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1 import numpy as np
2 from scipy import integrate
3 from mpl_toolkits.mplot3d import Axes3D
4 from HW1 import convert_rv_kep, kepler_J2_ODE
5 import matplotlib.pyplot as plt
6
7 # constants
8 params = {'mu_E': 398600.0,
9           'J2': 1.082626925638815e-03,
10           'R_E': 6378.1363,
11           'n_objjs': 2}
12
13 # orbit elems of first satellite
14 a = 10000.0 # [km]
15 e = 0.001 # [km]
16 inc = 40.0 # [deg]
17 Omega = 80.0 # [deg]
18 omega = 40.0 # [deg]
19 M_0 = 0.0 # [deg]
20 elems_1 = np.array([a, e, inc, Omega, omega, M_0])
21 # convert to state vector
22 x_1 = convert_rv_kep.convert_rv_kep('keplerian', elems_1, 0
23                                     .0, 'state').reshape(6)
24
25 # orbit elems of second satellite
26 a = 10000.0 # [km]
27 e = 0.8 # [km]
28 inc = 90.0 # [deg]
29 Omega = 80.0 # [deg]
30 omega = 40.0 # [deg]
31 M_0 = 0.0 # [deg]
32 elems_2 = np.array([a, e, inc, Omega, omega, M_0])
33 # convert to state vector
34 x_2 = convert_rv_kep.convert_rv_kep('keplerian', elems_2, 0
35                                     .0, 'state').reshape(6)
36
37 # # #
38 # setup the simulation
39 # calc the orbital period
40 T = 2 * np.pi * np.power(a, 1.5) / np.sqrt(params['mu_E'])
41 dt = 10.0 # [sec]
42 n_orbits = 15.0
43 tspan = np.arange(0.0, n_orbits*T, dt)
44
45 x_0 = np.concatenate((x_1, x_2))
46
47 # solve
48 x_sol = integrate.odeint(func=kepler_J2_ODE.kepler_J2_ODE,
49                           t=tspan, y0=x_0, tfirst=True, args=(params, ), rtol=1.0e-12

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47 , atol=1.0e-12)
48 print(x_sol.shape)
49 print(tspan[-1])
50
51 # plot first
52 font = {'family' : 'arial',
53         'weight' : 'normal',
54         'size'    : 12}
55 fig1 = plt.figure(1, figsize=(9, 4.5))
56 plt.rc('font', **font)
57 ax = fig1.gca(projection='3d')
58 ax.plot(x_sol[:, 0], x_sol[:, 1], x_sol[:, 2], linewidth=0.5)
59 ax.scatter(0.0, 0.0, 0.0, s=50, color='green')
60 ax.set_xlabel('X [km]')
61 ax.set_ylabel('Y [km]')
62 ax.set_zlabel('Z [km]')
63 #ax.set_title('First Satellite 3D Position')
64 plt.title('Satellite 1 Trajectory')
65 plt.legend(('Orbit', 'Earth'))
66 plt.show()
67
68
69 # plot second
70 fig2 = plt.figure(2, figsize=(9, 4.5))
71 ax = fig2.gca(projection='3d')
72 plt.rc('font', **font)
73 ax.plot(x_sol[:, 6], x_sol[:, 7], x_sol[:, 8], linewidth=0.5)
74 ax.scatter(0.0, 0.0, 0.0, s=50, color='green')
75 ax.set_xlabel('X [km]')
76 ax.set_ylabel('Y [km]')
77 ax.set_zlabel('Z [km]')
78 #ax.set_title('Second Satellite 3D Position')
79 plt.title('Satellite 2 Trajectory')
80 plt.legend(('Orbit', 'Earth'))
81 plt.show()
82
83 # calc & plot angular momentum and energy
84 momentum = np.zeros((tspan.shape[0], params['n_objs']))
85 energy = np.zeros((tspan.shape[0], params['n_objs']))
86 for i in range(tspan.shape[0]):
87     for j in range(params['n_objs']):
88         r = x_sol[i, 6*j:3+6*j]
89         v = x_sol[i, 3+6*j:6+6*j]
90         momentum[i, j] = np.linalg.norm(np.cross(r, v))
91         energy[i, j] = np.power(np.linalg.norm(v), 2.0) / 2
92         .0 - params['mu_E'] / np.linalg.norm(r)
93
94 # print out the momentum at the right times

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94 n_steps = np.shape(np.arange(0.0, T, dt))[0]
95 for i in range(int(n_orbits)):
96     for j in range(params['n_objs']):
97         r_vec = x_sol[i*n_steps, 6 * j:3 + 6 * j]
98         v_vec = x_sol[i*n_steps, 3 + 6 * j:6 + 6 * j]
99         r = np.linalg.norm(r_vec)
100        v = np.linalg.norm(v_vec)
101        print(r)
102        print(v)
103        h_vec = np.cross(r_vec, v_vec)
104        h = np.linalg.norm(h_vec)
105        energy = np.power(v, 2.0) / 2.0 - params['mu_E'] /
r
106        #print(h)
107        #print(energy)
108
```