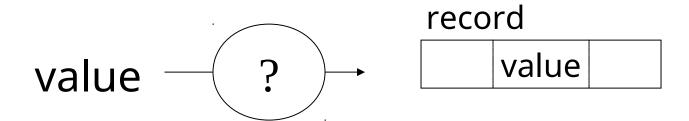
Ullman et al.: Database System Principles

Notes 4: Indexing

Chapter 4

Indexing & Hashing



Topics

- Conventional indexes
- B-trees
- Hashing schemes

- A single-level index is an auxiliary file that makes it more efficient to search for a record in the data file.
- The index is usually specified on one field of the file (although it could be specified on several fields).
- One form of an index is a file of entries <field value, pointer to record>, which is ordered by field value.
- The index is called an access path on the field.

- The index file usually occupies considerably less disk blocks than the data file because its entries are much smaller
- A binary search on the index yields a pointer to the file record

- Indexes can also be characterized as dense or sparse
 - A dense index has an index entry for every search key value (usually every record) in the data file.
 - A sparse (or nondense) index, on the other hand, has index entries for only some of the search values (typically one entry per data file block)

Sequential File

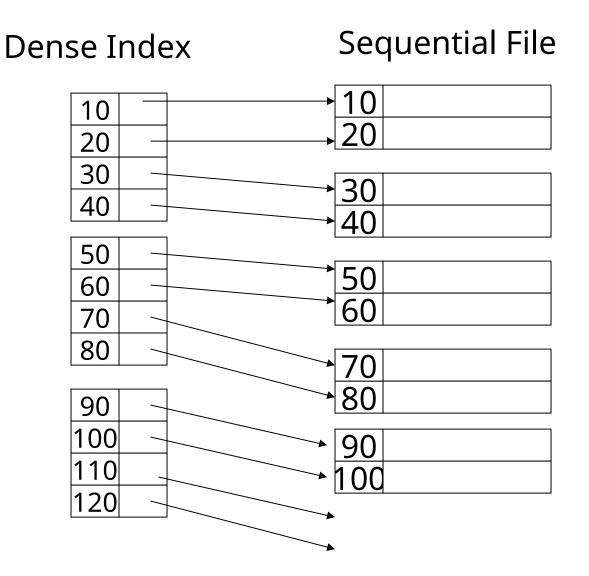
10	
20	

30	
40	

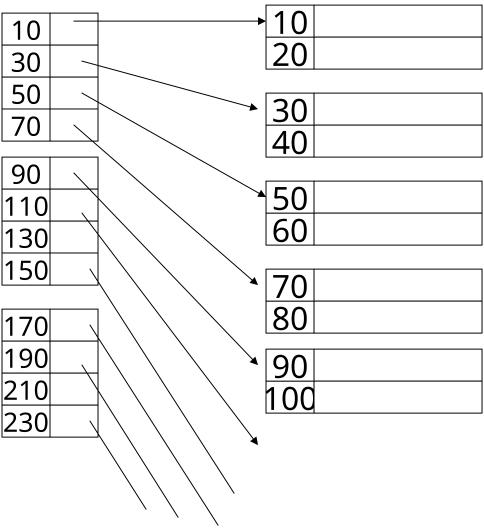
50	
60	

70	
80	

90	
100	

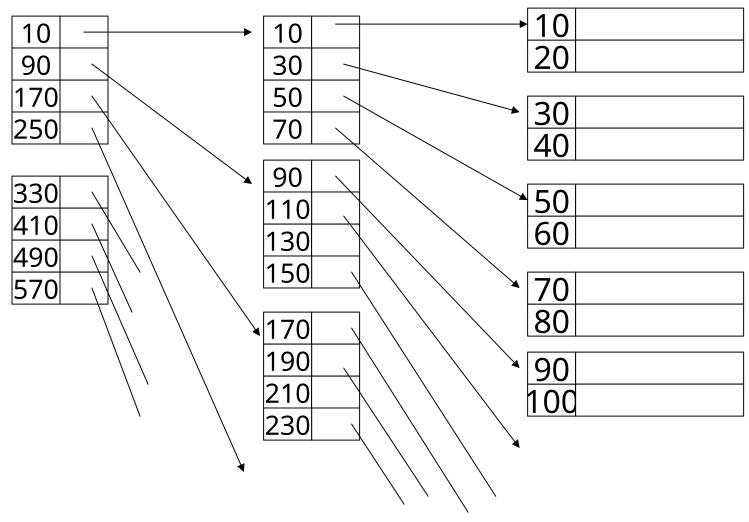


Sparse Index Sequential File



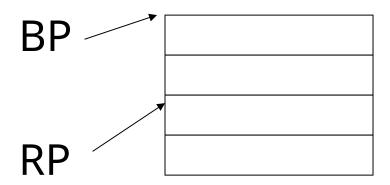
Sparse 2nd level

Sequential File



Notes on pointers:

(1) Block pointer (sparse index) can be smaller than record pointer



Sparse vs. Dense Tradeoff

- Sparse: Less index space per record can keep more of index in memory
- <u>Dense</u>: Can tell if any record exists without accessing file

(Later:

- sparse better for insertions
- dense needed for secondary indexes)

<u>Terms</u>

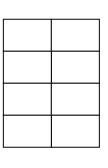
- Index sequential file
- Search key (≠ primary key)
- Primary index (on ordering field)
- Secondary index (on non-ordering field)
- Dense index (all Search Key values in)
- Sparse index
- Multi-level index

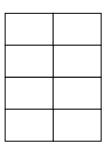
Next:

Duplicate keys

Deletion/Insertion

Secondary indexes





10	
10	

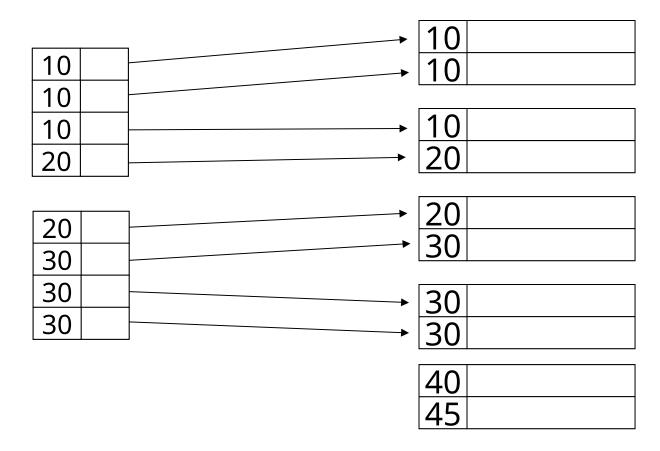
10	
20	

20	
30	

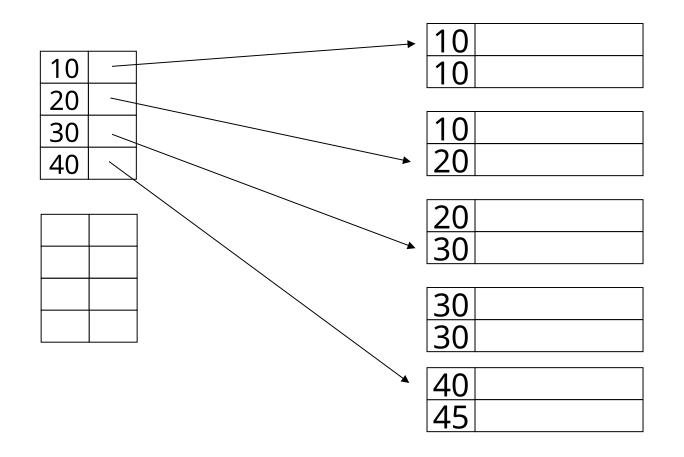
30	
30	

40	
45	

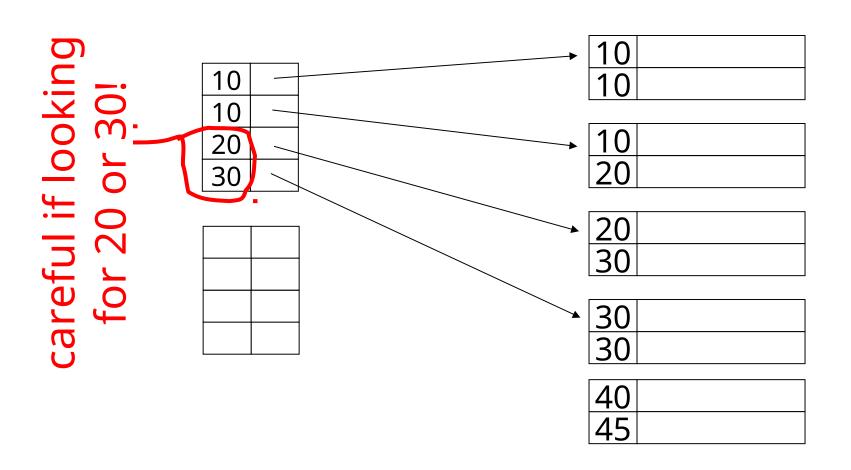
Duplicate keys Dense index, one way to implement?



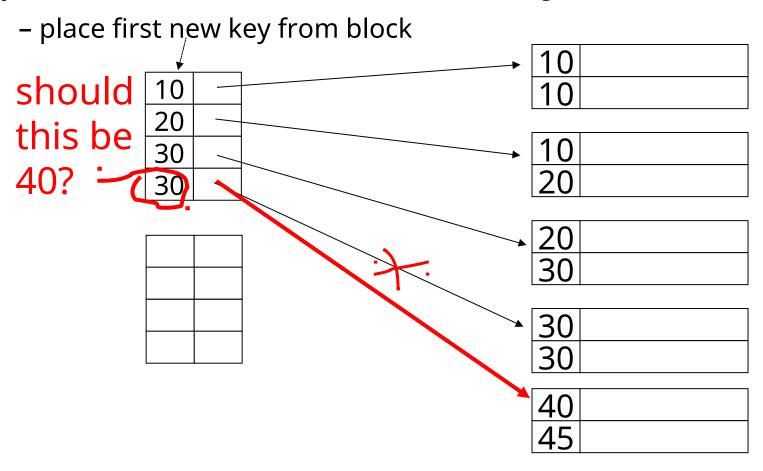
Dense index, better way?



Sparse index, one way?



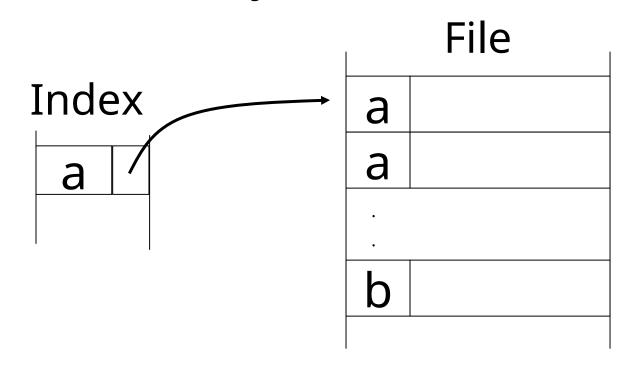
Sparse index, another way?

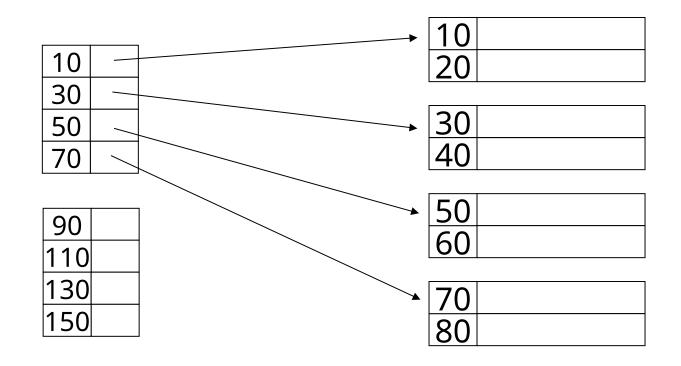


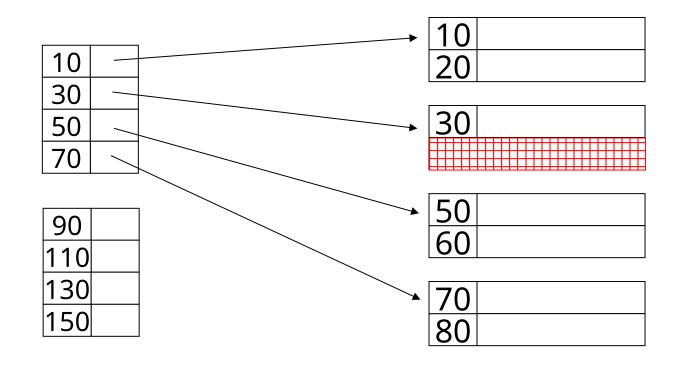
Summary

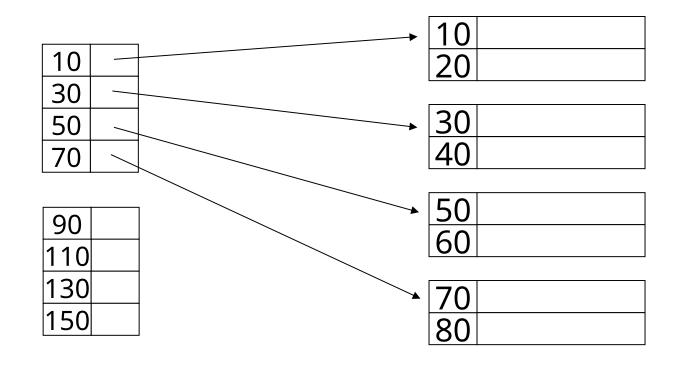
Duplicate values, primary index

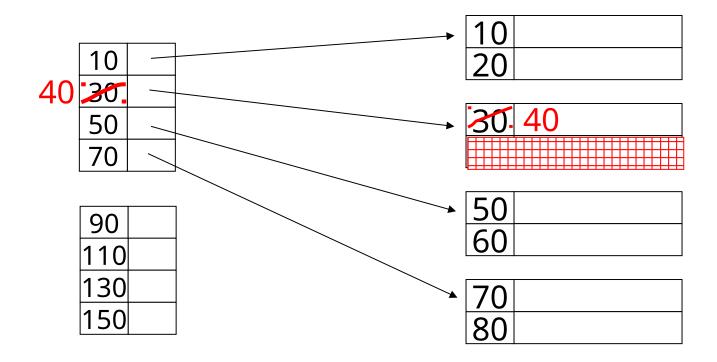
 Index may point to <u>first</u> instance of each value only



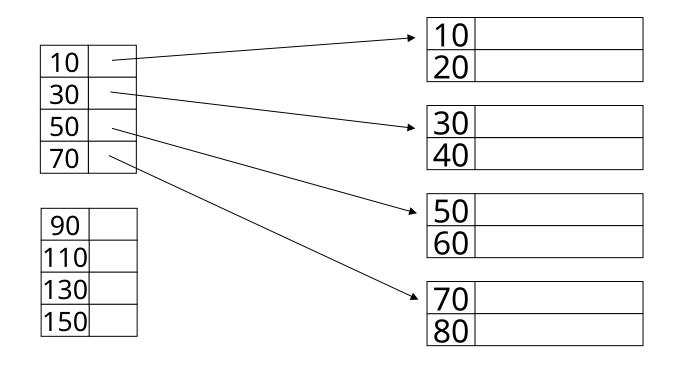




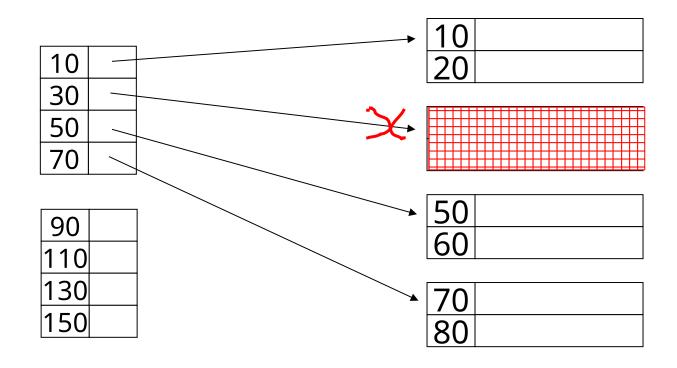




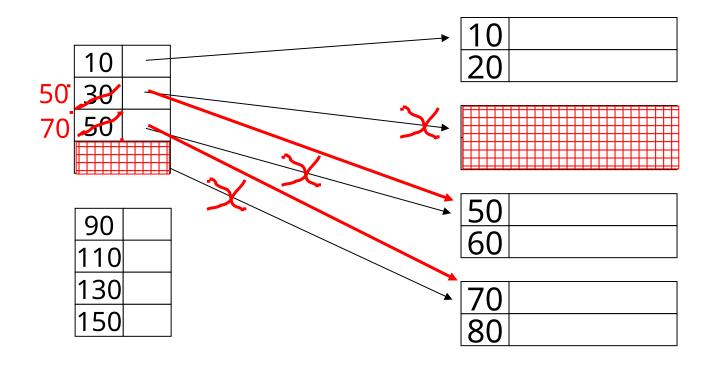
- delete records 30 & 40



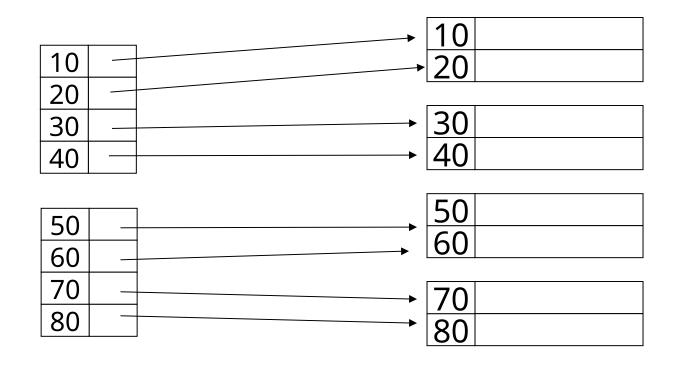
- delete records 30 & 40



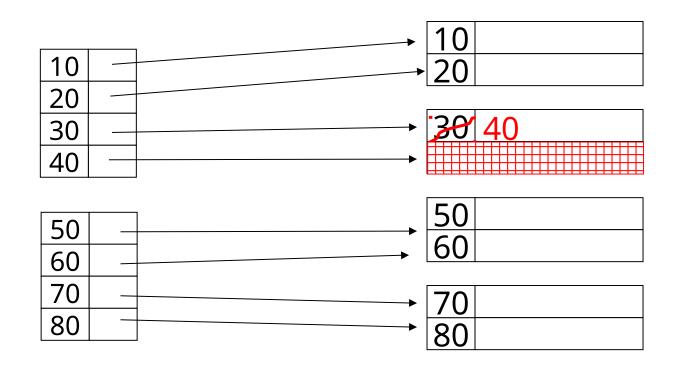
- delete records 30 & 40



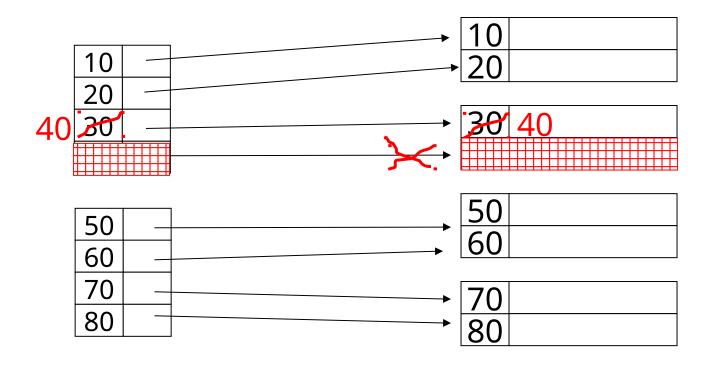
Deletion from dense index

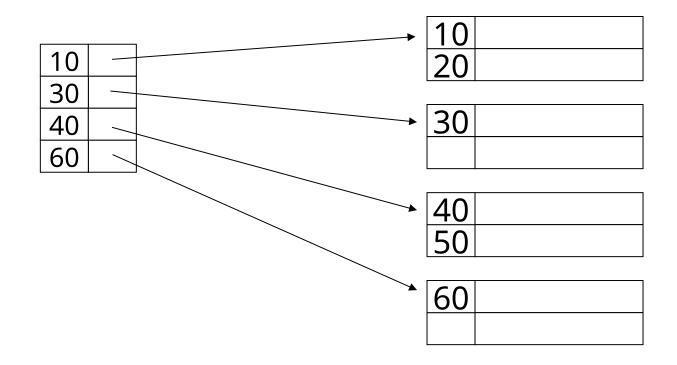


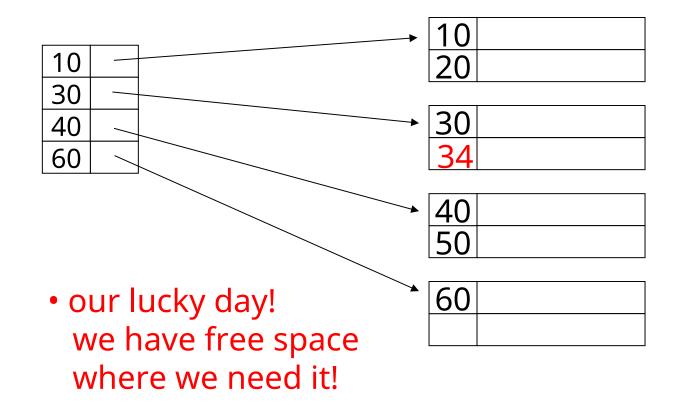
Deletion from dense index

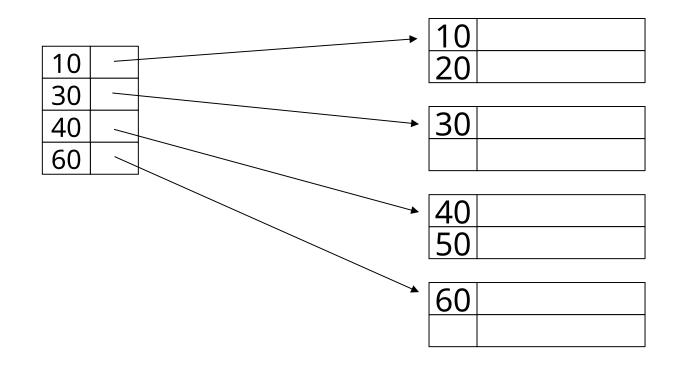


Deletion from dense index



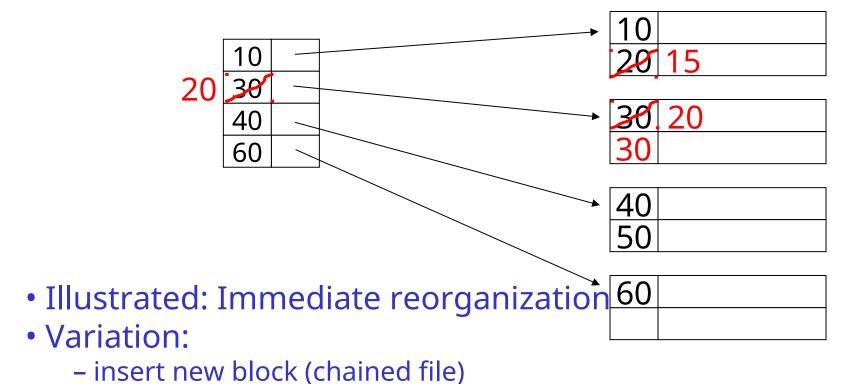




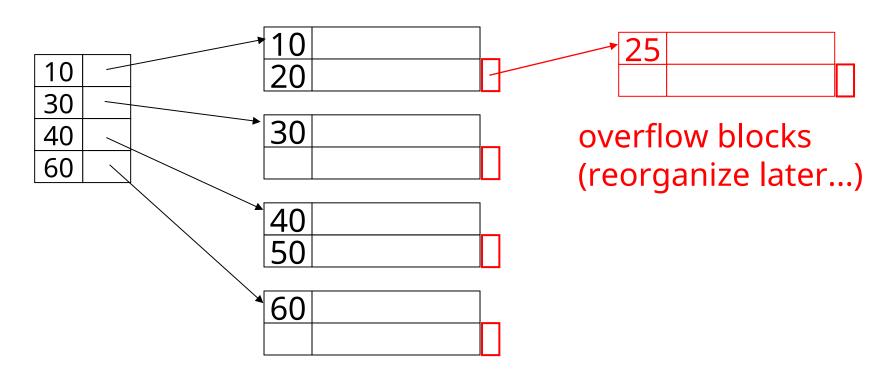


- insert record 15

- update index



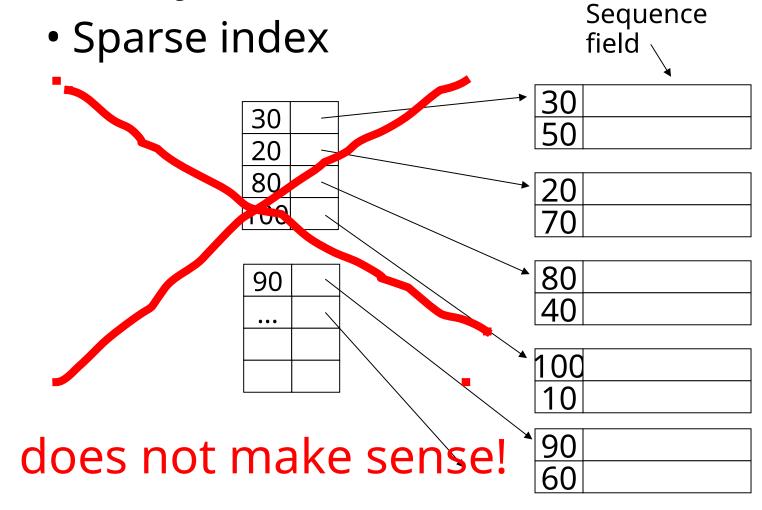
33



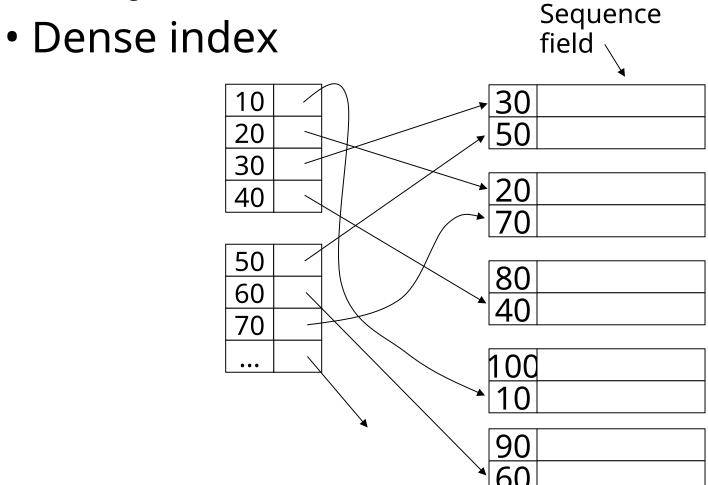
Insertion, dense index case

- Similar
- Often more expensive . . .

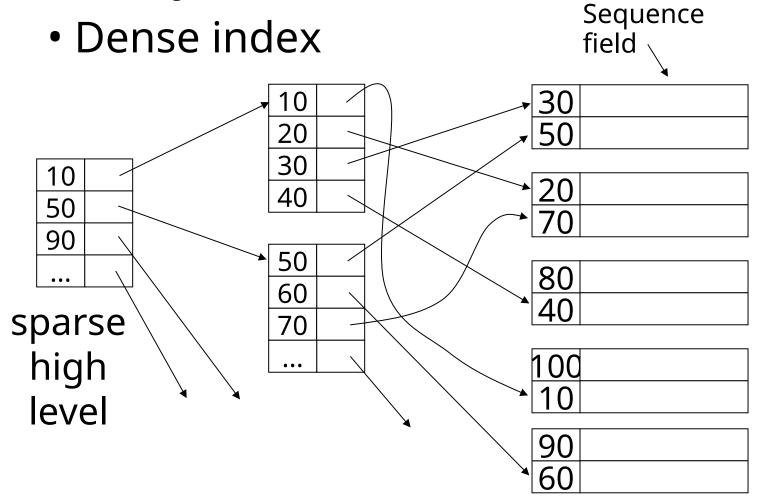
Secondary indexes



Secondary indexes



Secondary indexes



With secondary indexes:

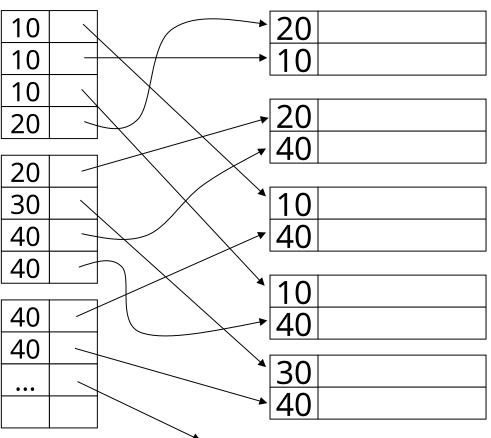
- Lowest level is dense
- Other levels are sparse

<u>Also:</u> Pointers are record pointers (not block pointers)

<u>Duplicate values & secondary</u> <u>indexes</u> one option...

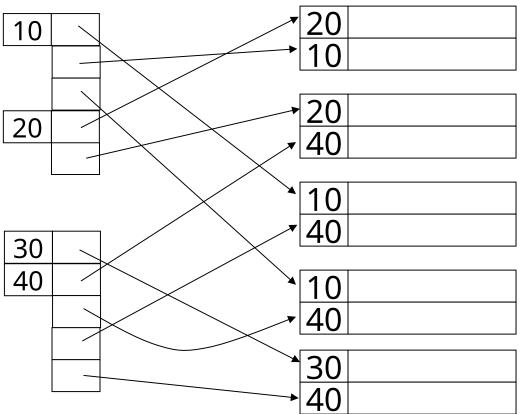
Problem: excess overhead!

- disk space
- search time

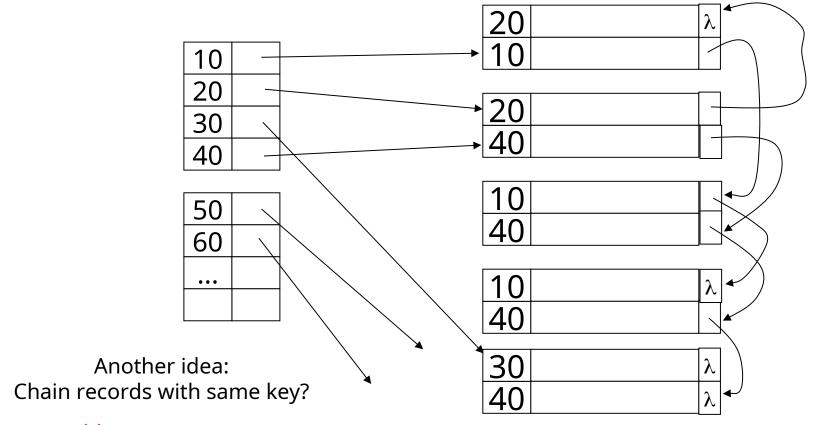


<u>Duplicate values & secondary</u> <u>indexes</u> <u>another option...</u>

Problem: variable size records in index!



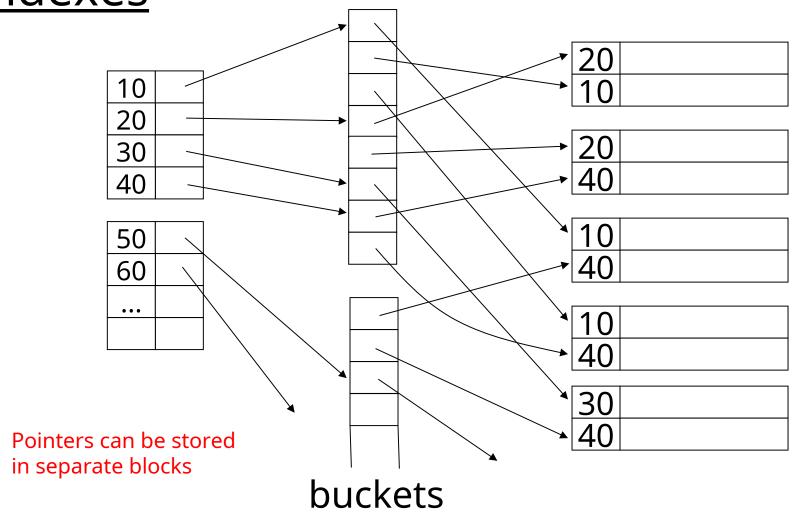
<u>Duplicate values & secondary</u> <u>indexes</u>



Problems:

- Need to add fields to records
- Need to follow chain to know records

<u>Duplicate values & secondary</u> indexes



Why "bucket" idea is useful

<u>Indexes</u>

Records

Name: primary

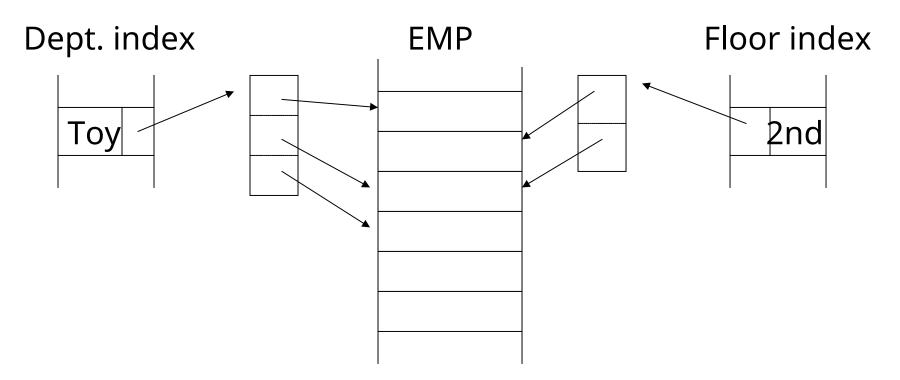
EMP (name, dept, floor,...)

Dept: secondary

Floor: secondary

See the following query

Query: Get employees in (Toy Dept) (2nd floor)



→ Intersect toy bucket and 2nd Floor bucket to get set of matching EMP's

Summary so far

- Conventional index
 - Basic Ideas: sparse, dense, multi-level...
 - Duplicate Keys
 - Deletion/Insertion
 - Secondary indexes

Conventional indexes

Advantage:

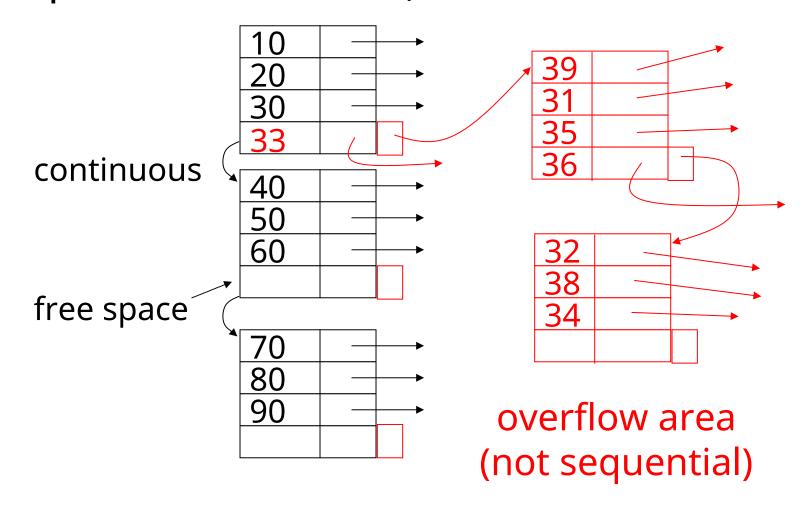
- Simple
- Index is sequential file good for scans

Disadvantage:

- Inserts expensive, and/or
- Lose sequentiality & balance

Example

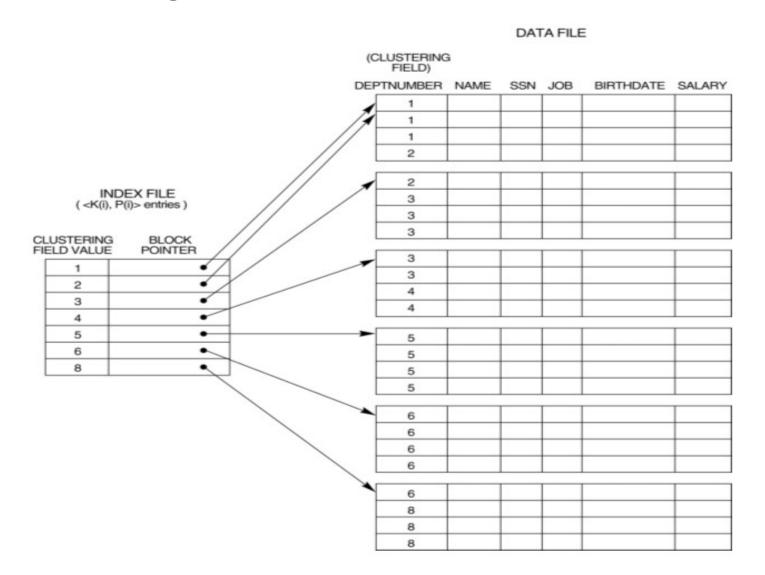
Index (sequential)



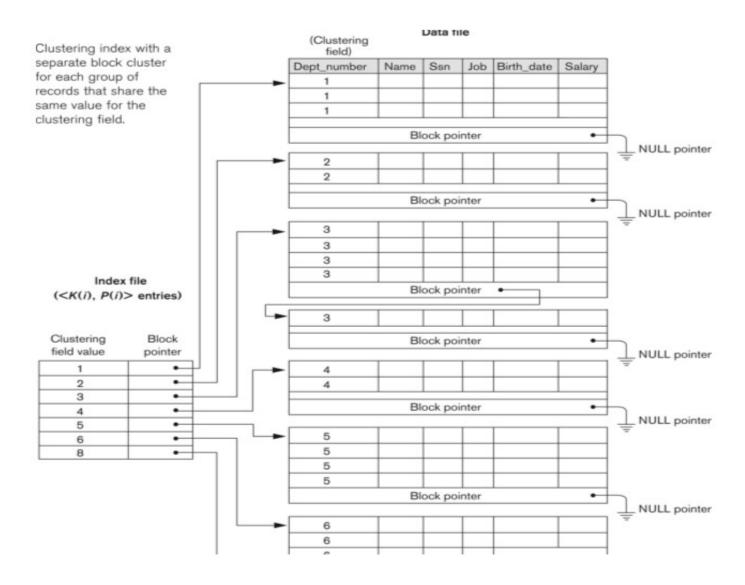
Clustering Index

- Defined on an ordered data file
- The data file is ordered on a *non-key field*.
- Includes one index entry for each distinct value of the field; the index entry points to the first data block that contains records with that field value.
- It is an example of *non-dense* index where Insertion and Deletion is relatively straightforward with a clustering index.

Clustering Index



Clustering Index version 2



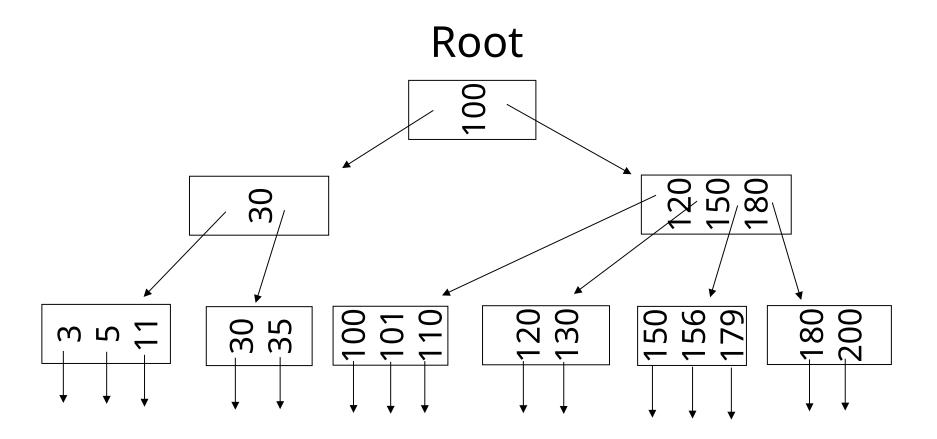
Outline:

- Conventional indexes
- B-Trees ⇒ NEXT
- Hashing schemes

- NEXT: Another type of index
 - Give up on sequentiality of index
 - Try to get "balance"

B+Tree Example

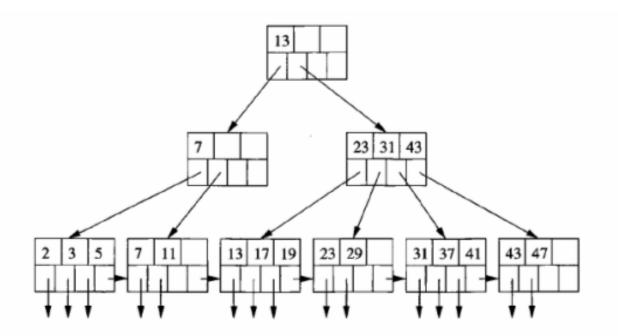
n=3



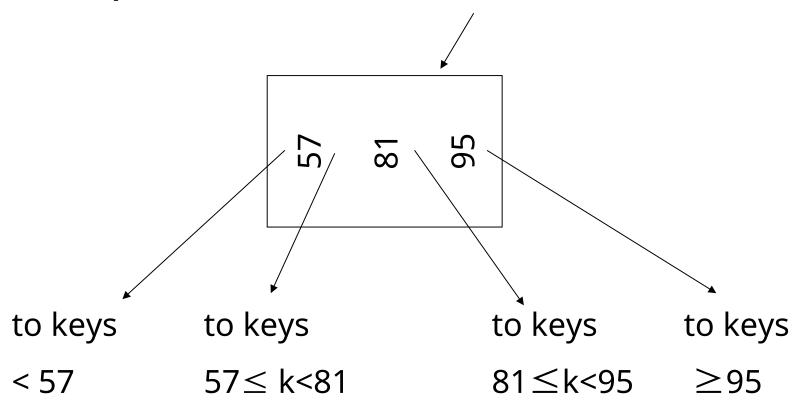
Lookup in a B+ tree

Useful for range queries too

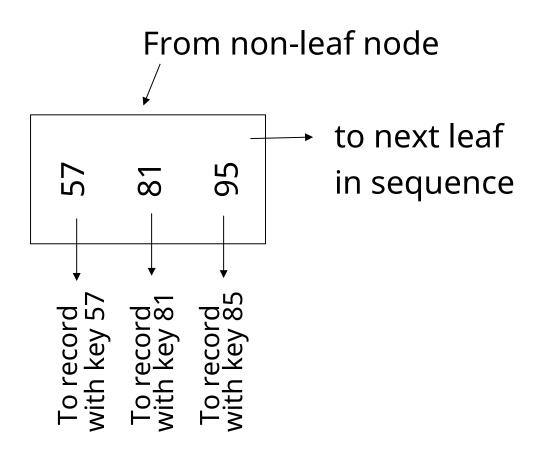
SELECT * FROM R WHERE R.o >= a AND R.o <= b;



Sample non-leaf

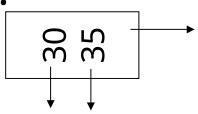


Sample leaf node:

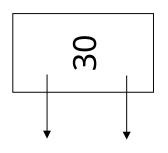


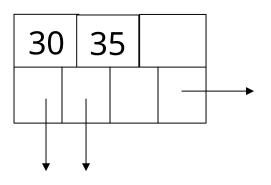
In textbook's notation n=3

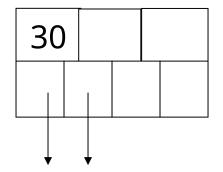
Leaf:



Non-leaf:







Size of nodes: n+1 pointers
n keys_

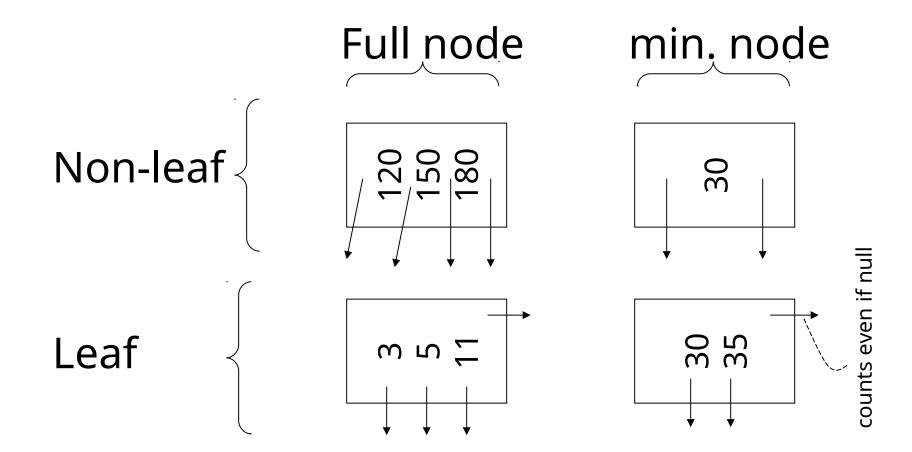
Don't want nodes to be too empty

Use at least

Non-leaf: [(n+1)/2] pointers

Leaf: [(n+1)/2] pointers to data

n=3



<u>B+tree rules</u> tree of order *n*

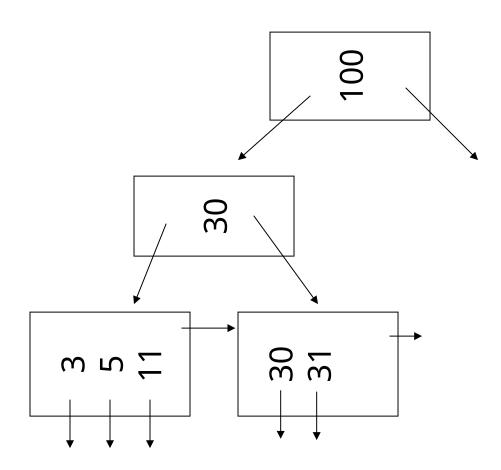
- (1) All leaves at same lowest level (balanced tree)
- (2) Pointers in leaves point to records except for "sequence pointer" (to next leaf)

(3) Number of pointers/keys for B+tree

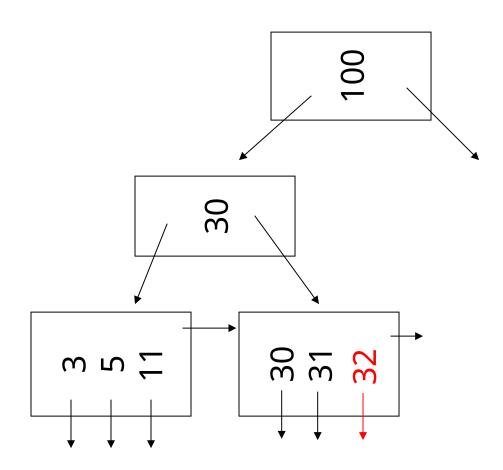
	Max ptrs	Max keys	Min ptrs⊸data	Min keys
Non-leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]- 1
Leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]
Root	n+1	n	1	1

<u>Insert into B+tree</u>

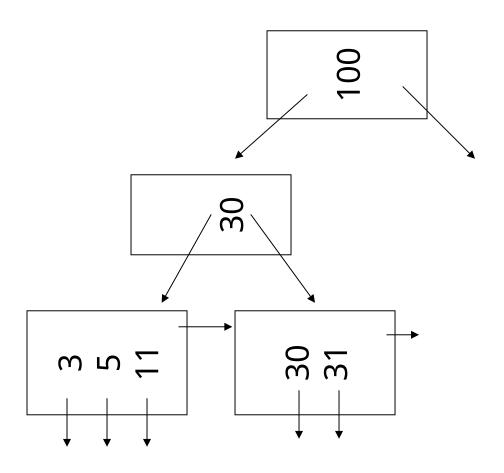
- (a) simple case
 - space available in leaf
- (b) leaf overflow
- (c) non-leaf overflow
- (d) new root



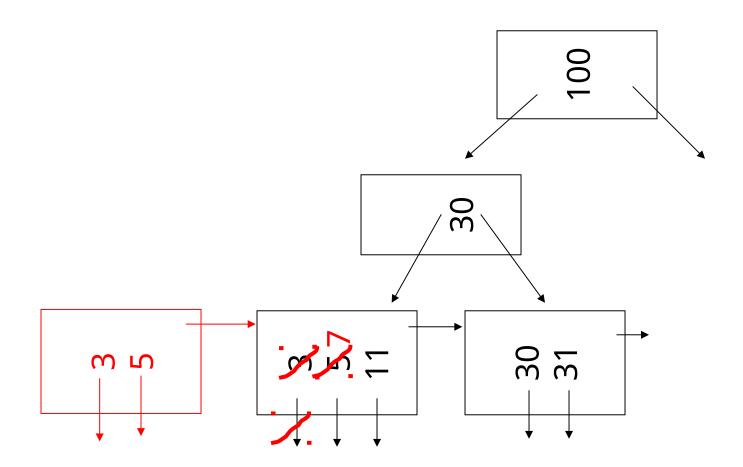
n=3



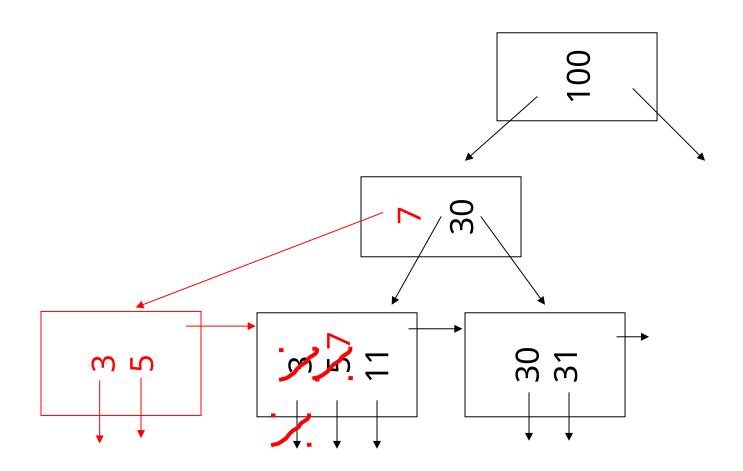




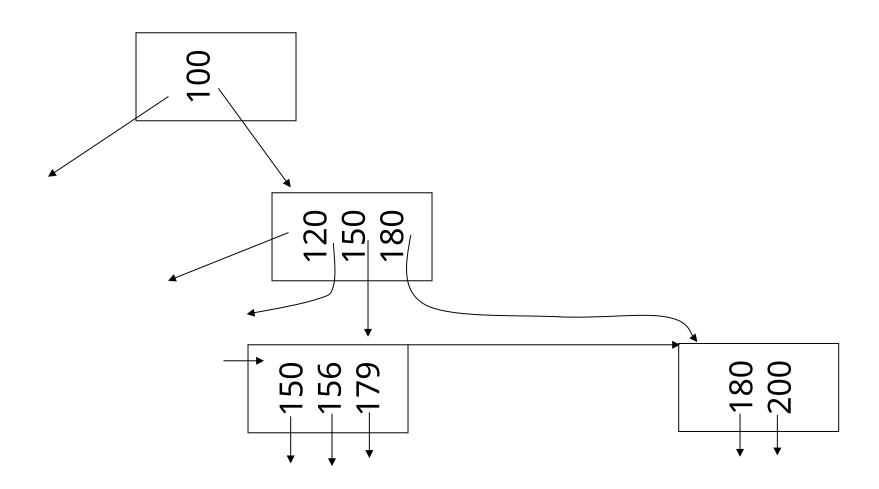




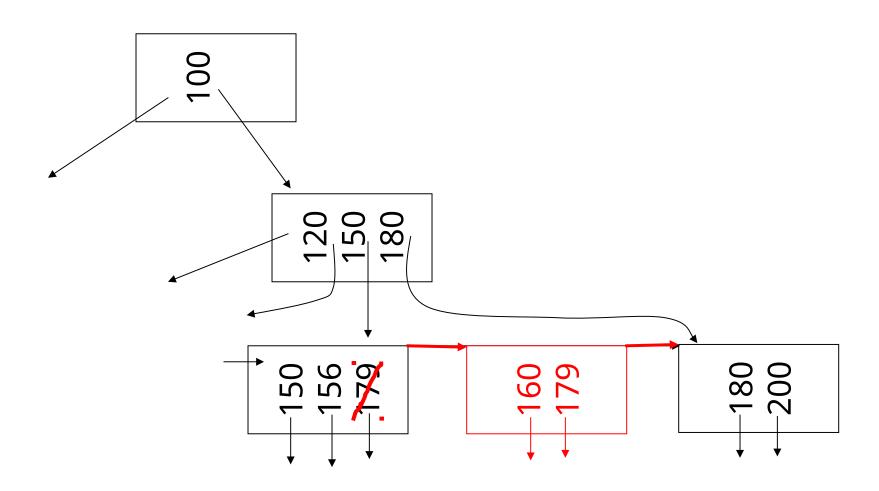




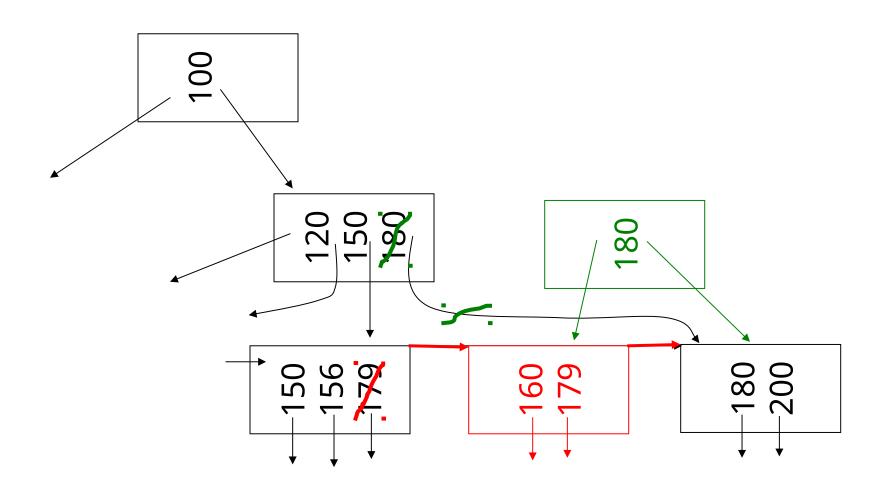






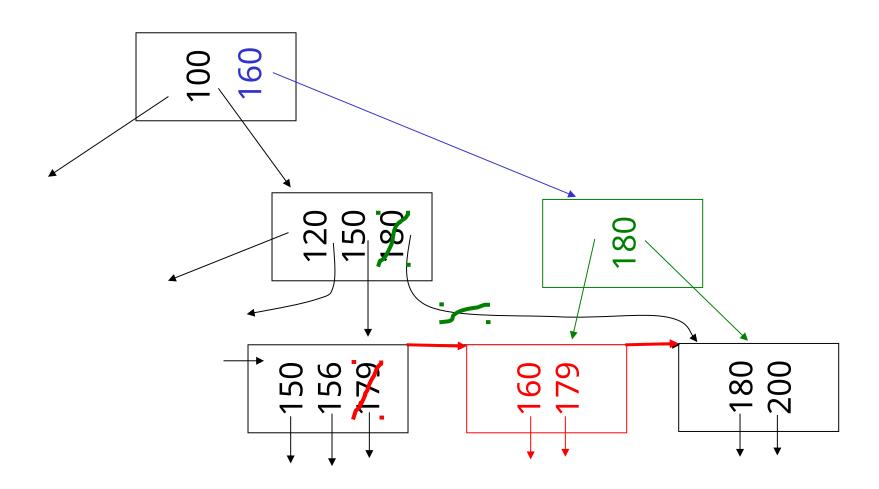


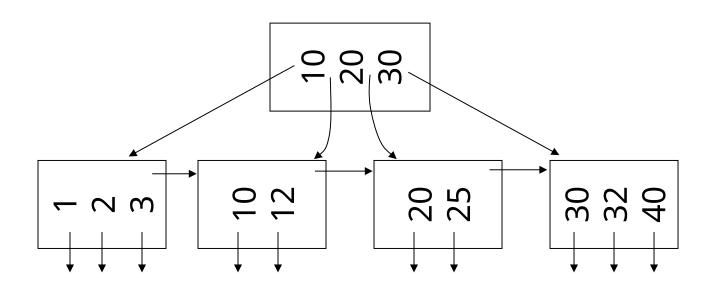


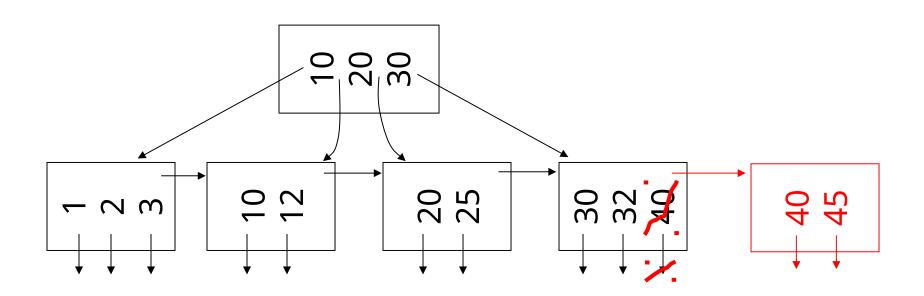


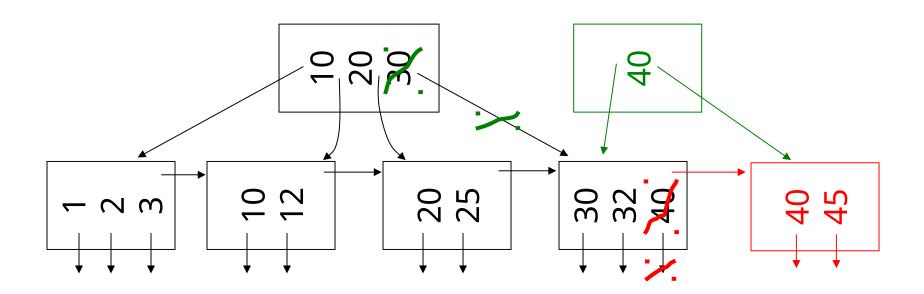
(c) Insert key = 160

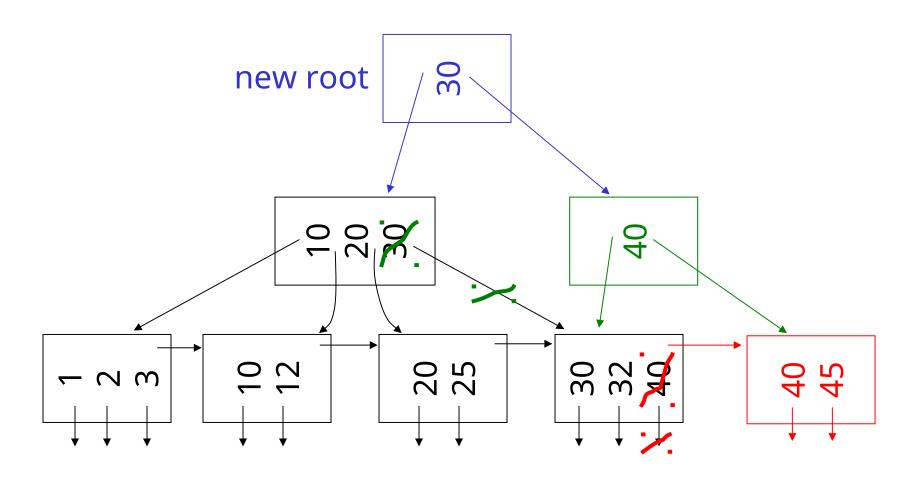










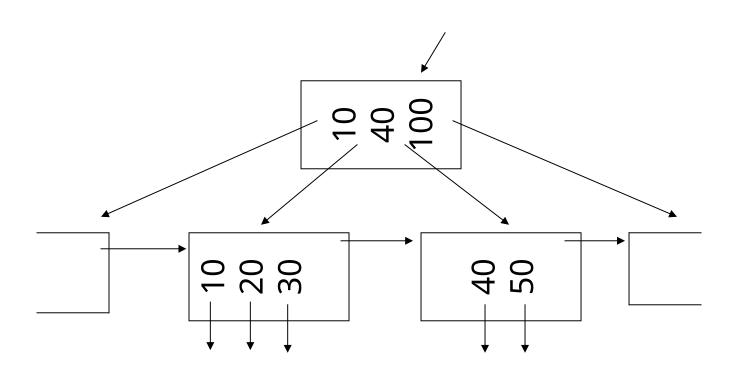


<u>Deletion from B+tree</u>

- (a) Simple case no example
- (b) Coalesce with neighbor (sibling)
- (c) Re-distribute keys
- (d) Cases (b) or (c) at non-leaf

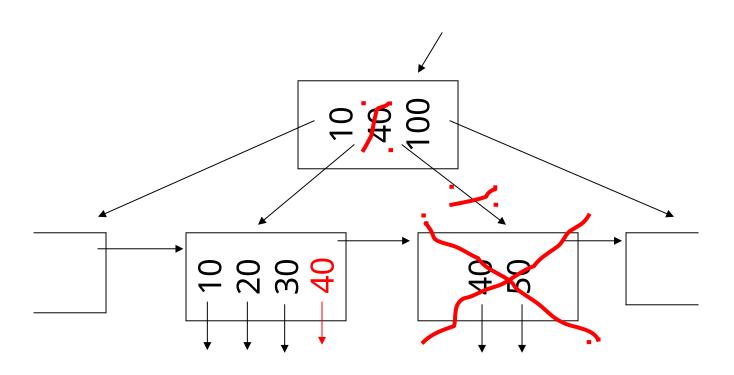
(b) Coalesce with sibling

n=4

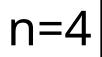


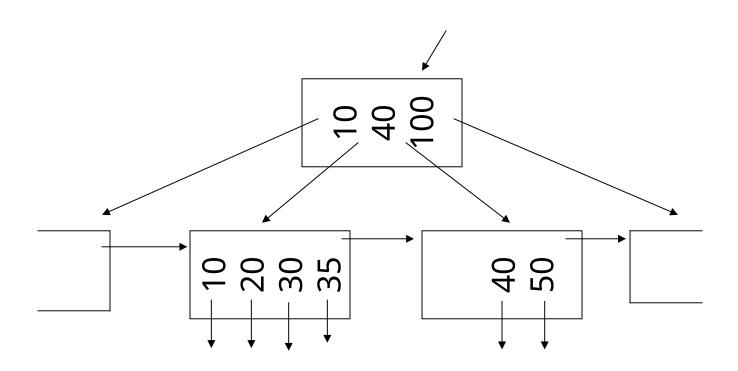
(b) Coalesce with sibling

n=4

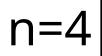


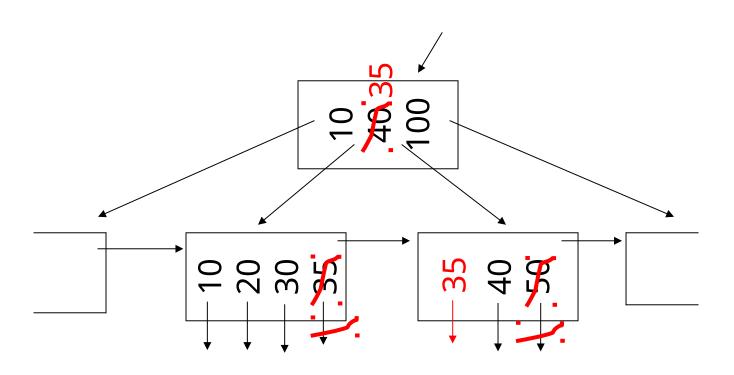
(c) Redistribute keys

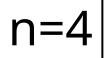


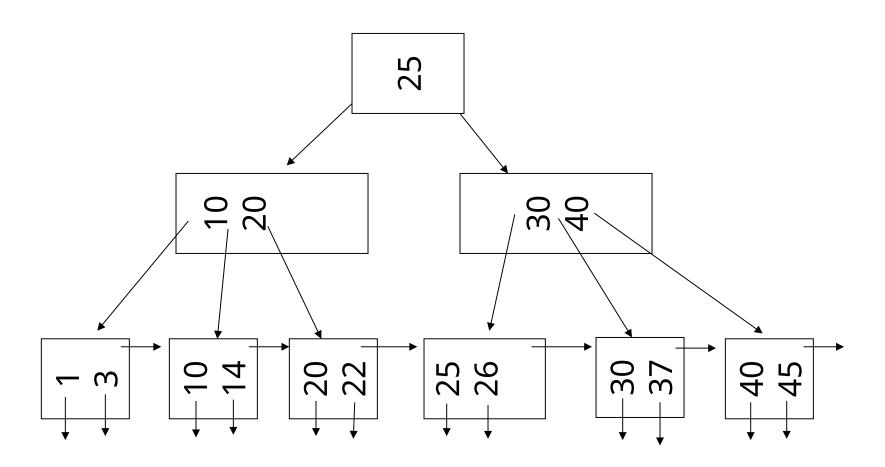


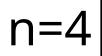
(c) Redistribute keys

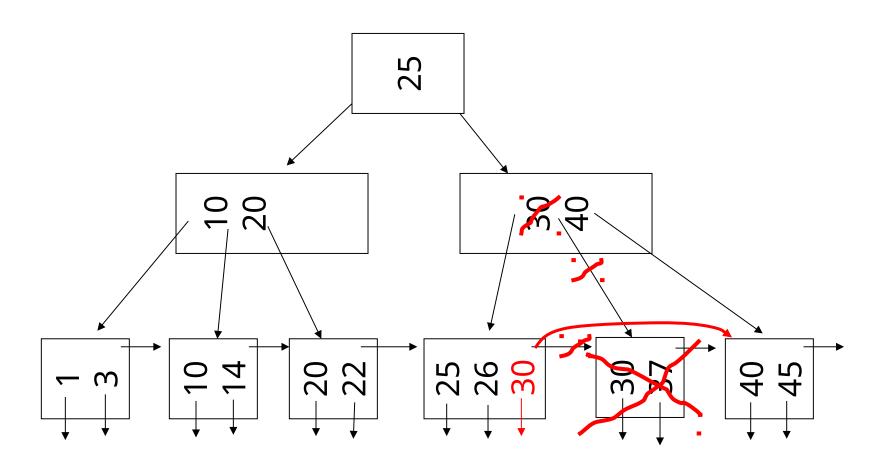


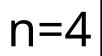


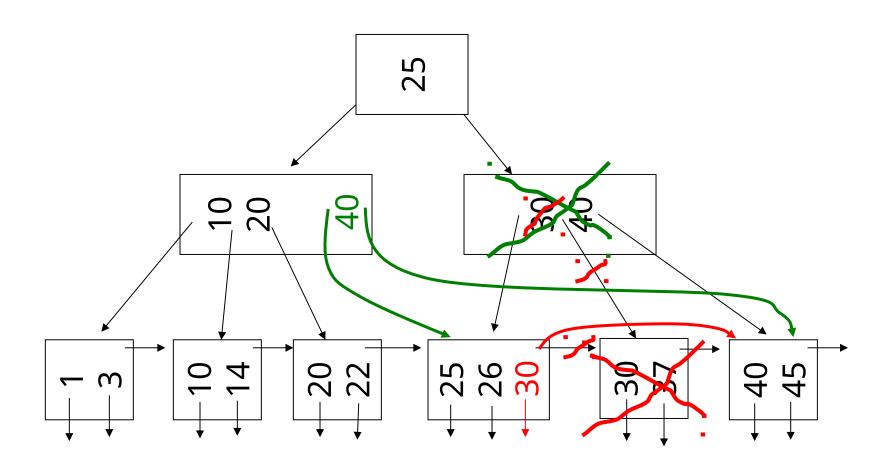


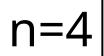


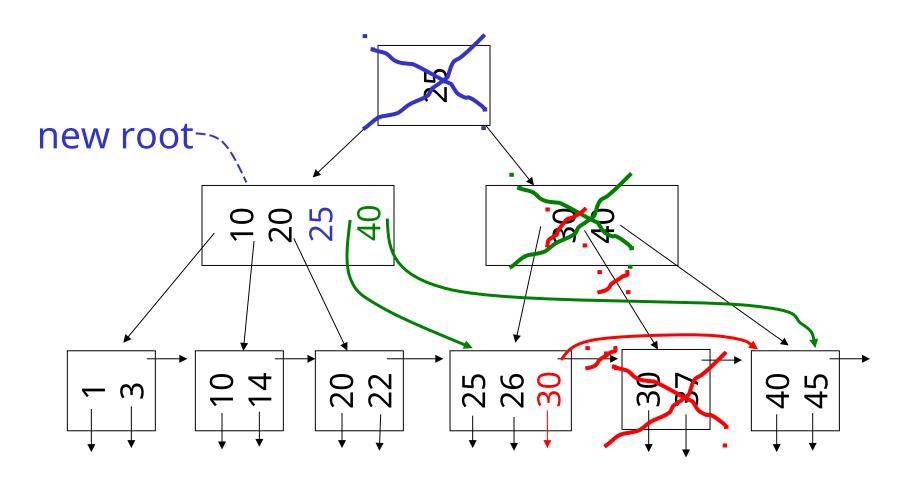












B+tree deletions in practice

- Often, coalescing is <u>not</u> implemented
 - Too hard and not worth it!

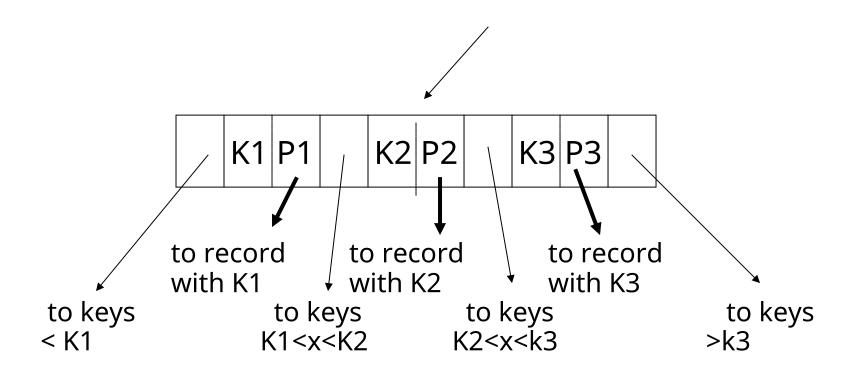
Speaking of buffering...
 Is LRU a good policy for B+tree buffers?

- → Of course not!
- → Should try to keep root in memory at all times

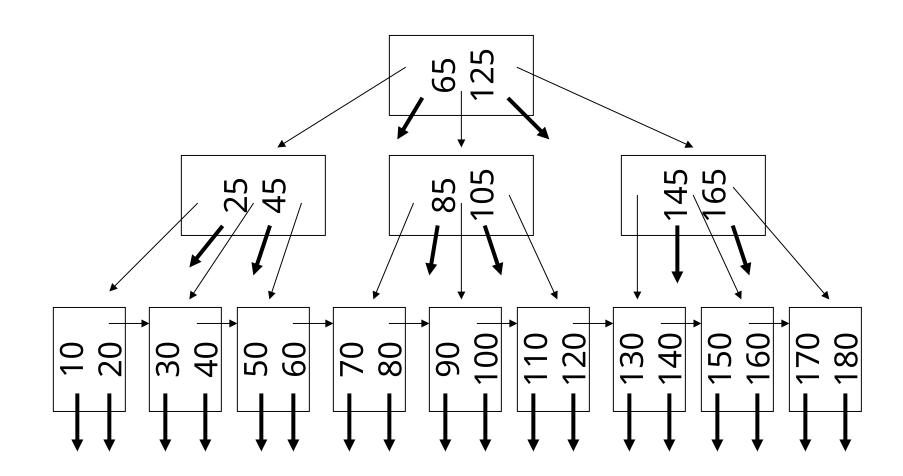
(and perhaps some nodes from second level)

Variation on B+tree: B-tree (no +)

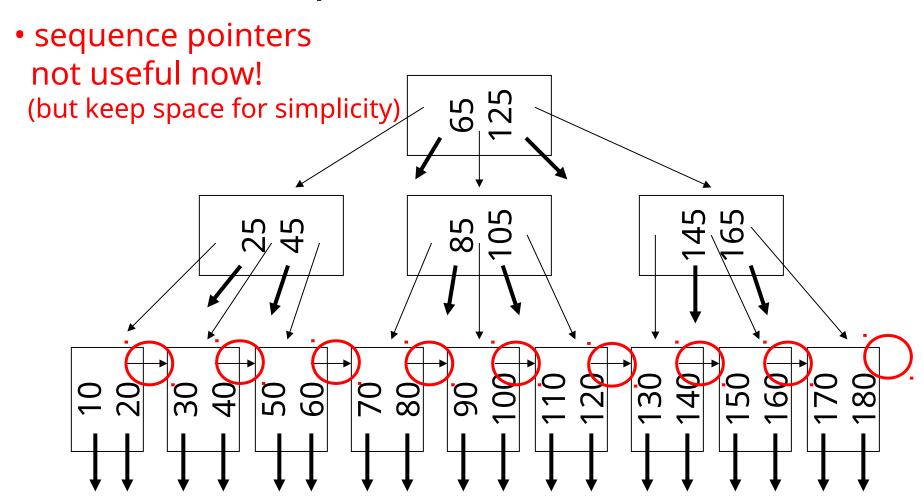
- Idea:
 - Avoid duplicate keys
 - Have record pointers in non-leaf nodes



B-tree example

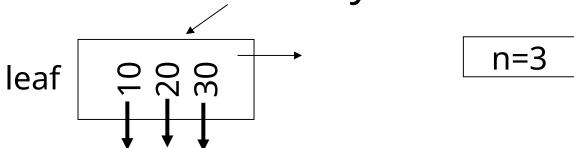


B-tree example



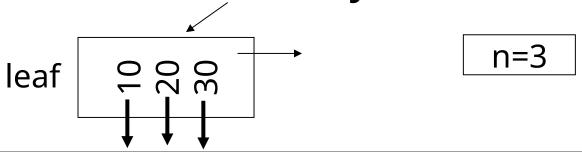
Note on inserts

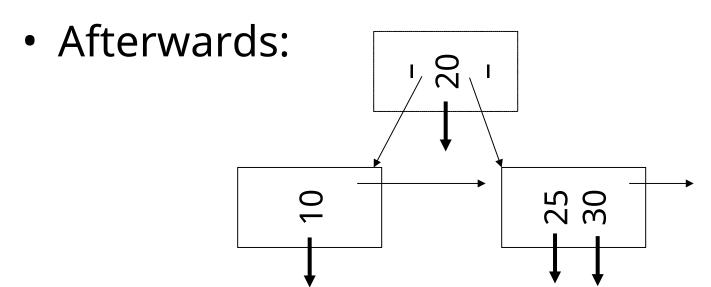
Say we insert record with key = 25



Note on inserts

Say we insert record with key = 25





So, for B-trees:

	MAX					
	Tree Ptrs	Rec k Ptrs	(eys	Tree Ptrs	Rec Ptrs	Keys
Non-leaf non-root	n+1	n	n	[(n+1)/2]	(n+1)/2]-1 [(r	ı+1)/2 []] -1
Leaf non-root	1	n	n	1	[n/2]	[n/2]
Root non-leaf	n+1	n	n	2	1	1
Root Leaf	1	n	n	1	1	1

Tradeoffs:

© B-trees have faster lookup than B+trees

- in B-tree, non-leaf & leaf different sizes
- (2) in B-tree, deletion more complicated

Tradeoffs:

© B-trees have faster lookup than B+trees

- in B-tree, non-leaf & leaf different sizes
- (2) in B-tree, deletion more complicated

→ B+trees preferred!

But note:

If blocks are fixed size
 (due to disk and buffering restrictions)

Then lookup for B+tree is actually better!!

Outline/summary

- Conventional Indexes
 - Sparse vs. dense
 - Primary vs. secondary
- B trees
 - B+trees vs. B-trees
 - B+trees vs. indexed sequential
- Hashing schemes --> Next