Exhaustification, free-choice, and additivity Evidence from Sakha da(yani)

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 - Negative Polarity Items (NPIs) with WH-words, numeral biir 'one' (1):
 - (1) [Kim da(γanɨ)] [biir da kinige-ni] aax-*(pa)-ta
 [who da(γanɨ)] [one da book-ACC] read-(NEG)-PST.3SG
 'Nobody read any book(s)', lit: 'Anybody didn't read any book(s)'
 - Grammatical in negative sentences, ungrammatical in positive
 - Full da(yani) or reduced da both acceptable with WH-NPIs. The short form is preferred following quantificational adjectives like biir 'one'.

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 'Nobody read any book(s)', lit: 'Anybody didn't read any book(s)'
 - Scalar focus particle (2):
 - (2) [Onnooyor studjen da(yani)] iti kinige-ni aax-(pa)-ta [even student da(yani)] that book-ACC read-(NEG)-PST.3SG 'Even the student (didn't) read that book'
 - da(yani) outside of WH-words, biir is not as sensitive to polarity
 - (2) Expresses that it is unexpected that the student would (or would not) read the book.

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 - Doubled in coordination constructions (3):
 - (3) Djulus [kofje da(yani] [čaj da(yani)] is-(pe)-te Djulus [coffee da(yani)] [tea da(yani)] drink-(NEG)-PST.3SG
 - a. Without NEG -pe: 'Djulus drank both coffee and tea'
 - b. With NEG -pe: 'Djulus drank neither coffee nor tea'

1. Introduction

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 - Why does positive da(yani)...da(yani) resolve to a conjunction 'both...and' meaning?

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 - Semantic alternatives of a disjunction/existential, interpreted by a covert exhaustifier (Sauerland 2004, Chierchia, Fox, Spector 2008, Crnič 2011, Szabolcsi 2017)
 - Chierchia's Grammatical Theory of Polarity Sensitivity (2004, 2013)
 - c. Cross-linguistic comparison? "What do we make of the cross-linguistic similarities and differences in the distribution and interpretation of the particles?"

Role	Sakha da(γanɨ)	Hungarian is/sem	Japanese -mo	see slide
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	kim da(ɣanɨ)	akárki is, senki		(30)
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	X da(ɣanɨ)			(31)
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 - a. [Tugu da(yani)] aax-*(pa)-t-im [what.ACC da(yani)] read-(NEG)-PST-1SG 'I didn't read anything'
 - b. [Xas biirdii kinige-ni] aax-t-im [how.much each book-ACC] read-PST-1SG
 'I read every single book'
 - c. [Tuox baar kinige-ni bari-tin] aax-t-im [what exist book-ACC every-ABL] read-PST-1SG 'I read all the books'
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- Shimoyama (2011)— Japanese -mo quantifier particle forms universals
 - so-called NPI WH-mo actually PPI (i.e. $[\forall < \neg]$ rather than $[\neg < \exists]$)

Da(yani) lacks a basic additive reading (I)

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- Basic additive use possible for Hungarian is/sem (7)
 - (7) Bill $\{is / sem\}$ ásított Bill $\{is / sem\}$ yawned
 - a. (Positive, is): 'BILL yawned, too'[Presupposition= Somebody other than Bill yawned]
 - b. (Negative, sem): 'BILL didn't yawn, either'
 [Presupposition= Somebody other than Bill didn't yawn]
 (Hungarian, Szabolcsi 2017: 461)

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 - (8) Djulus {#da(γanɨ) / emie} kofje is-(pe)-te Djulus { da(γanɨ) / also} coffee drink-(NEG)-PST.3SG (Positive, emie): 'DJULUS drank coffee, too' (Negative, emie): 'DJULUS didn't drink coffee, either'

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- Lacking a basic additive use makes $da(\gamma an i)$ a unique quantifier particle

Da(yani) does not appear in FCIs

- (9) [Kim $\{*da(yani) / bayarar\}$] alaadji sie-n söp buoluo [who $\{da(yani) / PTCL\}$] pancake eat-CVB can maybe (With bayarar): 'Anyone can eat pancakes' (Sakha)
- (10) [Bárki (is)] jön meg, engedd be [anyone is] come.3SG VRB.MODIFIER let.2SG.IMP VRB.MODIFIER 'Whoever arrives, let him in' / 'Let anybody who arrives in' (Hungarian, Halm 2016: 130)

Da(yani)'s scalar focus reading is compatible with free-choice implicature

- (11) Sakha
 - a. Iti kinige-ni [ehe-em da(yani)] aay-ian söp that book-ACC [grandfather-1SG da(yani)] read-FUT can
 - (i) 'Even MY GRANDFATHER can read that book'
 - (ii) 'Anyone can read that book, even MY GRANDFATHER'

- (12) Hungarian (Szabolcsi 2017: 460)
 - a. [Akár Mari is] nyerhet $[akár \ {\rm Mari} \ is] \ {\rm can.win}$ 'Anyone can win; to pick an arbitrary example, Mari'

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- da(yani) does not form FCIs, unlike Hungarian is in (12-a). (11-a) is a free-choice implicature over the even-use

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 - Szabolcsi (2017)— additive too quantifier particles cause recursive exhaustification of a subset of the alternatives
 - Da(yani) does not do so
 - Recursive exhaustification IS responsible for the 'both...and' reading of da(yani)...da(yani), thought it is caused by each instances of the particle activating the alternatives of its host disjunct

Exhaustification and The Grammatical Theory of Polarity Sensitivity

• Chierchia (2004, 2013)—

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 - (13) $\begin{array}{ll} \mathsf{O}_{\mathsf{ALT}}(\phi) = \phi \wedge \forall \psi \in \mathsf{ALT}[\psi \to \phi \subseteq \psi], \\ \mathsf{where} \ `\subseteq' \ \mathsf{means} \ `\mathsf{entails}' \end{array}$ (Chierchia 2013: 31)
 - O(nly) (13) asserts proposition with alternatives ϕ ("prejacent") and negates all alternatives of ϕ which ϕ does not entail. $\phi = T$, non-entailed ALT(ϕ)= F

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 where ' \subseteq ' means 'entails' (Chierchia 2013: 31)

- O(nly) (13) asserts proposition with alternatives ϕ ("prejacent") and negates all alternatives of ϕ which ϕ does not entail. $\phi = T$, non-entailed ALT(ϕ)= F
- If negation of ALT(ϕ) contradicts ϕ : ordinary scalars prune contradiction (Relevance); PIs become uninterpretable (ALTs not subject to Relevance)

- First, take a positive example
- (14) *Djulus [tugu da(γ ani)] aax-ta Djulus [what.ACC $da(\gamma ani)$] read-PST.3SG '*Djulus read anything'

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- (14) *Djulus [tugu da(yanɨ)] aax-ta
 Djulus [what.ACC da(yanɨ)] read-PST.3SG
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- $(15) \qquad \text{a.} \quad \llbracket \mathsf{tugu} \ \mathsf{da}(\gamma \mathsf{an} \dot{\boldsymbol{+}}) \rrbracket = \llbracket \mathsf{anything}_{\mathsf{NPI}} \rrbracket = \lambda \mathsf{P}_{\langle \mathsf{et}, \mathsf{t} \rangle}. \ \exists \mathsf{x} \ [\mathsf{THING}(\mathsf{x}) \land \mathsf{P}(\mathsf{x})]$
 - b. $[(14)] = \exists x[THING(x) \land READ(djulus, x)]$

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- (14) *Djulus [tugu da(γanɨ)] aax-ta Djulus [what.ACC da(γanɨ)] read-PST.3SG '*Djulus read anything'
- (15) a. $[[tugu \ da(\gamma ani)]] = [[anything_{NPI}]] = \lambda P_{\langle et,t \rangle}$. $\exists x \ [THING(x) \land P(x)]$ b. $[[(14)]] = \exists x [THING(x) \land READ(djulus, x)]$
 - Assume domain contains two things: Syntactic Structures and Aspects. (15-b) is equivalent to a disjunction (p \vee q) where $[\![p]\!]$ = 'Djulus read Syntactic Structures' and $[\![q]\!]$ = 'Djulus read Aspects'

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$$\underbrace{(\mathsf{p} \vee \mathsf{q}) \wedge \neg (\mathsf{p} \vee \mathsf{q})}_{\mathsf{Contradiction!}}$$

- Under negation . . .
 - (17) a. Djulus [tugu da(yanɨ)] aax-pa-ta
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 'Djulus didn't read anything'
 - b. $[(17-a)] = \neg \exists x [THING(x) \land READ(djulus, x)] = \neg (p \lor q)$

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- $\bullet \ \mathsf{ALT}(\neg(\mathsf{p}\vee\mathsf{q})) = \{\neg(\mathsf{p}\vee\mathsf{q}), \neg\mathsf{p}, \neg\mathsf{q}, \neg(\mathsf{p}\wedge\mathsf{q})\}$

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 - All of these alternatives are entailed by the prejacent $\neg(p \lor q)$. None can be eliminated by exhaustification. No contradiction

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 where ' $\phi <_{\mu} \psi$ '= ϕ is less likely than ψ w.r.t. a probability metric μ

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 - (20) *Djulus [biir da kinige-ni] aax-ta
 Djulus [one da book-ACC] read-PST.3SG
 '*Djulus read any book'
 - a. $[\![(20)]\!] = \exists x [n(x) \land \mathsf{BOOK}(x) \land \mathsf{READ}(\mathsf{djulus},\mathsf{book}) : |n| = 1]$
 - b. $ALT(20-a)=\{one\ book \Leftarrow two\ books \Leftarrow three\ books \Leftarrow ...\}$

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 - (21) $\mathsf{E}_{\mathsf{ALT}}(20) = \mathsf{one} \; \mathsf{book} \land \forall \mathsf{p} \in \mathsf{ALT}[\mathsf{one} \; \mathsf{book} <_{\mu} \mathsf{p}]$
 - a. i.e. one book $<_{\mu}$ two books $<_{\mu}$ three books... Unsatisfiable! *two* entails *one* (and so forth)



E(ven) exhaustification (II)

- Under negation, these entailments are reversed (22-b)
 - (22) Djulus [biir da kinige-ni] aax-pa-ta
 Djulus [one da book-ACC] read-NEG-PST.3SG
 'Djulus didn't read any book(s)'
 - a. $[\![(22)]\!] = \neg \exists x [n(x) \land \mathsf{BOOK}(x) \land \mathsf{READ}(\mathsf{djulus}, x) : |n| = 1]$
 - b. ALT(22-a)=

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 - a. $\begin{tabular}{ll} $[(22)]] = \neg \exists x [n(x) \land \mathsf{BOOK}(x) \land \mathsf{READ}(\mathsf{djulus},x) : |n| = 1] \end{tabular}$
 - b. ALT(22-a) =

 $\left\{ \neg \mathsf{one}\;\mathsf{book} \Rightarrow \neg \mathsf{two}\;\mathsf{books} \Rightarrow \neg \mathsf{three}\;\mathsf{books} \Rightarrow ... \right\}$

- (23) $\mathsf{E}_{\mathsf{ALT}}(22\text{-a}) = \neg \mathsf{one} \; \mathsf{book} \land \forall \mathsf{p} \in \mathsf{ALT}[\neg \mathsf{one} \; \mathsf{book} <_{\mu} \mathsf{p}]$
- (23) is satisfiable. See Crnič (2011, 2014)

Where do quantifier particles fit in? (I)

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- In languages like Sakha, Hungarian, quantifier particles are crucial to resulting meaning.
- Sakha WH-words without da(yani) are not NPIs (24-a). Likewise biir 'one' without da (24-b).
- (24) a. (i) Min [tugu da(γ ani)] aax-*(pa)-t-im I [what.ACC $da(\gamma ani)$] read-(NEG)-PST-1SG 'I didn't read anything'
 - (ii) Min [tugu] aax-(pa)-t-im? 'What did I (not) read?'
 - b. (i) Min [biir da kinige-ni] aax-*(pa)-t-im I [one da book-ACC] read-(NEG)-PST-1SG 'I didn't read anything'
 - (ii) Min [biir kinige-ni] aax-(pa)-t-im
 'I (didn't) read one book'

Where do quantifier particles fit in? (II)

- Hungarian vala-WH only NPIs with is/sem. Positive polarity items (PPIs) without is/sem (25-b) (Tóth 1999, Szabolcsi 2015, 2017)
 - (25) a. *(Nem) hiszem, hogy [vala-ki is] el jön (NEG) believe.1SG that [some-who is] PRT come.3SG 'I do not think that anyone will come'
 - b. (*Nem) hiszem, hogy [vala-ki] el jön'I think that someone will come' (Halm 2016: 144)

Where do quantifier particles fit in? (III)

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 - ▶ Existentials (e.g. *some*, WH-words) ALTs = $\langle \exists, \forall \rangle = \langle \lor, \land \rangle$
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- ullet Quantifier particles like $da(\gamma ani)$, is/sem activate these alternatives (i.e. make them obligatory)

3. NPIs and focus Focus with E(ven)

 even-focus reading of da(yani) a product of the particle activating the alternatives of an element under focus

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(26) [(onnooyor) Djulus da(yanɨ)] aax-(pa)-ta

[(even) Djulus da(yanɨ)] read-(NEG)-PST.3SG

'Even DJULUS (didn't) read'
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- Exhaustification with E(ven)— if the ALTs in (27-b) are probability ranked and Djulus is the least likely ALT, interpretable. Pragmatically ranked
- $\{(\neg) \text{READ(d)} < \mu(\neg) \text{READ(e)}, (\neg) \text{READ(d)} <_{\mu} \text{READ(s)} \}$ where X $<_{\mu}$ Y says 'X is pragmatically less likely than Y'

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 - da(yani)...da(yani)'s 'both...and' reading is a free-choice-like effect
- Connection to additivity—Szabolcsi's (2017) bifurcation of focus alternatives

- The signature property of free-choice is a modal scoping over a disjunction of alternatives (28-a) becoming **enriched** to a conjunction (28-b), where each of the alternatives are acceptable (Chierchia 2013: 89)
 - (28) Djulus can drink coffee, tea, or water.



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- a. $\Diamond(p \lor q \lor r)$ =D. can drink coffee, OR can drink tea, OR can drink water.
- b. $\Diamond p \wedge \Diamond q \wedge \Diamond r$ =D. can drink coffee AND can drink tea AND can drink water

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- enrichment of (28-a) to (28-b) a free-choice implicature involving *or*-disjunction.
- Chierchia (2013)— meaning of FCIs like English *any*, Italian *un N qualsiasi* 'any N whatsoever', German *irgend* 'some or other' similar reasoning

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- Consider a prejacent with three alternatives and no modal: $(p \lor q \lor r)$
- ALT(p \vee q \vee r) = $\begin{array}{c|cccc} \hline & & & & & & & \\ \hline (p \lor q \lor r) & & & & & \\ (p \lor q) & & & & & & \\ p & & & & & r \\ & & & & & & \\ p & & & & & r \\ & & & & & \\ & & & & & \\ \hline (p \land q \land r) & & & & \\ \hline \end{array} \right) \ \, \begin{array}{c} \text{(Prejacent)} \\ \text{(Subdomain ALTs)} \\ \text{(Scalar ALT)} \\ \end{array}$

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$$ALT(p \lor q) = \{(p \lor q), p, q, r\}$$

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 - Exhaustify not only the prejacent's alternatives, but also the alternatives of the subdomain alternatives. Will require a modal to be interpretable
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- $\begin{array}{c|c} \bullet & \mathsf{ALT}(\mathsf{p} \lor \mathsf{q} \lor \mathsf{r}) = \\ \hline & (\mathsf{p} \lor \mathsf{q} \lor \mathsf{r}) \\ & \mathsf{O}(\mathsf{p} \lor \mathsf{q}) & \mathsf{O}(\mathsf{q} \lor \mathsf{r}) & \mathsf{O}(\mathsf{p} \lor \mathsf{r}) \\ & \mathsf{Op} & \mathsf{Oq} & \mathsf{Or} \\ & (\mathsf{p} \land \mathsf{q} \land \mathsf{r}) & (\mathsf{Scalar} \ \mathsf{ALT}) \\ \hline \\ (29) & \mathsf{a.} & \mathsf{ALT}(\mathsf{p} \lor \mathsf{q}) = \{(\mathsf{p} \lor \mathsf{q}), & \mathsf{p}, \mathsf{q}, \mathsf{r}\} \\ & \mathsf{b.} \end{array}$

- Recursive exhaustification with O(nly) (Fox 2007, Fox and Katzir 2011, Chierchia, Fox and Spector 2008, Chierchia 2013)
 - Exhaustify not only the prejacent's alternatives, but also the alternatives of the subdomain alternatives. Will require a modal to be interpretable
- \bullet Consider a prejacent with three alternatives and no modal: (p \vee q \vee r)

(29) a.
$$ALT(p \lor q) = \{(p \lor q), p, q, r\}$$

$$entail (p \lor q)$$
b.
$$O_{ALT}(p \lor q) = (p \lor q) \land \neg r$$

$$\begin{array}{c|c} (p \lor q \lor r) \\ \hline O(p \lor q) \\ = [(p \lor q) = \land \neg r] \\ \hline O(p) \\ = [p \land \neg (q \lor r)] \\ \hline (p \land q \land r) \\ \hline \end{array} \begin{array}{c} (p \lor q \lor r) \\ \hline O(q \lor r) \\ = [(q \lor r) \land \neg p] \\ \hline O(q) \\ = [q \land \neg (p \lor r)] \\ \hline (p \land q \land r) \\ \hline \end{array} \begin{array}{c} O(p \lor r) \\ = [(p \lor r) \land \neg q] \\ \hline O(r) \\ = [r \land \neg (p \lor q)] \\ \hline \end{array}$$

FCIs through recursive exhaustification (II)

$$\begin{array}{|c|c|c|c|}\hline O(p\vee q) & & & & O(p\vee r)\\\hline O(p\vee q) & & & O(q\vee r)\\\hline O(p) & & & O(q)\\\hline = [p\wedge\neg(q\vee r)] & & O(q)\\\hline = [q\wedge\neg(p\vee r)] & & O(r)\\\hline (p\wedge q\wedge r) & & & [r\wedge\neg(p\vee q)]\\\hline \end{array}$$

$$\begin{array}{c} \text{(30)} & \text{O}_{\mathsf{Exh-ALT}}(\mathsf{p} \vee \mathsf{q} \vee \mathsf{r}) = \\ & \underbrace{(\mathsf{p} \vee \mathsf{q} \vee \mathsf{r}) \wedge \neg ((\mathsf{p} \vee \mathsf{q}) \wedge \neg \mathsf{r}) \wedge \neg (\mathsf{r} \wedge \neg (\mathsf{p} \vee \mathsf{q})) \wedge ... \wedge \neg (\mathsf{p} \wedge \mathsf{q} \wedge \mathsf{r})}_{\mathsf{prejacent}} \\ & \underbrace{\mathsf{Exhaustified domain ALTs}} \\ \end{array}$$

FCIs through recursive exhaustification (II)

$$\begin{array}{|c|c|c|c|}\hline O(p\vee q) & & & & O(p\vee r)\\\hline O(p\vee q) & & & O(q\vee r)\\\hline O(p) & & & O(q)\\\hline = [p\wedge\neg(q\vee r)] & & O(q)\\\hline = [q\wedge\neg(p\vee r)] & & O(r)\\\hline (p\wedge q\wedge r) & & & [r\wedge\neg(p\vee q)]\\\hline \end{array}$$

$$(30) \qquad O_{\mathsf{Exh-ALT}}(p \lor q \lor r) = \\ \underbrace{(p \lor q \lor r)}_{\mathsf{prejacent}} \underbrace{(\neg((p \lor q) \land \neg r)}_{(p \lor q) \to r} \land \underbrace{\neg(r \land \neg(p \lor q))}_{r \to (p \lor q)} \land \dots \land \neg(p \land q \land r)}_{\mathsf{Scalar-ALT}}$$

FCIs through recursive exhaustification (II)

$$\begin{array}{|c|c|c|}\hline & & & & & & & & \\ \hline O(p\vee q) & & & & & & & \\ =[(p\vee q)=\wedge\neg r] & & & & & & & \\ O(p) & & & & & & \\ =[p\wedge\neg(q\vee r)] & & & & & & \\ \hline O(q) & & & & & & \\ =[q\wedge\neg(p\vee r)] & & & & & & \\ \hline (p\vee q\vee r) & & & & & \\ \hline O(q\vee r) & & & & & \\ O(q) & & & & & \\ \hline O(q) & & & & & \\ =[q\wedge\neg(p\vee r)] & & & & & \\ \hline O(r) & & & & \\ &[p\wedge q\wedge r) & & & & \\ \hline \end{array}$$

(30)
$$O_{\mathsf{Exh-ALT}}(p \lor q \lor r) = \underbrace{(p \lor q \lor r) \land \neg((p \lor q) \land \neg r) \land \neg(r \land \neg(p \lor q))}_{\mathsf{prejacent}} \land \dots \land \neg(p \land q \land r)}_{\mathsf{(p \lor q)} \leftrightarrow r} \land \dots \land \neg(p \land q \land r)$$

FCIs through recursive exhaustification (II)

$$\begin{array}{c|c} (p \lor q \lor r) \\ \hline O(p \lor q) \\ = [(p \lor q) = \land \neg r] \\ \hline O(p) \\ = [p \land \neg (q \lor r)] \\ \hline (p \land q \land r) \\ \hline \end{array} \begin{array}{c} (p \lor q \lor r) \\ \hline O(q \lor r) \\ = [(q \lor r) \land \neg p] \\ \hline O(q) \\ = [q \land \neg (p \lor r)] \\ \hline (p \land q \land r) \\ \hline \end{array} \begin{array}{c} O(p \lor r) \\ = [(p \lor r) \land \neg q] \\ \hline O(r) \\ = [r \land \neg (p \lor q)] \\ \hline \end{array}$$

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$$S_{\mathsf{calar-ALT}}$$

FCIs through recursive exhaustification (II)

 $O_{\mathsf{E} \times \mathsf{h} - \mathsf{A} \mathsf{I} \mathsf{T}}(\mathsf{p} \vee \mathsf{q} \vee \mathsf{r}) =$

• After exhaustifying the subdomain ALTs, exhaustify the prejacent (p \lor q \lor r) with respect to these (pre-exhaustified) alternatives:

$$\begin{array}{|c|c|c|c|}\hline O(p\vee q) & & & & O(p\vee r)\\\hline O(p\vee q) & & & O(q\vee r)\\\hline O(p) & & & O(q)\\\hline = [p\wedge\neg(q\vee r)] & & O(q)\\\hline = [q\wedge\neg(p\vee r)] & & O(r)\\\hline (p\wedge q\wedge r) & & & O(r)\\\hline \end{array}$$

$$(p \lor q \lor r) \land \neg ((p \lor q) \land \neg r) \land \neg (r \land \neg (p \lor q)) \land \dots \land \neg (p \land q \land r)$$

$$prejacent \qquad (p \lor q) \rightarrow r \qquad r \rightarrow (p \lor q) \qquad Scalar-ALT$$

$$(p \lor q) \leftrightarrow r$$

$$a. = (p \lor q \lor r) \land (p \leftrightarrow q \leftrightarrow r) \land \neg (p \land q \land r) \qquad Contradiction!$$

(30)

 If we repeat the above steps with a possibility modal, exhaustification produces the free-choice reading.

FCISs through recursive exhaustification (III)

 If we repeat the above steps with a possibility modal, exhaustification produces the free-choice reading.

$$\begin{array}{ll} \text{(31)} & \text{a.} & \text{O}_{\mathsf{Exh-ALT}}(\lozenge(\mathsf{p}\vee\mathsf{q}\vee\mathsf{r})) = \\ & & \lozenge(\mathsf{p}\vee\mathsf{q}\vee\mathsf{r}) \land \neg \mathsf{O}(\lozenge\mathsf{p}\vee\mathsf{q}) \land \dots \land \neg \lozenge(\mathsf{p}\land\mathsf{q}\land\mathsf{r}) \\ & \text{b.} & = \lozenge(\mathsf{p}\vee\mathsf{q}\vee\mathsf{r}) \land (\lozenge\mathsf{p}\leftrightarrow\lozenge\mathsf{q}\leftrightarrow\lozenge\mathsf{r}) \land \neg \lozenge(\mathsf{p}\land\mathsf{q}\land\mathsf{r}) \\ \end{array}$$

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 Each alternative is acceptable in some world, so long as all alternatives are not true in any single world

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$$\begin{array}{ll} \text{(31)} & \text{ a. } & \text{O}_{\mathsf{Exh-ALT}}(\lozenge(p \lor q \lor r)) = \\ & & \lozenge(p \lor q \lor r) \land \neg O(\lozenge p \lor q) \land \dots \land \neg \lozenge(p \land q \land r) \\ & \text{ b. } & = \lozenge(p \lor q \lor r) \land (\lozenge p \leftrightarrow \lozenge q \leftrightarrow \lozenge r) \land \neg \lozenge(p \land q \land r) \\ \end{array}$$

 Each alternative is acceptable in some world, so long as all alternatives are not true in any single world

Why does da(yani) not form FCIs?

• It only activates the alternatives of the prejacent, NOT the alternatives of the subdomain alternatives. i.e. it only forces simple exhaustification

Positive da(yani)...da(yani) is free-choice like

• Positive $da(\gamma ani)...da(\gamma ani)$ coordination resembles the strengthening of a disjunction to a conjunction seen in free-choice

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 - (32) a. Djulus [kofje da(γ ani čaj da(γ ani)] is-te Djulus [coffee $da(\gamma ani)$ tea $da(\gamma ani)$] drink-PST.3SG 'Djulus drank both coffee and tea'
 - b. Djulus [kofje da(yani) čaj da(yani)] is-pe-te Djulus [coffee da(yani) tea da(yani)] drink-NEG-PST.3SG
 - (i) 'Djulus didn't drink coffee or tea' $\sqrt{[\neg(p \lor q)]}$
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- $da(\gamma ani)...da(\gamma ani)$ cannot scope over negation (32-b-ii)
- No modal in required for both...and reading (32-a)

Strengthening or to and

- If no stronger scalar alternative (p \land q) is present, recursive exhaustification with O(nly) can strengthen or to and
 - Bowler (2014) on Warlpiri manu 'or/and', Bar-Lev and Margulis (2014) on Hebrew kol 'all/any', see Szabolcsi (2017: 461) for others

b.

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 - (33) a. $ALT(p \lor q) = \{p \lor q, p, q\}$ b.

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$$\begin{array}{ccc} \text{(33)} & \text{ a.} & \text{ALT}(p \vee q) = \{p \vee q, p, q\} \\ & \text{ b.} & \text{O}_{\mathsf{Exh-D-ALT}}(p \vee q) = \underbrace{(p \vee q)}_{\mathsf{prejacent}} \wedge \neg \mathsf{O}(p) \wedge \neg \mathsf{O}(q) \\ \end{array}$$

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$$\underbrace{((p \lor q) \land (p \leftrightarrow q))}_{p \leftrightarrow q} \equiv (p \land q)$$

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Hebrew *kol* 'all/any', see Szabolcsi (2017: 461) for others

(33)

a.
$$ALT(p \lor q) = \{p \lor q, p, q\}$$

b. $O_{Exh-D-ALT(p\lor q)} = \underbrace{(p \lor q)}_{prejacent} \land \underbrace{\neg O(p)}_{p \to q} \land \underbrace{\neg O(q)}_{q \to p}$

$$\underbrace{\neg (p \land \neg q)}_{p \to q} \underbrace{\neg (q \land \neg p)}_{q \to p}$$

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Absence of stronger scalar alternative is key

• If the scalar alternative is included, we would reach a contradiction:

$$ightharpoonup = (p \lor q) \land (p \leftrightarrow q) \land \neg (p \land q) = \bot$$

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Absence of stronger scalar alternative is key

- If the scalar alternative is included, we would reach a contradiction:
 - $ightharpoonup = (p \lor q) \land (p \leftrightarrow q) \land \neg(p \land q) = \bot$
- Sakha da(ɣanɨ)...da(ɣanɨ) underlyingly disjunction. Da(ɣanɨ) activates each disjunct's ALTs, resulting in recurs EXH. Doubling a morphosyntactic reflex of recurs EXH

(34) [Bill is] ástított
[Bill is] yawn.PST.3SG

'BILL yawned, too' (Hungarian, Szabolcsi 2017: 462)
Bill yawned AND somebody other than Bill yawned

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 - (36) a. BI-ALT(34)= $\{\{b\}, \{m \lor k\}\}\$ = $[b \lor (m \lor k)]$ b.

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 - $(36) \qquad \text{a.} \qquad \text{BI-ALT}(34) = \left\{ \{b\}, \{m \vee k\} \right\} \\ \text{b.} \qquad O_{\mathsf{Exh-BI-ALT}}(b) = \underbrace{\textbf{b}}_{\mathsf{prejacent}} \land \neg O(b) \land \neg O(m \vee k)$

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 - (36) a. BI-ALT(34)= $\{\{b\}, \{m \lor k\}\}\$ = $[b \lor (m \lor k)]$ b. $O_{E \lor b \to RI \to AI \to (b)} = b \land (b \leftrightarrow (m \lor k))$

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- Result (36-b) is the additive presupposition: Bill IS yawned = T only if one of the ALTs Mary yawned, Katalin yawned is T.

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(36) a. BI-ALT(34)=
$$\{\{b\}, \{m \lor k\}\}\$$
 = $[b \lor (m \lor k)]$
b. $O_{\mathsf{E} \mathsf{x} \mathsf{h} - \mathsf{B} \mathsf{l} - \mathsf{ALT}}(b) = b \land (b \leftrightarrow (m \lor k))$

- Result (36-b) is the additive presupposition: Bill IS yawned = T only if one of the ALTs Mary yawned, Katalin yawned is T.
- Sakha da(yani) lacks basic additive reading because it does not bifurcate its alternatives

5. Conclusion

- Sakha $da(\gamma ani)$ is a particle which activates alternatives of a host disjunction
- When the host is a low-point of scale existential like a WH-word or biir 'one', activation of alternatives forms NPI
- When the host is a focused element, the elements are not inherently ordered, rather only being ordered by pragmatic context
- When it marks each disjunct in a disjunction phrase, da(yani) results in a
 'both...and' reading in positive sentences, but an 'or' reading scoping under
 negation. The positive reading is a result of each alternative (disjunct) being
 marked as having obligatorily active alternatives, resulting in recursive
 exhaustification, strengthening the disjunction to a conjunction
- By itself, da(yani) does not encode that alternatives need be recursively exhaustified (i.e. it does not pre-exhaustify, nor does it bifurcate alternatives), explaining its lack of FCI, basic additive uses

Acknowledgments

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Additional notes and data Transcription

- Native Cyrillic for the particle is <дађаны>. Other romanizations include:
 - dayanı (Krueger 1962: 115)
 - dayanï (Stachowski and Menz 1998: 423)
 - daqany (Vinokurova 2005; Baker and Vinokurova 2010)

Additional notes and data Licensing of da(yani) (I)

- Da(yani) NPIs are licensed by many negative morphemes, such as verbal negation with -BA (see (1)), negative copulas suox (37-a) and ilik (37-b), negative converb -BAkkA (37-c), and the prohibitive -ImA (37-d)
 - (37) a. [Tuox da(yani) siala] {suox / *baar} suruj-but-um [what da(yani) purpose] {NEG.COP / COP} write-PST-1sG 'I wrote for no reason'
 - b. [Kim da(yani)] [biir da kinige] aax-a ilik [who da(yani)] [one da book] read-CVB COP.not_yet 'Nobody has read any book(s) yet' (Lit. 'Anybody has not read any book yet'
 - c. [Tugu da(yanɨ)] aax-pakka ereeri üören-n-im [what.ACC da(yanɨ)] read-NEG.CVB though study-PST-1SG 'I studied without reading anything'
 - d. [Tugu da(yani)] {aay-ima / *aax} [what.ACC da(yani)] {read-NEG.IMP / read.IMP} 'Don't read anything!'

Additional notes and data Licensing of da(yani) (II)

- $Da(\gamma ani)$ NPIs also licensed by the comparative case morpheme $-T\bar{A}\gamma ar$ (38)
 - (38) Tujara [kim-neeyer da(yani)] uhun Tujara [who-CMPR da(yani)] tall 'Tujara is taller than anyone'
- Not licensed in antecedent of conditionals (39-a) or polar questions (39-b)
 - (39) a. *[Tujara [tugu da(yanɨ)] onŋor-doyuna] Djulus čaj [Tujara [what.ACC da(yanɨ)] repair-COND.3SG] Djulus tea kut-an bier-iexteex pour-CVB give-FUT.3SG Intended: 'If Tujara repairs anything, Djulus will serve tea'
 - b. *[Kim da(yani)] kofje ih-er=ij? [who da(yani)] coffee drink-PRES.3SG=Q Intended: 'Does anyone drink coffee?'
- These NPIs thus strict (or "strong") NPIs, requiring Anti-Additive licensers rather just simply Downward Entailing (Zwarts 1998, Gajewski 2011)

Additional notes and data Licensing of da(yani) (III)

- $Da(\gamma ani)$ NPIs are not negative-concord items. Fail main diagnostic—ability to serve as a negative fragment answer to a non-negative question (Zanuttini and Portner 2003, Chierchia 2013: 238)
 - (40) Question: Tugu beyehee aax-pɨk-kɨn=ɨj?
 what.ACC yesterday read-PST-2SG=Q
 'What did you read yesterday?'
 - a. Negative answers:
 - (i) #Tugu da(yanɨ)
 what.ACC da(yanɨ)
 intended: 'nothing'
 - (ii) Tugu da(γ ani) aax-pa-tay-im what.ACC $da(\gamma ani)$ read-NEG-PST-1SG 'I didn't read anything'

Additional notes and data: Sakha, Hungarian, and Japanese NPIs

- (41) a. Sakha da(γanɨ)
 - (i) Min [kimi da(γanɨ)] kör-*(bö)-t-üm
 I [who.ACC da(γanɨ)] see-(NEG)-PST-1SG
 'I didn't see anyone'
 - b. Hungarian is/sem
 - (i) Pál *(nem) látott [sen-ki-t]
 Paul (NEG) saw sem-who-ACC
 'Paul did not see anybody'
 - (ii) Pál *(nem) mondta, hogy Mária [vala-ki-t is] látott Paul (NEG) said that Mary [vala-who is] saw 'Paul did not say that Mary saw anybody' (Tóth 1999: 126)
 - c. Japanese -mo
 - (i) Yoko-ga [gakusei-o **dare-mo**] syootaisi-*(nakat)-ta Yoko-NOM [student-ACC who-mo] invite-(NEG)-PST 'Yoko didn't invite any student' (Shimoyama 2011: 417)

(Tóth 1999: 125)

Additional notes and data: Even particle

- (42) a. Sakha da(γanɨ)
 - (i) [?(Onnooyor) studjen da(yani)] iti kinige-ni aax-ta [(even) student da(yani)] that book-ACC read-PST.3SG 'Even THE STUDENT read that book'
 - (ii) [(Onnooyor) studjen da(yani)] iti kinige-ni aax-pa-ta [(even) student da(yani)] that book-ACC read-NEG-PST.3SG 'Even THE STUDENT didn't read that book'
 - b. Hungarian is/sem
 - (i) Éva szerenscére [még János-t is] meg hívta
 Eve luckily [even John-ACC is] VRB.MODIFIER invite.PST

 'Eve luckily invited even John' (Kiss 2004: 108)
 - (ii) Nem jött el [egy diák sem]

 NEG come.PST VRB.MODIFIER [one student sem]
 - 'No student came' / 'Not even one student came' (Kiss 2004: 140)
 - c. Japanese -mo
 - (i) [Sono syoonin-mo] damatteita
 [that witness-mo] was.silent

 'Even that witness was silent / That witness was also silent'

 (Shimovan

(Shimoyama 2006: 145)

(ii) John-wa [hon A -mo] yom-ana-katta John-top [book A -mo] read-NEG-PST'John didn't even read book A'

(Nakanishi 2006: 142)

Additional notes and data: Doubled in 'both...and' coordination

- (43) a. Sakha da(yanɨ)
 - (i) [Djulus da(yani) Tujara da(yani)] kofje is-pit-ter
 [Djulus da(yani) Tujara da(yani)] coffee drink-PST-3PL
 'Both D. and T. drank coffee'
 - (ii) Min [kinige da(yani) aax-t-im) suruk da(yani) suruj-d-um] I [book da(yani) read-PST-1SG letter da(yani) write-PST-1SG] 'I both read a book and wrote a letter' / 'In addition to reading a book, I even wrote a letter'
 - b. Hungarian is/sem
 - (i) [Kati is Mari is] alud-t [Kati is Mari is] sleep-pst.3sg 'Both K. and M. slept' / 'K. as well as M. slept'
 - (Szabolcsi 2018: 5)

- c. Japanese -mo
 - (i) Takashi-wa [tyuukan-siken-ni-mo kimatu-siken-ni-mo] ukat-ta Takashi-TOP [midterm-exam-DAT-mo term.end-exam-DAT-mo] pass-PST 'T. passed both the midterm and the final' (Shimoyama 2011: 439)

Additional notes and data: Doubled in 'neither...nor' coordination

(44) a. Sakha

(i) [Djulus da(γanɨ) Tujara da(γanɨ) kofje is-pe-tex-ter
 [Djulus da(γanɨ) Tujara da(γanɨ)] coffee drink-NEG-PST-3PL
 'Neither D. nor T. drank coffee'

b. Hungarian

- (i) [Kati sem (és) Mari sem] alud-t[Kati sem (and) Mari sem] sleep-pst.3sg
- (ii) [Sem Kati sem Mari] nem alud-t [sem Kati sem Mari] NEG sleep-PST.3SG 'Neither K. nor M. slept'

(Szabolcsi 2018: 20)

c. Japanese

(i) Takashi-wa [tyuukan-siken-ni-mo kimatu-siken-ni-mo]
Takashi-ToP [midterm-exam-dat-mo term.end-exam-dat-mo]
ukara-nakat-ta
pass-NEG-PST

'T. didn't pass the midterm or the final' / 'For both the midterm and the final, T. didn't pass them' (Shimoyama 2011: 439)

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