



The Objective Function in Classification (Cross Entropy)

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Cross-entropy is a measure of the difference between two probability distributions for a given random variable or set of events.

ID	Actual	Predicted probabilities
ID6	1	0.94
ID1	1	0.90
ID7	1	0.78
ID8	0	0.56
ID2	0	0.51
ID3	1	0.47
ID4	1	0.32
ID5	0	0.10



ID	Actual	Predicted probabilities	Corrected Probabilities
ID6	1	0.94	0.94
ID1	1	0.90	0.90
ID7	1	0.78	0.78
ID8	0	0.56	0.44
ID2	0	0.51	0.49
ID3	1	0.47	0.47
ID4	1	0.32	0.32
ID5	0	0.10	0.90



The Objective Function in Classification

Now, we take the log of the corrected probabilities (Log(Corrected probabilities)):

ID	Actual	Predicted probabilities	Corrected Probabilities	Log
ID6	1	0.94	0.94	-0.0268721464
ID1	1	0.90	0.90	-0.0457574906
ID7	1	0.78	0.78	-0.1079053973
ID8	0	0.56	0.44	-0.3565473235
ID2	0	0.51	0.49	-0.30980392
ID3	1	0.47	0.47	-0.3279021421
ID4	1	0.32	0.32	-0.4948500217
ID5	0	0.10	0.90	-0.0457574906



Log Loss

The negative average of corrected probabilities is the Log loss or Binary cross-entropy:

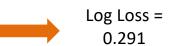
$$- \frac{1}{N} \sum_{i=1}^{N} (\log(p_i))$$

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Log Loss Example- Model A

Observation	Actual Training Label/Class	Prediction Score	Corrected Prediction Score	Log(Corre cted Prediction Score)
1	Yes	0.9	0.9	-0.046
2	No	0.2	0.8	-0.097
3	Yes	0.8	0.8	-0.097
4	Yes	0.1	0.1	-1
5	Yes	0.7	0.7	-0.155
6	Yes	0.3	0.3	-0.522
7	No	0.4	0.6	-0.222
8	No	0.3	0.7	-0.155
9	No	0.4	0.6	-0.222
10	No	0.6	0.4	-0.398





Log Loss Exercise- Model B

Calculate Log Loss for Model B and compare with that of Model A. Which model is better?

Observation	Actual Training Label/Class	Prediction Score	Corrected Prediction Score	Log(Corre cted Prediction Score)
1	Yes	1.0		
2	No	0.1		
3	Yes	0.9		
4	Yes	0.4		
5	Yes	0.8		
6	Yes	0.4		
7	No	0.3		
8	No	0.2		
9	No	0.3		
10	No	0.5		



