

#### Section 4.

(1) Yes. Different samples' order may cause different cluster centers, the number of clusters will cause different clustering results.

(2) Yes. If the sample is an outlier, then the distance to its nearest token will be greater than the threshold, (i.e.,  $\text{dist}(x_n, \text{token}_n) > h$ ), then the sample will become a new token, instead of being merged to other clusters.

(3) If  $h$  is a small number, then more samples will not be merged into existed clusters, in this case, these samples will become new cluster centers, and the total number of clusters is more than  $K$ -means.

If  $h$  is a big number, then most samples will be merged into pre-defined  $K$  clusters, in this case, all samples can be classified into  $K$  classes, which is the same number in  $K$ -means.

If token clustering and  $K$ -means have the same initial centers, i.e. the initial number of clusters are the same, then token clustering will have at least  $K$  clusters in the end. If the initial number of clusters in token clustering is less than  $K$ -means, then with a proper threshold, the number of clusters will increase and equal to  $K$  in the end.

(4) In GMM, we set two components  $N(x_n | \mu_1, \Sigma_1)$  and  $N(x_n | \mu_2, \Sigma_2)$  to represent the distribution of pixels in houses and background otherwise.

Then the model will be  $p(x_n | \lambda_k, \mu_k, \Sigma_k) = \sum_{k \in \{1,2\}} \lambda_k N(x_n | \mu_k, \Sigma_k)$

After training (EM), when we predict a pixel  $x_i$ , if  $N(x_i | \mu_1, \Sigma_1) > N(x_i | \mu_2, \Sigma_2)$  then it's a pixel in house (foreground), otherwise it's in background.

(5) No. Some images may have different colors or different number of contents.

(6) Data augmentation for training set. For example, rotation, flipping and clipping, to increase the amount of our training set.

Complex distributions. In this example, we can combine different kinds of probability distribution models to increase the complexity of our model.

