Tutorial-I Norme-Anshul Kumar Sec-SPLZ Design And Analysis of Algorithmy And 1. Asymptotic Notations are the Mathematical Notations used to idescribe the running time of an Algarikum when the inputs tends to va limiting value. The efficiency is measured with The help of asymptotic natations (1) Big-O notation represents upper bound of the running time of an algarithm f(n) = O(g(n))f(n)

classmate (2) amya Natatian (SL) represents the lower bound of the running time of an algorithm. $f(n) = \Omega(g(n))$ (.g(n) (3) Theta Natation (0) above and below used for analyzing average-case complisity
of an algorith Cz(g(n) (f(n) f(n)=0(g(n)) c, 9(n) $C_1g(n) \leq f(n) < C_2g(n)$

for (== 1 ton) { Ans2. 1=1*2; 1=1,2,4,8,16 $\Delta=1, \gamma=2$ t = a 8 k-1 $h = (1)(2)^{k-1}$ h = 2 k-1 (taking log both sides) log n = log 2k-1 oc(log 2R = A) $log_n = k-1$ K = 1 + log n T.C. = O(log_n) Als.

Ans.
$$T(n) = \begin{cases} 3T(n-1) & \text{if } h > 0 \\ 1 & \text{otherwise} \end{cases}$$

$$T(0) = 1 & (n \neq 0)$$

$$T(n-1) = 3T(n-2) - 0$$

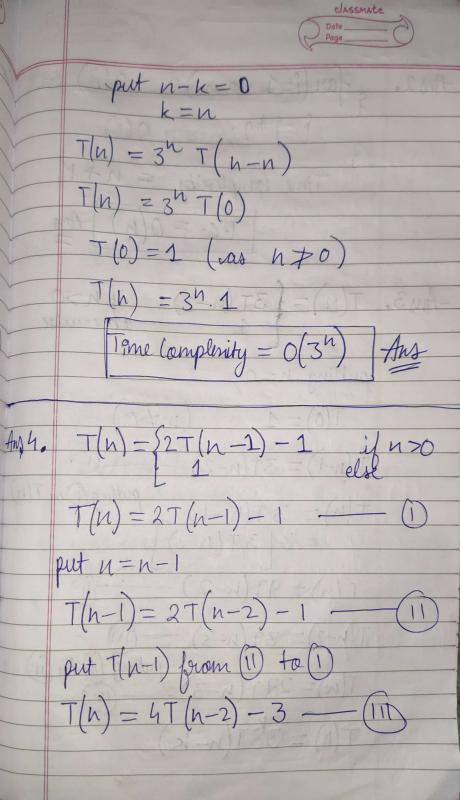
$$T(n) = 3T(n-1) & \text{putting } 0 \text{ in } T(n)$$

$$T(n) = 9T(n-2) - 0$$

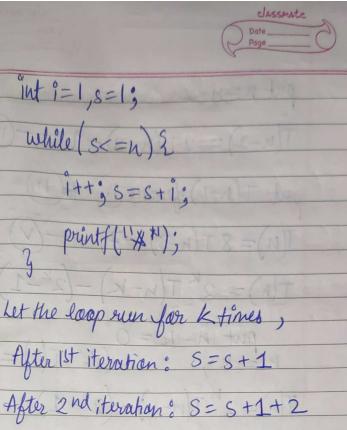
$$T(n-2) = 3T(n-3) - 0$$

$$T(n) = 27T(n-3) - 0$$

$$T(n) = 3^{K}T(n-K)$$



put n=n-2 T(n-2) = 2T(n-3) - 1 - (1)put T(n-2) from (1) to (1) T(n) = 8T(n-3) - 7 - (V) $T(h) = 2^{k} T(h-k) - (2^{k}-1)$ put n-k=0 k=n, (°° T(0)=1) $T(n) = 2^{h} T(n-n) - (2^{h}-1)$ $T(n) = 2^{h} T(0) - 2^{h} + 1$ $T(n) = 2^{h} - 2^{h} + 1$ T(n) = O(1) Au(K(1+K)) C= K NED (61)0 (3



After 2nd iteration: S=S+1+2 It goes on for k times, as long as

"int =1,8=1;

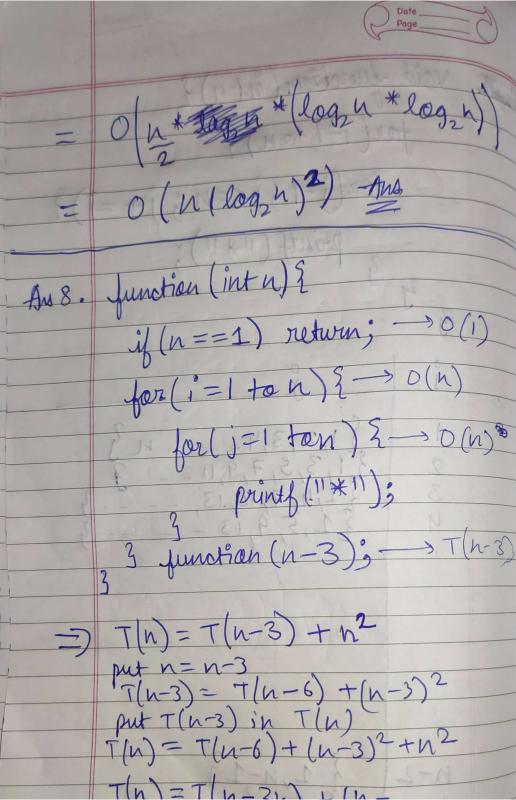
while (s<=n) {

Any 5.

S'is less than equal to n' 1+2+ THE +K <= h =) $\left(\left(\left(\frac{1+k}{2} \right) \right) < = h$ = $\left(\frac{k^2+k}{2}\right) < = n$ =) O(K2) <= h =) K = O (Jn) Time Complexity.

void function (int 11) { Ans 6. inti, count = 0; for (i=1; i*i<=n; i++){ 2 count ++; = 1*1<=N = 1 <= n (taking sweat both sides) \sqrt{n} $1 = 1+1+1---+1 (\sqrt{n} + imy)$ 0 = 1T.C. = O(Nn) / And

Aust. void function (int n) { int i, j, k, court = 0; for(i=n/2; i<=n; i+t)? for(j=1;j<=n;j=j*2){ for(k=1; k==n; k=k*2){ count++; n/2 log2n lagen * logen log n * log n log 4 1/2+1 Oh/2+2 lag n 1/2+3 lagen*logen lag_n



void function (int n) { Aus 9. for(i=1ton){ for ()=1;j<=n;j+=i)?