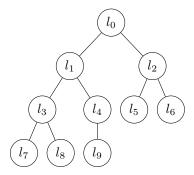
Sorting

$$l = (l_0, l_1, l_2, \dots, l_{n-1})$$

$$l_0 \le l_1 \le \dots \le l_{n-1}$$

On a tree



Heaps

Heap: complete binary tree.

Max heap: each parent bigger than children.

Min heap: each parent smaller than children.

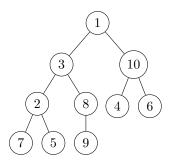
Check for min/max heap in (n-1) comparisons.

To min or max heap

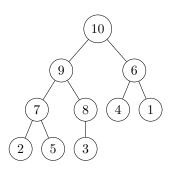
- 1. Start with last node, moving backwards.
- 2. Compare node to children, swap if needed.
- 3. Swap parent down tree until we have a heap.

Example heap

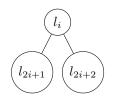
Sort ascending \rightarrow use max heap.



Last five nodes have no children. Sixth-last has one child, is smaller so swap. Now have a heap from sixth-last. Same for seventh-last: swap 2 for 5. Third node is a heap. Second node swaps 9 for 3, and filters down swapping 3 for 8. Finally, the root is swapped with 1 and then 6.



As an array



Heap Sort

- 1. Convert complete binary tree to heap.
- 2. Swap root for last child, ignore last child.
- 3. Repeat n-1 times.

Comparisons

To heap: