

# Battery Internal Resistance

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## Goals

To calculate the internal resistance of the 12V marine batteries in our possession in the lab. The link to purchase them is [here](#), and I have not found the datasheet for the batteries yet, with a curve of voltage vs. state of charge (SOC).

## Methodology

A battery's internal resistance manifests as a small resistance in series with the load. When we measure the battery terminals without anything between them (unloaded case), we get the true voltage of the battery. When we add a load resistor between the terminals, we get a voltage divider consisting of the load resistor and the internal resistance. The voltage across the load resistor  $R_2$  is given by  $V_{loaded} = V_{unloaded} \cdot \frac{R_2}{(R_{internal} + R_2)}$ .

Thus, the internal resistance can be calculated by  $(R_{internal} + R_2) = \frac{V_{unloaded}}{V_{loaded}} \cdot R_2$ ,

$$R_{internal} = \frac{V_{unloaded}}{V_{loaded}} \cdot R_2 - R_2 = \left( \frac{V_{unloaded}}{V_{loaded}} - 1 \right) \cdot R_2.$$

I connected a 100Ω and a 6.8Ω 5W resistor across the terminals of all three batteries that we have in the lab. The internal resistances for each test are shown below.

```
In [ ]: import numpy as np
import pandas as pd
from pint import UnitRegistry

# use pint
units = UnitRegistry()
units.default_format = "~P.2f"
```

```
In [ ]: def calculate_R1(Vin, Vout, R2):
    R1 = R2 * (Vin / Vout - 1)
    return R1

# testing 3 batteries
unloaded = np.array([12.55, 12.62, 12.86])
loaded_100ohm = np.array([12.54, 12.57, 12.85])
loaded_6_8ohm = np.array([12.24, 11.99, 12.60])

print(f"Calculated internal resistance using a 100Ω resistor: {calculate_R1(unloaded, loaded_100ohm, 100)}")
print(f"Calculated internal resistance using a 6.8Ω resistor: {calculate_R1(unloaded, loaded_6_8ohm, 6.8)}")
```

Calculated internal resistance using a  $100\Omega$  resistor: [0.07974482 0.39777247 0.07782101]

Calculated internal resistance using a  $6.8\Omega$  resistor: [0.17222222 0.35729775 0.14031746]

Using a smaller load resistance yields more precise measurements. The  $100\Omega$  and  $6.8\Omega$  resistors gave similar orders of magnitude.

The internal resistance of the first and last batteries is on the order of  $100\text{m}\Omega$ . This is a typical value for a battery's internal resistance. The middle battery has an abnormally high internal resistance approaching  $400\text{m}\Omega$ . This might be a sign that the middle battery is older or damaged.