

CSE 5524 HW 3 Utkarsh Pratap Singh Jadon

Question 1

Import necessary libraries

```
In [526... import matplotlib.pyplot as plt
import matplotlib.image as mpimg
from skimage.color import rgb2gray
import cv2 as cv
import numpy as np
import math
from PIL import Image
import glob
import os
from os import listdir
from os.path import join, isfile
from skimage import morphology
from skimage import measure, color
```

Read and resize input RGB image

```
In [481... image1 = Image.open('Q1_Input Image.png') #Creates image object of original image

# R = (Mr * 2^N) + 1
# C = (Mc * 2^N) + 1

# Here, N=3, and by taking Mr=80 & Mc=50, we get R=641 & C=401

inputImageResized = image1.resize((641, 401)) #Resizes original input RGB image
inputImageResized.save('Input RGB Image Resized.png') #Saves resized input RGB image

plt.imshow(inputImageResized) #Displays resized input RGB image
print(inputImageResized.size) #Prints size of resized input RGB image
```

(641, 401)



Convert resized RGB image to single channel grayscale image

```
In [482... image2 = cv.imread('Input RGB Image Resized.png') #Creates image object of resized image
inputImageResizedGray = cv.cvtColor(image2, cv.COLOR_BGR2GRAY) #Convert resized image to grayscale
plt.imshow(inputImageResizedGray, cmap='gray') #Displays resized grayscale image

# print(image2.shape) #Prints shape of resized RGB image
print(inputImageResizedGray.shape) #Print shape of resized single channel grayscale image
```

```
(401, 641)
```



Create two separable Gaussian mask kernels: Wm and Wn

```
In [483... #G(m,n) = w(m) * w(n) where w = [0.25-0.5*a 0.25 a 0.25 0.25-0.5a]
#Here a=0.4, hence w = [0.05 0.25 0.4 0.25 0.05]
```

```
wm = np.array([[0.05,0.25,0.4,0.25,0.05]])
wn = wm.transpose()
```

```
print(wm)
print(wn)
```

```
[[0.05 0.25 0.4 0.25 0.05]]
[[0.05]
 [0.25]
 [0.4 ]
 [0.25]
 [0.05]]
```

Create 1D Gaussian Blur function across columns using Wm kernel

```
In [487... def gaussianBlurColumn(inputImageResizedGray):

    a,b = inputImageResizedGray.shape #Gets number of rows (or height) (a) and number of columns (b)
    wmImage = np.zeros((a,b)) #Creates a vector with 'a' rows and 'b' columns
    i=0
    j=0
    while(i<a):
        while(j<b-4):
            wmImage[i][j+2] = wm[0][0]*inputImageResizedGray[i][j] + wm[0][1]*inputImageResizedGray[i][j+1] + wm[0][2]*inputImageResizedGray[i][j+2] + wm[0][3]*inputImageResizedGray[i][j+3] + wm[0][4]*inputImageResizedGray[i][j+4]
            j+=1
```

```

        i+=1
        j=0

    return wmImage

```

1D Gaussian Blur across row using Wn kernel for Level 1

```

In [489... def gaussianBlurRow(wmImage):

    c,d = wmImage.shape #Gets number of rows (or height) (x) and number of columns (y)
    wnImage = np.zeros((c,d))
    i=0
    j=0
    while(j<d):
        while(i<c-4):
            wnImage[i+2][j] = wn[0][0]*wmImage[i][j] + wn[1][0]*wmImage[i+1][j] + wn[2][0]*wmImage[i+2][j]
            i+=1
        j+=1
        i=0
    return wnImage

```

Create interpolation function

```

In [490... def interpolation(input_img):

    a,b = input_img.shape #Gives rows (height) (a) and columns (width) (b)
    output_img = np.zeros((2*a - 1, 2*b - 1)) #Creates blank image (=0) c

    i=0
    j=0

    while(i<(2*a - 1)):
        while(j<(2*b - 1)):
            if(j%2==0):
                output_img[i][j] = input_img[math.floor(i/2)][math.floor(j/2)]
            else:
                output_img[i][j] = (input_img[math.floor(i/2)][math.floor(j/2)] + input_img[math.floor(i/2)][math.floor(j/2)+1]) / 2
            j+=1
        i+=1
        j=0

    i=1
    while(i<(2*a - 1)):
        output_img[i] = (output_img[i-1] + output_img[i+1]) / 2
        i+=2

    return output_img

```

Perform gaussian blurring and downsampling to get Level 1

```

In [491... blurredColumn1 = gaussianBlurColumn(inputImageResizedGray)
        blurredRow1 = gaussianBlurRow(blurredColumn1)

```

```
gaussianPyramidLevel1 = blurredRow1[0::2,0::2]
plt.imshow(gaussianPyramidLevel1, cmap='gray')
```

Out[491]: <matplotlib.image.AxesImage at 0x7febd227b370>



Perform gaussian blurring and downsampling to get Level 2

```
In [492... blurredColumn2 = gaussianBlurColumn(gaussianPyramidLevel1)
blurredRow2 = gaussianBlurRow(blurredColumn2)
gaussianPyramidLevel2 = blurredRow2[0::2,0::2]
plt.imshow(gaussianPyramidLevel2, cmap='gray')
```

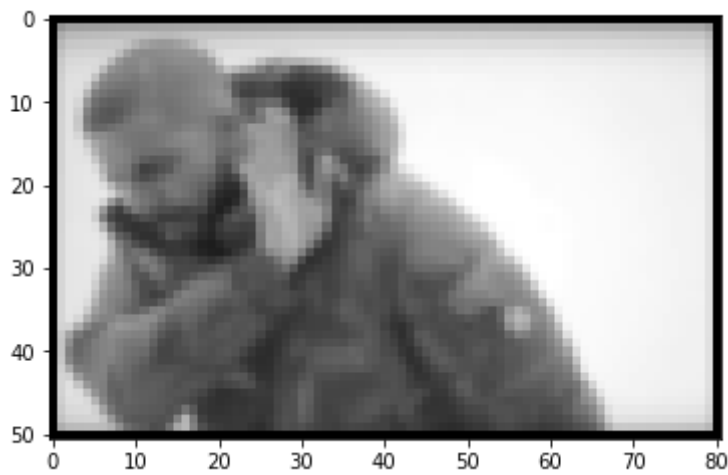
Out[492]: <matplotlib.image.AxesImage at 0x7febd26bc280>



Perform gaussian blurring and downsampling to get Level 3

```
In [493... blurredColumn3 = gaussianBlurColumn(gaussianPyramidLevel2)
blurredRow3 = gaussianBlurRow(blurredColumn3)
gaussianPyramidLevel3 = blurredRow3[0::2,0::2]
plt.imshow(gaussianPyramidLevel3, cmap='gray')
```

Out[493]: <matplotlib.image.AxesImage at 0x7febd2772400>



Get interpolation estimates for N=2, N=1, and N=0 levels

```
In [494... #Following section is to get interpolation estimates for N=2 from Gaussian pyra

interpolationLevel2 = interpolation(gaussianPyramidLevel3)
#plt.imshow(interpolationLevel2, cmap='gray')

#Following section is to get interpolation estimates for N=1 from Gaussian pyra

interpolationLevel1 = interpolation(gaussianPyramidLevel2)
#plt.imshow(interpolationLevel1, cmap='gray')

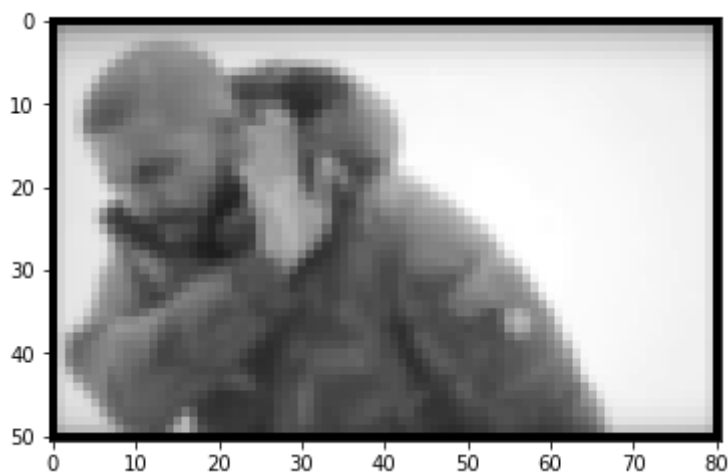
#Following section is to get interpolation estimates for N=0 from Gaussian pyra

interpolationLevel0 = interpolation(gaussianPyramidLevel1)
#plt.imshow(interpolationLevel0, cmap='gray')
```

Get Laplacian pyramid for N=3

```
In [495... laplacianPyramidLevel3 = gaussianPyramidLevel3
plt.imshow(laplacianPyramidLevel3, cmap='gray')
```

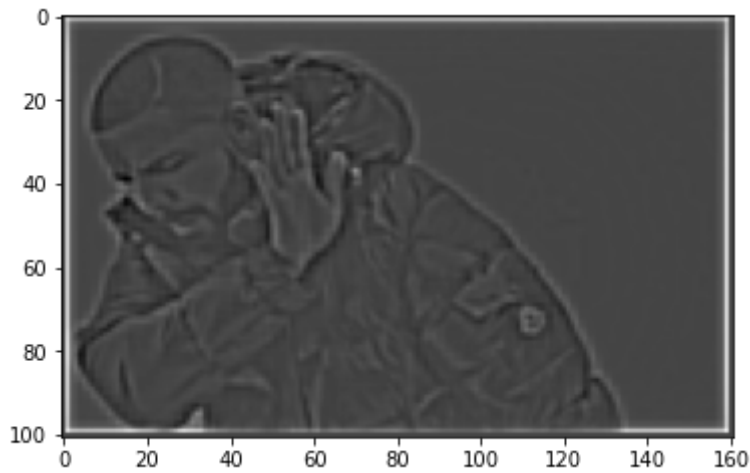
```
Out[495]: <matplotlib.image.AxesImage at 0x7febd28e76d0>
```



Get Laplacian pyramid for N=2

```
In [496... laplacianPyramidLevel2 = gaussianPyramidLevel2 - interpolationLevel2
plt.imshow(laplacianPyramidLevel2, cmap='gray')
```

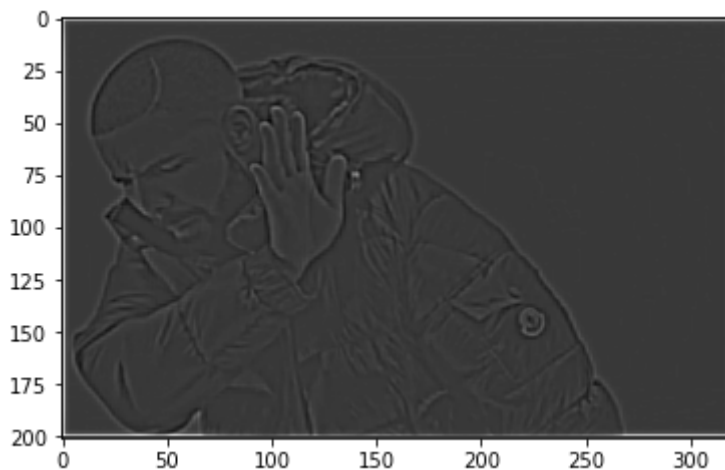
```
Out[496]: <matplotlib.image.AxesImage at 0x7fe63ba0d4f0>
```



Get Laplacian pyramid for N=1

```
In [497... laplacianPyramidLevel1 = gaussianPyramidLevel1 - interpolationLevel1
plt.imshow(laplacianPyramidLevel1, cmap='gray')
```

```
Out[497]: <matplotlib.image.AxesImage at 0x7fec7008b520>
```



Get Laplacian pyramid for N=0

```
In [498... laplacianPyramidLevel0 = inputImageResizedGray - interpolationLevel0
plt.imshow(laplacianPyramidLevel0, cmap='gray')
```

```
Out[498]: <matplotlib.image.AxesImage at 0x7febd2d98b50>
```

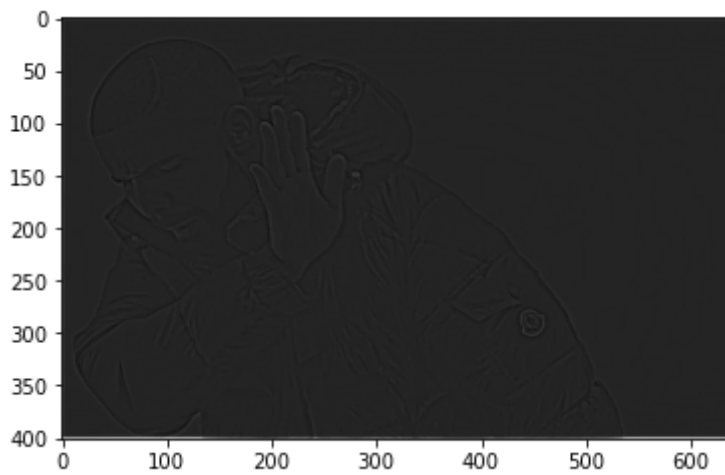


Image reconstruction for N=3

```
In [499... reconstructedImageLevel3 = laplacianPyramidLevel3  
plt.imshow(reconstructedImageLevel3, cmap='gray')
```

```
Out[499]: <matplotlib.image.AxesImage at 0x7fec75b3aa30>
```

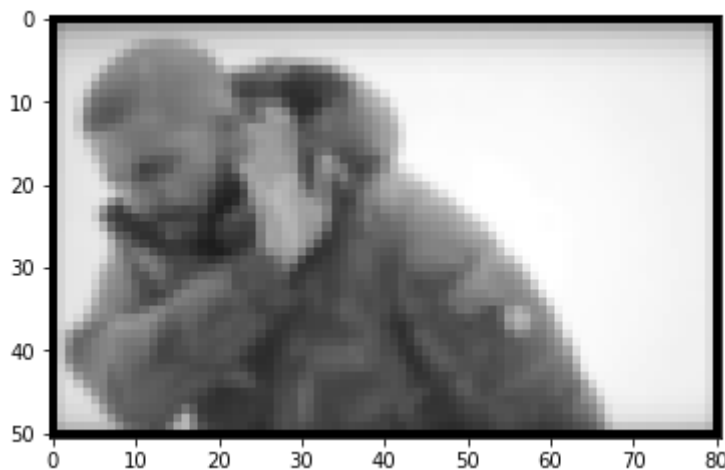


Image reconstruction for N=2

```
In [500... reconstructedImageLevel2 = laplacianPyramidLevel2 + interpolationLevel2  
plt.imshow(reconstructedImageLevel2, cmap='gray')
```

```
Out[500]: <matplotlib.image.AxesImage at 0x7febd2d6d610>
```



Image reconstruction for N=1

```
In [501... reconstructedImageLevel1 = laplacianPyramidLevel1 + interpolationLevel1  
plt.imshow(reconstructedImageLevel1, cmap='gray')
```

```
Out[501]: <matplotlib.image.AxesImage at 0x7fecc2eb94c0>
```

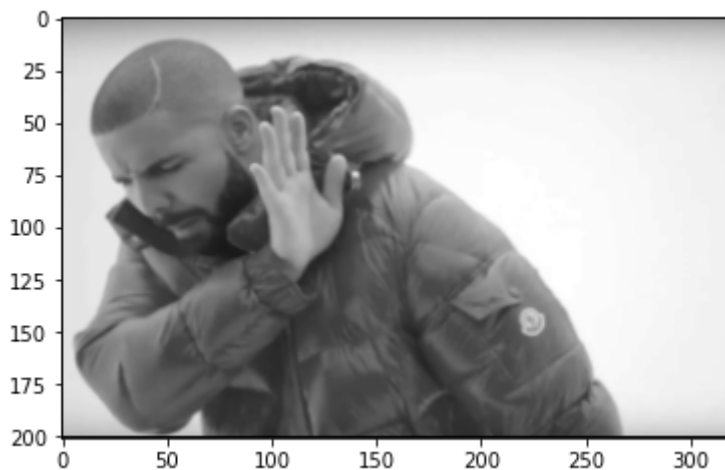


Image reconstruction for N=0

```
In [248... reconstructedImageLevel0 = laplacianPyramidLevel0 + interpolationLevel0  
plt.imshow(reconstructedImageLevel0, cmap='gray')
```

```
Out[248]: <matplotlib.image.AxesImage at 0x7fec8130a4c0>
```




Discussion

Original images require a lot of computation to send/receive. With the use of a Laplacian pyramid, we can send and reconstruct the original image with much less time and more efficiency.

Question 2

```
In [507... background000 = cv.imread('bg000.bmp')           #Reads input image
background000 = np.asarray(background000,dtype=np.float64)   #Converts input image to float64
foreground = cv.imread('walk.bmp')                           #Reads foreground image
foreground = np.asarray(foreground,dtype=np.float64)         #Converts foreground image to float64

a,b,c = background000.shape                                  #Gets rows(a), columns(b), and channels(c)

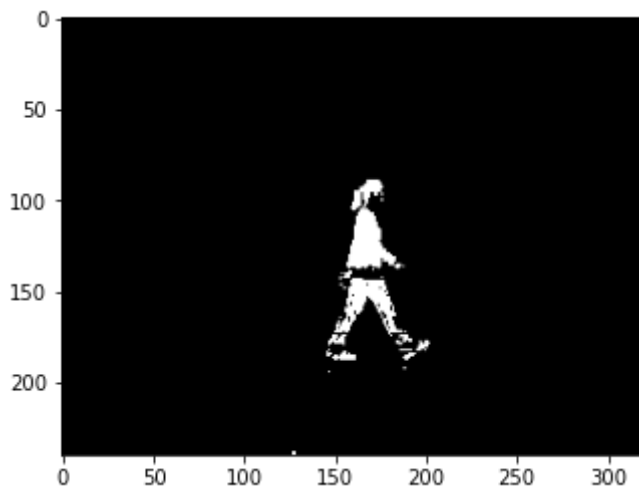
outputImage = np.zeros((a,b,c))                             #Creates a zero image with same dimensions as background000

i=0
j=0
k=0
T=80                                                         #Set threshold value

while(k<c):
    while(i<a):
        while(j<b):
            if(abs(background000[i][j][k] - foreground[i][j][k]) > T):
                outputImage[i][j][k] = 1
            j+=1
        i+=1
        j=0
    k+=1
    i=0
    j=0

plt.imshow(outputImage,cmap='gray')
```

Out[507]: <matplotlib.image.AxesImage at 0x7febd34530a0>



Discussion

For lower threshold values, we see that along with foreground, more than required sections of background are also retained. And for higher values of threshold, less than required sections of foreground are retained. Hence, values around $T=60$ gives an acceptable background subtraction for type 1

Question 3

```
In [509... #Following section reads multiple background images

backgroundImages = [cv.imread(file) for file in glob.glob("bg images/*.bmp")]

a,b,c = backgroundImages[0].shape    #Gets rows, columns, and channels in background image
i=0    #For rows
j=0    #For columns
k=0    #For channel
l=0    #To access images for average
m=0    #To access images for variance
add=0
square=0
pixelAverage = np.zeros((a,b,c))
pixelAverage = np.asarray(pixelAverage,dtype=np.float64)
pixelVariance = np.zeros((a,b,c))
pixelVariance = np.asarray(pixelVariance,dtype=np.float64)

#Following section generates matrix with average values of pixels in time domain

for k in range(c):
    for i in range(a):
        for j in range(b):

            for l in range(30):
                add += backgroundImages[l][i][j][k]
            pixelAverage[i][j][k] = add/30
            add = 0

            for m in range(30):
                square += ((backgroundImages[m][i][j][k] - pixelAverage[i][j][k])
```

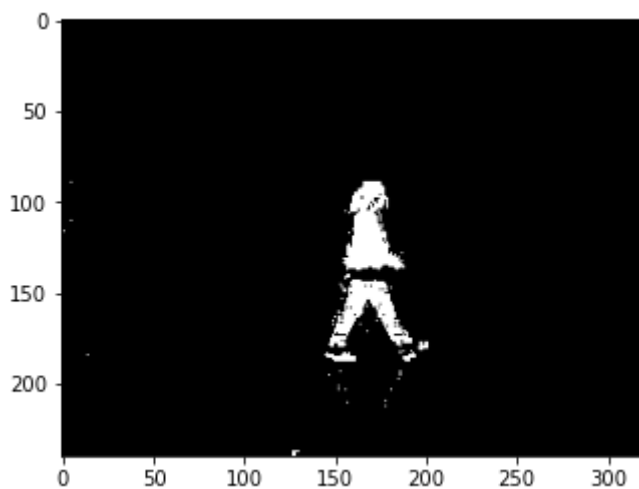
```
pixelVariance[i][j][k] = square/30
square = 0
```

```
In [510]: T=15      #Set threshhold value

outputImage = np.zeros((a,b,c))
outputImage = ((foreground - pixelAverage)**2) / (pixelVariance) > T**2
outputImage = np.asarray(outputImage,dtype=np.float64)
plt.imshow(outputImage,cmap='gray')
```

```
/var/folders/_z/7q8tzcpd3s7cr5lz406qzcw0000gn/T/ipykernel_2393/1705601871.py:
4: RuntimeWarning: divide by zero encountered in true_divide
  outputImage = ((foreground - pixelAverage)**2) / (pixelVariance) > T**2
/var/folders/_z/7q8tzcpd3s7cr5lz406qzcw0000gn/T/ipykernel_2393/1705601871.py:
4: RuntimeWarning: invalid value encountered in true_divide
  outputImage = ((foreground - pixelAverage)**2) / (pixelVariance) > T**2
```

```
Out[510]: <matplotlib.image.AxesImage at 0x7fecc2eff2b0>
```



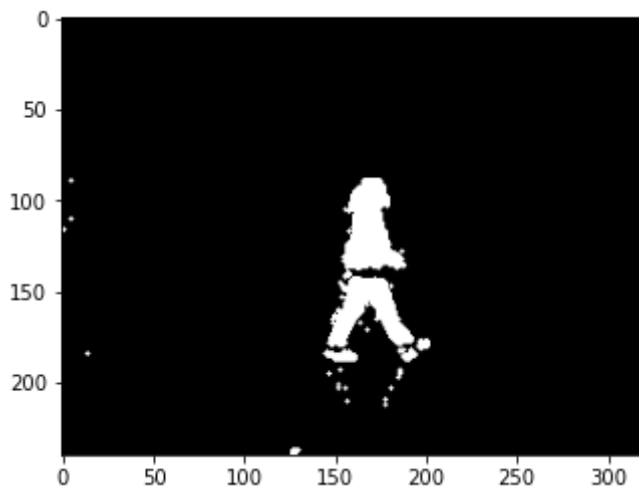
Discussion

We see that a much more recognizable subtraction is done using this method. Also, the threshold value required for this technique (15) is much lower than what was required in background subtraction 1 (60) to get acceptable output

Question 4

```
In [459]: dilatedImage = morphology.dilation(outputImage)
plt.imshow(dilatedImage,cmap='gray')
```

```
Out[459]: <matplotlib.image.AxesImage at 0x7febd1fbe220>
```



Discussion

Dilation adds pixels to the boundary of object in an image. Here, we see that the object has more white pixels than the original binary image.

Question 5

```
In [531... L,num = measure.label(dilatedImage,connectivity=2,return_num=True)
print('Number of regions is',num)
```

Number of regions is 18

In []: