Homework 2: Horseshoe Vortex Method

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1. Efecto del alargamiento en el $c_{L,\alpha}$

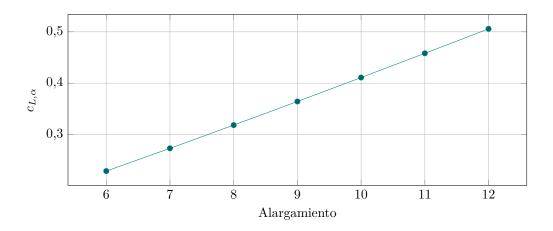


Figura 1: Caption

2. Efecto de la flecha en el $c_{L,\alpha}$ y el x_{ac}

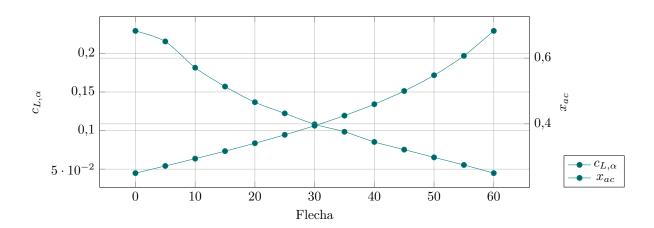


Figura 2: Caption

3. Efecto del estrechamiento en la distribución de sustentación local

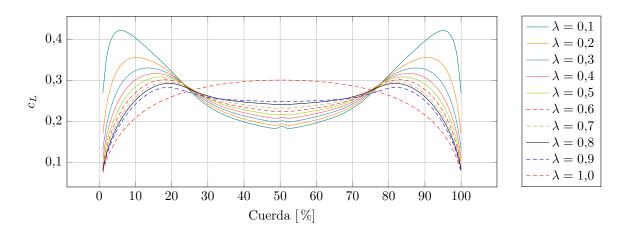


Figura 3: Caption

4. Efecto del estrechamiento y la flecha en el factor de eficiencia de Oswald

5. Apéndice: Código

```
function [ midPoints, controlPoints, bounded_nodes, trailing_nodes, panelAngles,
       panel Areas \ ] \ = \ wing\_discretization (aspect Ratio \, , \ taper Ratio \, , \ quarter Chord Sweep \, ,
       angleOfAttack, wingTipTwist, nPanels)
    % wing_discretization: Returns a vector of points along the quarter chord line of the
     % wing, each centered along the y axis of every panel. Also returns the control points
    \% at 3c/4 and the angle of every panel after applying angle of attack and twist.
    midPoints = zeros(nPanels, 3);
    controlPoints = zeros(nPanels, 3);
    bounded_nodes = zeros(nPanels+1, 3);
    trailing_nodes = zeros(nPanels+1, 3);
    panelAngles = zeros(nPanels, 1);
    panelAreas = zeros(nPanels, 1);
    %Compute y, which is distributed linearly
    panelWidth = 1/nPanels;
    lastY = 0.5 - panelWidth/2;
    midPoints(:, 2) = linspace(-lastY, lastY, nPanels);
    controlPoints (:, 2) = linspace(-lastY, lastY, nPanels);
    bounded\_nodes\left(:,\ 2\right) \ = \ \underset{}{\texttt{linspace}}\left(-0.5,\ 0.5\,,\ nPanels+1\right);
    trailing_nodes(:, 2) = linspace(-0.5, 0.5, nPanels+1);
    %Compute some needed constants
    surfaceArea = 1/aspectRatio;
    chordRoot = 2*surfaceArea/(1+taperRatio);
    chordTip = taperRatio*chordRoot;
    \%\operatorname{Find} equation of sweep(y) = x(y) for quarter chord points
    sweepSlope = tand(90-quarterChordSweep);
    sweepOrd = -sweepSlope*0.25*chordRoot;
    \%\operatorname{Find} equation for twist, which has a zero y-intercept
    twistSlope = wingTipTwist/0.5;
    for i = 1:nPanels
       chord = chordRoot + (chordTip - chordRoot) / 0.5 * abs(midPoints(i, 2));
       panelAreas(i) = chord*panelWidth;
29
       panelAngles(i) = twistSlope * abs(midPoints(i, 2)) + angleOfAttack;
       \% Calculate x position, if sweep is 90 degrees, the slope will be infinity
```

```
if isinf(sweepSlope)
          midPoints(i, 1) = 0.25*chord;
33
         bounded_nodes(i, 1) = 0.25*chord;
       _{\rm else}
           \begin{array}{ll} if & midPoints(i \;,\; 2) > 0 \\ & midPoints(i \;,\; 1) = (midPoints(i \;,\; 2) - sweepOrd) \; / \; sweepSlope \;; \end{array} 
            bounded_nodes(i, 1) = (bounded_nodes(i, 2) - sweepOrd) / sweepSlope;
39
            midPoints(i, 1) = (midPoints(i, 2) + sweepOrd) / -sweepSlope;
            bounded_nodes(i, 1) = (bounded_nodes(i, 2) + sweepOrd) / -sweepSlope;
41
         end
       end
       trailing\_nodes(i\,,\ 1) \,=\, bounded\_nodes(i\,,\ 1) \,+\, 20;
       \%\,\mathrm{Correction} due to panel angle
45
       midPoints(i, 1) = midPoints(i, 1) + chord * (1 - cosd(panelAngles(i)));
       \% \ Calculate \ z \ position
47
       midPoints(i\,,\ 3)\,=\,sind(panelAngles(i))\ *\ chord\,;
       % Calculate control point position
49
       controlPoints(i\,,\ 1) = midPoints(i\,,\ 1) + chord/2 + (1 - cosd(panelAngles(i)))/4;
       controlPoints(i, 3) = sind(panelAngles(i)) * chord/4;
     end
     % Last bounded and trailing node
     if isinf(sweepSlope)
       bounded_nodes(nPanels+1, 1) = 0.25*chord;
       trailing_nodes(nPanels+1, 1) = bounded_nodes(nPanels+1, 1) + 20;
       bounded\_nodes(\,nPanels+1,\ 1)\ =\ (bounded\_nodes(\,nPanels+1,\ 2)\ -\ sweepOrd)\ \ /\ \ sweepSlope\,;
       trailing\_nodes(nPanels+1, 1) = bounded\_nodes(nPanels+1, 1) + 20;
     end
  end
```

wing_discretization.m

```
function coordinates = rectangular_horseshoe(midPoint, panelAngle, nPanels)
panelWidth = 1 / nPanels;
coordinates = zeros(4, 3);
% Points b, c, a, d
coordinates(2, :) = [ midPoint(1) midPoint(2)-panelWidth/2 midPoint(3) ];
coordinates(3, :) = [ midPoint(1) midPoint(2)+panelWidth/2 midPoint(3) ];
coordinates(1, :) = [ midPoint(1)+20 coordinates(2,2) -sind(panelAngle)*20 ];
coordinates(4, :) = [ midPoint(1)+20 coordinates(3,2) -sind(panelAngle)*20 ];
end
```

$rectangular_horseshoe.m$

```
function induced Velocity = compute_induced_velocity(xa, xb, xp, circulation)
              % Cross products
            x = (xp(2)-xa(2))*(xp(3)-xb(3)) - (xp(3)-xa(3))*(xp(2)-xb(2));
           y = -(xp(1)-xa(1))*(xp(3)-xb(3)) + (xp(3)-xa(3))*(xp(1)-xb(1));
             z \, = \, (\, xp \, (1) - xa \, (1) \,) \, * (\, xp \, (2) - xb \, (2) \,) \, - \, (\, xp \, (2) - xa \, (2) \,) \, * (\, xp \, (1) - xb \, (1) \,) \, ;
             d = x*x + y*y + z*z;
             r1 = \sqrt{(xp(1)-xa(1))*(xp(1)-xa(1)) + (xp(2)-xa(2))*(xp(2)-xa(2)) + (xp(3)-xa(3))*(xp(2)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3)-xa(3))*(xp(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa
                           (3)-xa(3)):
             r2 = \sqrt{(xp(1)-xb(1))*(xp(1)-xb(1)) + (xp(2)-xb(2))*(xp(2)-xb(2)) + (xp(3)-xb(3))*(xp(2)-xb(2))}
                             (3)-xb(3));
                We set the induced velocity to zero if r1, r2 or their cross product is less
                %than a small constant, to avoid dividing by zero
              if d<(10^-6) || r2<(10^-6) || r1<(10^-6)
                           inducedVelocity = [0; 0; 0];
                           ror1 = (xb(1)-xa(1))*(xp(1)-xa(1)) + (xb(2)-xa(2))*(xp(2)-xa(2)) + (xb(3)-xa(3))*(xp(2)-xa(2)) + (xb(3)-xa(3))*(xp(2)-xa(3))*(xp(2)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3))*(xp(3)-xa(3)-xa(3))*(xp(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa(3)-xa
                            (3)-xa(3);
                           ror2 = (xb(1)-xa(1))*(xp(1)-xb(1)) + (xb(2)-xa(2))*(xp(2)-xb(2)) + (xb(3)-xa(3))*(xp(2)-xb(2)) + (xb(3)-xa(3))*(xp(2)-xb(2)) + (xb(3)-xa(3))*(xp(2)-xb(2)) + (xb(3)-xa(3))*(xp(3)-xb(3)) + (xb(3)-xa(3)) + (xb(3)-xa(3)-xa(3)) + (xb(3)-xa(3) + (xb(3)-xa(3)) + (xb(3)-xa(3)) + (xb(3)-xa(3)) + (xb(3)-x
                           (3)-xb(3);
                          com = (circulation/(4*pi*d))*((ror1/r1)-(ror2/r2));
                           inducedVelocity = [x*com; y*com; z*com];
             end
```

compute_induced_velocity.m

quarter chord sweep.m

```
wingTipTwist, horseshoeShape, nPanels)
          %HVM: Computes the lift coefficient of a wing using the Horseshoe Vortex Method
         %horseshoeShape: can be 'rectangular' or 'trapezoidal'
         density = 1.25;
         freestream Velocity = [ 1 0 0 ];
         % Perform wing discretization
         [ midPoints, controlPoints, bounded nodes, trailing nodes, panelAngles, panelAreas ] =
             wing\_discretization (aspectRatio\;,\; taperRatio\;,\; quarterChordSweep\;,\; angleOfAttack\;,\; taperRatio\;,\; taperRatio
             wingTipTwist, nPanels);
         % Initialize variables
         influenceCoefficients = zeros(nPanels, nPanels);
         RHS = zeros(nPanels, 1);
         for i = 1: nPanels
             midPoint = [ midPoints(i, 1) midPoints(i, 2) midPoints(i, 3) ];
             normalUnitVector = [ sind(panelAngles(i)) 0 cosd(panelAngles(i)) ];
13
             for j = 1:nPanels
                 midPoint = [ midPoints(j, 1) midPoints(j, 2) midPoints(j, 3) ];
                 if strcmp(horseshoeShape, 'rectangular')
                     horseshoe = rectangular_horseshoe(midPoint, panelAngles(j), nPanels);
                    horseshoe = [ trailing_nodes(j,:); bounded_nodes(j,:); bounded_nodes(j+1,:);
             trailing_nodes(j+1,:);
                 inducedVelocity = zeros(3,1);
21
                 for k = 1:3
                    inducedVelocity = inducedVelocity + compute_induced_velocity(horseshoe(k,:),
23
             horseshoe(k+1,:), controlPoints(i,:), 1);
                 influenceCoefficients(i, j) = dot(inducedVelocity, normalUnitVector);
25
             end
            RHS(i) = -dot(freestreamVelocity, normalUnitVector);
27
         circulation = influenceCoefficients \ RHS;
          %Compute lift
         lift = zeros(nPanels, 1);
31
         for i = 1:nPanels
            lift(i) = density * freestreamVelocity(1) * circulation(i) / nPanels;
         end
         wingLift = sum(lift);
35
         %Compute lift coefficient
         cL = 2 / freestreamVelocity(1) * aspectRatio * sum(circulation/nPanels);
          %Compute local lift distribution
        cLY = \, 2*circulation./\,panelAreas/nPanels/freestreamVelocity\,(1)\,;
         % Compute moment
         momentLE = zeros(nPanels);
41
         for i = 1:nPanels
            momentLE(i) = lift(i) * midPoints(i, 1) * cosd(panelAngles(i));
43
         chordRoot = 2/aspectRatio/(1+taperRatio);
         geometricChord = (2/3)*chordRoot*((1+taperRatio+taperRatio^2)/(1+taperRatio));
        cMLE = ((-2)/(freestreamVelocity(1)/aspectRatio*geometricChord))*sum(momentLE);
         [ alpha_i local_drag cDi ] = compute_cdi(nPanels, midPoints, panelAngles, circulation,
             1/aspectRatio);
    end
```

```
aspectRatios = 6:12;
  taperRatio = 1;
  quarterChordSweep = 0;
  wingTipTwist = 0;
  horseshoeShape = 'rectangular';
  nPanels = 100;
  % Initialize output vector
  cLAlphas = [];
  for aspectRatio = aspectRatios
    \%\,\mathrm{Compute}\ \mathrm{cL} for -2 and 2 degrees so we can draw a line
    [ cL1 ] = HVM(aspectRatio, taperRatio, quarterChordSweep, -2, wingTipTwist,
      horseshoeShape, nPanels);
    [ cL2 ] = HVM(aspectRatio, taperRatio, quarterChordSweep, 2, wingTipTwist,
      horseshoeShape, nPanels);
    cLAlphas = [cLAlphas; (cL2-cL1)/4];
  end
15
  csvwrite('data/hw2_1.csv', [ aspectRatios' cLAlphas ]);
```

hw2 1.m

```
aspectRatio = 6;
   taperRatio = 1;
   leadingEdgeSweeps = 0:5:60;
   wingTipTwist = 0;
   horseshoeShape = 'rectangular';
   nPanels = 100;
   % Initialize output vectors
  cLAlphas = [];
   aerodynamicCenters = [];
{\tiny 10 \mid \textbf{for} \ leadingEdgeSweep} = {\tiny leadingEdgeSweeps}
     % Although unnecessary for a unitary taper ratio, we calculate the quarter chord sweep
       angle
     quarterChordSweep = quarter_chord_sweep(leadingEdgeSweep, aspectRatio, taperRatio);
      \%Compute cL for -2 and 2 degrees so we can draw a line
     [ \  \, \text{cL1} \  \, ] = \text{HVM}(\text{aspectRatio} \,, \  \, \text{taperRatio} \,, \  \, \text{quarterChordSweep} \,, \  \, -2, \  \, \text{wingTipTwist} \,,
14
       horseshoeShape, nPanels);
     [ \ cL2 \ ] = HVM(aspectRatio \,, \ taperRatio \,, \ quarterChordSweep \,, \ 2 \,, \ wingTipTwist \,,
       horseshoeShape, nPanels);
     cLAlphas = \left[ \begin{array}{cc} cLAlphas \, ; & (cL2-cL1)/4 \end{array} \right];
     aerodynamicCenters = [aerodynamicCenters; 0.25 + tand(quarterChordSweep)/6*(1+2*)]
        taperRatio)/(1+taperRatio)];
  csvwrite('data/hw2_2.csv', [ leadingEdgeSweeps' cLAlphas aerodynamicCenters ]);
```

hw2 2.m

```
aspectRatio = 5;
taperRatios = 0.1:0.1:1;
quarterChordSweep = 0;
wingTipTwist = 0;
horseshoeShape = 'rectangular';
nPanels = 100;
% Initialize output vectors
panels = (1:nPanels);
cLYs = [];
for taperRatio = taperRatios
  \%Compute cL for -2 and 2 degrees so we can draw a line
  [ \ \text{cL1} \ ] = \text{HVM}( aspectRatio \,, \ taperRatio \,, \ quarterChordSweep \,, \ -2, \ wingTipTwist \,,
    horseshoeShape, nPanels);
  [ cL2 ] = HVM(aspectRatio, taperRatio, quarterChordSweep, 2, wingTipTwist,
    horseshoeShape, nPanels);
  cLAlpha = (cL2-cL1)/4;
  % Find angle of attack for a 0.25 lift coefficient
  alpha = 0.25/cLAlpha;
```

 $hw2_3.m$

```
aspectRatios = [4810];
           taperRatios = 0.1:0.1:1;
           quarterChordSweep = 0;
           wingTipTwist = 0;
           horseshoeShape = 'rectangular';
           nPanels = 100;
             % Initialize output vector
           oswaldFactors = [];
for aspectRatio = aspectRatios
                    oswaldFactorsColumn = [];
                    for taperRatio = taperRatios
                              [ \ cL, \ cLY, \ cDi \ ] = HVM (aspectRatio \,, \ taperRatio \,, \ quarterChordSweep \,, \ -2, \ wingTipTwist \,, \ constant \,, \ description \,,
                              horseshoeShape, nPanels);
                              oswaldFactorsColumn \; = \; [ \; oswaldFactorsColumn \; ; \; cL^2/cDi/pi/aspectRatio \; ] \; ; \; \\
                   oswaldFactors = [ oswaldFactors oswaldFactorsColumn ];
16 end
18 csvwrite('data/hw2_4_aspect.csv', [ [ -1 aspectRatios ]; taperRatios' oswaldFactors ]);
```

 $hw2_4$ _aspect.m

```
aspectRatio = 8;
  taperRatios = 0.1:0.1:1;
  quarterChordSweeps = [ 0 30 60 ];
  wingTipTwist = 0;
  horseshoeShape = 'rectangular';
  nPanels = 100;
   % Initialize output vector
  oswaldFactors = [];
  for quarterChordSweep = quarterChordSweeps
    oswaldFactorsColumn = [];
    for taperRatio = taperRatios
       [ \ cL, \ cLY, \ cDi \ ] = HVM (aspectRatio \,, \ taperRatio \,, \ quarterChordSweep \,, \ -2, \ wingTipTwist \,, \ constant \,, \ description \,)
12
       horseshoeShape, nPanels);
      oswaldFactorsColumn; cL^2/cDi/pi/aspectRatio ];
    oswaldFactors = [ oswaldFactors oswaldFactorsColumn ];
  csvwrite('data/hw2_4_sweep.csv', [ [ -1 quarterChordSweeps ]; taperRatios' oswaldFactors
```

hw2 4 sweep.m

```
hw2_1;
hw2_2;
hw2_3;
hw2_4_aspect;
hw2_4_sweep;
```

shia_lebouf.m