



$$H_{sc} = I_1 \omega_1 + J_s (\omega_1 + \dot{\Omega})$$

$$\dot{H}_{sc} = I_1 \dot{\omega}_1 + J_s (\dot{\omega}_1 + \ddot{\Omega}) = 0$$

$$(I_1 + J_s) \dot{\omega}_1 + J_s \ddot{\Omega} = 0 \quad (1)$$

$$H_w = J_s (\omega_1 + \dot{\Omega})$$

$$\dot{H}_w = J_s (\dot{\omega}_1 + \ddot{\Omega}) = u_s$$

$$J_s \dot{\omega}_1 + J_s \ddot{\Omega} = u_s \quad (2)$$

State space:

$$\begin{bmatrix} (I_1 + J_s) & J_s \\ J_s & J_s \end{bmatrix} \begin{bmatrix} \dot{\omega}_1 \\ \ddot{\Omega} \end{bmatrix} = \begin{bmatrix} 0 \\ u_s \end{bmatrix}$$

Used Mathematica:

$$\begin{bmatrix} \dot{\omega}_1 \\ \ddot{\Omega} \end{bmatrix} = \begin{bmatrix} -\frac{u_s}{I_1} \\ \frac{(I_1 + J_s) u_s}{I_1 J_s} \end{bmatrix}$$

$$\int d(\omega_1) = \int -\frac{u_s}{I_1} dt$$

$$\omega_1(t) = -\frac{u_s}{I_1} t + \omega_0$$

$$\int d\Omega = \int -\frac{u_s}{I_1} t + \omega_0 dt$$

$$\Omega(t) = -\frac{1}{2} \frac{u_s}{I_1} t^2 + \omega_0 t + \Omega_0$$

$$\Omega(t) = \frac{(I_1 + J_s) u_s}{I_1 J_s} t + \Omega_0$$