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1 # convert_rv_kep
2 # translate between the state vector and classical
  keplerian orbit elements
3 # Inputs:
4 #   input_flag - type of state being inputted
5 #   x - the numbers
6 #   delta_t - time elapsed since t_0
7 #   output_flag - type of state being outputted
8
9
10 # imports
11 import numpy as np
12
13
14 # # #
15 def convert_rv_kep(input_flag, x_vec, delta_t, output_flag)
  :
16
17     # define some constants
18     mu_E = 398600.0 # [km^3/s^2] standard gravitational
      parameter of the Earth
19
20     # Handle various cases, if none then it just returns
21     # keplerian to state vector
22     if input_flag == 'keplerian' and output_flag == 'state'
  :
23         # parse
24         a = x_vec[0] # [km]
25         ecc = x_vec[1] # [none]
26         inc = np.deg2rad(x_vec[2]) # [deg]
27         Omega = np.deg2rad(x_vec[3]) # [deg]
28         omega = np.deg2rad(x_vec[4]) # [deg]
29         M_0 = np.deg2rad(x_vec[5]) # [deg]
30
31         if ecc < 1.0:
32             M = M_0 + np.sqrt(mu_E / np.power(a, 3.0)) *
delta_t
33             f = convert_M_to_f(M, 6, ecc)
34         else:
35             n = np.sqrt(mu_E / np.power(-a, 3.0))
36             N = M_0 + n*delta_t
37             f = convert_M_to_f(N, 6, ecc)
38
39         theta = omega + f
40
41         p = a * (1.0 - np.power(ecc, 2.0))
42
43         h = np.sqrt(mu_E * p)
44
45         r = p / (1.0 + ecc*np.cos(f))

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46
47     r_x = r * (np.cos(0mega)*np.cos(theta) - np.sin(
Omega)*np.sin(theta)*np.cos(inc))
48     r_y = r * (np.sin(0mega)*np.cos(theta) + np.cos(
Omega)*np.sin(theta)*np.cos(inc))
49     r_z = r * (np.sin(theta)*np.sin(inc))
50
51     v_x = -mu_E / h * (np.cos(0mega)*(np.sin(theta) +
ecc*np.sin(omega)) + np.sin(0mega)*(np.cos(theta) + ecc*np.
cos(omega))*np.cos(inc))
52     v_y = -mu_E / h * (np.sin(0mega)*(np.sin(theta) +
ecc*np.sin(omega)) - np.cos(0mega)*(np.cos(theta) + ecc*np.
cos(omega))*np.cos(inc))
53     v_z = mu_E / h * (np.cos(theta) + ecc*np.cos(omega)
)*np.sin(inc)
54
55     x_out = np.array([r_x, r_y, r_z, v_x, v_y]
, [v_z]))
56
57     return x_out
58
59     # state vector to keplerian
60     elif input_flag == 'state' and output_flag == '
keplerian':
61         # parse
62         x = x_vec[0]
63         y = x_vec[1]
64         z = x_vec[2]
65         xd = x_vec[3]
66         yd = x_vec[4]
67         zd = x_vec[5]
68
69         r_vec = np.array([x, y, z])
70         v_vec = np.array([xd, yd, zd])
71
72         r = np.linalg.norm(r_vec)
73         v = np.linalg.norm(v_vec)
74
75         one_over_a = 2.0 / r - np.power(v, 2.0) / mu_E
76         a = 1.0 / one_over_a
77
78         h_vec = np.cross(r_vec, v_vec)
79         h = np.linalg.norm(h_vec)
80
81         ecc_vec = np.cross(v_vec, h_vec) / mu_E - r_vec / r
82         ecc = np.linalg.norm(ecc_vec)
83
84         ihat_e = ecc_vec / ecc
85         ihat_h = h_vec / h
86         ihat_p = np.cross(ihat_h, ihat_e)

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87
88     PN = np.array([ihat_e.T, ihat_p.T, ihat_h.T])
89
90     Omega = np.arctan2(PN[2, 0], -PN[2, 1])
91     inc = np.arccos(PN[2, 2])
92     omega = np.arctan2(PN[0, 2], PN[1, 2])
93     ihat_r = r_vec / r
94     f = np.arctan2(np.dot(np.cross(ihat_e, ihat_r),
    ihat_h), np.dot(ihat_e, ihat_r))
95     if ecc < 1.0:
96         E = 2.0*np.arctan(np.tan(f/2.0) / np.sqrt((1.0
    + ecc)/(1.0 - ecc)))
97         M = E - ecc*np.sin(E)
98         n = np.sqrt(mu_E / np.power(a, 3.0))
99     else:
100         H = 2.0*np.arctanh(np.tan(f/2) / np.sqrt((ecc
    + 1.0) / (ecc - 1.0)))
101         M = ecc*np.sinh(H) - H
102         n = np.sqrt(mu_E / np.power(-a, 3.0))
103
104     M_0 = M - n * delta_t
105     if M_0 < 0:
106         M_0 = M_0 + 2 * np.pi
107
108     return np.array([[a], [ecc], [np.rad2deg(inc)], [
    np.rad2deg(Omega)], [np.rad2deg(omega)], [np.rad2deg(M_0)]
    ])
109
110
111     # flags are the same
112     elif input_flag == output_flag:
113         return x
114     # inputs are wrong
115     else:
116         raise ValueError('Incorrect input or output flags'
    )
117
118
119 # subroutine for newton's method to solve keplers equation
    for E (eccentric anomaly)
120 # Inputs:
121 #   x_0 - [deg] initial guess
122 #   n_iter - [none] number of iterations to be completed
123 #   ecc - eccentricity of orbit
124 # Outputs:
125 #   x_k - final solution
126 def convert_M_to_f(x_0, n_iter, ecc):
127
128     # iterate
129     x_k = x_0

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130     for k in range(n_iter):
131         # elliptic case
132         if ecc < 1.0:
133             x_k = x_k - (x_0 - (x_k - ecc*np.sin(x_k)))/-(
134             1.0 - ecc*np.cos(x_k))
135         # hyperbolic case
136         else:
137             x_k = x_k - (x_0 - (ecc*np.sinh(x_k) - x_k))/-
138             (ecc*np.cosh(x_k) - 1)
139         # elliptic case
140         if ecc < 1.0:
141             f = 2.0 * np.arctan(np.sqrt((ecc + 1.0)/(1.0 - ecc
142             )) * np.tan(x_k / 2.0))
143         # hyperbolic case
144         else:
145             f = 2.0 * np.arctan(np.sqrt((ecc + 1.0) / (ecc - 1
146             .0)) * np.tanh(x_k / 2.0))
147     return f

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