

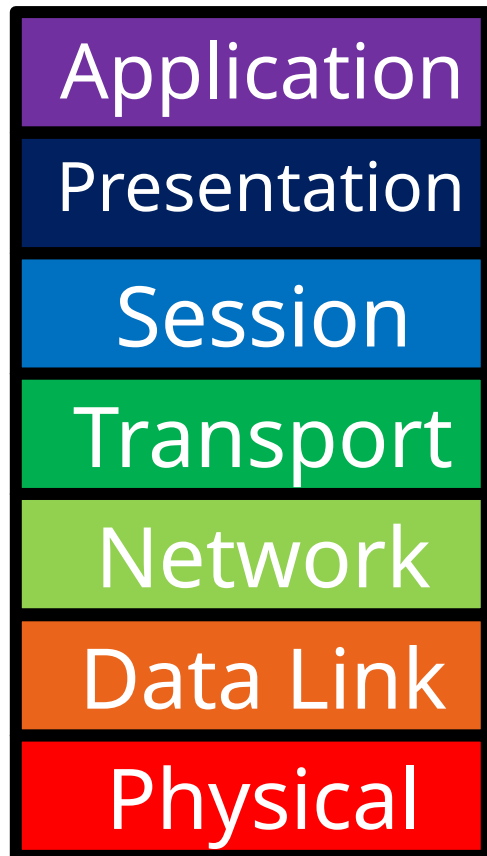
Computer Networks

Lecture 2: Data Link

Based on slides from D. Choffnes Northeastern U. and P. Gill from StonyBrook University
Revised Autumn 2015 by S. Laki

Data Link Layer

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□ Function:

- Send blocks of data (**frames**) between physical devices
- Regulate access to the physical media

□ Key challenge:

- How to delineate frames?
- How to detect errors?
- How to perform **media access control (MAC)**?
- How to recover from and avoid **collisions**?

- ❑ Framing
- ❑ Error Checking and Reliability
- ❑ Media Access Control
 - ❑ 802.3 Ethernet
 - ❑ 802.11 Wifi

Framing

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- ❑ Physical layer determines how bits are encoded
- ❑ Next step, how to encode blocks of data
 - Packet switched networks
 - Each packet includes routing information
 - Data boundaries must be known so headers can be read
- ❑ Types of framing
 - Byte oriented protocols
 - Bit oriented protocols
 - Clock based protocols

Byte Oriented: Byte Stuffing

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- Add **FLAG** bytes as sentinel to the beginning and end of the data
- Problem: what if **FLAG** appears in the data?
 - Add a special **DLE** (Data Link Escape) character before **FLAG**
 - What if **DLE** appears in the data? Add **DLE** before it.
 - Similar to escape sequences in C
 - `printf("You must \"escape\" quotes in strings");`
 - `printf("You must \\escape\\ forward slashes as well");`
- Used by Point-to-Point protocol, e.g. modem, DSL, cellular

Byte Oriented: Byte Counting

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- Sender: insert length of the data in bytes at the beginning of each frame
- Receiver: extract the length and read that many bytes
- What happens if there is an error transmitting the count field?

Bit Oriented: Bit Stuffing

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01111110

Data

01111110

- Add sentinels to the start and end of data (similarly to byte stuffing)
 - Both sentinels are the same
 - Example: 01111110 in High-level Data Link Protocol (HDLC)
- Sender: insert a 0 after each 11111 in data
 - Known as “bit stuffing”
- Receiver: after seeing 11111 in the data...
 - 11111**0** □ remove the 0 (it was stuffed)
 - 11111**1** □ look at one more bit
 - 11111**10** □ end of frame
 - 11111**11** □ error! Discard the frame
- Disadvantage: 20% overhead at worst
- What happens if error in sentinel transmission?

Clock-based Framing: SONET

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- **Synchronous Optical Network**
 - Transmission over very fast optical links
 - STS- n , e.g. STS-1: 51.84 Mbps, STS-768: 36.7 Gbps
- STS-1 frames based on fixed sized frames
 - $9 \times 90 = 810$ bytes □ after 810 bytes look for start

Special start pattern

90 Columns

Overhead

Payload

- Bits are encoded
- Payload is XOF to avoid long Seq

- ❑ Framing
- ❑ Error Checking
- ❑ Media Access Control
 - ❑ 802.3 Ethernet
 - ❑ 802.11 Wifi

Dealing with Noise

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- The physical world is inherently noisy
 - Interference from electrical cables
 - Cross-talk from radio transmissions, microwave ovens
 - Solar storms
- How to detect bit-errors in transmissions?
- How to recover from errors?

Naïve Error Detection

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- Idea: send two copies of each frame
 - if (memcmp(frame1, frame2) != 0) { OH NOES, AN ERROR! }
- Why is this a bad idea?
 - Extremely high overhead
 - Poor protection against errors
 - Twice the data means twice the chance for bit errors

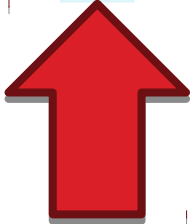
Parity Bits

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- Idea: add extra bits to keep the number of 1s **even**
 - Example: 7-bit ASCII characters + 1 parity bit

0101001 1 1101001 0 1011110 1 0001110 1 0110100 1

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- Detects 1-bit errors and some 2-bit errors
- Not reliable against bursty errors

Error control



□ Error Control Strategies

- Error Correcting codes (Forward Error Correction (FEC))
- Error detection and retransmission Automatic Repeat Request (ARQ)

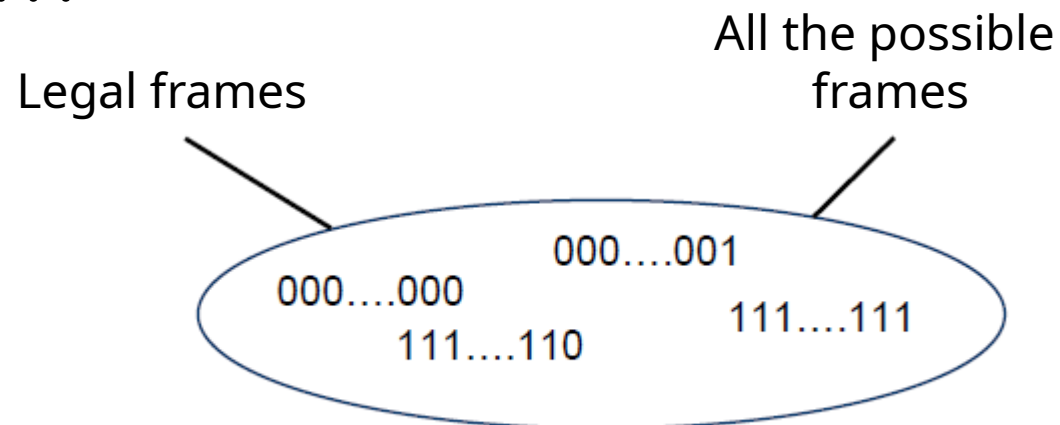
Error control

□ Objectives

- Error detection
 - with correction
 - Forward error correction
 - without correction -> e.g. drop a frame
 - Backward error correction
 - The erroneous frame needs to be retransmitted
- Error correction
 - without error detection
 - e.g. in voice transmission

Redundancy

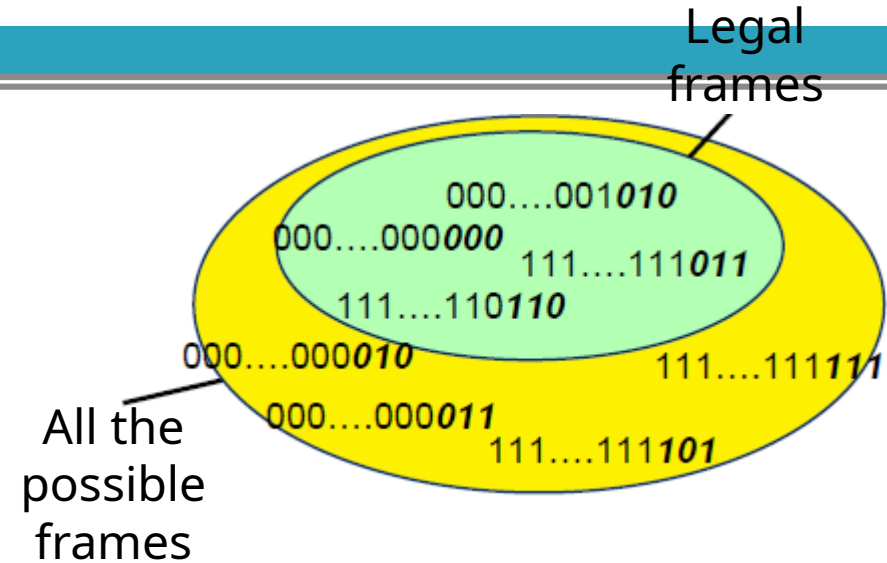
- Redundancy is required for error control
- Without redundancy
 - 2^m possible data messages can be represented as data on m bits
 - They all are legal!!!
 - Each error results a new legal data message
- How to detect errors???



Error-correcting codes

Redundancy

- A frame consists of
 - m data bits (message)
 - r redundant/check bits
 - The total length $n = m + r$



- This n-bit unit is referred to as an n-bit codeword!

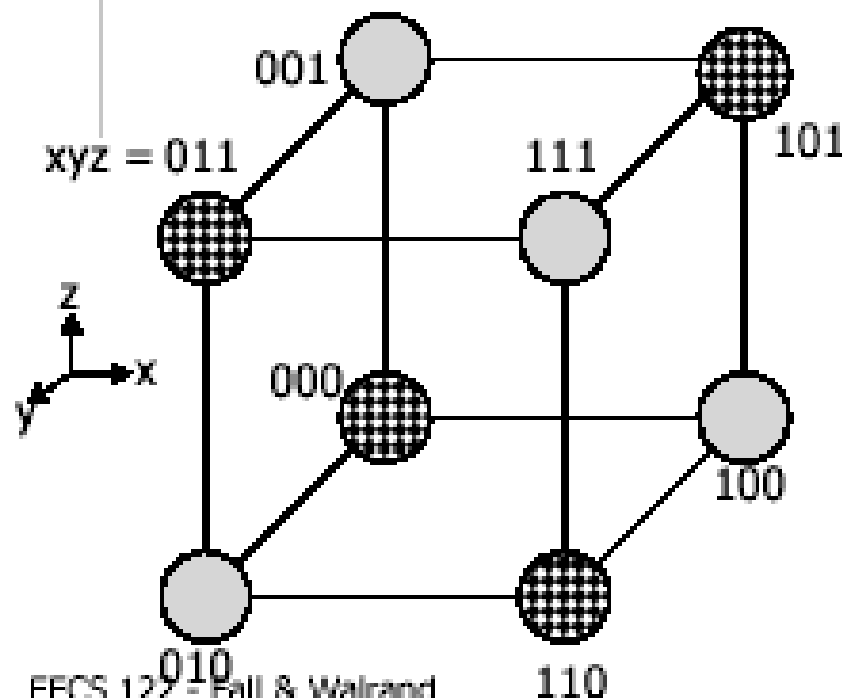
Error Control Codes

How Codes Work: Words and Codewords

◆ Code = subset of possible words: Codewords

◆ Example:

$n = 3$ bits \Rightarrow 8 words; codewords: subset



Words:

000, 001, 010, 011
100, 101, 110, 111

Code:

000, 011, 101, 110

Send only codewords

Hamming distance

- The **Hamming distance** between two codewords is the number of differences between corresponding bits.

1. The Hamming distance $d(000, 011)$ is 2 because

$000 \oplus 011$ is 011 (two 1s)

2. The Hamming distance $d(10101, 11110)$ is 3 because

$10101 \oplus 11110$ is 01011 (three 1s)

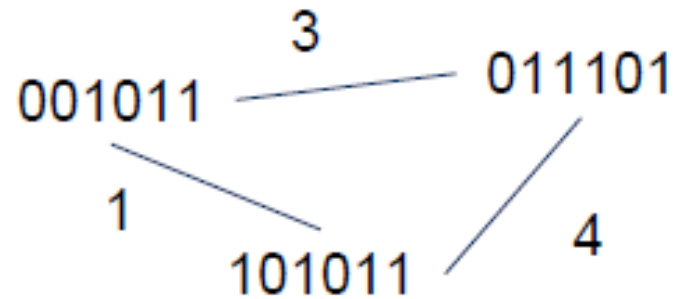
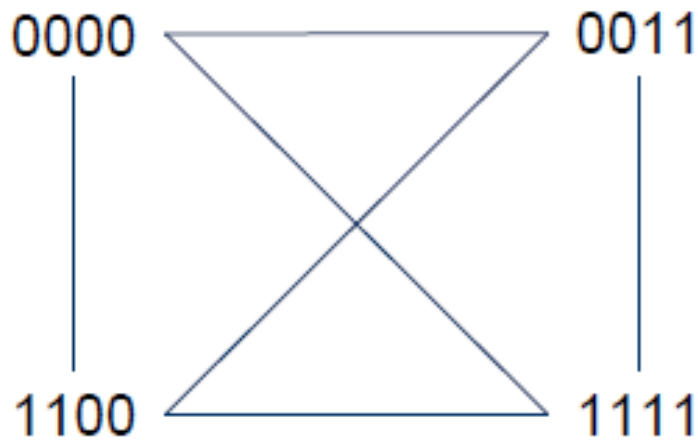
Hamming distance

- If not all the 2^n possible codewords are used
 - Set of legal codewords $=: S$
- Hamming distance of the complete code
 - The smallest Hamming distance of between all the possible pairs in the set of legal codewords (S)

$$d(S) = \min_{x,y \in S, x \neq y} d(x, y)$$

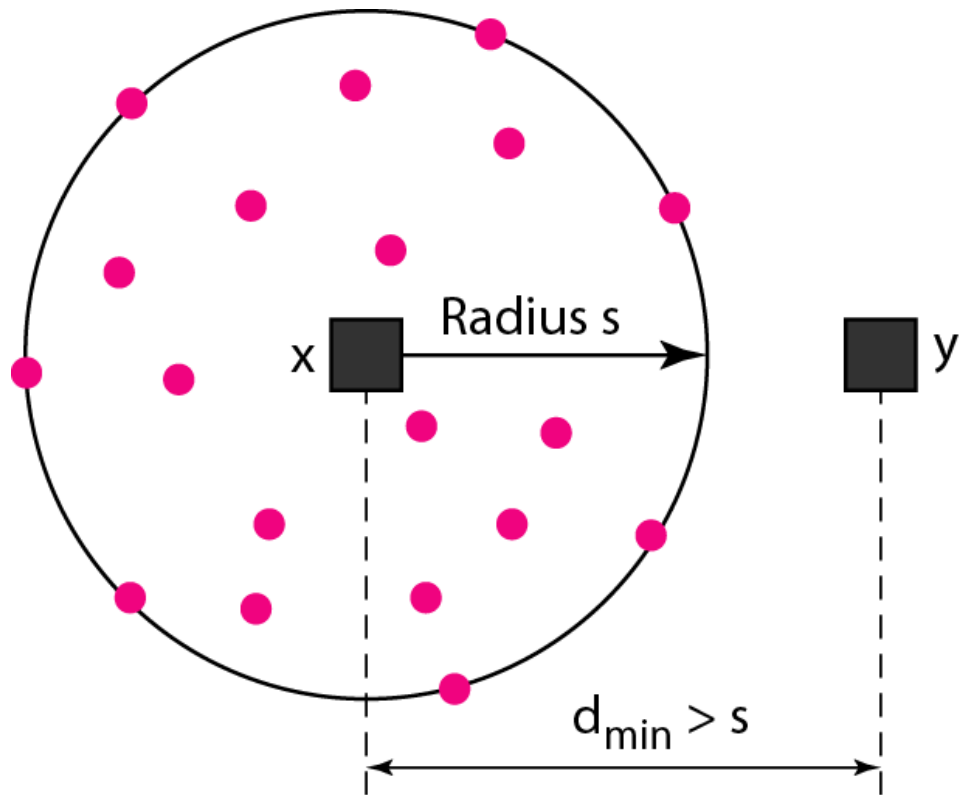
What is the Hamming distance?

- Two examples:



Error detection

To detect d errors, you need a distance $d+1$ code.



Legend



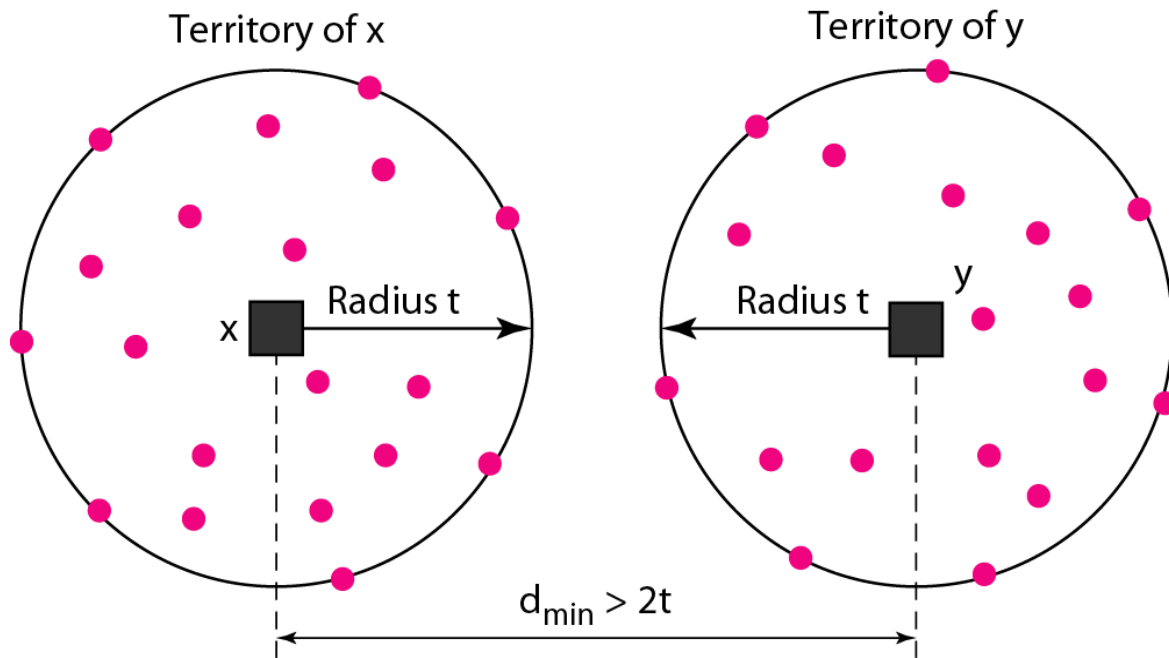
Any valid codeword



Any corrupted codeword
with 0 to s errors

Error correction

To correct d errors, you need a distance $2d+1$ code.



Legend

- Any valid codeword
- Any corrupted codeword with 1 to t errors

Example



$S = \{$ 00000000,
00001111,
11110000,
11111111
 $\}$

Parity bit – already discussed

- A single parity bit is appended to the data
 - Chosen according to the number of 1 bits in the message
 - odd or even

- An example using even parity
 - Original message: 1011010
 - A 0 bit is added to the end: 10110100
 - $m=8$ and $r=1$ in this case

- The distance of this code is 2, since any single-bit error produces a codeword with the wrong parity.

Checksums

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- Idea:
 - Add up the bytes in the data
 - Include the sum in the frame



- Use ones-complement arithmetic
- Lower overhead than parity: 16 bits per frame
- But, not resilient to errors
 - Why? $1\ 101001 + 0\ 101001 = 10010010$
- Used in UDP, TCP, and IP

Cyclic Redundancy Check (CRC)

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- Uses field theory to compute a semi-unique value for a given message

- Much better performance than previous approaches
 - Fixed size overhead per frame (usually 32-bits)
 - Quick to implement in hardware
 - Only 1 in 2^{32} chance of missing an error with 32-bit CRC

CRC (Cyclic Redundancy Check)

□ Polynomial code

- Treating bit strings as representations of polynomials with coefficients of 0 and 1.

□ CRC

- Add k bits of redundant data to an n -bit message.
- Represent n -bit message as an $n-1$ degree polynomial;
 - e.g., MSG=10011010 corresponds to $M(x) = x^7 + x^4 + x^3 + x^1$.
- Let k be the degree of some divisor polynomial $G(x)$;
 - e.g., $G(x) = x^3 + x^2 + 1$.
 - Generator polynomial
 - Agreed upon it in advance

CRC

- Transmit polynomial $P(x)$ that is evenly divisible by $G(x)$, and receive polynomial $P(x) + E(x)$;
 - $E(x)=0$ implies no errors.

- Recipient divides $(P(x) + E(x))$ by $G(x)$;
 - the remainder will be zero in only two cases:
 - $E(x)$ was zero (i.e. there was no error),
 - or $E(x)$ is exactly divisible by $C(x)$.

- Choose $G(x)$ to make second case extremely rare.

A basic example with numbers

- Make all legal messages divisible by 3
- If you want to send 10
 - First multiply by 4 to get 40
 - Now add 2 to make it divisible by 3 = 42
- When the data is received ..
 - Divide by 3, if there is no remainder there is no error
 - If no error, divide by 4 to get sent message
- If we receive 43, 44, 41, 40, then error
- 45 would not be recognized as an error

Mod 2 arithmetic

- Operations are done modulo 2

A	B	A + B
0	0	0
0	1	1
1	0	1
1	1	0

A	B	A - B
0	0	0
0	1	1
1	0	1
1	1	0

A	B	A · B
0	0	0
0	1	0
1	0	0
1	1	1

```
0110111011
+ 1101010110
= 1011101101
```

```
1111
+1010
=====
0101
```

```
11001
x 101
=====
11001
+ 11001
=====
1111101
```

A basic example with polynomials

□ Sender:

- multiply $M(x) = x^7 + x^4 + x^3 + x^1$ by x^k ; for our example, we get
 - $x^{10} + x^7 + x^6 + x^4 (10011010000)$;
- divide result by $C(x) (1101)$;

		11111001	
Generator	1101	10011010000	Message
		1101	
		1001	
		1101	
		1000	
		1101	
		1011	
		1101	
		1100	
		1101	
		1000	
		1101	
		101	Remainder

Send $10011010000 + 101 = 10011010101$,
since this must be exactly divisible by $C(x)$;

Further properties

- Want to ensure that $G(x)$ does not divide evenly into polynomial $E(x)$.
- All single-bit errors, as long as the x^k and x^0 terms have non-zero coefficients.
- All double-bit errors, as long as $G(x)$ has a factor with at least three terms.
- Any odd number of errors, as long as $G(x)$ contains the factor $(x + 1)$.
- Any “burst” error (i.e sequence of consecutive errored bits) for which the length of the burst is less than k bits.
- Most burst errors of larger than k bits can also be detected.

Even Parity

Actually consists of using $x+1$ polynomial

Given message 0111, multiply by x to get 01110

Now divide by $x+1=11$

$$\begin{array}{r} 0101 \\ 11 \overline{) 01110} \\ \underline{11} \\ 0010 \\ \underline{11} \end{array}$$

1=remainder

Message = $01110+1=01111$ even parity

□ Common polynomials for $C(x)$:

CRC	$C(x)$
CRC-8	$x^8 + x^2 + x^1 + 1$
CRC-10	$x^{10} + x^9 + x^5 + x^4 + x^1 + 1$
CRC-12	$x^{12} + x^{11} + x^3 + x^2 + x^1 + 1$
CRC-16	$x^{16} + x^{15} + x^2 + 1$
CRC-CCITT	$x^{16} + x^{12} + x^5 + 1$
CRC-32	$x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$