Hash functions

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Binary functions

$$f:\{0,1\}^* \to \{0,1\}^*$$

- f is a function that converts strings over $\{0,1\}$ into other strings over $\{0,1\}$.
- f can be viewed as a map, a subset of $\{0,1\}^* \times \{0,1\}^*$ where no two first elements are equal and every element in $\{0,1\}^*$ is a first element.
- For example, $(0110, 11111101) \in \{0, 1\}^* \times \{0, 1\}^*$.

Hash functions

$$f:\{0,1\}^*\to\{0,1\}^n$$

- A (binary) hash function is a function where the output is of fixed size.
- In the example above, $\{0,1\}^n$ has size 2^n .
- Any set of fixed size will do, but we usually use $\{0,1\}^n$ for some $n \in \mathbb{N}$.
- For example, we could use $\{0, 1, 00, 01, 10, 11\}$ instead.

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Using Hexadecimal

The benefit of using hex is that it saves space while being easy to convert to. Every nibble becomes a hex symbol.

0	0000	1	0001	2	0010	3	0011
4	0100	5	0101	6	0110	7	0111
8	1000	9	1001	Α	1010	В	1011
C	1100	D	1101	Е	1110	F	1111

Example

0100	0111	0100	1101	0100	1001	0101	0100
4	7	4	D	4	9	5	4

Try 010010010110000101101110 in your own time.

Common hash functions

Input string

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Outputs

MD5	4EC47B38AE21FD11A5E4993995097861
SHA1	67481B1FF7E145067C12B7C6C5E681CD7EFDEDD6
SHA256	BE9863B550CC931D220E7EB08B7AFE44B70ED467A5015F34ED9DECA1B84F7A2D
CRC32	FE7E4F25

Try yourself

Try "Colorless green ideas sleep furiously" and the empty string.

Properties

Uniform: outputs should have the same probability as each other.

Prefect: every input gives a different output.

Minimal: outputs form a coninuous range of bit strings.

Cryptographic: difficult to calculate the input from the output.

Deterministic: always the same output for a given input.

Loop-up tables

Exercise

Write an algorithm that counts the number of bits set in an integer.