

data don't speak for themselves

a quick introduction to Bayesian statistics

João P. Faria

Bayesian Stats



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Welcome everyone! Thank you for coming.

We had a few courses about Bayesian statistics in the past given by Michael Bazot and Alex and by Pascal Bordé.

I decided to do this course because that was already 2 years ago, and because those courses did not focus on learning statistics from intuition.

I think that's important, and whether or not I'll be able to do it myself I'll leave for you to judge.

Just to mention that the title is only in part a joke, as we will see by the end.

Disclaimer

I'm not a statistician.

I never gave this course before.

I borrowed (heavily) from material presented in the references.

But, unless otherwise noted, all opinions are my own.

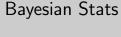


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Outline

- main differences between frequentist and Bayesian statistics
 - problems with p-values, confidence intervals and null hypothesis testing
- the basic rules of probability theory
- how to assign probability distributions
 - the role of priors
 - the likelihood
- the simplest models in Bayesian statistics
 - linear regression
 - beta-binomial model
 - hierarchical models



└─Outline

2016-02-08

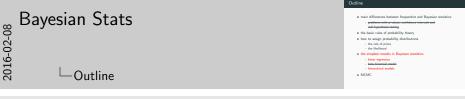
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This is the outline that I sent to Carlos and that he sent to you when announcing the course.

I hadn't prepared the course yet when I wrote this so there's a few things that I won't have time to cover.

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 - hierarchical models
- MCMC



I will only speak very briefly about frequentist statistics
I'll speak about p-values and confidence intervals only if someone asks.

These simple models in red I will only discuss in the practical classes, but not the beta-binomial model

And I will speak about MCMC today.

Of course you can ask whatever questions you want, but I will put up these Q/A slides at every section and I would ask you to save your questions until one of these shows up.

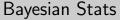
So... questions already?

Introduction

Bayesian Stats —Introduction

Introduction

• statistical inference was invented because of astronomy (this claim is not based on an in-depth search)



-Introduction

-brief historical sketch

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brief historical sketch

Let's start with a bit of history.

I think it's fair to say that statistics started with people trying to solve astronomy problems.

the initial concerns were about observational errors and how to combine observations by different people

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- Tycho Brahe, Galileo, Legendre, Laplace, Gauss used and developed statistical methods

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-Introduction

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this was formalised (maybe most famously) by Gauss

but many great names worked on predicting the position of astronomical objects, for example

they were using essentially Bayesian methods.

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- $\bullet \sim 20 \text{th}$ century, astronomers focused on least-squares techniques, and heuristic procedures

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in the 20th century, statistics turned its attention to biological and social sciences

and it kept developing but

new statistical concepts such as maximum likelihood emerged only slowly in astronomy

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in the late 1990s some collaborations between astronomers and statisticians started emerging

mainly problems in cosmology and image reconstruction

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- statistics today is mostly Bayesian (many) astronomers are (very) sceptical of (sophisticated) statistics

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and today we're at this stage where

most research in statistics is Bayesian

and I think it's still fair to say that many astronomers have this inherent, a priori scepticism for statistical analyses

which is because of many different reasons, one of which is certainly lack of training

Consider n independent measurements of the same quantity, under identical conditions

Calculate their mean \bar{x} and standard deviation σ



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frequentist and Bayesian

frequentist and Bayesian

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Consider n independent measurements of the same quantity, under identical conditions

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$$\mu = \bar{x} \pm \frac{\sigma}{\sqrt{n}}$$



frequentist and Bayesian

 $\mu = \hat{x} \pm \frac{\sigma}{\sqrt{g}}$

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$$p(\bar{x} - \frac{\sigma}{\sqrt{n}} \le \mu \le \bar{x} + \frac{\sigma}{\sqrt{n}}) = 68\%$$



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what you think this means: what it actually means:

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Bayesian Stats

—Introduction

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frequentist and Bayesian

under identical conditions

__frequentist and Bayesian

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Consider n independent measurements of the same quantity, under identical conditions

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what you want it to mean: what it actually means:

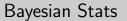
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Bayesian Stats under identical conditions -Introduction $\mu = \hat{x} \pm \frac{\sigma}{\sqrt{\sigma}}$ $p(\bar{x} - \frac{\sigma}{2} \le \mu \le \bar{x} + \frac{\sigma}{2}) = 68\%$ $p(\mu - \frac{\sigma}{2} \le \bar{x} \le \mu + \frac{\sigma}{2}) = 68\%$ frequentist and Bayesian

frequentist and Bayesian

Here is the main difference:

- Frequentists assign a probability to what is *random*
- Bayesians assign a probability to what is <u>unknown</u>



-Introduction

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Infrequentist and Bayesian

frequentist and Bayesian

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Blocks

Three different block environments are pre-defined and may be styled with an optional background color.

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—Introduction

└─Blocks

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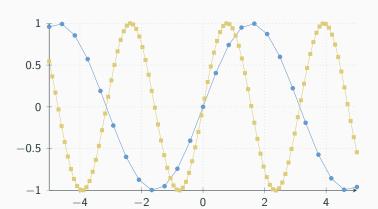
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Bayesian Stats
—Introduction
—Math

 $e = \lim_{n \to \infty} \left(1 + \frac{1}{n}\right)^n$

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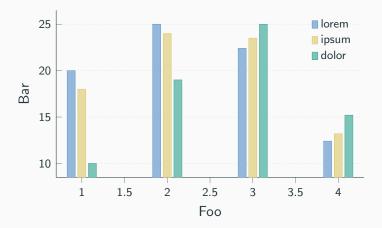
Line plots







Bar charts









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└─Quotes

Veni, Vidi, Vici

Veni, Vidi, Vici



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References

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Conclusion

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—Conclusion

Conclusion

Summary

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Q/A everything

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References I



P. Figueira, J. P. Faria, E. Delgado-Mena, V. Z. Adibekyan,

S. G. Sousa, N. C. Santos, and G. Israelian.

Exoplanet hosts reveal lithium depletion. Results from a homogeneous statistical analysis.

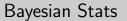
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Kepler-447b: a hot-Jupiter with an extremely grazing transit.

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-Conclusion

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A next step in exoplanetology: exo-moons.

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