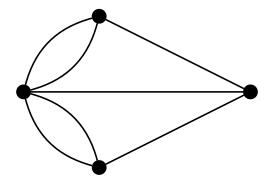
Graphs

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Drawing a Turing machine



Non-deterministic Turing machine

- **The usual** Turing machines are often called deterministic Turing machines.
- **Deterministic** Turing machines have exactly one row in their state table for every combination of (non-terminal) state and tape symbol.
- **This means** there is only one path to follow at a given point in time.
- **Nondeterministic** Turing machines can have any number of rows for each state/symbol (including none).
- **Essentially** they allow for parallel computation they can branch into two or more paths at the same time.

Non-deterministic Turing machine and languages

- Languages are accepted by non-deterministic Turing machines, where an input string is accepted if any branch ends in the accept state.
 - Deciders if a non-deterministic Turing machine always halts on all branches of computation, no matter what the input, then we say it decides the language it accepts.
 - Any language that is accepted (or decided) by a non-deterministic Turing machine has some deterministic Turing machine that accepts (or decides) it. So non-deterministic Turing machines don't really have any extra abilities over deterministic ones.

Non-deterministic polynomial time

Definition

A decision problem is in the NP complexity class if it is decidable by a non-deterministic Turing Machine in polynomial time.

P is a subset of NP

Note that every deterministic Turing machine is also a non-deterministic one, by our definitions. The P complexity class is a subset of NP because of this.

Equivalent definition

An equivalent definition of NP that you may come across is that NP is the set of languages A that can be verified in polynomial time. By verified we mean that a deterministic Turing machine can accept a language $\{wc\}$ where w is in A and c is some string, called the certificate for w.