



$$(iv) f_4(x) = \frac{2}{\pi\sqrt{3}}(1 + x^2/3)^{-2}$$

```
# Set parameters
Nsim <- 1000
q <- 8
# Set Function
fx <- function(x){
  (2/(pi*sqrt(3)))*(1+x^2/3)^(-2)
}

## Generate Uniform
U <- runif(Nsim,0,1)
x <- fx(U)
estx <- cumsum(x)/1:Nsim

## dyadic symetries
resid <- U%2^(-q)
simx <- matrix(resid,ncol=2^q,nrow=Nsim)
simx[,2^(q-1)+1:2^q] <- 2^(-q)-simx[,2^(q-1)+1:2^q]
for (i in 1:2^q){
  simx[,i] <- simx[,i] + (i-1)*2^(-q)
}
xsym <- fx(simx)
estint <- cumsum(apply(xsym,1,mean))/(1:Nsim)

## Sum up
print(paste0("The raw variance is ",var(estx)," The variance with antithetic variable is ", var(estint)
            ,"The raw mean is ", mean(estx)," The mean with antithetic variables is ",mean(estint)))
```

```
## [1] "The raw variance is 6.68384962391457e-06 The variance with antithetic variable is 1.90607093035838e-10The raw mean is 0.303640666200224 The mean with antithetic variables is 0.304488000391739"
```