

Set- I


VAAGDEVI COLLEGE OF ENGINEERING

AUTONOMOUS

P.O.BOLLIKUNTA, WARANGAL – 506 005

B. TECH II YEAR I SEMESTER, I - MID EXAMINATIONS SEPTEMBER- 2024

Mathematical and Statistical Foundation

[CSM]

(R23 REGULATION)

Max. Marks: 30

Time: 2 Hours

Note: This question Paper Contains two parts. Part A & B

Course Outcomes for Assessment in this Test:

COs	Course Outcome
1	Apply the number theory concepts to cryptography domain
2	Apply the concepts of probability and distributions to some case studies
3	Correlate the material of one unit to the material in other units

PART – A (10 X 1 = 10 Marks)
CHOOSE THE CORRECT ANSWER

Marks

1.	GCD of 28 and 36 is [] a) 4 b) 2 c) 3 d) 1	1
2.	Find the GCD of 48, 72, 108 [] a) 21 b) 12 c) 6 d) 1	1
3.	LCM of 90 and 144 [] a) 520 b) 620 c) 720 d) 420	1
4.	Second Fermat number is [] a) 13 b) 23 c) 19 d) 17	1
5.	If the probability density function of a random variable is given by $f(x) = k(1-x^2)$, $0 < x < 1$ find the value of K [] a) $\frac{1}{2}$ b) $\frac{1}{3}$ c) $\frac{2}{3}$ d) $\frac{3}{2}$	1
FILL IN THE BLANKS		
6.	The regression line of X on Y is _____	1
7.	By the method of least squares the normal equations of the regression line $Y = a + bx$ are	1
8.	Formula to find angle between two regression lines is given by $\tan \Theta = \dots\dots\dots$	1
9.	What are the types of random variables	1
10.	Mean and variance of Binominal distribution _____	1

PART – B ANSWER ANY FOUR OF THE FOLLOWING (4X 5 = 20 Marks)		Marks	Mapping COs	Bloom's Taxonomy Levels																		
1.	Solve the system of congruences using Chinese remainder theorem $x \equiv 3 \pmod{5}$ $x \equiv 1 \pmod{7}$ $x \equiv 6 \pmod{8}$	5	1	BL- 5																		
2.	Solve the linear congruence $9x \equiv 6 \pmod{15}$	5	1	BL- 4																		
3.	Solve the system $2x_1 + 5x_2 + 6x_3 \equiv 3 \pmod{7}$ $2x_1 + x_3 \equiv 4 \pmod{7}$, $x_1 + 2x_2 + 3x_3 \equiv 1 \pmod{7}$	5	1	BL- 5																		
4.	Find the regression line of Y on X and the regression line of X on Y from the following data <table border="1"><tr><td>X</td><td>1</td><td>5</td><td>3</td><td>2</td><td>1</td><td>1</td><td>7</td><td>3</td></tr><tr><td>Y</td><td>6</td><td>1</td><td>0</td><td>0</td><td>1</td><td>2</td><td>1</td><td>5</td></tr></table>	X	1	5	3	2	1	1	7	3	Y	6	1	0	0	1	2	1	5	5	2	BL- 4
X	1	5	3	2	1	1	7	3														
Y	6	1	0	0	1	2	1	5														
5.	Two dies are thrown once the random variable assigns to sum, write the distribution function, find the mean and variance.	5	2	BL- 3																		
6.	A random variable X has the following probability distribution <table border="1"><tr><td>X</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr><tr><td>Y</td><td>0</td><td>K</td><td>2k</td><td>2k</td><td>3k</td><td>K²</td><td>2K²</td><td>7k²+k</td></tr></table> Find i) Value of K ii) P (x<6) iii) P (x ≥ 6) iv) P(0<x<5)	X	0	1	2	3	4	5	6	7	Y	0	K	2k	2k	3k	K ²	2K ²	7k ² +k	5	2	BL – 3, 5
X	0	1	2	3	4	5	6	7														
Y	0	K	2k	2k	3k	K ²	2K ²	7k ² +k														