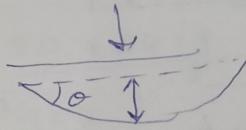
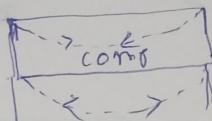
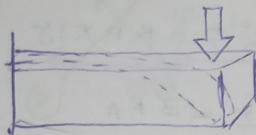


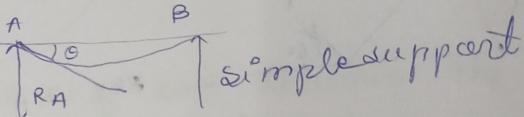
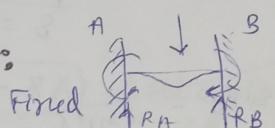
CHAPTER 6

SHEAR FORCE AND BENDING MOMENT

Shear and Bending force:



Different supports:



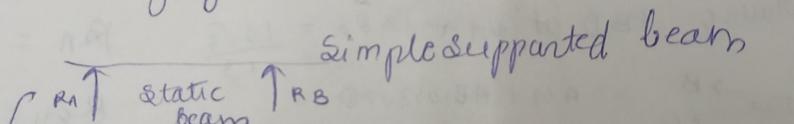
becoz hinges balance torques

Symb. all: → uniform load throughout the length.

: → varying load throughout the length.

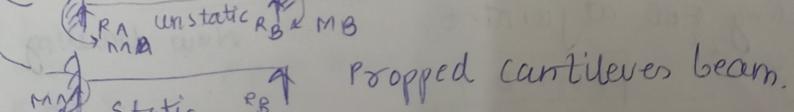
Types of supports:

Exactly 2/1 Support

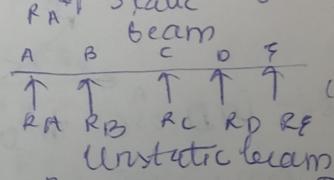


cantilever beam

fixed beam



continuous beam.



static beam → total Reaction + Moment ≤ 3

unstatic beam → total Reaction + Moment > 3

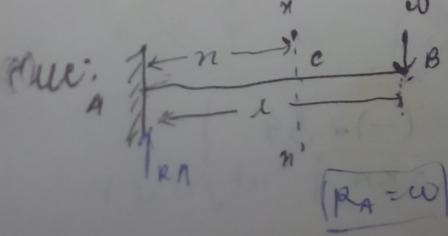
A B C D overhanging beams,

$$SF \text{ at } B = -w$$

SF at C = -w [w is constant throughout length]

SF just right of A = -w

CF at A = 0 [+w - w]



Shear diagram: A | B SF (-w)

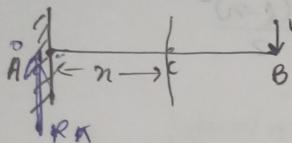
Shear forces

Algebraic sum of all forces either taking right or left from the section should be equal and opposite.

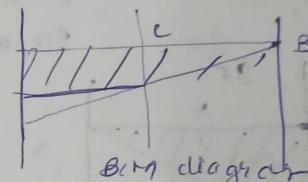
Bending moment:

Algebraic sum of all moments either taking right or left from the section should be equal and opposite.

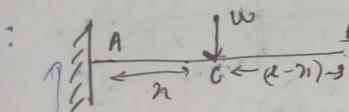
Ques: Find BM and draw BM diagram:



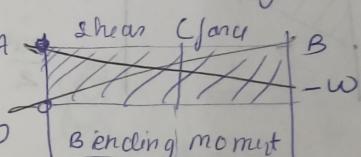
$$\begin{aligned} \text{BM at } B &= 0 \\ \text{at } C &= -w(l-n) \\ \text{at } A &= -wl \end{aligned}$$



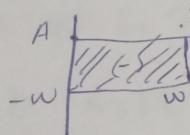
Ques: Find SF and BM also draw diagram?



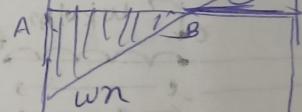
$$\begin{aligned} \text{SF at } B &= 0 \\ \text{at } C &= w(l-n) \\ \text{at } A &= -w \end{aligned}$$



* if we are calculating from R to L then at A = -wn



if we are moving from Right to left

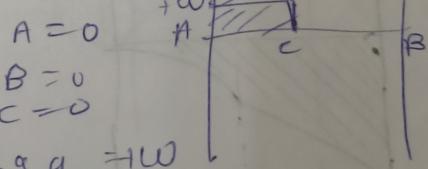


consider section on B - no force is there on right hence SF = 0.

[NOTE: for calculating SF we need to consider from direction]

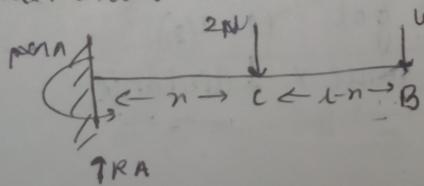
if we a

* if we calculating from L to R: the SF at A = 0



just right a +wl

Ques: draw SF and BM diagram!



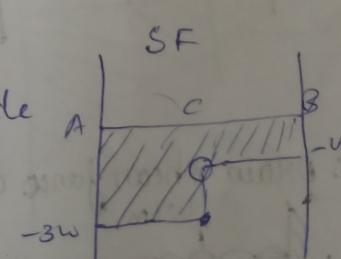
$$RA = 3w \uparrow$$

when consider Rn side

$$BF \text{ at } B = -w$$

$$SF \text{ at } C = -3w$$

$$SF \text{ at } A = 0$$



$$BM \text{ at } B = 2(wl) - 3(wl) \quad B = 0 \quad (\because \text{No force on right side})$$

$$\text{at } B = (-l - 2w)w$$

$$BM \text{ at } A = 2wl(l-n) + (l-n)w - wl(l-n) \quad A = (wn + wl) - wl - 2wn$$

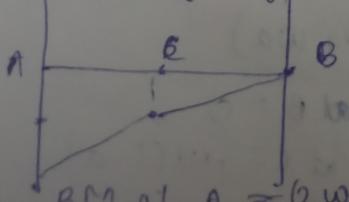
No force
on right
side

$$A = -wl + wn$$

$$BM \text{ at } A = -3wl - wl(l-n)$$

$$= -3wl - wl + wl \quad A = -2wl - wl$$

Bending diagram



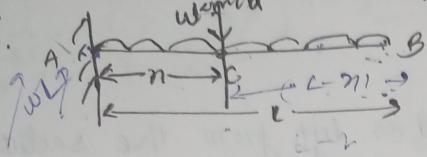
$$BM \text{ at } A = (2wl) - wl(l-n)$$

$$A = -wl - 2wl$$

$$BM \text{ at } A = -2wl - wl$$

[Note: for calculating SF and BM always take 1 side and calculate all forces on that side only + Force acting on that point. This also apply for Bending Moment.]

Ques: Find the Shear force and Bending moment diagram. [ieprgt]



$$\begin{aligned} \text{SF at } B &= 0 \\ \text{SF at } C &= -w(L-n) \\ \text{SF at } A &= -wL \end{aligned}$$

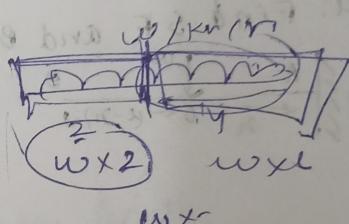
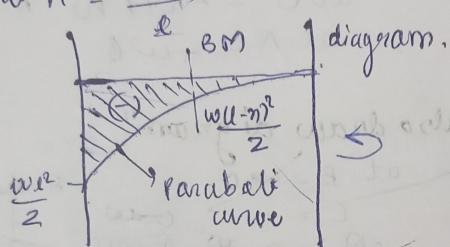
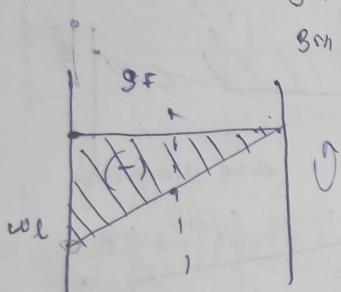
$$w \text{ kN/m}$$

Bending moment:

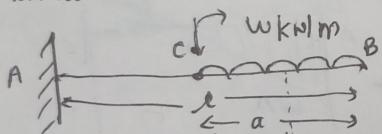
$$\text{BM at } B = 0$$

$$\text{BM at } C = -w(L-n)x \times w(L-n)/2 = -w(L-n)^2/2$$

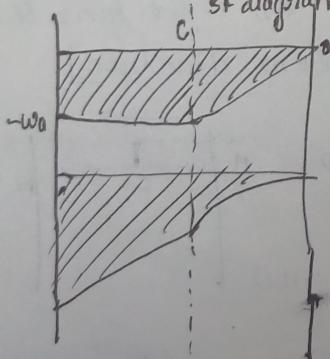
$$\text{BM at } A = -wL^2$$



Ques: Draw shear force and bending moment diagram:



$$\begin{aligned} \text{SF at } B &= 0 \\ \text{SF at } C &= -w(a) = -wa \\ \text{SF at } A &= -w(l-a) \end{aligned}$$



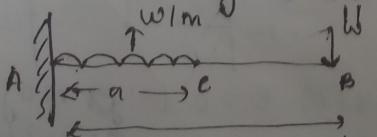
$$\begin{aligned} \text{BM at } B &= 0 \\ \text{BM at } C &= -w(l-a)a - \frac{wa \cdot a^2}{2} \quad [\text{since } w \text{ will act at } a/2 \text{ distance}] \\ &= -w \frac{a^2}{2} \end{aligned}$$

$$\text{BM at } A = -(l-a)(l-a/2) - wa$$

[1 distance of force CB is $(l-a) + \frac{a}{2}$]
∴ we got $(l-a/2)$

Hence force \times 1 distance

Ques: Draw shear force and bending moment diagram:



Shear force:

$$\text{SF at } B = 0 - w$$

$$\text{SF at } C = -2w$$

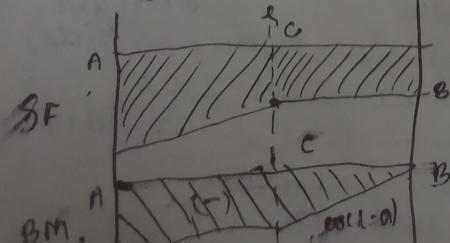
$$\text{SF at } A = -(w+wa)$$

Bending moment:

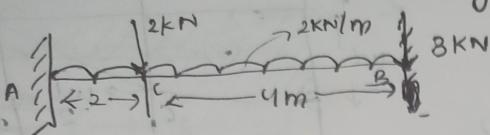
$$\text{BM at } B = 0$$

$$\text{BM at } C = -w(l-a)$$

$$\text{BM at } A = -wa - \frac{wa^2}{2}$$



Ques: Find the Shear and Bending Moment diagrams for the following:

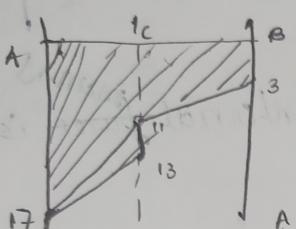


$$SF: \text{at } B = -3 \text{ kN}$$

$$SF \text{ right at } C = (-2)(4) - 3$$

$$SF \text{ at } A = -3 - 2 \times 6 - 2$$

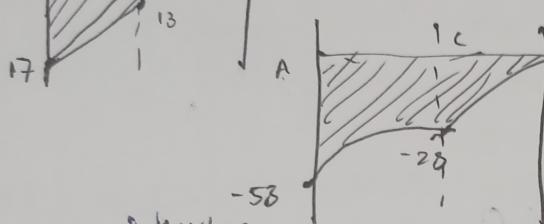
$$SF \text{ at } C = (-2)(4) - 3 - 2$$



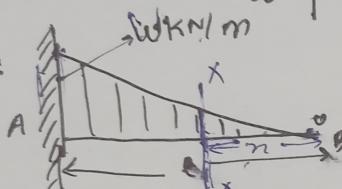
$$BM: \text{at } B = 0$$

$$\text{right at } C = -(3)(4) - (2)(2) \times (4)$$

$$BM \text{ at } A = -(2)(2) + (2)(6) \times (3) \\ = -(3)(6) \\ = -58$$



Ques:



$$SF: \text{at } B = 0$$

$$\text{at } A =$$

w_m force acting on section m

$$\frac{W}{l} = \frac{w_m}{n}$$

$$SF \text{ at } B = 0$$

$$SF \text{ at } C, n = \cancel{\left(\frac{w_m}{n} \right) \left(\frac{l}{2} \right)} = -\cancel{\frac{w_m}{n}} = \text{Area} = \frac{1}{2} n w_m = \frac{1}{2} w_m \frac{n^2}{l}$$

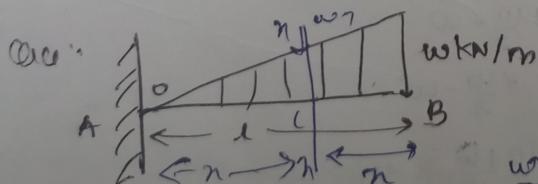
$$SF \text{ at } A, l \times 0 = l = \frac{-w_m}{t} = -w$$

$$= \frac{1}{2} w_m \times l = -\frac{1}{2} w_m l = -\frac{1}{2} w L$$

$$BM \text{ at } B = 0$$

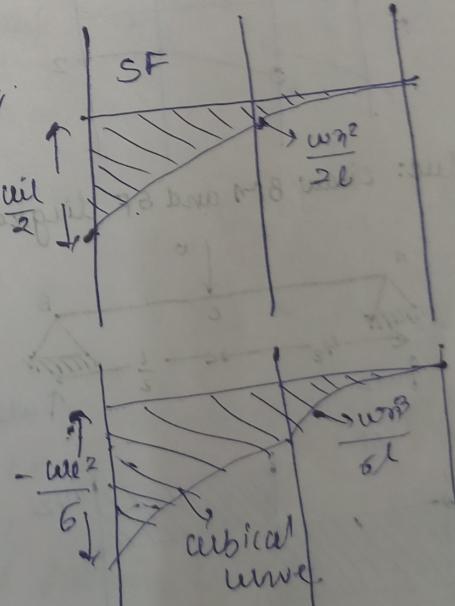
$$BM \text{ at } C = \left(-\frac{w_m l^2}{2l} \right) \frac{n}{3}$$

$$BM \text{ at } A = \left(-\frac{w L}{2} \right) \left(\frac{l}{3} \right) = -\frac{w L^2}{6}$$



$$\frac{w_m n}{l-n} = \frac{w}{L}$$

$$w_m = \frac{w}{L} (L-n)$$



$$SF \text{ at } B =$$

we will consider Reaction at A and moment because we will consider left hand side.

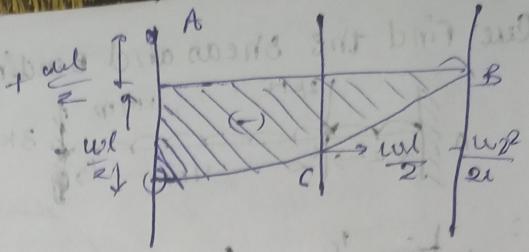
$$\therefore R_A = \frac{wl}{2} \left[\frac{1}{2} \times B \times n \right]$$

$$M_A = \frac{wL^2}{3} \left[\cdot \cdot \left(\frac{wl}{2} \right) \left(\frac{2l}{3} \right) \right]$$

$$SF \text{ at } WA = +\frac{wl}{2}$$

$$SF \text{ at } C = +\frac{wl}{2} - \frac{w\pi^2}{2l}$$

$$SF \text{ at } B = \frac{wl}{2} - \frac{1}{2}wl = 0$$



$$BM \text{ at } A =$$

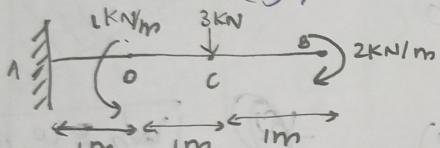
* at hinge joint the moment is always zero, until external moment is applied on the free end.

$$BM \text{ at } A = \frac{wl^2}{3}$$

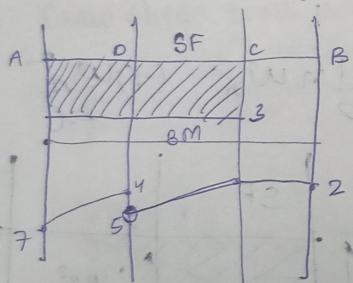
$$BM \text{ at } C = \left(\frac{2l}{3}\right) \left(\frac{wl}{2} - \frac{w\pi^2}{2l}\right)$$

$$BM \text{ at } B = \left(\frac{2l}{3}\right) \left(\frac{wl}{2} - \frac{1}{2}wl\right) = 0$$

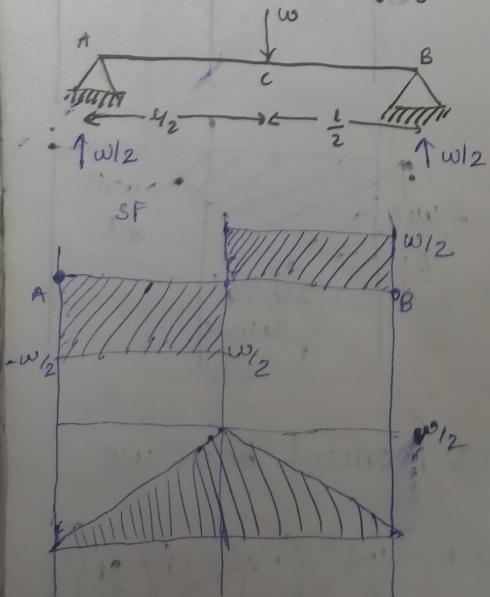
Ques:



Draw BM and SF diagram:



Ques: Draw BM and SF diagram:



due to symmetry $RA \& RB = w/2$

$$SF \text{ at } B = +w/2$$

$$SF \text{ at } C = +\frac{w}{2} - w$$

$$SF \text{ at } A = \frac{+w}{2} - w$$

$$SF \text{ at } A = \frac{w}{2} + \frac{w}{2} - w = 0$$

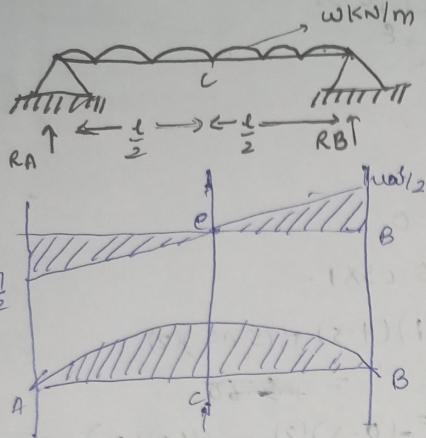
$$BM \text{ at } B = 0$$

$$BM \text{ at } C = \frac{w \times l}{2} = +\frac{wl}{4}$$

$$BM \text{ at } A = \frac{w \times l}{2} - \frac{wl}{2} = 0$$

NOTE: in cantilever beam we get BM (-) because $\therefore BM = +$ best hence get

Ques: Draw BM and SF diagram of this system:



$$RA + RB = wL \text{ and by symmetry}$$

$$RA = RB = \frac{wL}{2}$$

$$SF \text{ at } B = \frac{wl}{2}$$

$$SF \text{ at } C = \frac{wl}{2} + \frac{wl}{2} = wL.$$

$$SF \text{ at } A = -wL + wL = 0$$

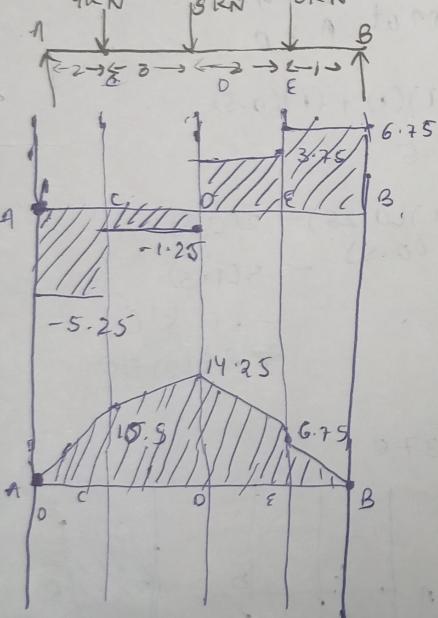
$$BM \text{ at } B = 0$$

$$BM \text{ at } C = +\frac{wl^2}{2} - \frac{wl}{2} \times \frac{l}{2} = \frac{wl^2}{4} - \frac{wl^2}{8} = \frac{wl^2}{8}$$

$$BM \text{ at right of } A = \frac{wl^2}{8} \quad BM \text{ at } A = 0.$$

[NOTE: the point where shear force is zero changing its sign from + to - (ve) maximum BM occurs]

Ques: Draw BM and SF diagram of this system:



$$\therefore RA + RB = 9 \quad (\Sigma V = 0)$$

$$\Sigma MA = 0: \quad (2)(-4) + (2)(-5) + (7)(-2) \neq RB \times 8 = 6$$

$$= +8 + 20 + 21 = RB \times 8$$

$$RB = \frac{57}{8} \quad RB = 6.75$$

$$RA = 5 - 6.75 \quad RA = 5.25$$

$$SF \text{ at } B = +6.75 \uparrow$$

$$SF \text{ at } E = 3.75 \uparrow$$

$$SF \text{ at } E = -1.25$$

$$SF \text{ at } C = -5.25$$

$$SF \text{ at right} = -5.25$$

$$SF \text{ at } A = 0$$

$$BM \text{ at } B = 0$$

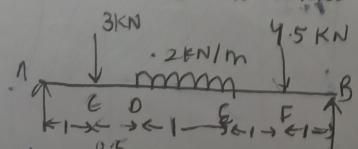
$$BM \text{ at } E = 6.75 \times 1$$

$$BM \text{ at } D = 2(-3) + (6.75)(3) = 14.25 \uparrow$$

$$BM \text{ at } C = 10.5$$

$$BM \text{ at } A = 0$$

Ques: Calculate and draw the Shear force diagram for following system:



$$\Sigma V = 0: \quad RA + RB = 3 + 4.5 + ?$$

$$RA + RB = 9.5$$

$$\Sigma MA = 0: \quad (-3)(1) + (4.5)(3.5)$$

$$SF \text{ at } B = 5.05 \text{ kN} \quad -2(2) \neq RB(4.5) = 0$$

$$SF \text{ at } F = 0.55 \text{ kN} \quad RB = 5.05 \text{ kN}$$

$$SF \text{ at } E = 0.55 \text{ kN} \quad RA = 9.45 \text{ kN}$$

$$SF \text{ at } D = -1.45 \text{ kN}$$

$$SF \text{ at } C = -3.05 \text{ kN}$$

$$SF \text{ at } A = -4.45 \text{ kN}$$

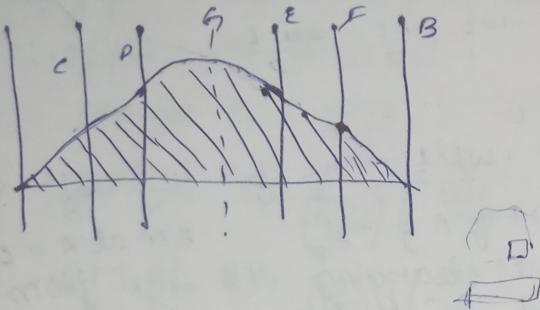
To calculate length of GE we get:

$$\therefore \frac{n}{0.55} = \frac{1-n}{1.45}$$

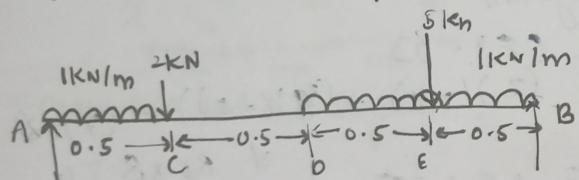
$$\boxed{n = 0.275}$$

$$\therefore EC = 0.275$$

Now we will calculate



Ques: Find SF and BM:



$$\boxed{R_B = 5.0625}$$

$$\boxed{R_A = 3.4375}$$

$$SF \text{ at } B = 5.0625 \uparrow$$

$$SF \text{ at } E = 5.0625 - 5 = 1(0.5) = -0.4375$$

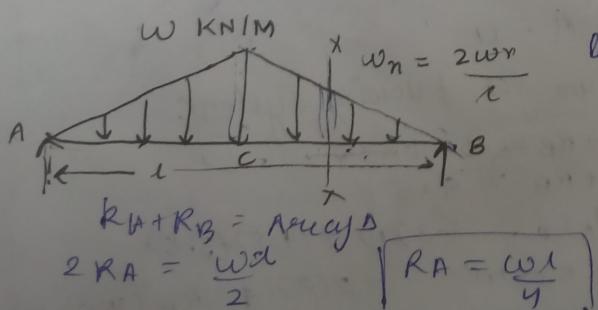
$$SF \text{ at } D = -6 + 5.0625 = -0.9375 \downarrow$$

$$SF \text{ at } C = -2.9375$$

$$SF \text{ at } A = 0.$$

$$SF \text{ at right of } A = -3.4375$$

Ques: Find SF and BM:



$$R_A + R_B = w_n l$$

$$2R_A = \frac{w_n l}{2}$$

$$SF \text{ at } B = wL/y$$

$$SF \text{ at section } n = \frac{1}{2} w_n n, n = \frac{1}{2} \frac{w_n l^2}{l} + (wL)$$

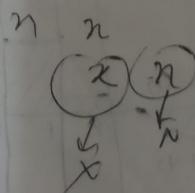
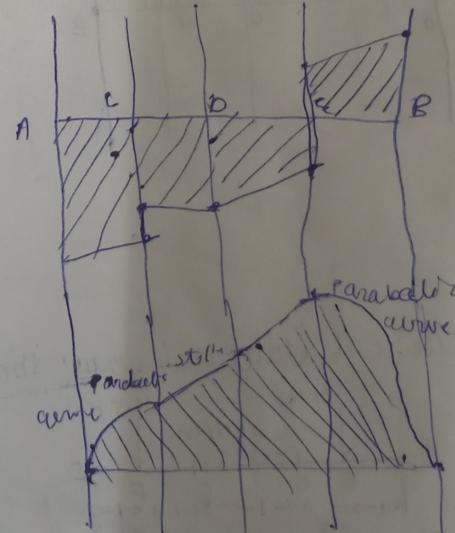
$$SF \text{ at } C = \frac{1}{2} wL + \frac{1}{4} wL = \frac{3}{4} wL$$

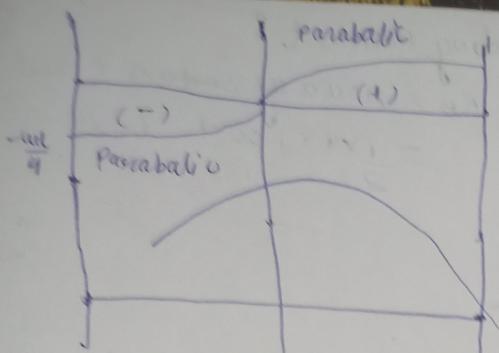
$$\frac{n}{w_n} = \frac{l}{\frac{w_n l}{2}}$$

leg similar

triang

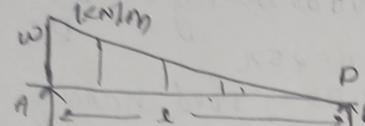
$$\boxed{w_n = \frac{2wL}{l}}$$





$$BM \text{ at } C = +\frac{wl}{4} \times \frac{l}{2} - \left[\frac{wl}{2} \cdot \frac{l}{2} \right] = \frac{wl^2}{12}$$

$\times \perp \text{ distn}$

Ques:  find deflection and Bending moment?

Sol: $RA + RB = \frac{1}{2} Lw$

$$SMA = 0 \quad RB \times l - \frac{wl \times l}{2} \times \frac{1}{3} = 0 \quad RB = \frac{wl}{6} \quad \text{from eqn (1)} \quad RA = \frac{wl}{3}$$

w_n is the load at section n-n.

$$\therefore SF \text{ at } B = +\frac{wl}{6} \quad \text{by similar triangle, we get } w_n = \frac{w_n \cdot n}{l}$$

$$SF \text{ at n-section} = \frac{wl}{6} - \frac{w_n \cdot n}{l} = \frac{wl}{6} - \frac{w_n^2}{l^2}$$

$$SF \text{ at } A \text{ (just right)} = -\frac{wl}{3}$$

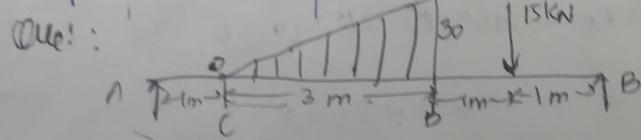
to find F point $BF = 0$

$$\frac{w_n^2}{l^2} = \frac{wl}{6} \quad n = \frac{l}{\sqrt{3}}$$

hence $BF = \frac{l}{\sqrt{3}}$

BM at C where SF is zero. so

$$BM \text{ at } C = \frac{wl^2}{9\sqrt{3}}$$



$$RA + RB = 15 + 30 \times \frac{1}{2} \times 3$$

$$= 15 + 45 = 60$$

$\therefore SF \text{ at } B =$

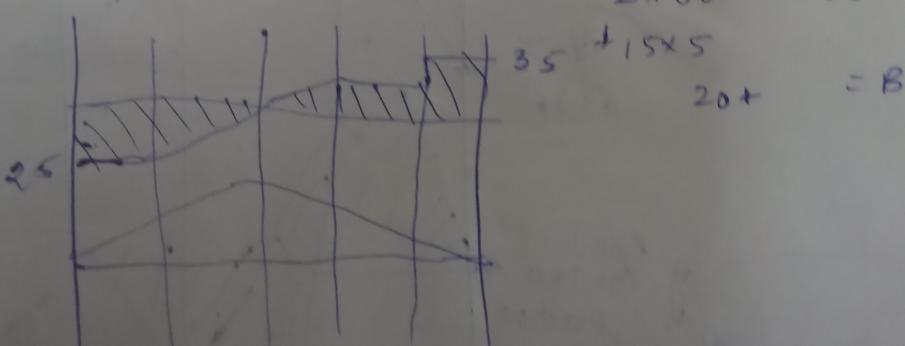
$$SMA = 0: 2 \times 60 = B \times 6$$

$$\frac{1}{2} \frac{l}{\sqrt{3}} \times 100 = \frac{l}{\sqrt{3}}$$

$$\frac{w \cdot l}{\sqrt{3}} \times \frac{l}{2\sqrt{3}}$$

$$\frac{wl \times 2l}{\sqrt{3} \times 2\sqrt{3}} = \frac{wl}{3}$$

$$\frac{2l}{\sqrt{3}}$$



and the first building
and the second

and the third building
and the fourth building

and the fifth building

and the sixth

and the seventh building
and the eighth building

and the ninth building
and the tenth building

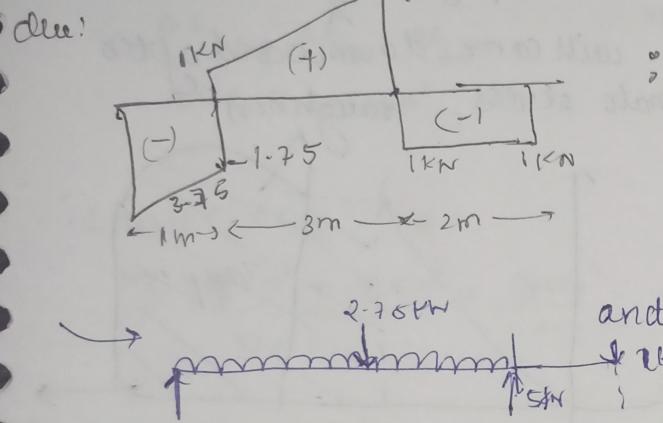
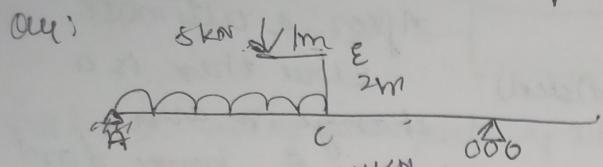
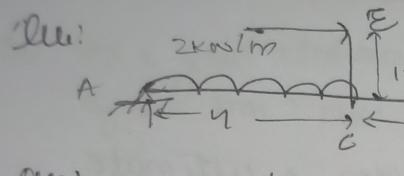
and the eleventh building
and the twelfth building

and the thirteenth building
and the fourteenth building

and the fifteenth building
and the sixteenth building

The number from one to eleven the first twelve buildings
and the next the next number is the next number
the remaining the last two buildings numbered
one to two

and the next two buildings



10m rightmost to left, value of w is constant hence a point load by 10kN at rightmost.

then carrying load whose $w = \frac{4-1}{3} = 1\text{ kN}$.

at another point $1 - w = 10 - 7.5$

and then varying load. $w = 2.75$

minimum point of the variation of w is the point of least resistance and provides the minimum deflection due to maximum deflection occurring at the point of zero load.