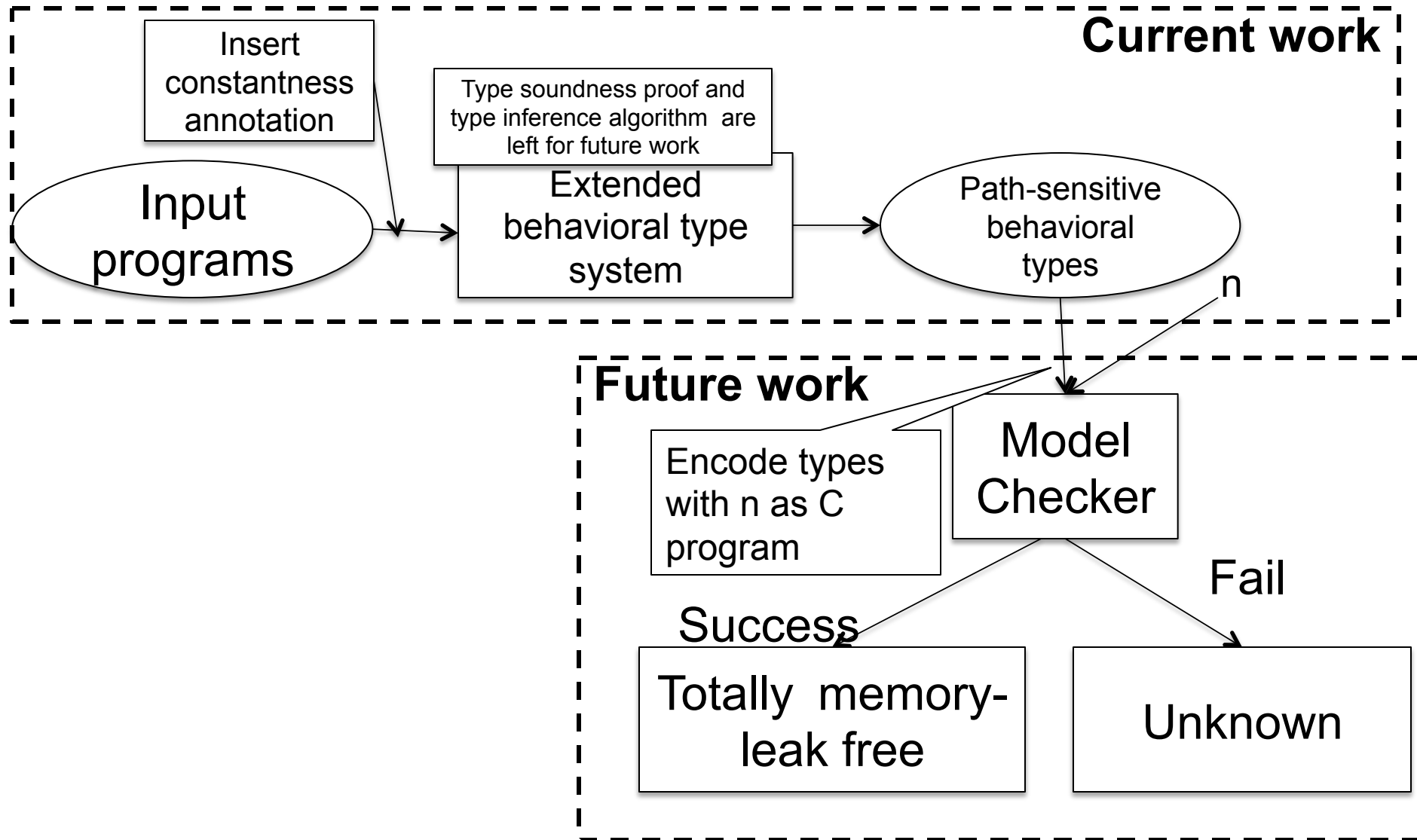
■ Intuitively, at every running step, the number of memory cells a program consumes cannot exceed the number of cells it requires.



Outline

- Language
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Overview of current work



overview of verification

```
let x = malloc() in
let y = malloc() in
  ifnull(*y) then let x1 = malloc() in *x ← x1 else skip;
  /* do-something but not change the value of *y */
  ifnull(*y) then free(*x) else skip
free(x); free(y)
```

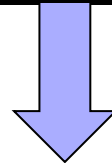
Manually
inserted
by a
programmer

```
let x = malloc() in
let y = malloc() in
  const(*y) /* inserted by a programmer */
  (
    ifnull(*y) then let x1 = malloc() in *x ← x1 else skip;
    /* do-something but not change the value of *y */
    ifnull(*y) then free(*x) else skip
  );
free(x); free(y)
```

Future work:
automated
insertion

Overview of verification

```
let x = malloc() in
let y = malloc() in
  const(*y)
  (
    ifnull(*y) then let x1 = malloc() in *x ← x1 else skip;
    /* do-something but not change the value of *y */
    ifnull(*y) then free(*x) else skip
  );
free(x); free(y)
```



Type inference of our type system

$P = \text{malloc}; \text{malloc}; \text{const}(*y)((*y)(\text{malloc}, 0); (*y)(\text{free}, 0)); \text{free}; \text{free}$

automatically abstracted by our current type system

Overview of verification

$P = \text{malloc}; \text{malloc}; \text{const}(*y)((*y)(\text{malloc}, 0); (*y)(\text{free}, 0)); \text{free}; \text{free}$

with n ↓ Encoding by C

Future work

```
int y;  
M(); M();  
y = randV();  
if(y) { M(); } else { ; }  
if(y) { F(); } else { ; }  
F(); F();
```

```
int M() {  
    n = n - 1;  
    assert(n >= 0);  
}
```

```
int randV() {  
    srand((unsigned)time(NULL));  
    return rand()%2; }
```

```
void F() {  
    n = n + 1 ;  
}
```

Model
Checker

Success

Fail

$OK_n(P)$
holds

Unknown



Outline

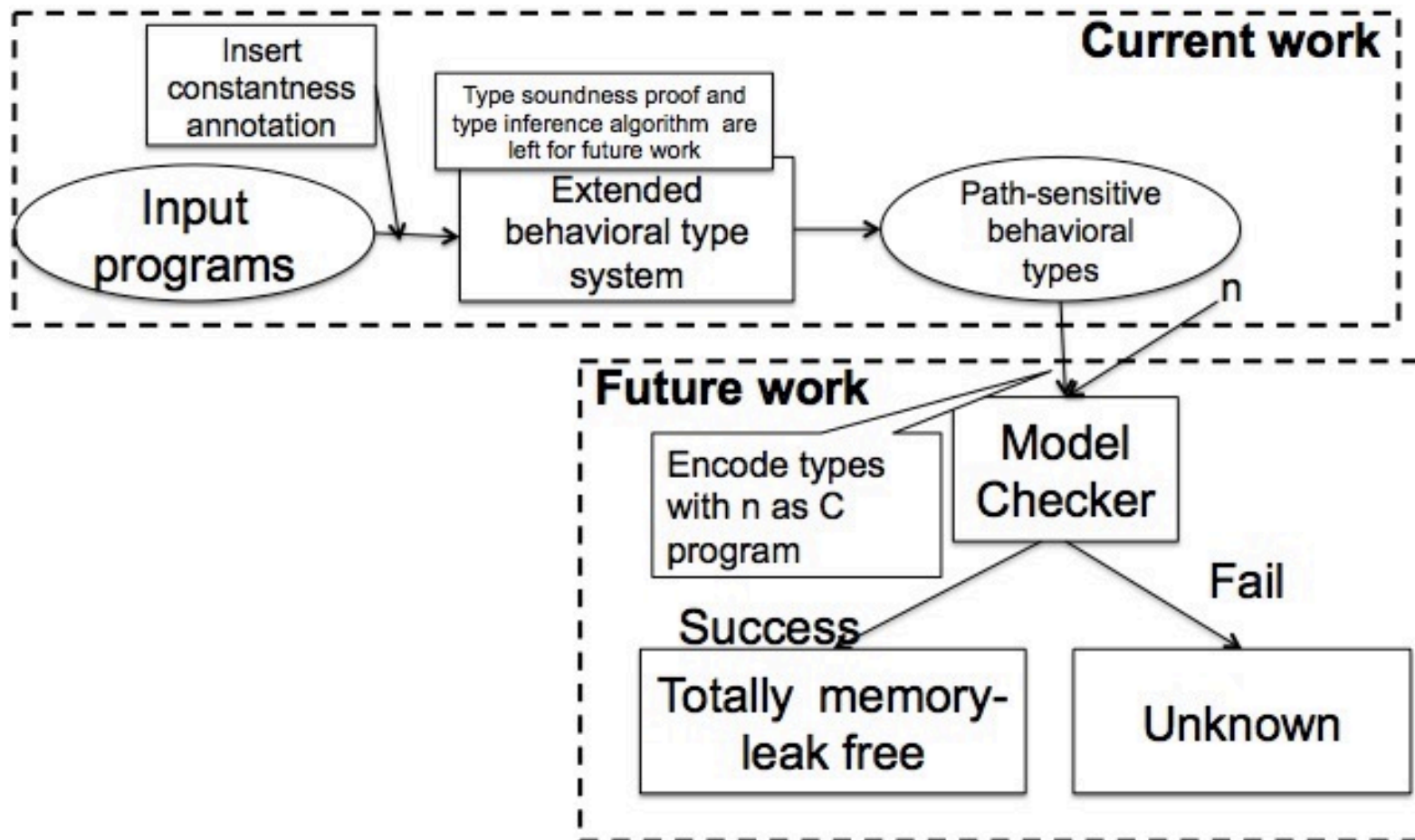
- Language
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- Overview of verification
- **Related work**
- Conclusion
- Future work

Related work

- Behavioral type system are widely used for
 - Static verification of resource-usage [Igarashi&Kobayashi ACMTPLS'05],etc
 - Static verification of deadlock-freedom [Kobayashi Acta inf'05]
- Static memory-leak freedom verification [Heine&Lam PLDI'03], [Suenaga&Kobayashi APLAS'09], etc
 - Partial memory-leak freedom
 - Lack of illegal accesses
- Our previous behavioral type system[Tan&Suenaga&Igarashi PPL2015]
 - Total memory-leak freedom

Conclusion

- Path-sensitive behavioral type: describes more information of the behavior of a program



Future work

- Type inference algorithm for our extended type system
- Experiments
- Automated insertion of constantness annotation

