Regular expressions

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Regular expressions

$$(0.0|1.1).(0.1)^*.(0.0|1.1)$$

- Regular expressions are strings that represent patterns of text.
- The strings can contain special characters.
- Brackets can be used to group characters together.
- Regular expressions are used to search other strings for patterns.

Special characters

- . means concatenate. So, a.b means an a followed by a b.
- means or. So, a|b means an a or a b.
- * means zero or more times. So, a^* means zero or more a's.

Examples of regular expressions

- a.b.c a single a followed by a single b followed by a single c.
- $a.b.c^*$ an a followed by a b followed by zero or more c's.
 - a|b.c an a, or a b followed by a c.
- (a|b).c an a or a b, followed by a c.
- $0.0.(0|1)^*$ all strings of 0's and 1' that begin with two zeros.
 - 1* any number of 1's (including empty string).

Precedence

- 1. Always apply * first.
- 2. Apply . after * but before |.
- 3. Apply | last.
- 4. Treat bracketed groups as individual characters.

Languages of regular expressions

This is a list of regular expressions over an alphabet A and the languages they define.

- \emptyset the empty language ($\{\}$).
- ϵ the language containing the empty string $(\{\epsilon\})$.
- a the language containing any symbol a from A ($\{a\}$).
- r.s the concatenation of the languages defined by regular expressions r and s.
- r|s the union of the languages of regular expressions r and s.
- r^* the star of the language defined by regular expression r.

Infix and postfix

It is sometimes convenient to re-write expressions in postfix. This applies to lots of different expressions, not just regular expressions.

Example

Convert an infix mathematical expression (left) to postfix (right):

$$(3+4) \times 5 \longrightarrow 34 + 5 \times$$

Example

Converting an infix regular expression (left) to postfix (right):

$$a.(b.b)^*.a \rightarrow abb.^*.a.$$

Note we often omit the . in infix notation: " $a(bb)^*a$ " but can't in postfix. However, the brackets aren't needed in postfix.

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