Formulario 1

#### Fórmulas de Derivadas

1. 
$$\frac{d}{dx}[c] = 0$$
 cualquier número  $c$ 

$$2. \ \frac{d}{dx}[x] = 1$$

$$3. \ \frac{d}{dx}[x^n] = nx^{n-1}$$

4. 
$$\frac{d}{dx}[c \cdot x^n] = c \cdot \frac{d}{dx}[x^n] = cnx^{n-1}$$

$$5. \ \frac{d}{dx}[u \pm v] = u' \pm v'$$

$$6. \ \frac{d}{dx}[u \cdot v] = uv' + vu'$$

$$7. \ \frac{d}{dx} \left[ \frac{u}{v} \right] = \frac{vu' - uv'}{v^2}$$

8. 
$$\frac{d}{dx}[u^n] = nu^{n-1} \cdot u'$$

9. 
$$\frac{d}{dx}[c \cdot u^n] = c\frac{d}{dx}[u^n] = cnu^{n-1} \cdot u'$$

$$10. \ \frac{d}{dx}[\, \mathrm{sen}\, u] = \, \mathrm{cos}u \cdot u'$$

11. 
$$\frac{d}{dx}[\cos u] = -\sin u \cdot u'$$

12. 
$$\frac{d}{dx}[\tan u] = \sec^2 u \cdot u'$$

13. 
$$\frac{d}{dx}[\cot u] = -\csc^2 u \cdot u'$$

14. 
$$\frac{d}{dx}[\sec u] = \sec u \cdot \tan u \cdot u'$$

15. 
$$\frac{d}{dx}[\csc u] = -\csc u \cdot \cot u \cdot u'$$

16. 
$$\frac{d}{dx}[\arcsin u] = \frac{u'}{\sqrt{1 - u^2}}$$

17. 
$$\frac{d}{dx}[\arccos u] = \frac{-u'}{\sqrt{1-u^2}}$$

18. 
$$\frac{d}{dx}[\arctan u] = \frac{u'}{1+u^2}$$

19. 
$$\frac{d}{dx}[\arctan u] = \frac{-u'}{1+u^2}$$

20. 
$$\frac{d}{dx}[\operatorname{arcsec} u] = \frac{u'}{u\sqrt{u^2 - 1}}$$

21. 
$$\frac{d}{dx}[\operatorname{arccsc} u] = \frac{-u'}{u\sqrt{u^2 - 1}}$$

$$22. \ \frac{d}{dx}[a^u] = a^u \ln a \cdot u'$$

$$23. \ \frac{d}{dx}[e^u] = e^u \cdot u'$$

24. 
$$\frac{d}{dx}[\log_a u] = \frac{u'}{u \ln a}$$

$$25. \ \frac{d}{dx}[\ln u] = \frac{u'}{u}$$

26. 
$$\frac{d}{dx}[\operatorname{senh} u] = \cosh u \cdot u'$$

27. 
$$\frac{d}{dx}[\cosh u] = \sinh u \cdot u'$$

28. 
$$\frac{d}{dx}[\tanh u] = \operatorname{sech}^2 u \cdot u'$$

29. 
$$\frac{d}{dx}[\operatorname{ctgh} u] = -\operatorname{csch}^2 u \cdot u'$$

30. 
$$\frac{d}{dx}[\operatorname{sech} u] = -\operatorname{sech} u \cdot \tanh u \cdot u'$$

31. 
$$\frac{d}{dx}[\operatorname{csch} u] = -\operatorname{csch} u \cdot \operatorname{ctgh} u \cdot u'$$

32. 
$$\frac{d}{dx}[\operatorname{senh}^{-1}u] = \frac{u'}{\sqrt{u^2 + 1}}$$

33. 
$$\frac{d}{dx}[\cosh^{-1}u] = \frac{u'}{\sqrt{u^2 - 1}}$$

34. 
$$\frac{d}{dx}[\tanh^{-1}u] = \frac{u'}{1-u^2}$$

35. 
$$\frac{d}{dx}[\operatorname{ctgh}^{-1}u] = \frac{u'}{1-u^2}$$

36. 
$$\frac{d}{dx}[\operatorname{sech}^{-1}u] = \frac{-u'}{u\sqrt{1-u^2}}$$

37. 
$$\frac{d}{dx}[\operatorname{csch}^{-1}u] = \frac{-u'}{u\sqrt{1+u^2}}$$

# 1. Identidades trigonométricas

1. 
$$\operatorname{sen} x = \frac{1}{\csc x}$$

2. 
$$\sec x = \frac{1}{\cos x}$$

3. 
$$\tan x = \frac{1}{\cot x}$$

9. 
$$\sin^2 x + \cos^2 x = 1$$

12. 
$$\cos^2 u = \frac{1 + \cos 2u}{2}$$

$$4. \cos x = \frac{1}{\sin x}$$

$$5. \ \cos x = \frac{1}{\sec x}$$

$$6. \cot x = \frac{1}{\tan x}$$

10. 
$$1 + \tan^2 x = \sec^2 x$$

13. 
$$\sin^2 u = \frac{1 - \cos 2u}{2}$$

15. 
$$\cos 2u = \cos^2 u - \sin^2 u = 1 - 2 \sin^2 u = 2 \cos^2 u - 1$$

7. 
$$\tan x = \frac{\sin x}{\cos x}$$

$$8. \cot x = \frac{\cos x}{\sin x}$$

11. 
$$1 + \cot^2 x = \csc^2 x$$

14. 
$$\tan^2 u = \frac{1 - \cos 2u}{1 + \cos 2u}$$

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16. 
$$\sin 2u = 2 \sin u \cos u$$

17. 
$$\tan 2u = \frac{2\tan u}{1 - \tan^2 u}$$

18. 
$$\operatorname{sen}(\cos^{-1} x) = \sqrt{1 - x^2}$$

20. 
$$\sec(\tan^{-1} x) = \sqrt{1 + x^2}$$

19. 
$$\cos(\sin^{-1}x) = \sqrt{1-x^2}$$

21. 
$$\tan(\sec^{-1} x) = \begin{cases} \sqrt{x^2 - 1} & \text{si } x \ge 1, \\ -\sqrt{x^2 - 1} & \text{si } x \le 1 \end{cases}$$

22. 
$$\cos A \cos B = \frac{1}{2} \cos[A - B] + \frac{1}{2} \cos[A + B]$$

24. 
$$sen A \cos B = \frac{1}{2} sen[A - B] + \frac{1}{2} sen[A + B]$$

23. 
$$\sin A \cos B = \frac{1}{2} \cos[A - B] - \frac{1}{2} \cos[A + B]$$

25. 
$$\operatorname{sen}[-\theta] = -\operatorname{sen}[\theta]$$
 26.  $\operatorname{cos}[-\theta] = \operatorname{cos}[\theta]$ 

27. 
$$\cos[n\pi] = [-1]^n$$
 28.  $\sin[n\pi] = 0$ 

28. 
$$sen[n\pi] = 0$$

29. 
$$\operatorname{senh} x = \frac{e^x - e^{-x}}{2}$$

31. 
$$\tanh x = \frac{\mathrm{senh}x}{\mathrm{cosh}x}$$

33. 
$$\operatorname{sech} x = \frac{1}{\cosh x}$$

30. 
$$\cosh x = \frac{e^x + e^{-x}}{2}$$

32. 
$$\operatorname{csch} x = \frac{1}{\operatorname{senh} x}$$

34. 
$$\coth x = \frac{\cosh x}{\sinh x}$$

### **Radicales**

35. 
$$\sqrt[n]{a^m} = a^{\frac{m}{n}}$$

$$36. \sqrt[n]{ab} = \sqrt[n]{a}\sqrt[n]{b}$$

$$37. \sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$$

$$38. \sqrt[m]{\sqrt[n]{a}} = \sqrt[mn]{a}$$

## **Exponentes**

39. 
$$a^n = a \cdot a \cdot a \cdot a \cdot a$$

40. 
$$a^0 = 1$$

41. 
$$a^{-n} = \frac{1}{a^n}$$

$$42. \ a^m a^n = a^{m+n}$$

43. 
$$\frac{a^m}{a^n} = a^{m-n}$$

$$44. \ (a^m)^n = a^{mn}$$

$$45. (ab)^n = a^n b^n$$

42. 
$$a^m a^n = a^{m+n}$$
 43.  $\frac{a^m}{a^n} = a^{m-n}$  44.  $(a^m)^n = a^{mn}$  45.  $(ab)^n = a^n b^n$  46.  $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$ 

## Logaritmos

47. 
$$ln(1) = 0$$

$$48. \ \ln xy = \ln x + \ln y$$

49. 
$$\ln \frac{x}{y} = \ln x - \ln y$$
 50.  $\ln x^p = p \ln x$ 

$$50. \ln x^p = p \ln x$$

51. 
$$ln(e) = 1$$

52. 
$$\ln(e^x) = x \ln(e) = x(1) = x$$
 53.  $e^{\ln x} = x$ 

$$53. e^{\ln x} = x$$