

Image matching and visual search

Local features and geometry

Yannis Avrithis

National Technical University of Athens
Image, Video and Multimedia Systems Laboratory
Image and Video Analysis Group

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Outline

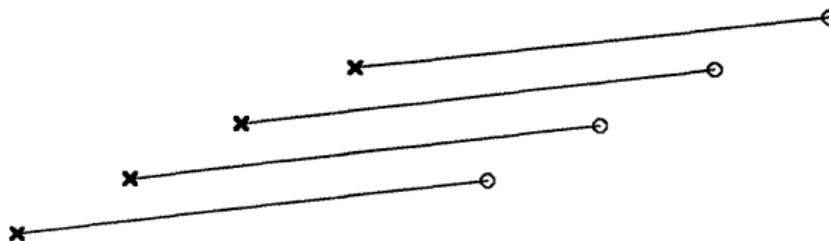
- ① Visual search, local features and bag-of-words
- ② Local features based on distance maps
- ③ Geometry indexing: feature map hashing
- ④ Relaxed spatial matching and re-ranking
- ⑤ Photo collections: view clustering and scene maps
- ⑥ Location and landmark recognition
- ⑦ Implementation: ivl library

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- 1 Visual search, local features and bag-of-words
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- 3 Geometry indexing: feature map hashing
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Matching local feature points

[Scott and Longuet-Higgins 1991]



- given two sets of points $a_i, i = 1, \dots, m$ and $b_j, j = 1, \dots, n$ on the same plane, let d_{ij} be the distance between a_i and b_j
- following earlier theories of Ullman and Marr, the problem is to associate points a_i and b_j in a **one-to-one correspondence** such that the **sum of squared distances** between corresponding points is minimized

A spectral approach

- ① construct the $m \times n$ proximity matrix G with elements

$$g_{ij} = \exp(-d_{ij}^2/2\sigma^2)$$

- ② perform singular value decomposition of G

$$G = USV^T$$

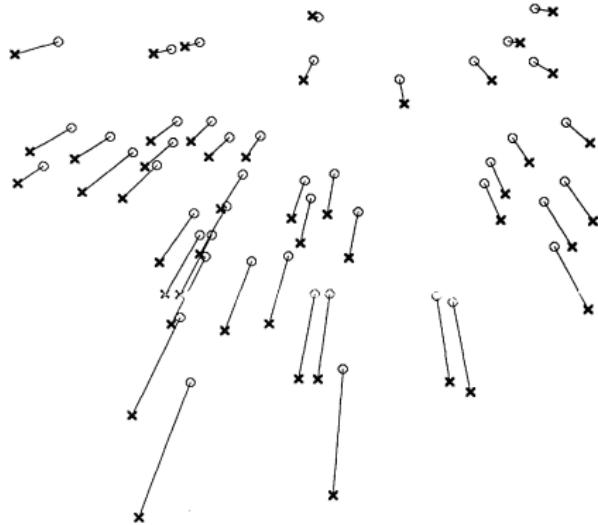
where U, V are orthogonal matrices of dimension m, n and S is a non-negative diagonal $m \times n$ matrix

- ③ replace each diagonal element s_{ij} of S by 1 and reconstruct

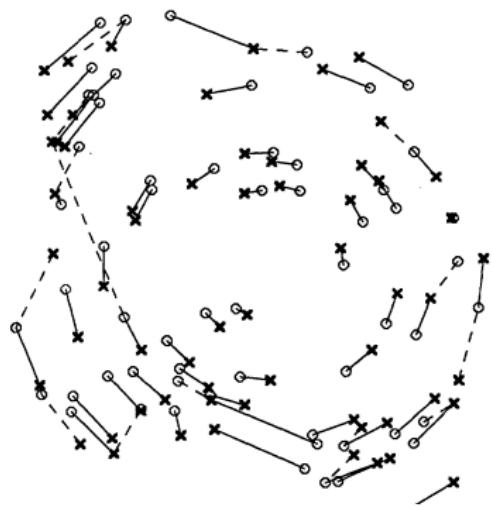
$$P = UEV^T$$

- ④ finally, associate points a_i and b_j if element p_{ij} of P is the greatest element in its row and its column

A spectral approach



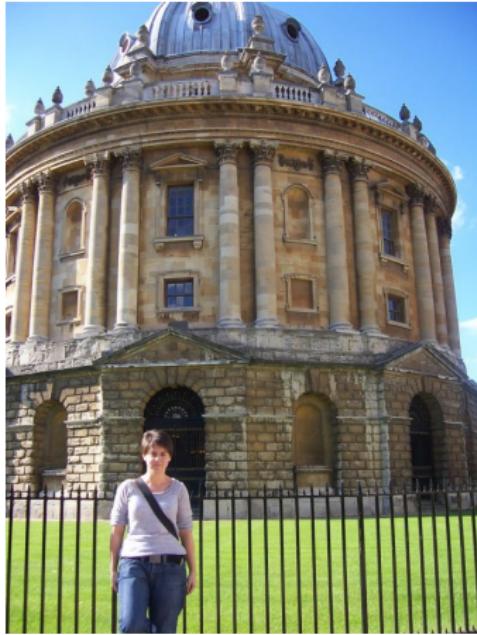
scale, translation



rotation

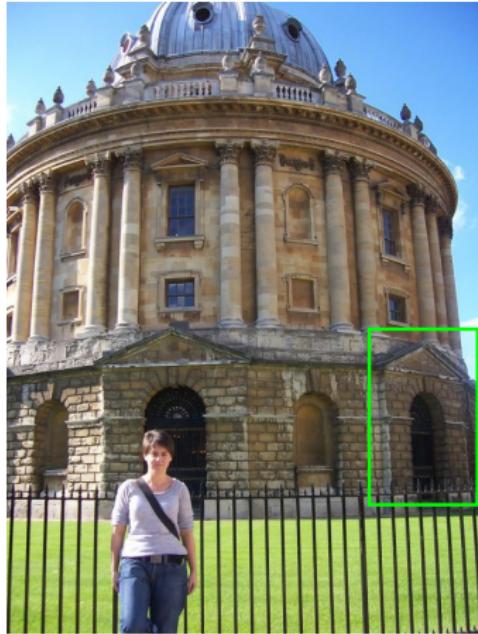
Matching discriminative local features

[Lowe 1999]



Matching discriminative local features

[Lowe 1999]

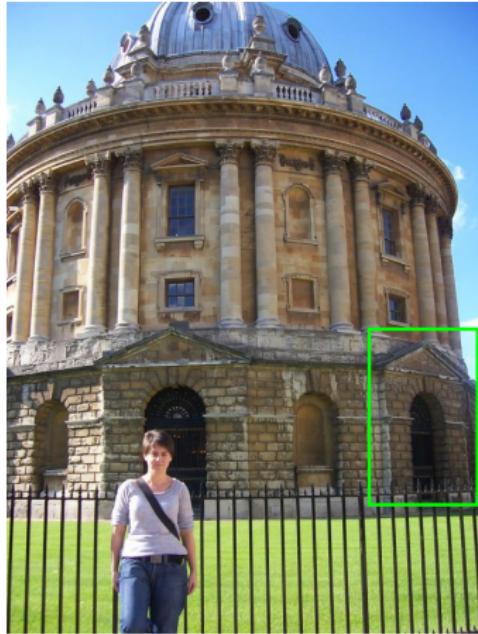


features

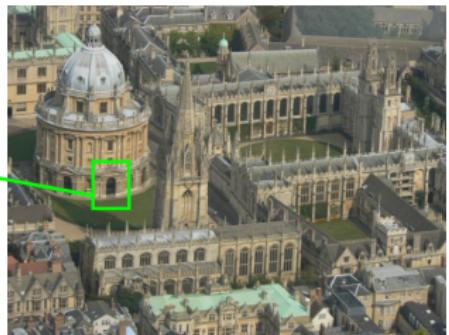
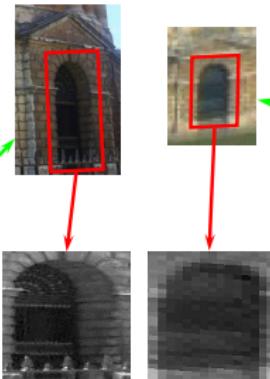


Matching discriminative local features

[Lowe 1999]



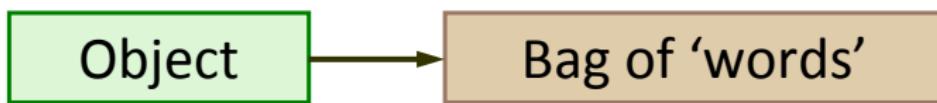
features



normalized features

Forget about geometry: bag-of-words

[Sivic and Zisserman 2003]



Vector quantization → visual words

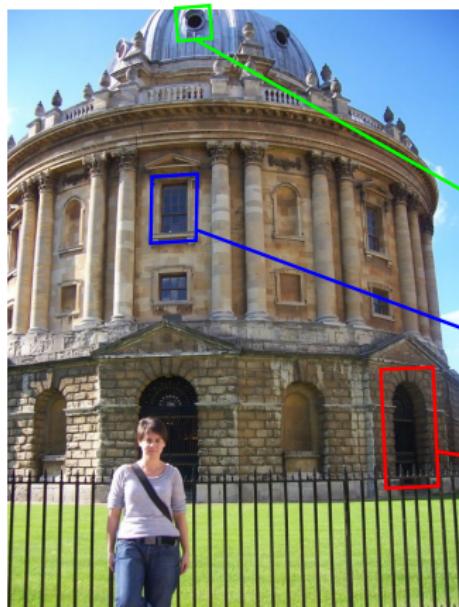


query

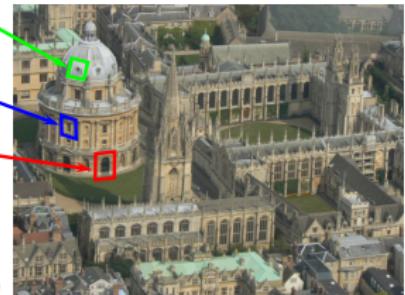


15

Vector quantization → visual words

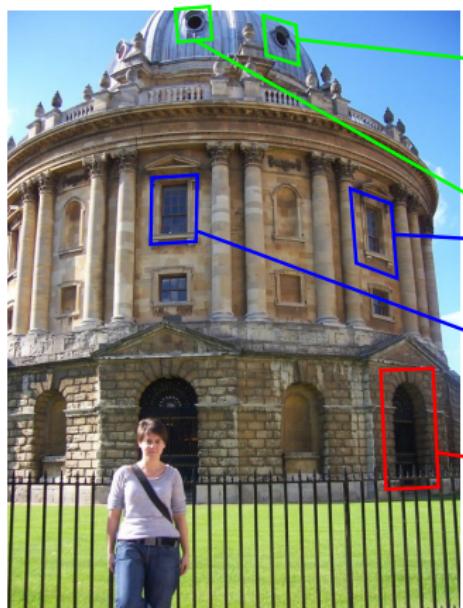


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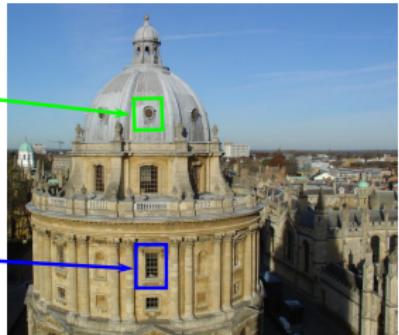
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Vector quantization → visual words

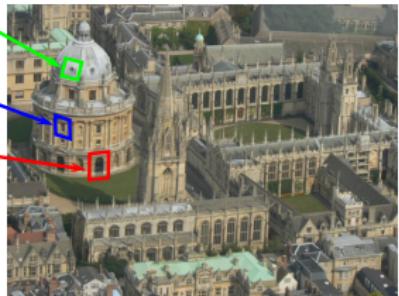


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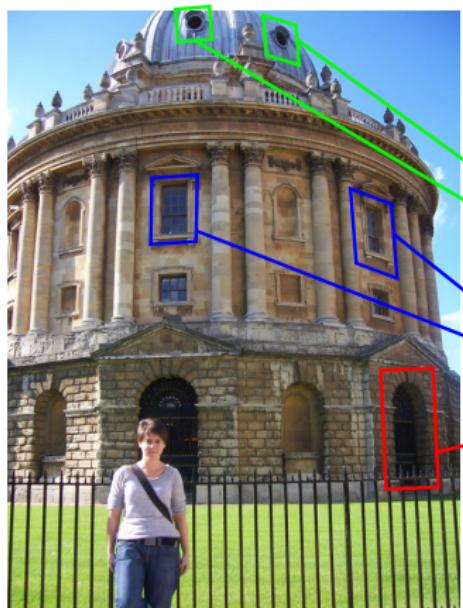
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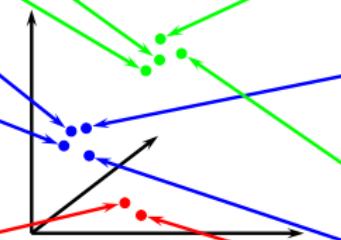
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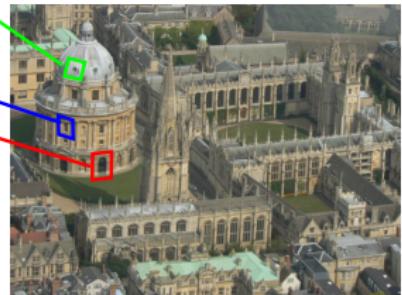
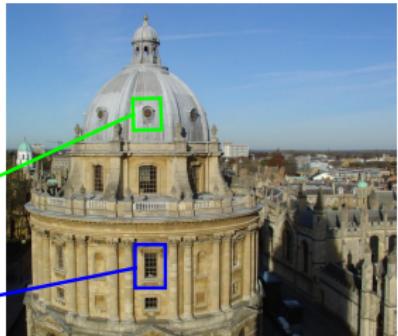
Vector quantization → visual words



query

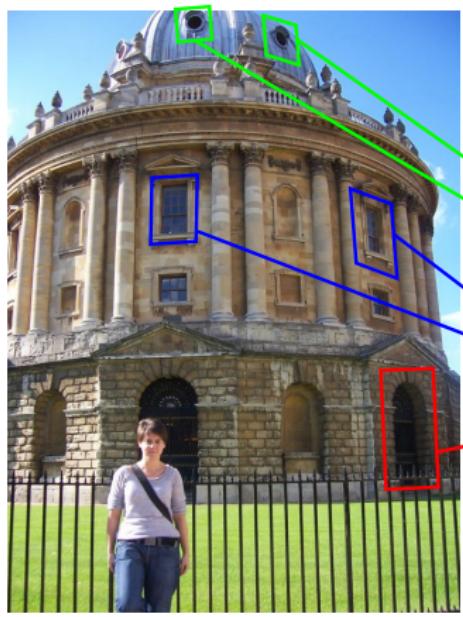


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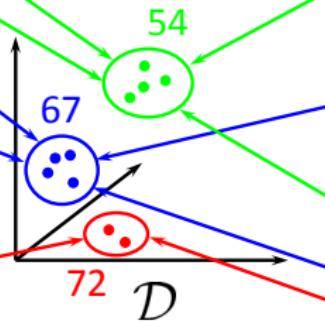


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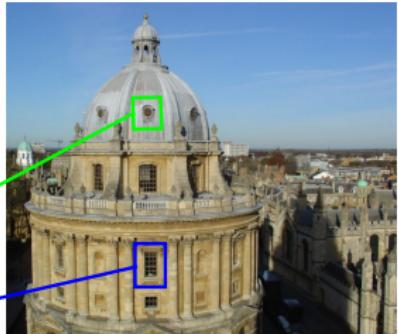
Vector quantization → visual words



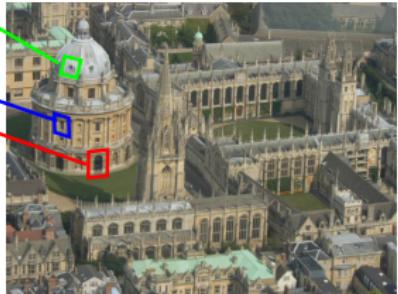
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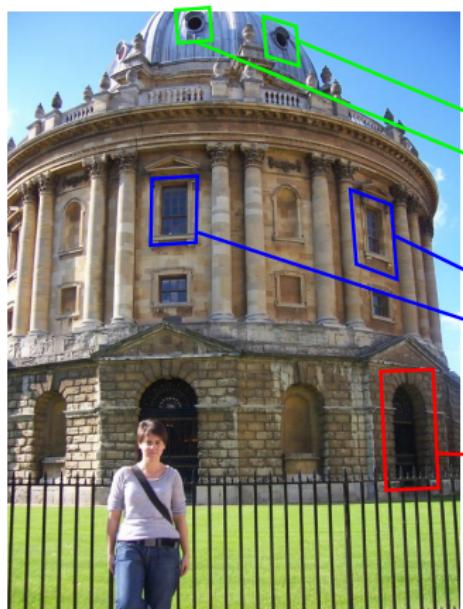
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15



Vector quantization → visual words

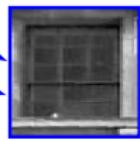


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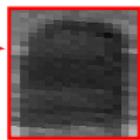
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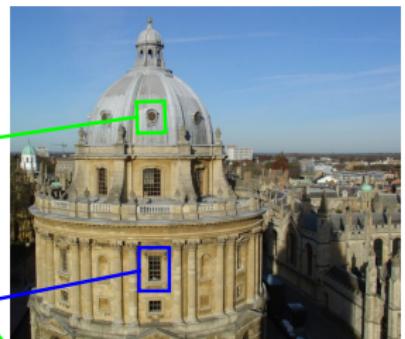
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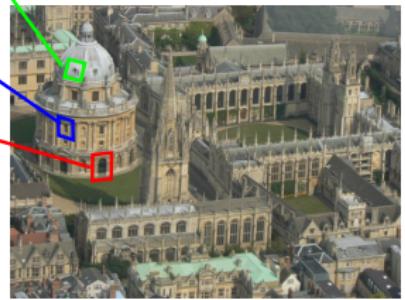
72



19



15



Inverted file indexing

54	
67	
72	

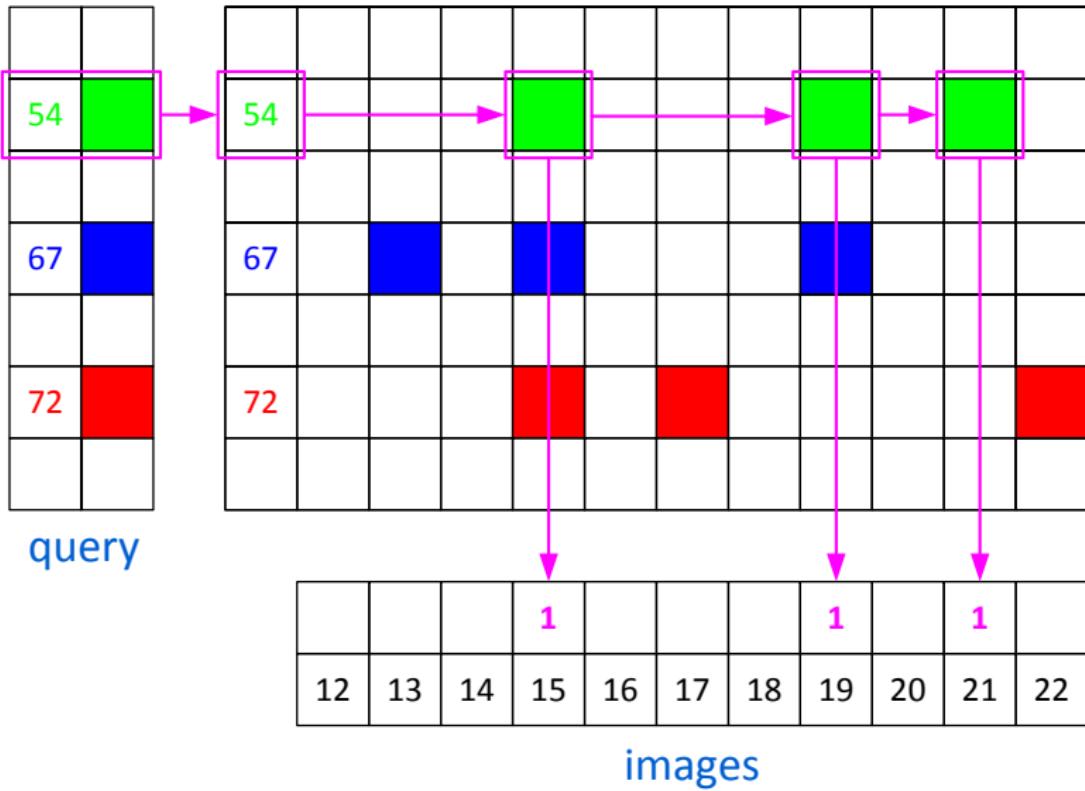
query

54																									
67																									
72																									

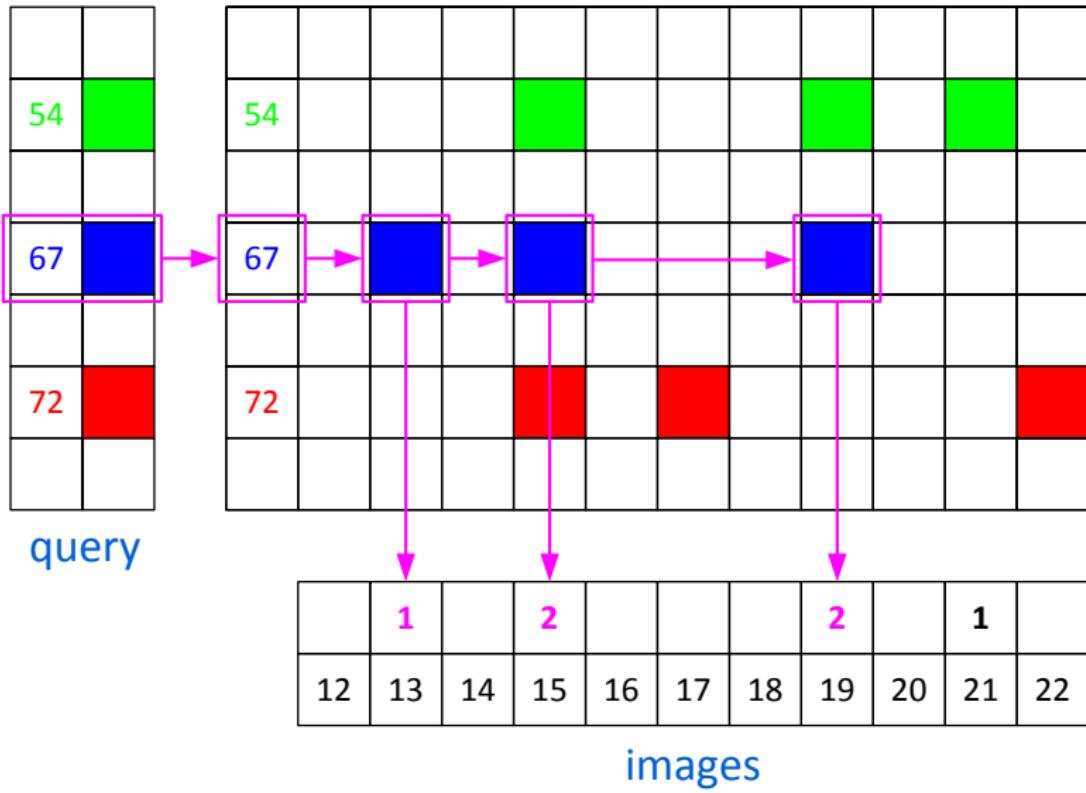
12	13	14	15	16	17	18	19	20	21	22															

images

Inverted file indexing



Inverted file indexing



Inverted file indexing

54	
67	
72	

query

54																							
67																							
72																							

	1		3			1		2		1	1
12	13	14	15	16	17	18	19	20	21	22	

images

Inverted file indexing

54	
67	
72	

query

ranked shortlist

	1		3		1		2		1	1
12	13	14	15	16	17	18	19	20	21	22

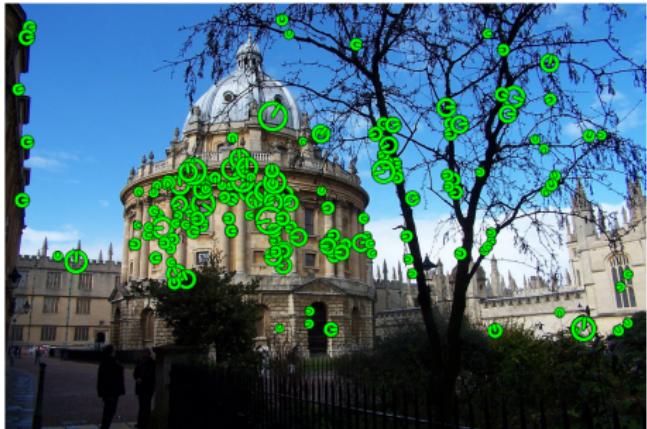
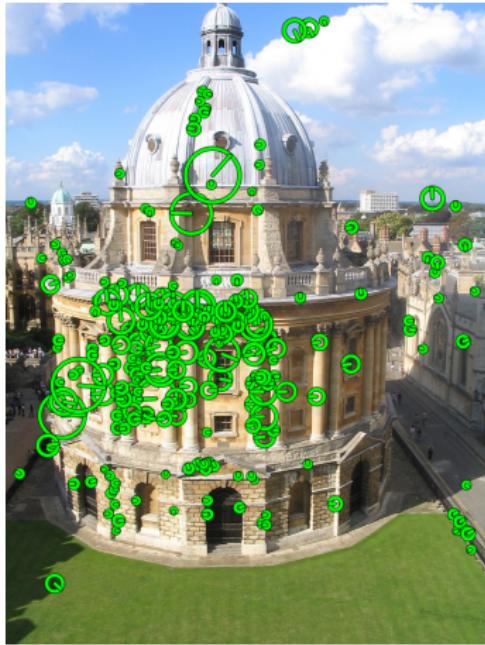
images

Back to geometry: re-ranking



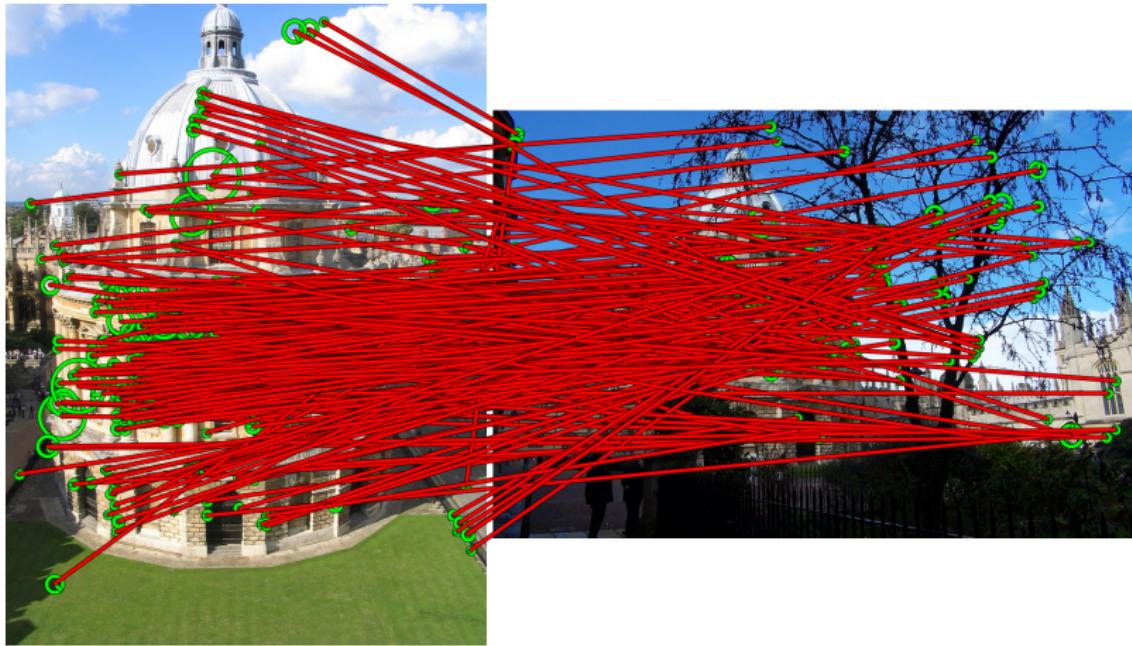
original images

Back to geometry: re-ranking



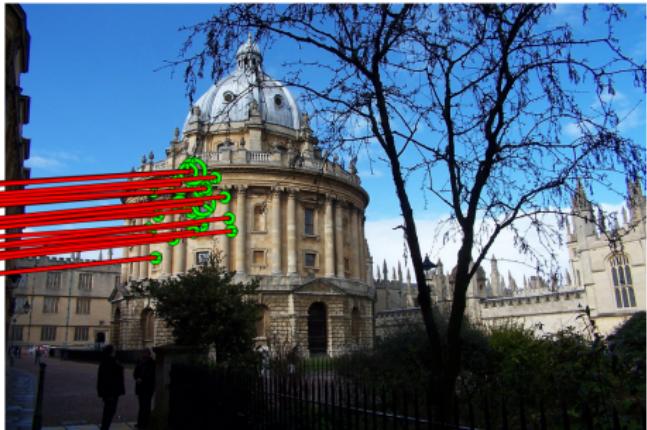
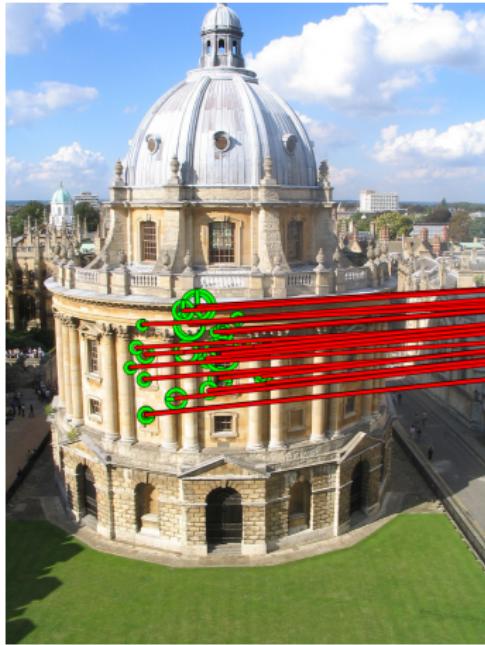
local features

Back to geometry: re-ranking



tentative correspondences

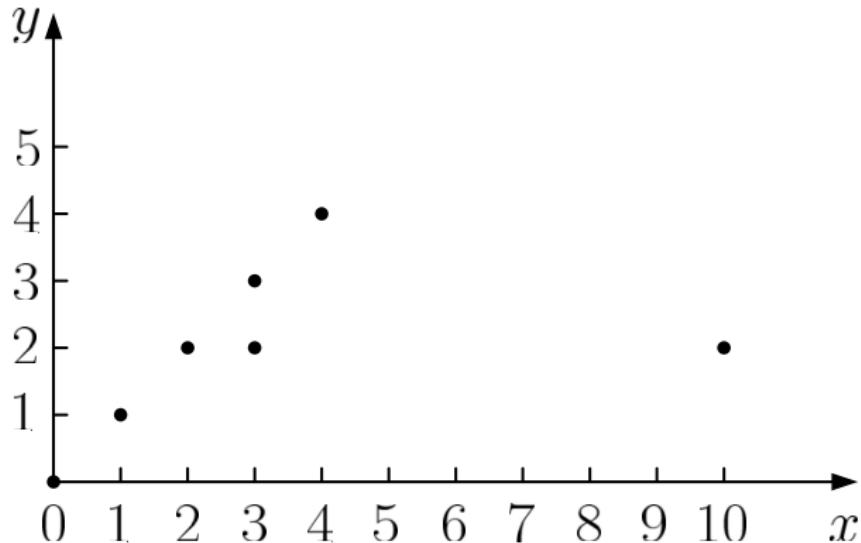
Back to geometry: re-ranking



RANSAC inliers

RANSAC

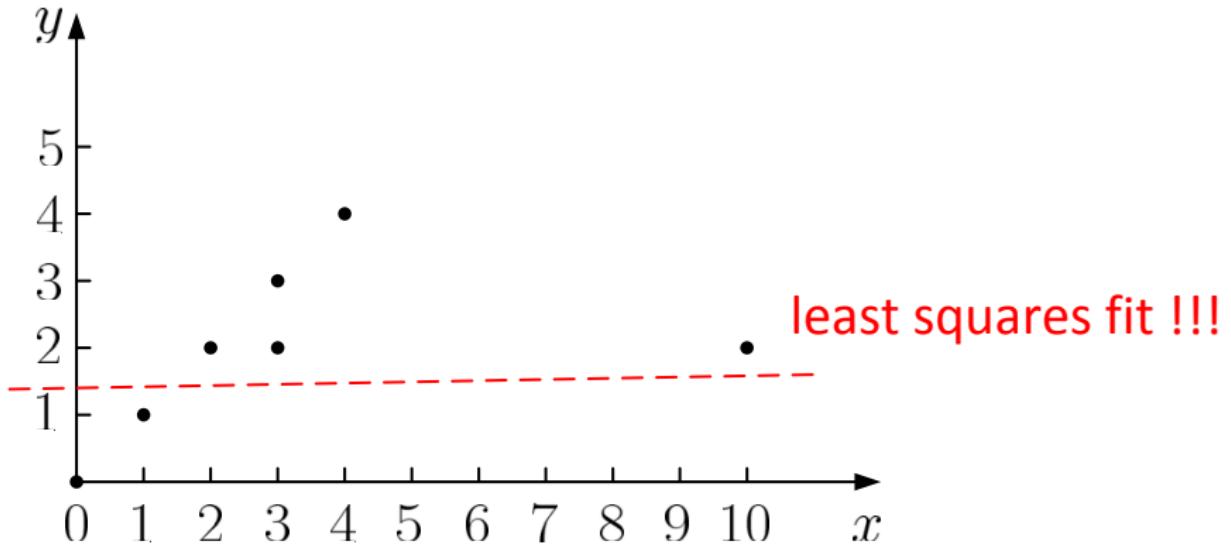
[Fischler and Bolles 1981]



problem: fit line to data

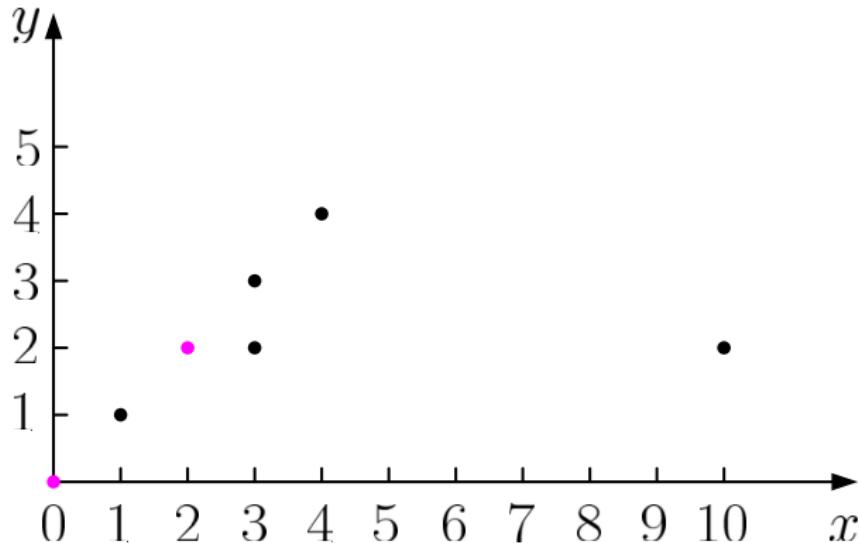
RANSAC

[Fischler and Bolles 1981]



RANSAC

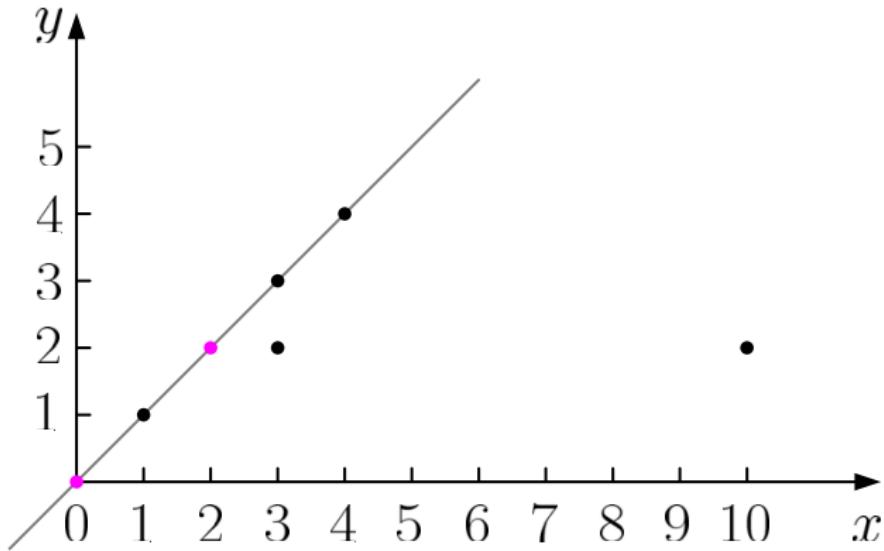
[Fischler and Bolles 1981]



solution: choose 2 random points ...

RANSAC

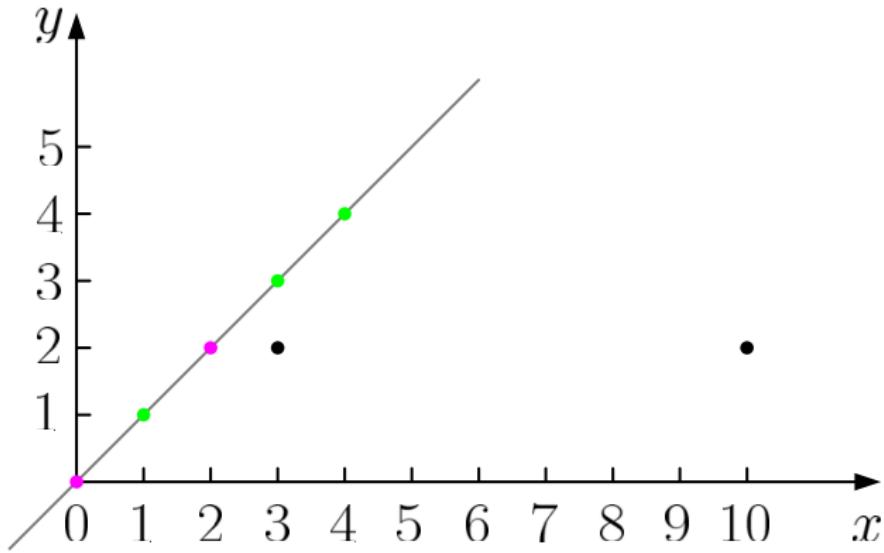
[Fischler and Bolles 1981]



... fit line to them ...

RANSAC

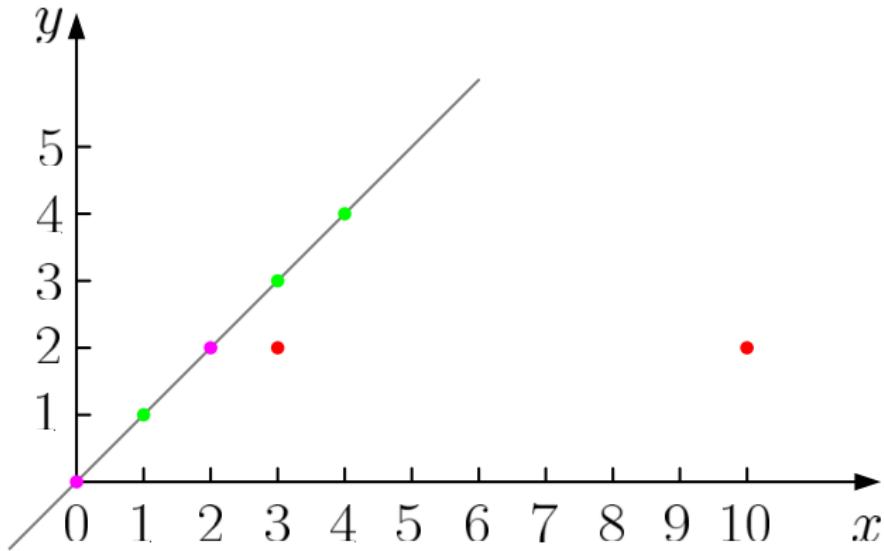
[Fischler and Bolles 1981]



... classify remaining points to inliers ...

RANSAC

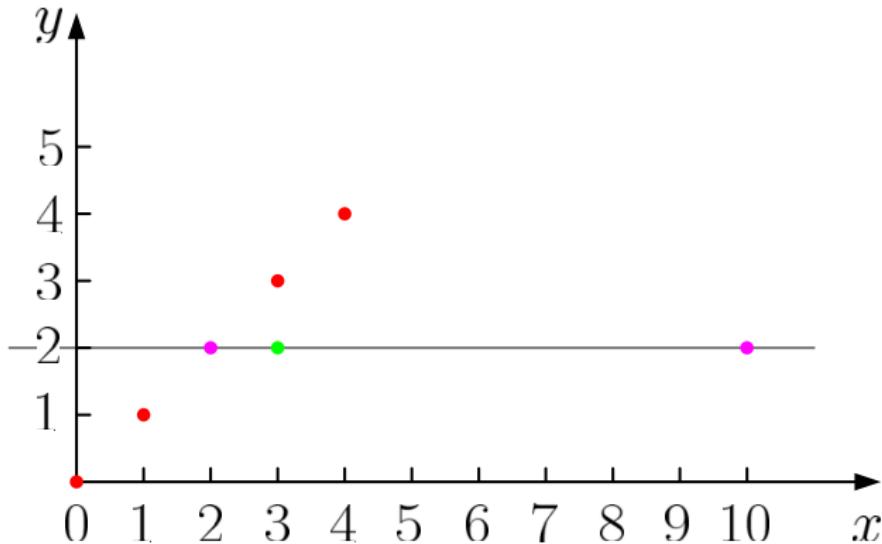
[Fischler and Bolles 1981]



... and outliers

RANSAC

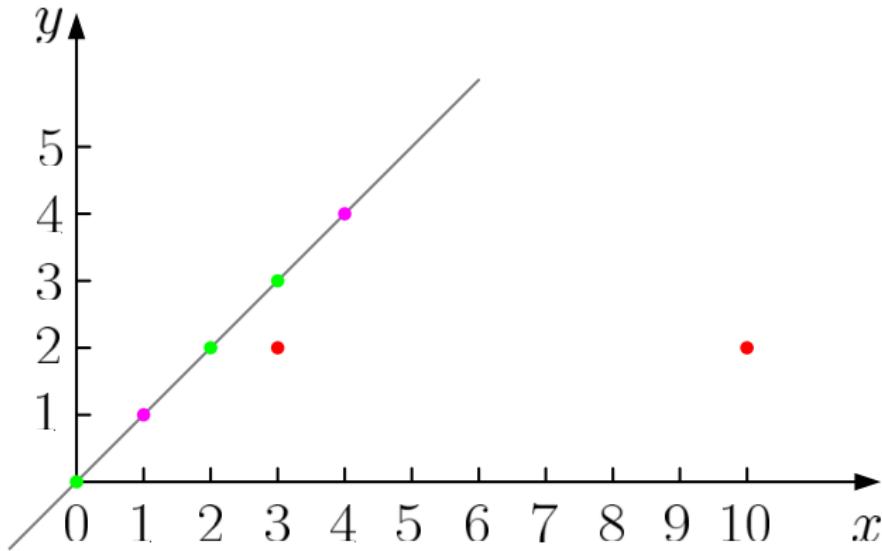
[Fischler and Bolles 1981]



repeat ...

RANSAC

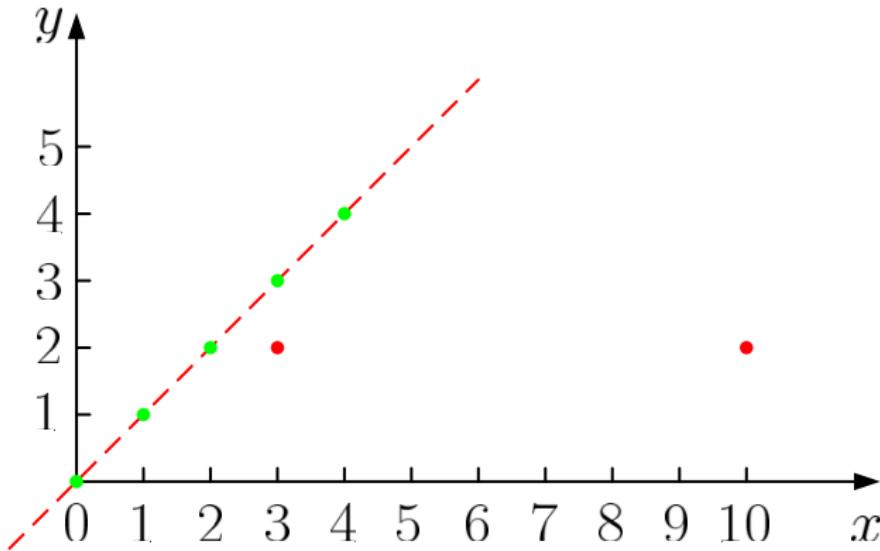
[Fischler and Bolles 1981]



... and repeat

RANSAC

[Fischler and Bolles 1981]



finally: maximum inliers

Outline

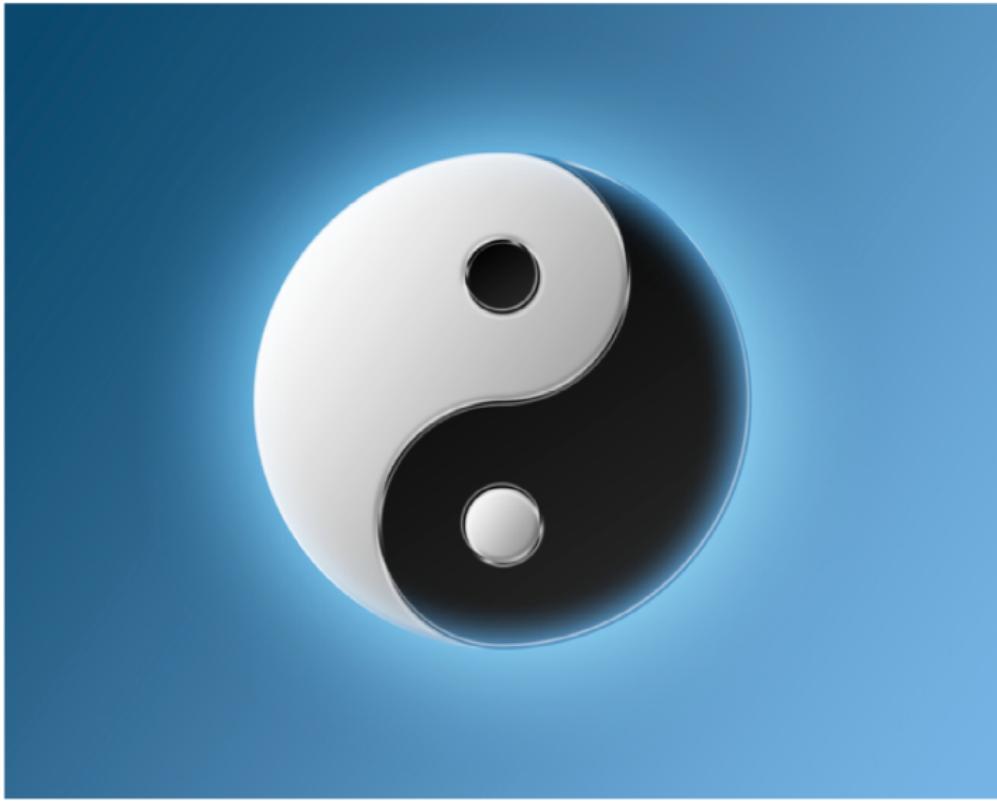
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Edge-based feature detection

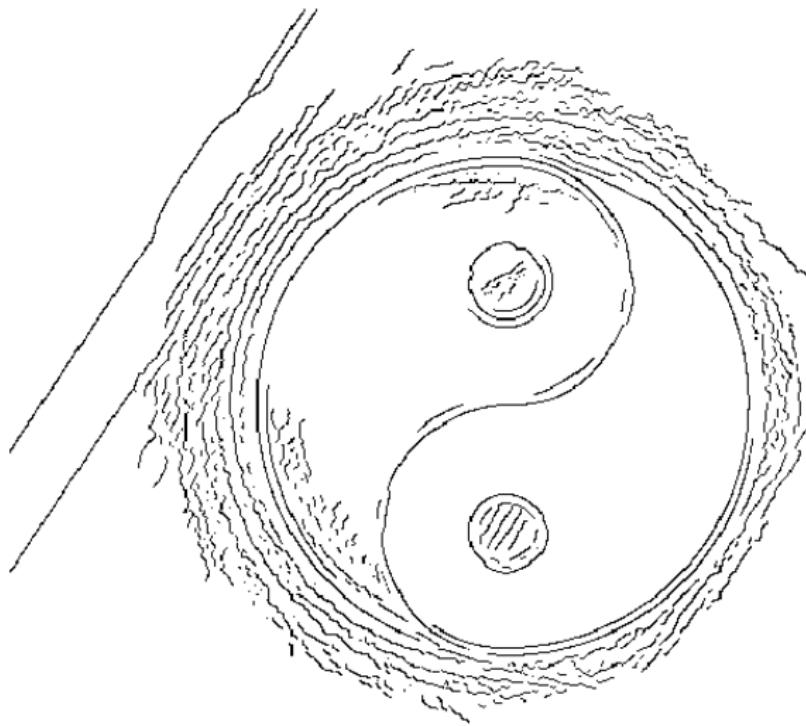
[Rapantzikos and Avrithis 2010]

- Blob-like regions starting from single-scale edges
- local maxima of Euclidean distance transform expected to lie in region interior or close to ridges
- greedily merge maxima guided by edge strength, to reproduce the effect of smoothing in scale-space evolution
- regions of arbitrary shape and scale, unaffected by spurious or disconnected edges

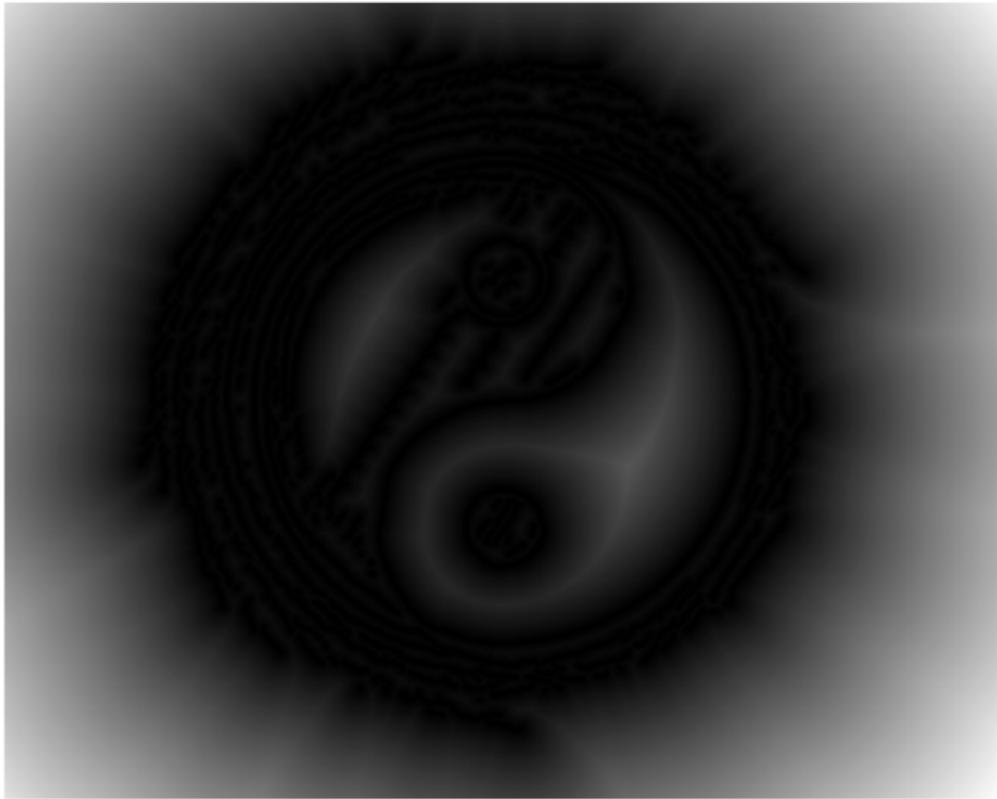
Original image



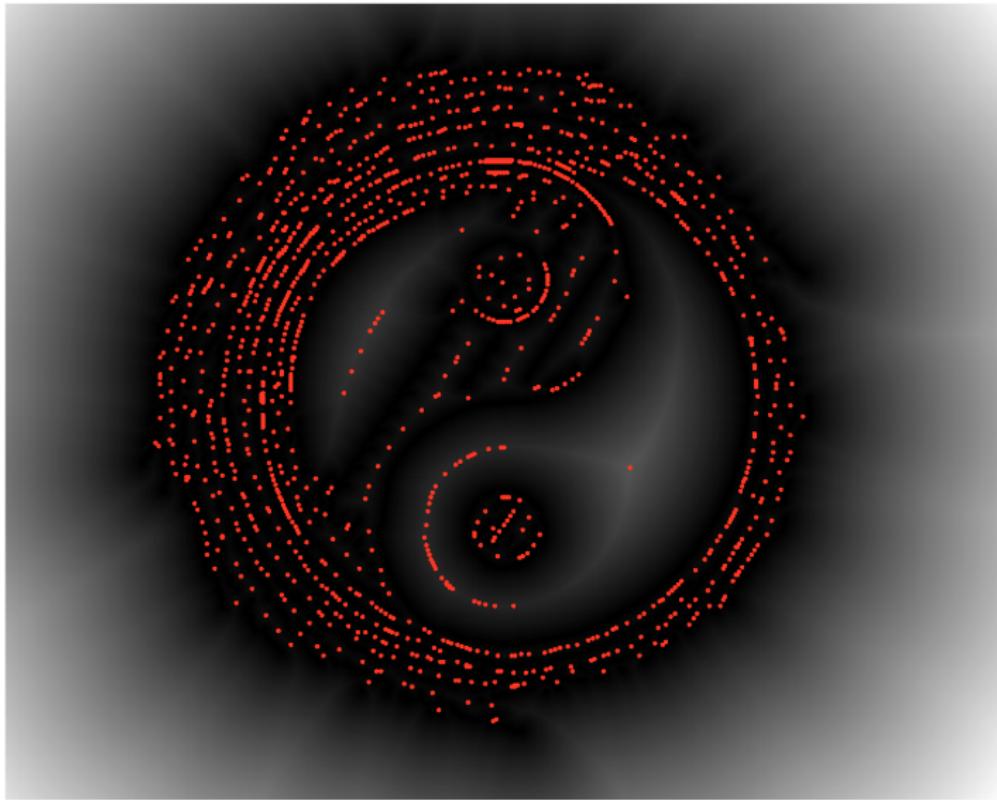
Binary edge map



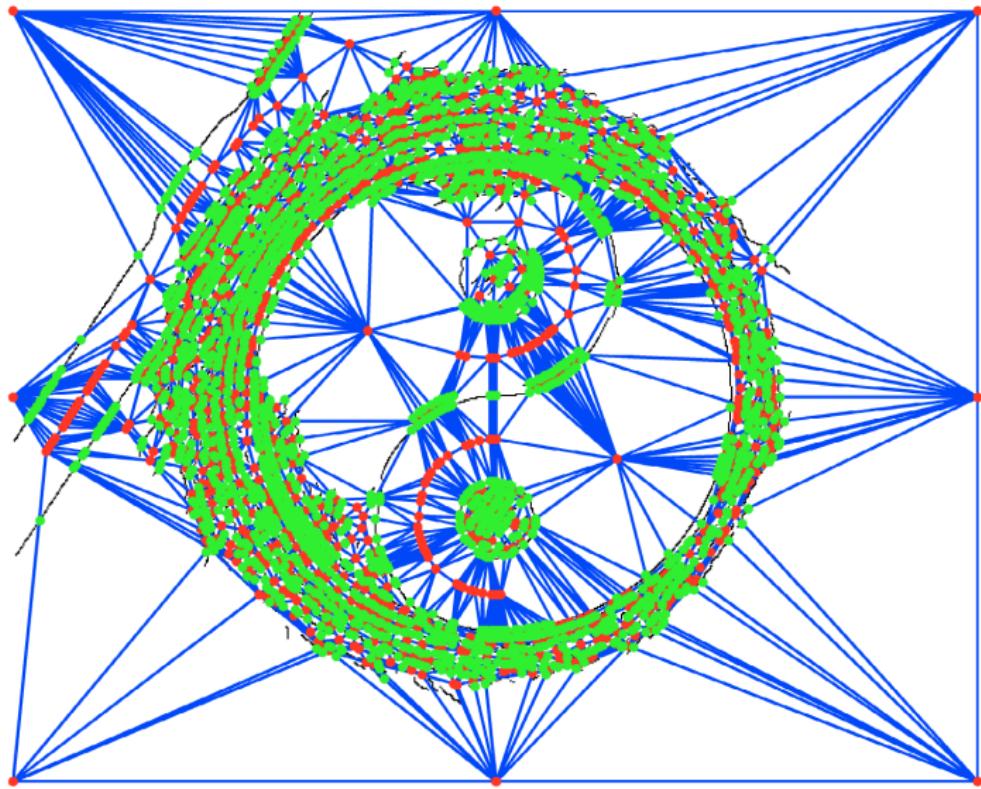
Binary distance map



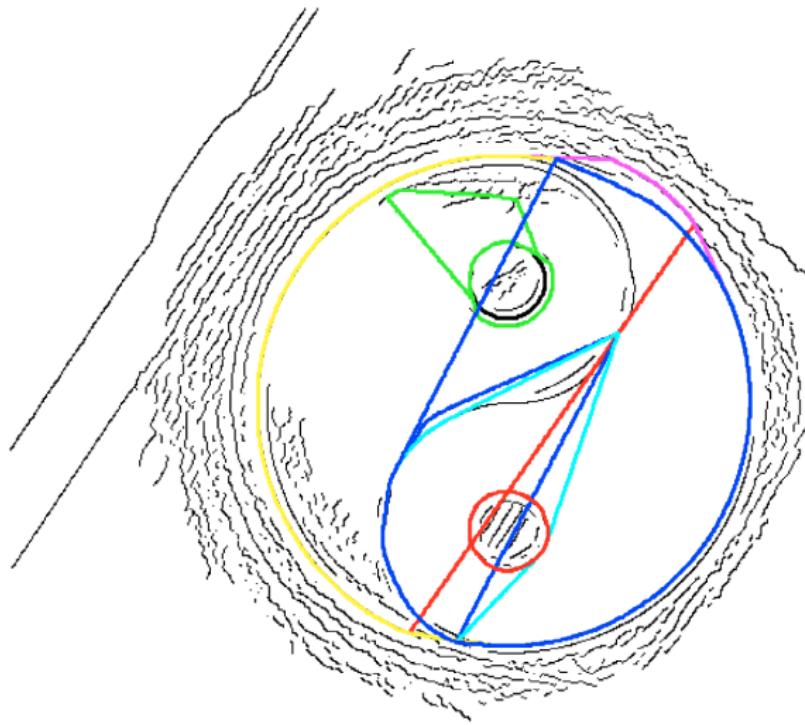
Distance map + local maxima



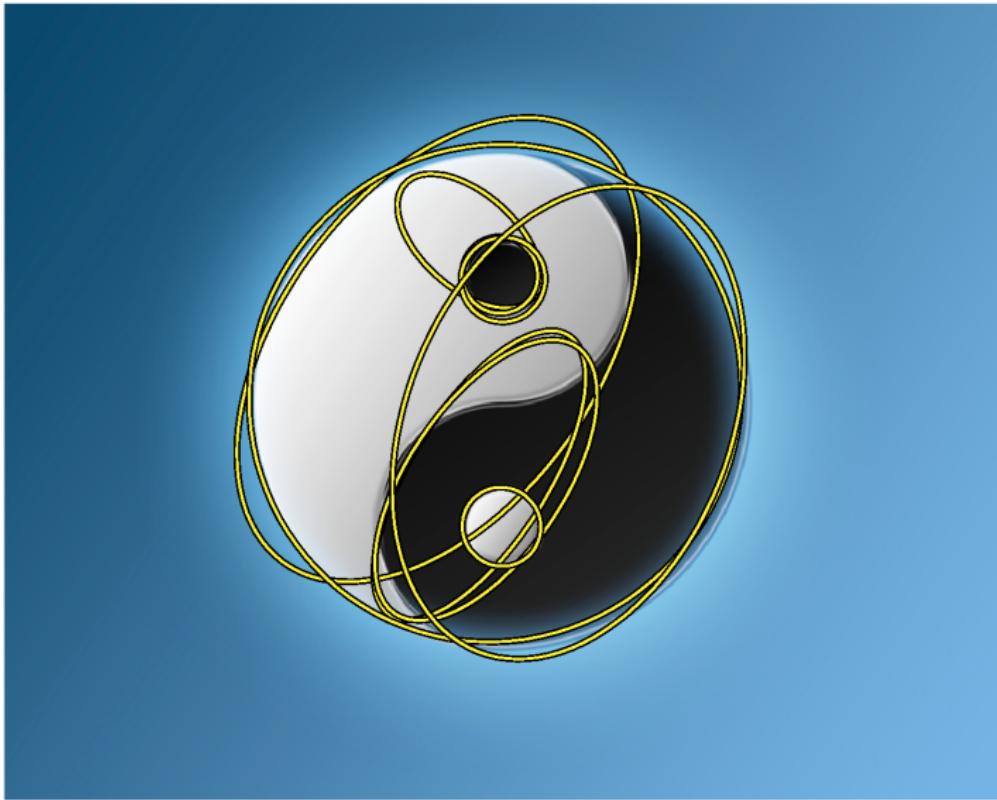
Delaunay triangulation



Convex hulls of selected regions



Original image + features

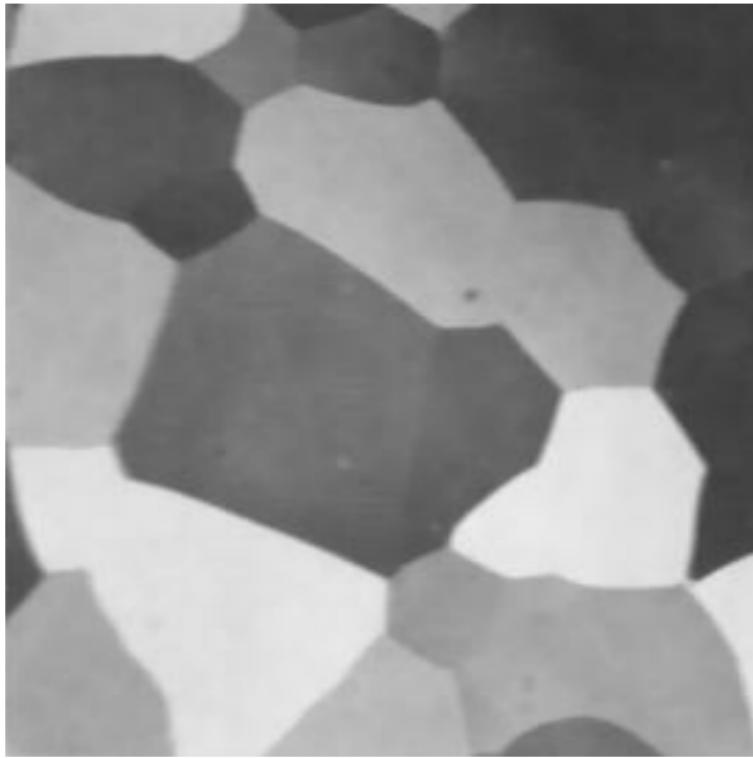


A weighted approach

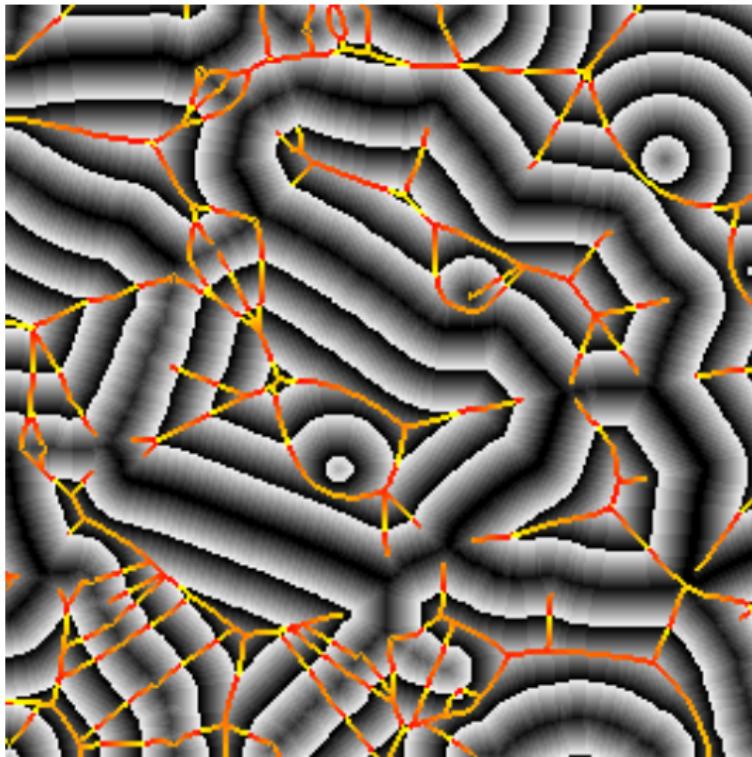
[Avrithis and Rapantzikos 2011, unpublished]

- Weighted distance map directly from image gradient
- Weighted medial capturing region structure and topology
- Very simple selection criterion: is a region well-enclosed by boundaries?
- Again, arbitrary shape and scale, without explicit scale-space construction
- Affordable speed—1s for an 1Mpixel image, on average

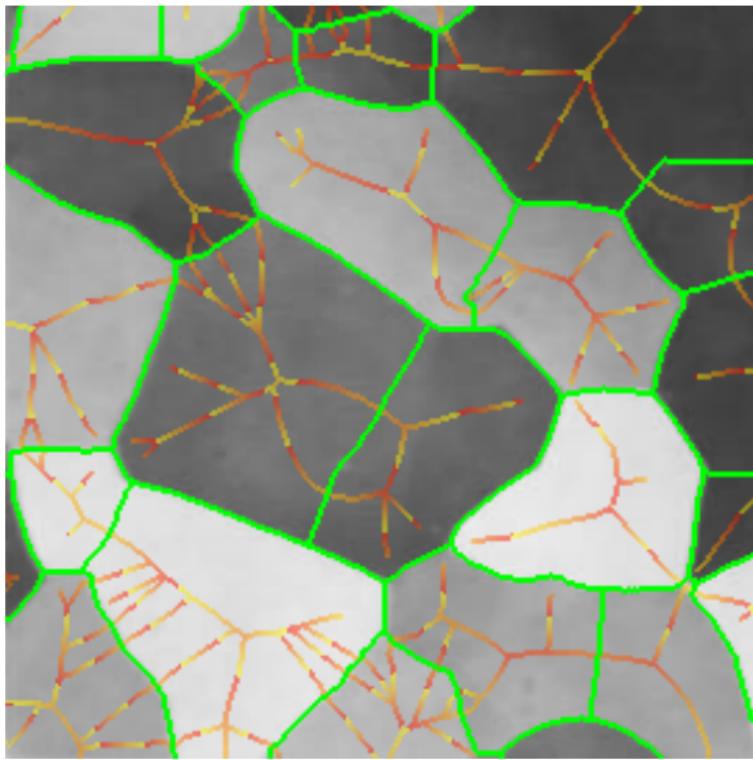
Original image



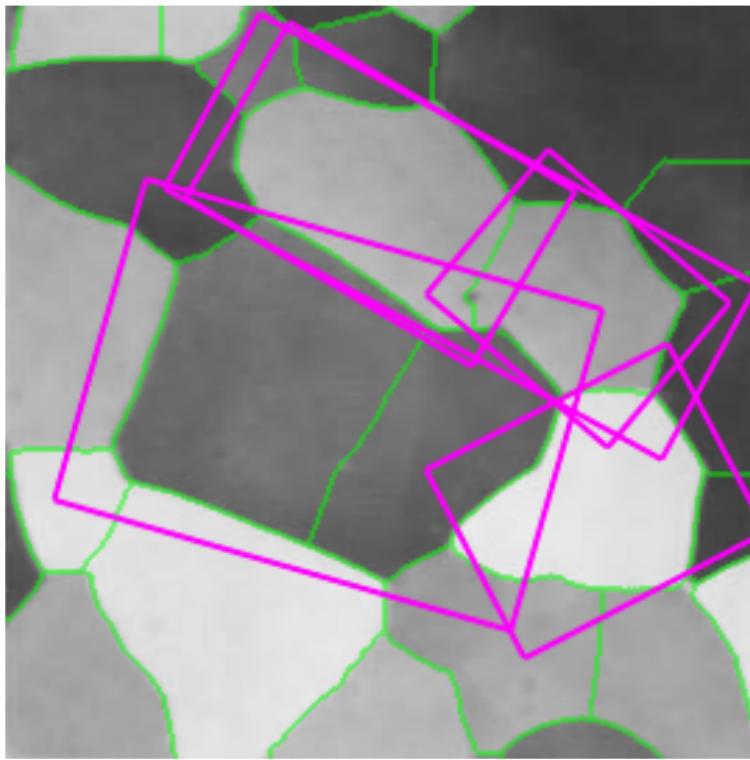
Weighted distance map and medial



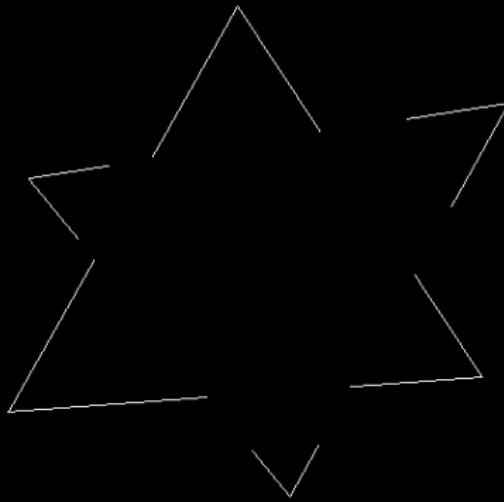
Region/boundary duality



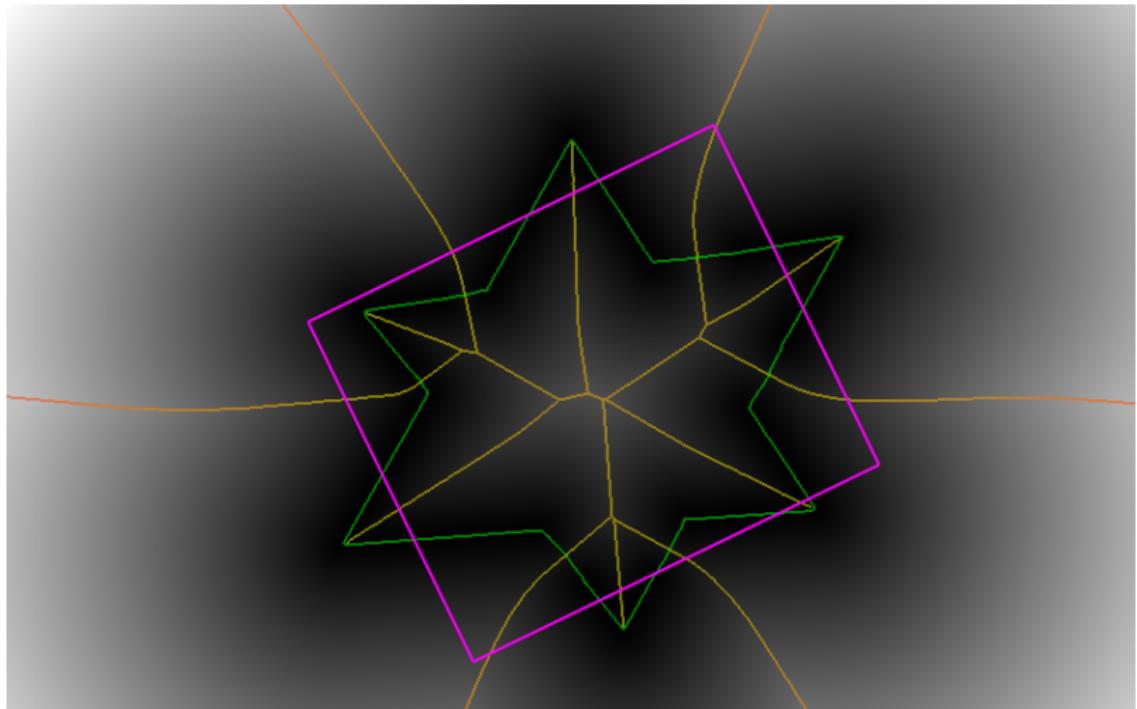
Original image + features



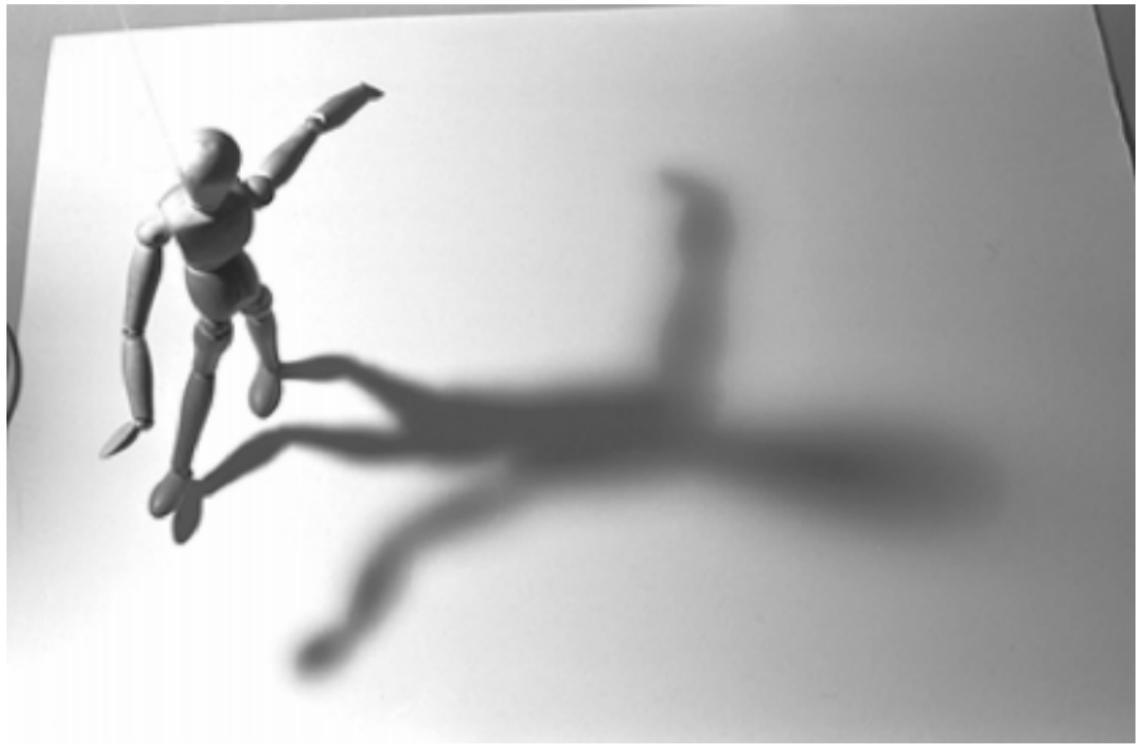
The challenge of shape



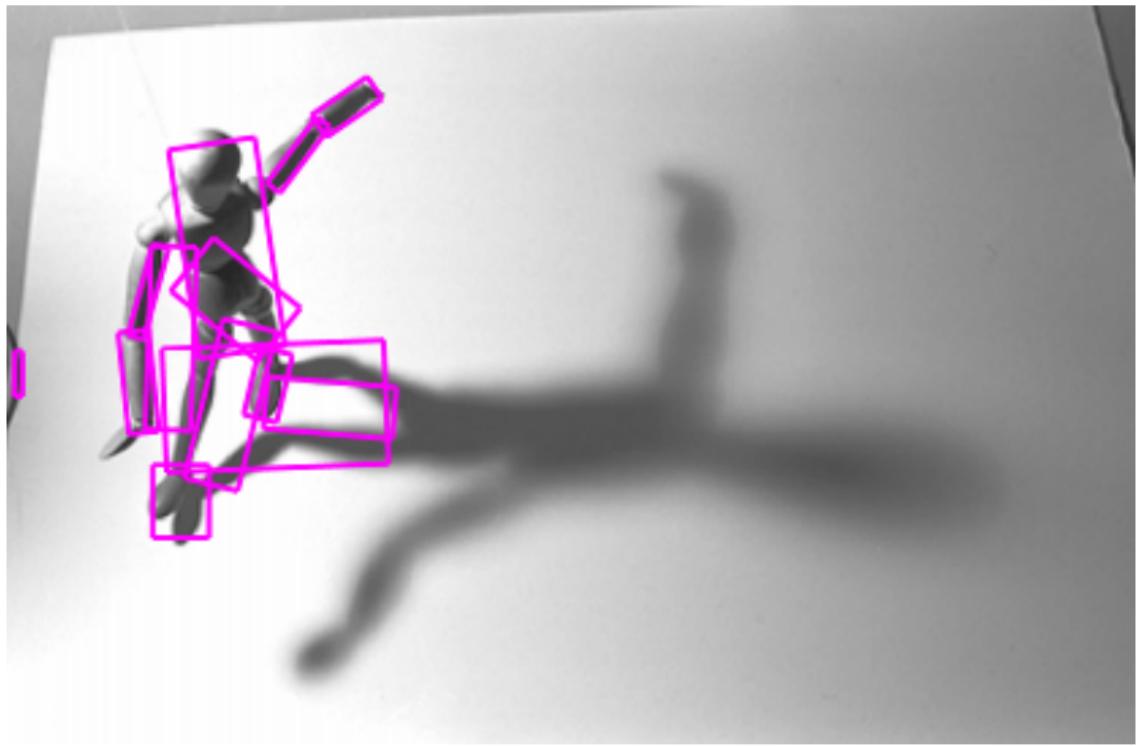
The challenge of shape



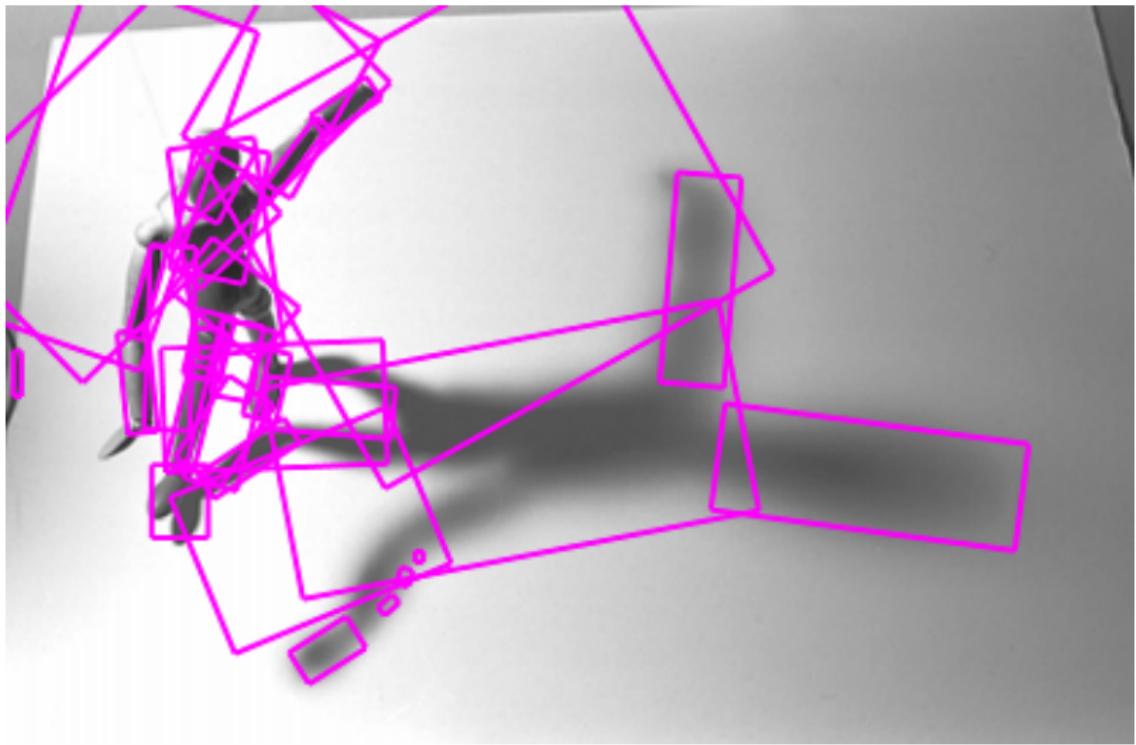
The challenge of scale



The challenge of scale



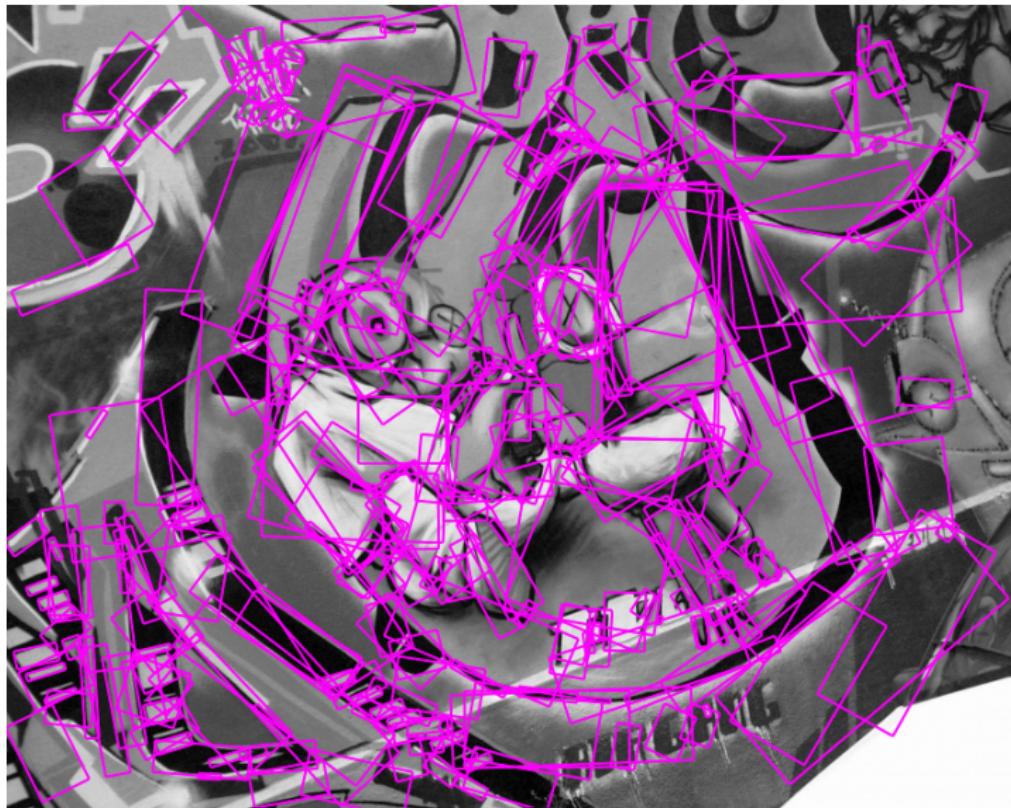
The challenge of scale



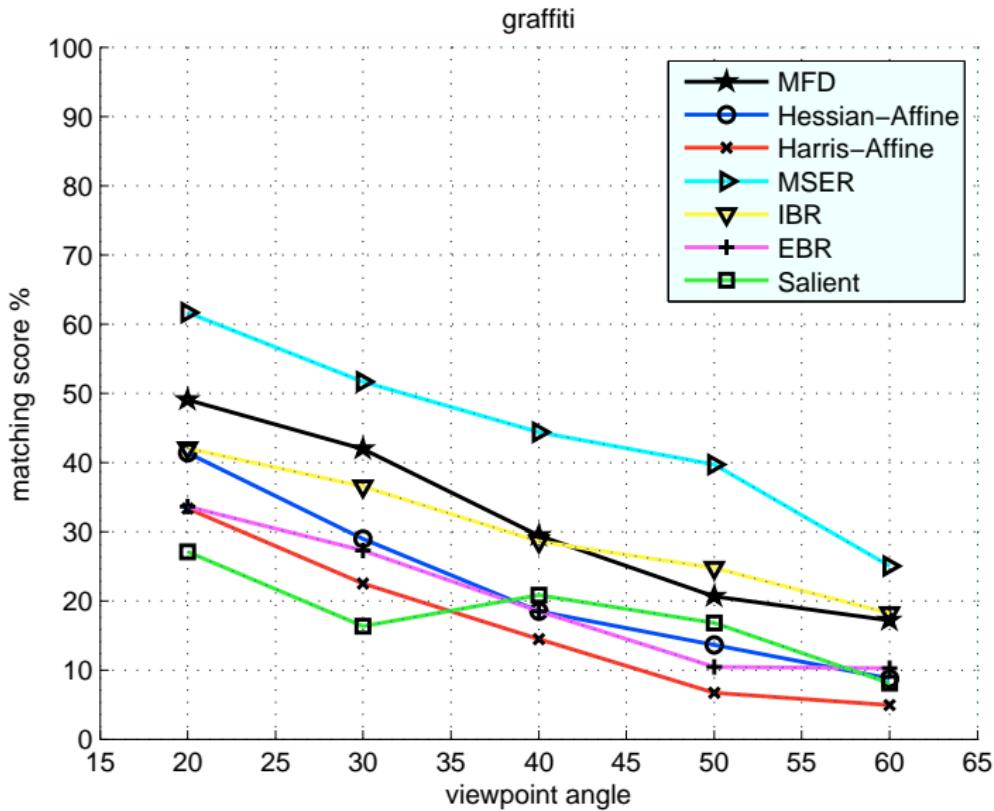
Viewpoint: graffiti scene



Viewpoint: graffiti scene



Viewpoint: graffiti scene



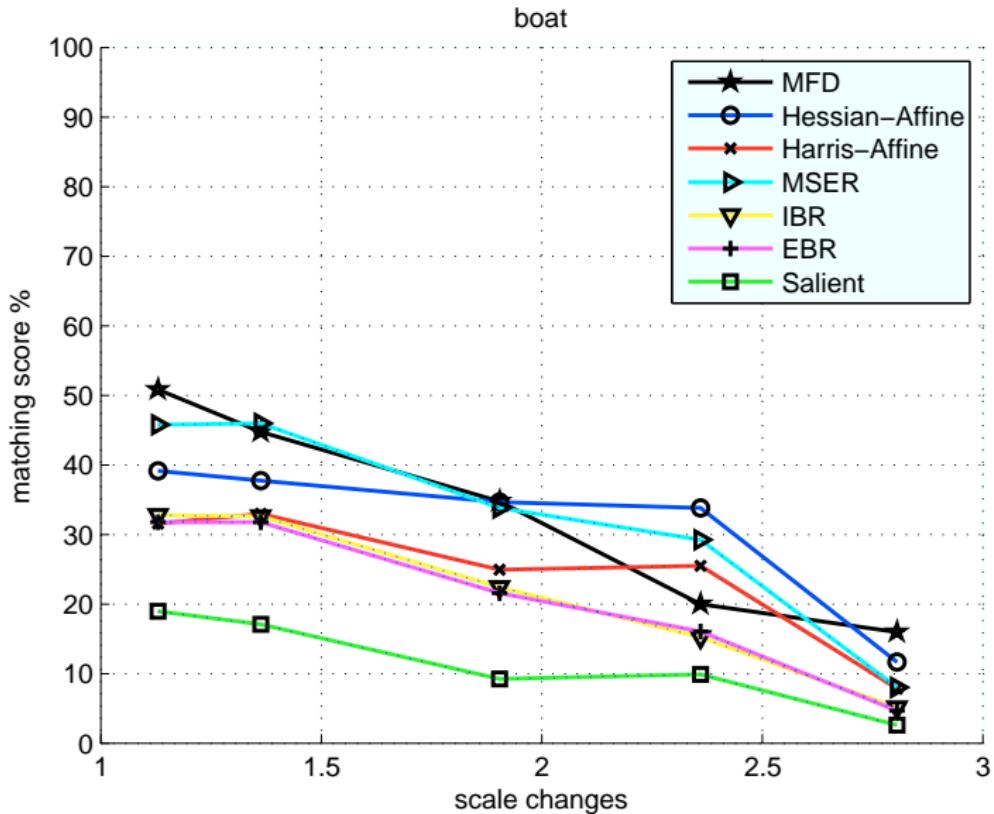
Scale + rotation: boat scene



Scale + rotation: boat scene



Scale + rotation: boat scene



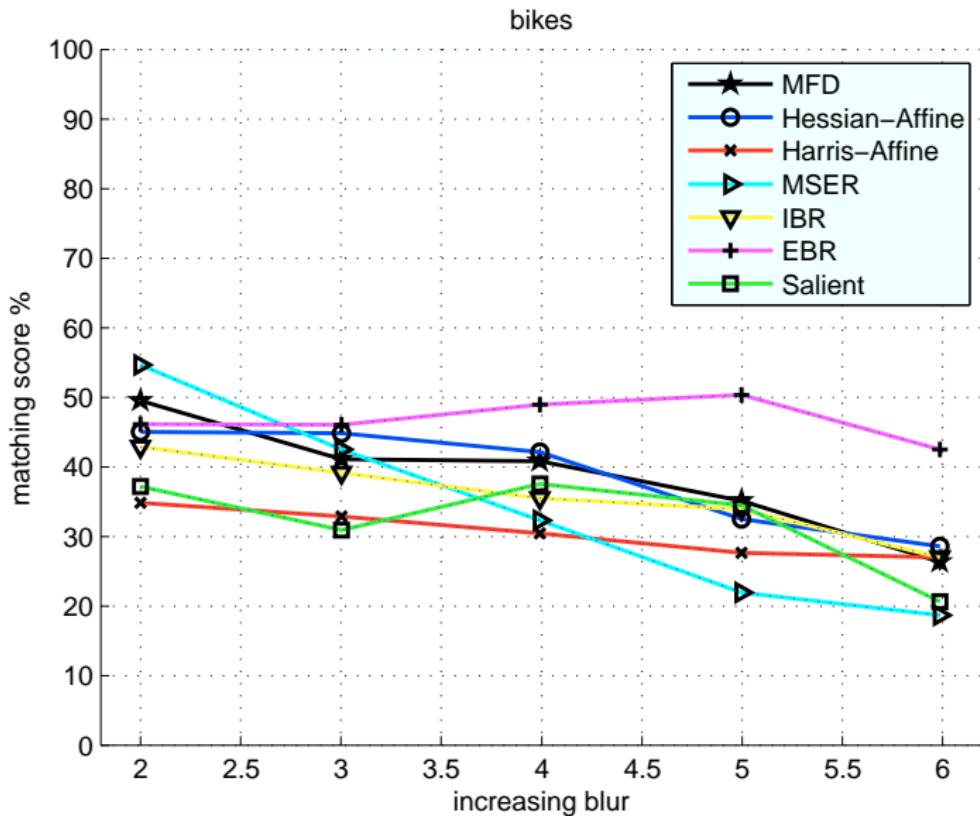
Blur: bikes scene



Blur: bikes scene



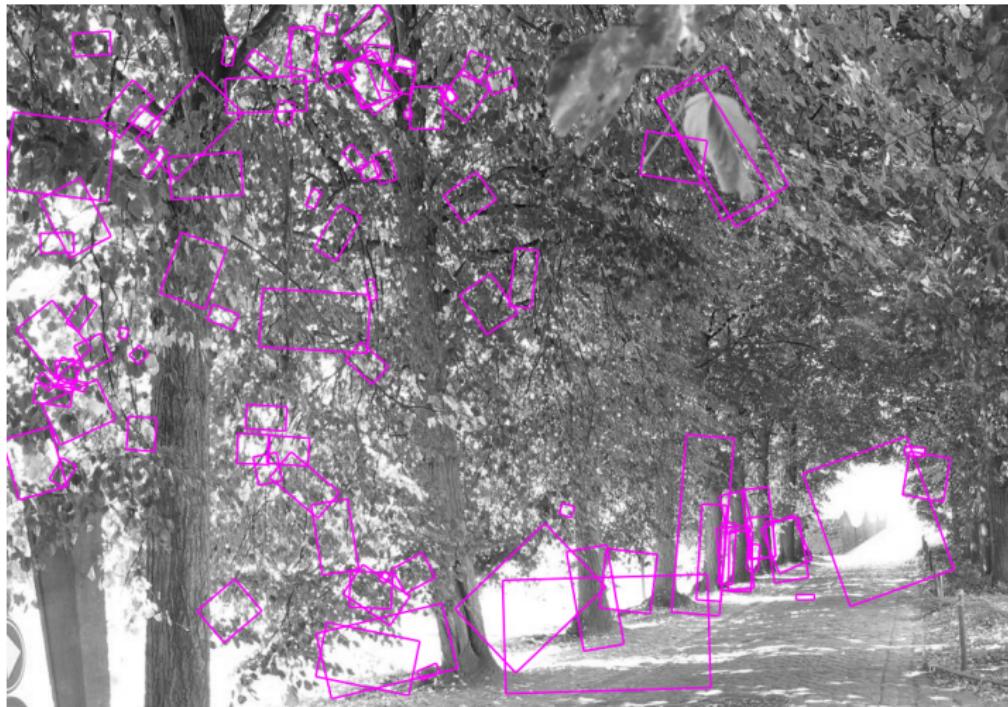
Blur: bikes scene



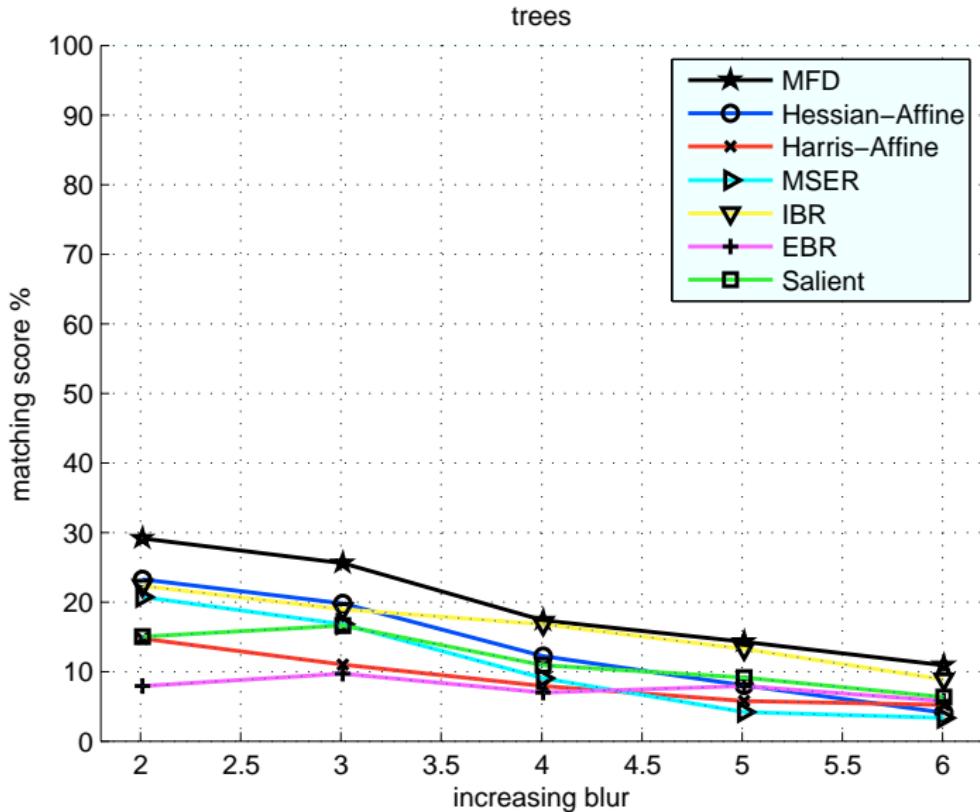
Texture + blur: trees scene



Texture + blur: trees scene



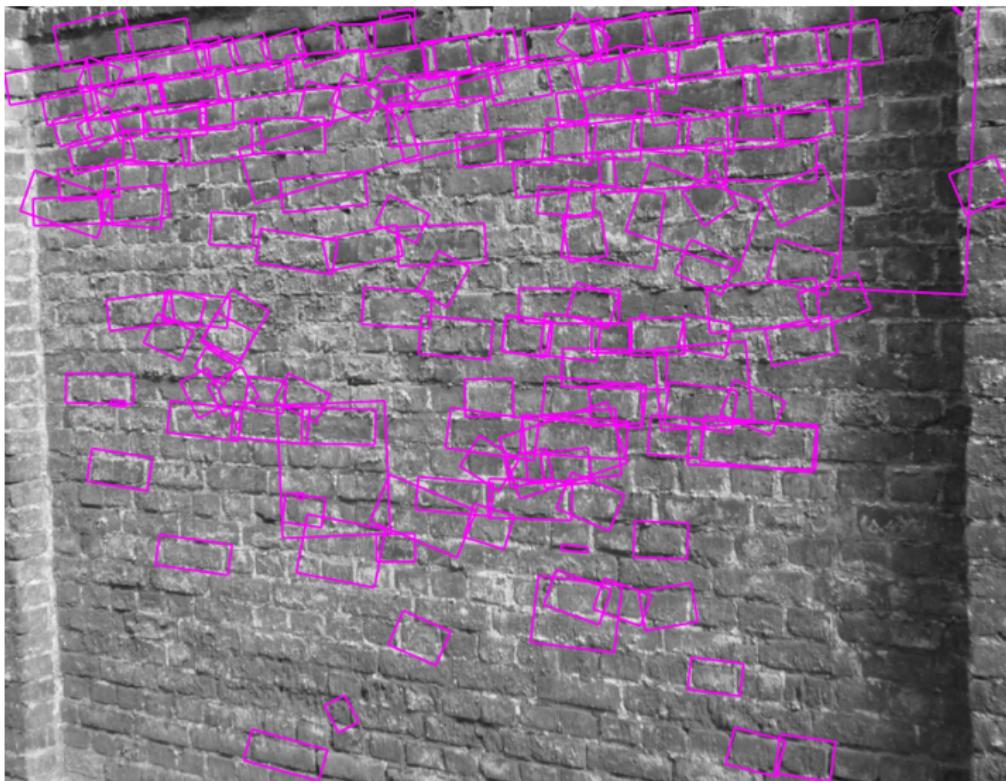
Texture + blur: trees scene



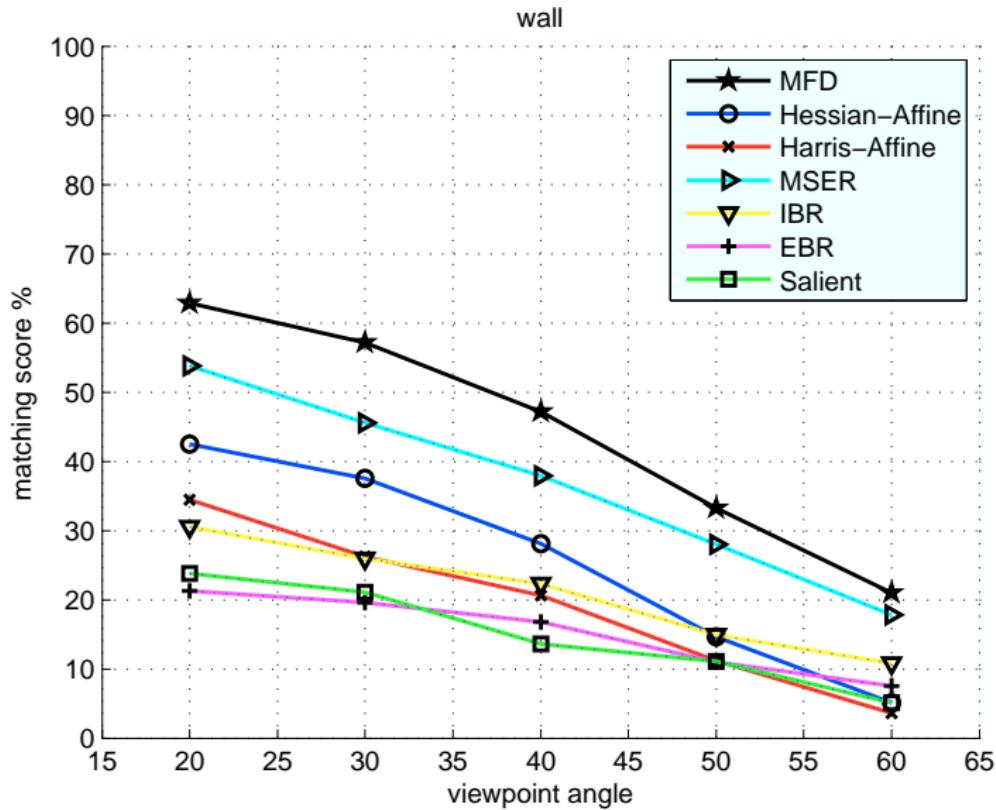
Viewpoint: wall scene



Viewpoint: wall scene



Viewpoint: wall scene

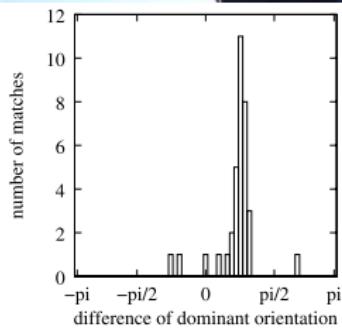
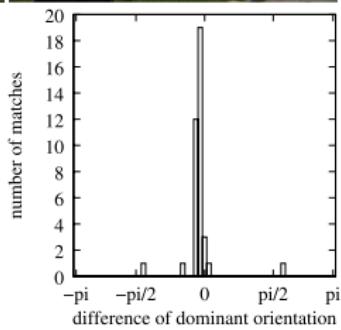
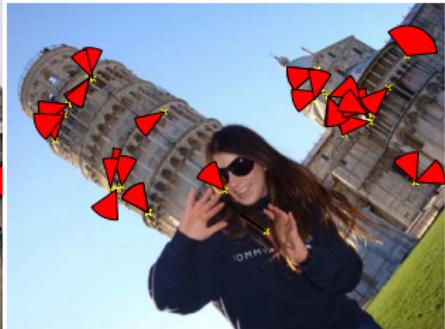
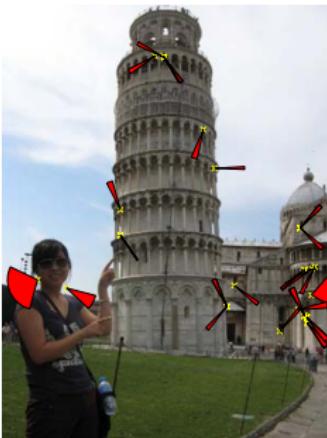
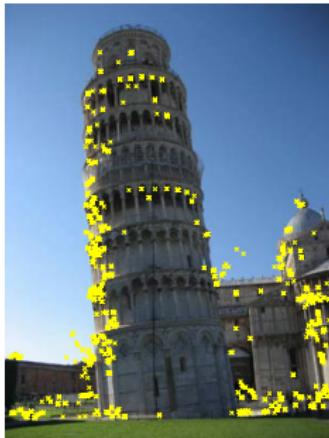


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Weak geometric consistency (WGC)

[Jegou et al. 2008]



Weak geometric consistency

- when an image undergoes rotation or scaling, the orientation and scale of local features is consistently modified
- quantize orientation and scale differences between feature pairs
- maintain several scores for each image, one for each difference bin
- this is not enough to recover a full transformation, but does improve ranking

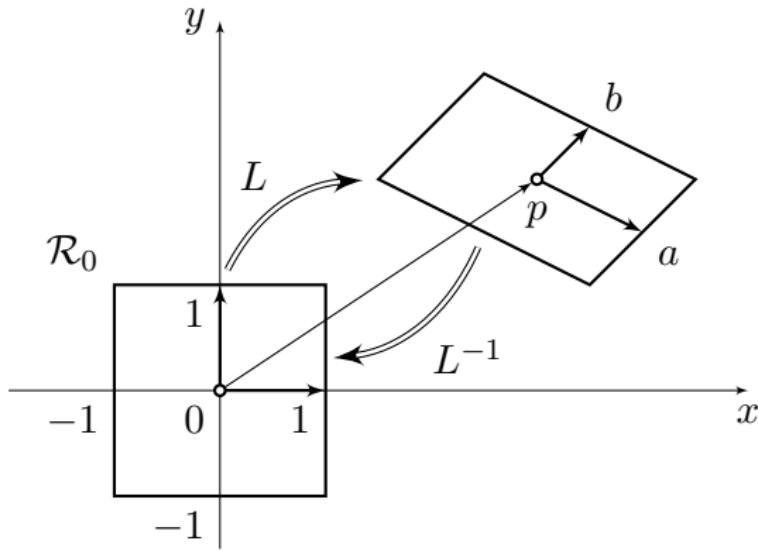
Feature map hashing

[Avrithis et al. 2010]

- estimate image alignment via **single correspondence**
- for each feature construct a **feature map** encoding normalized positions and appearance of all remaining features
- represent an image by a collection of such feature maps
- RANSAC-like matching is reduced to a number of **set intersections**

Local patches

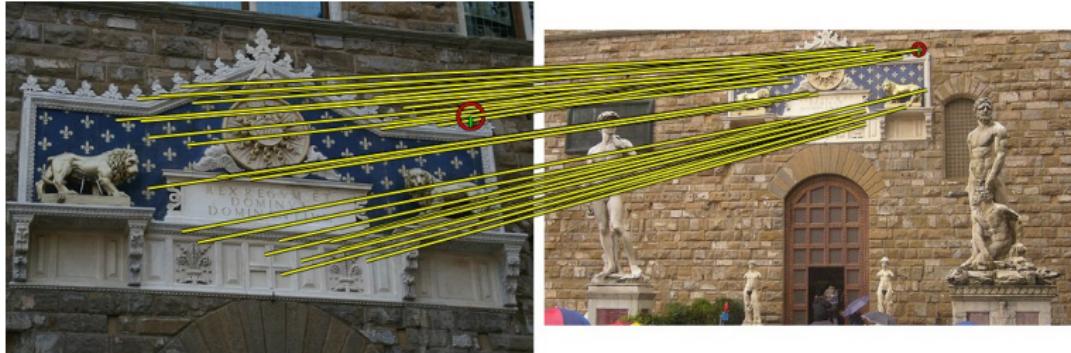
- each local feature is associated with an image patch L , which also represents an affine transform
- the **rectified** patch \mathcal{R}_0 is transformed to the patch via L
- the patch is rectified back to \mathcal{R}_0 via L^{-1}



Fast spatial matching (FSM)

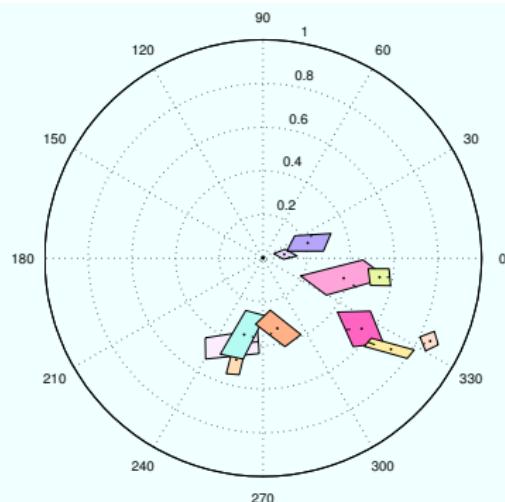
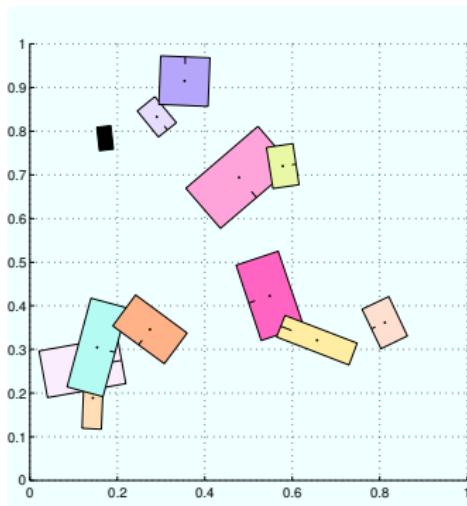
[Philbin et al. 2007]

- single patch correspondence $L \leftrightarrow R$
- the transformation from one patch to the other is RL^{-1}
- each correspondence provides a transformation hypothesis
- transformation hypotheses are now $O(n)$; we can compute them all



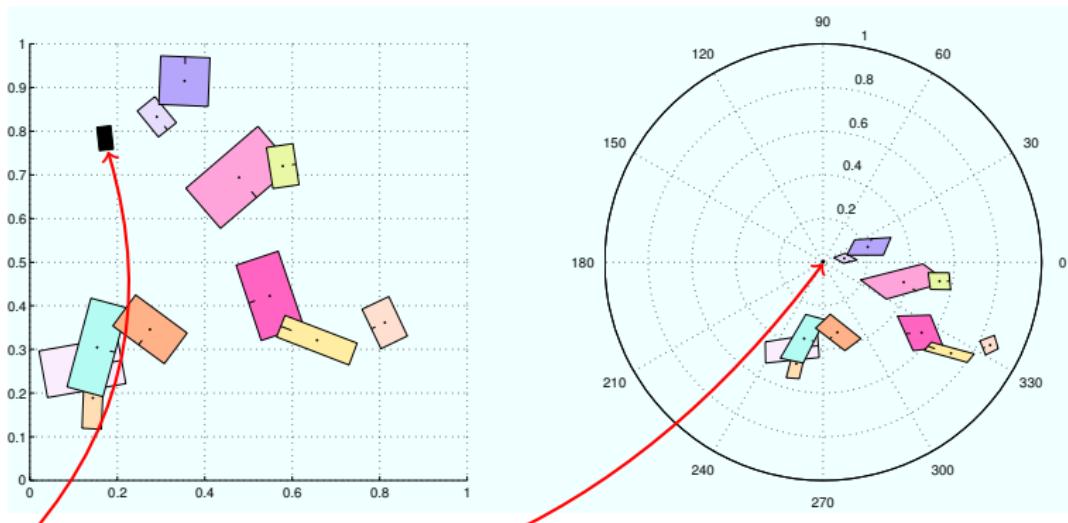
Feature set rectification

- rectify both feature sets by transformations L^{-1} and R^{-1} , then compare
- rectify the entire set of features **in advance**



Feature set rectification

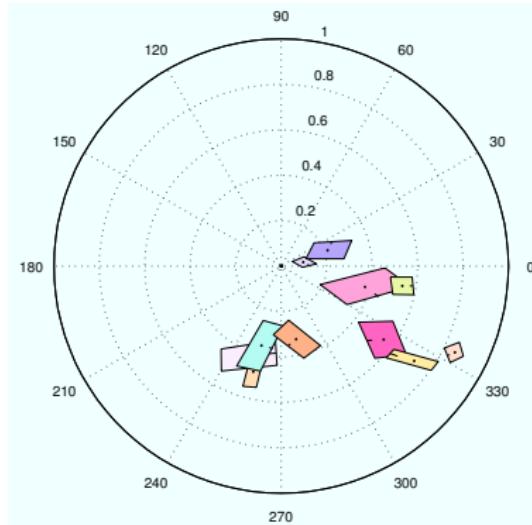
- rectify both feature sets by transformations L^{-1} and R^{-1} , then compare
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origin

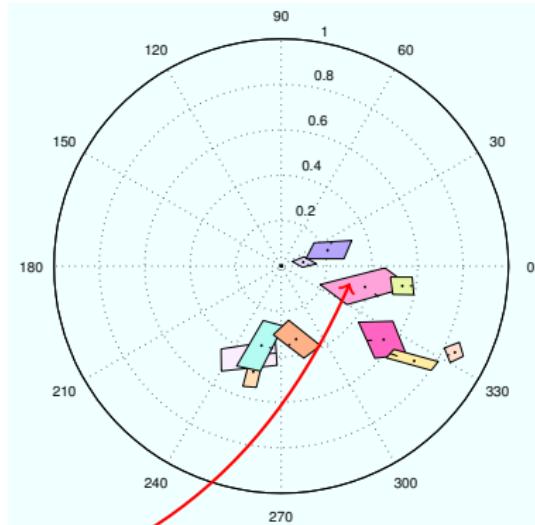
Spatial quantization

- encode positions in polar coordinates (ρ, θ)
- quantize positions in the rectified frames
- define **spatial codebook** $\mathcal{U} \subseteq \mathbb{R}^2$ with $|\mathcal{U}| = k_\rho \times k_\theta = k_u$ bins



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$$\tilde{\rho} = 1, \tilde{\theta} = 11$$

$$k_\rho = 5, k_\theta = 12$$

Feature maps

- represent an image by a local feature set P
- define the joint (visual-spatial) codebook $\mathcal{W} = \mathcal{V} \times \mathcal{U}$ with $|\mathcal{W}| = k_v k_u = k$ bins
- to construct a feature map we rectify a feature set and assign rectified features to spatial bins and visual words

$$f_P(\hat{x}) = h_{\mathcal{W}}(P^{(\hat{x})})$$

- there is a different map for each origin; represent each image with a feature map collection F_P
- can be seen as a local descriptor encoding the global feature set rectified in a local coordinate frame

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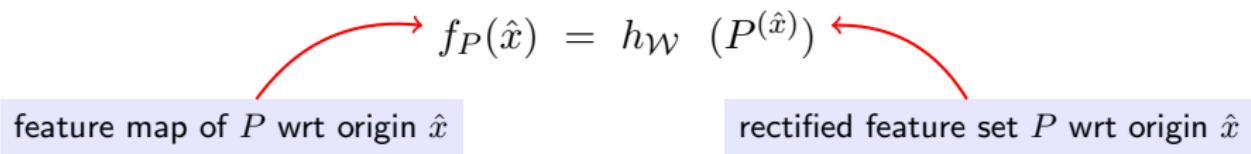
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feature map of P wrt origin \hat{x}

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Feature maps

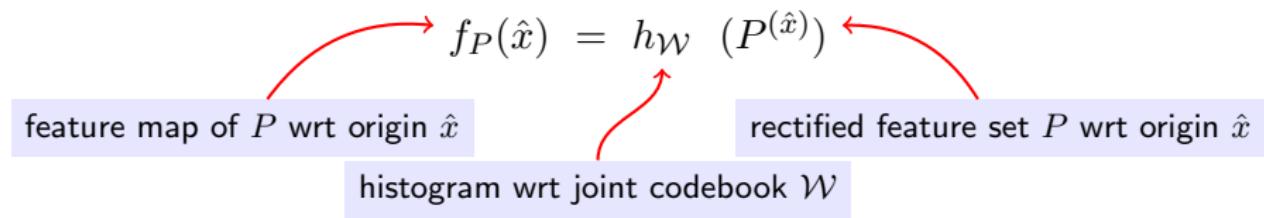
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Feature maps

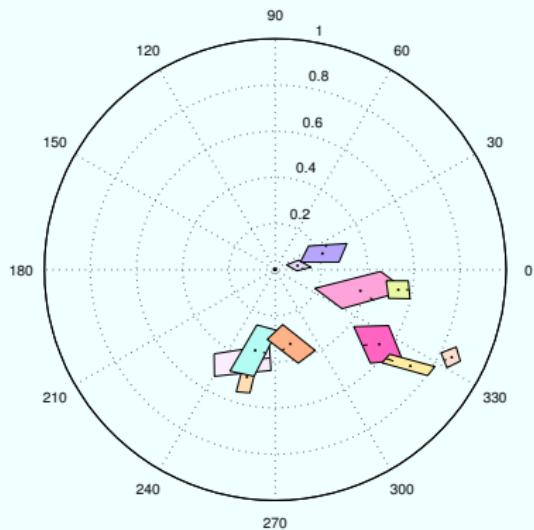
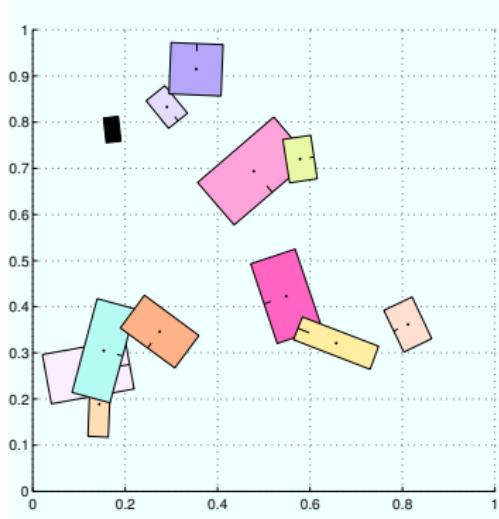
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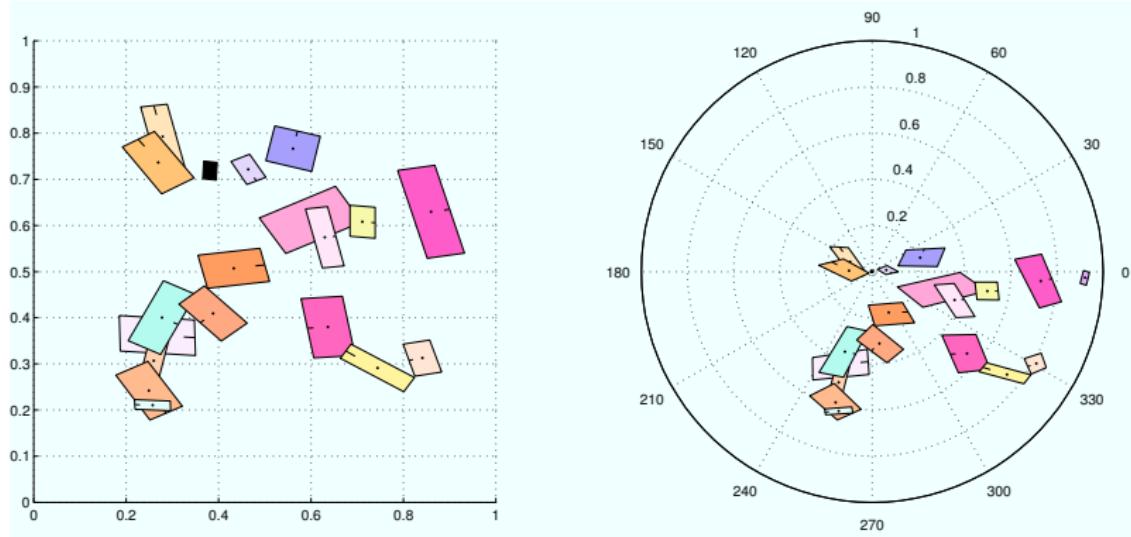
Feature maps—example

- well aligned feature sets are likely to have maps with a high degree of overlap



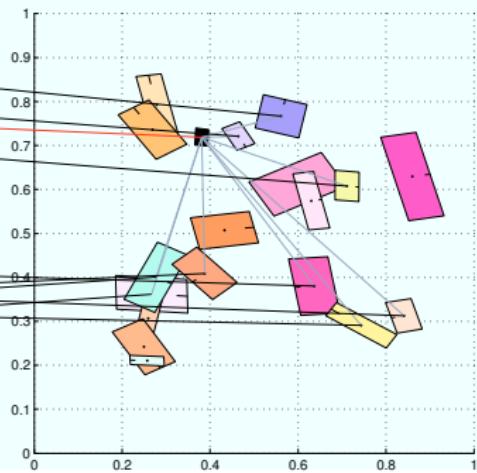
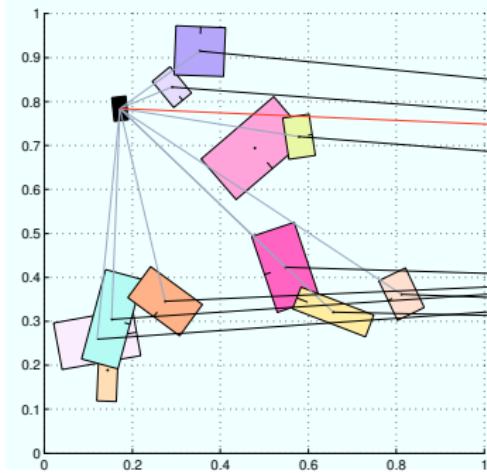
Feature maps—example

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Feature map similarity

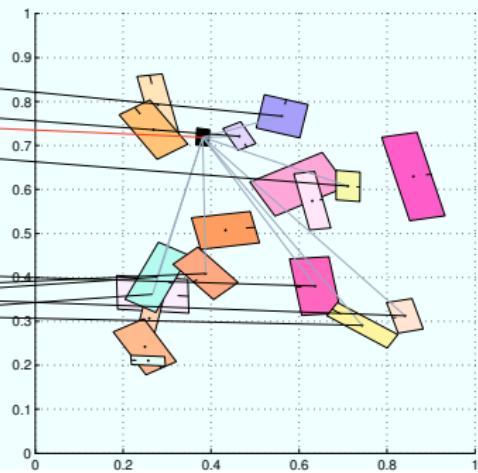
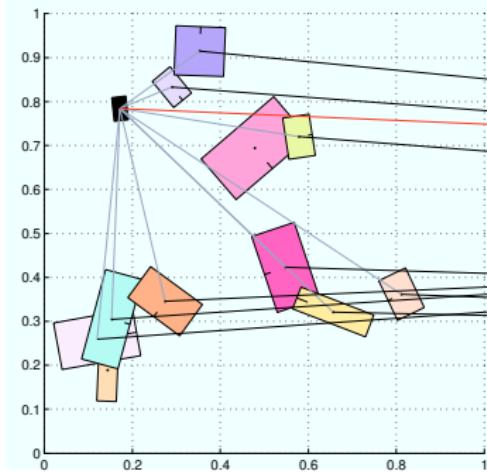
$$S_F(P, Q) = \max_{v \in V(P, Q)} \max_{\substack{\hat{x} \in H_v(P) \\ \hat{y} \in H_v(Q)}} f_P^T(\hat{x}) \cdot f_Q(\hat{y})$$



Feature map similarity

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feature map of image P wrt origin \hat{x}

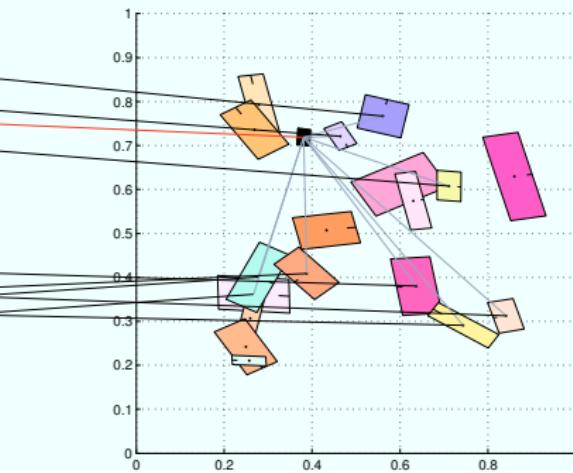
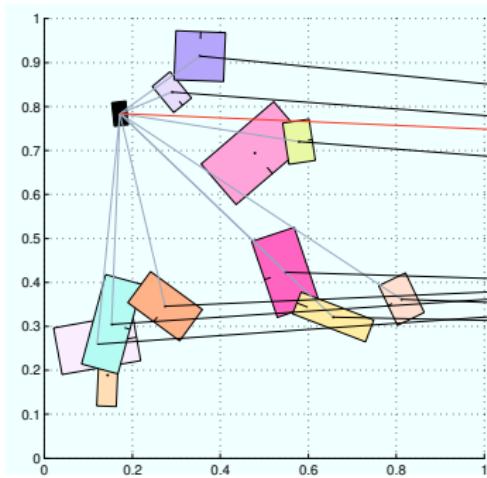


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feature map of image P wrt origin \hat{x}

feature map of image Q wrt origin \hat{y}



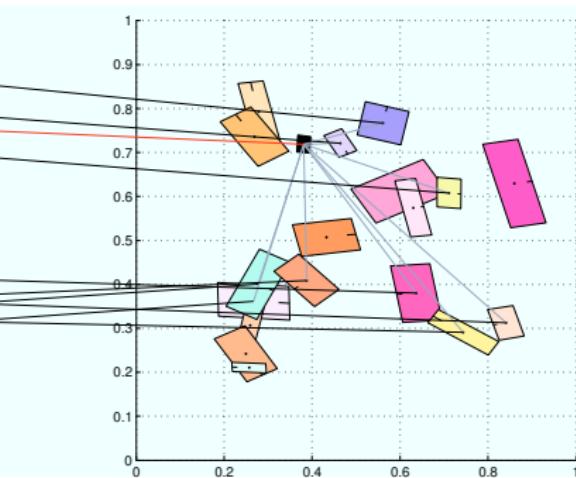
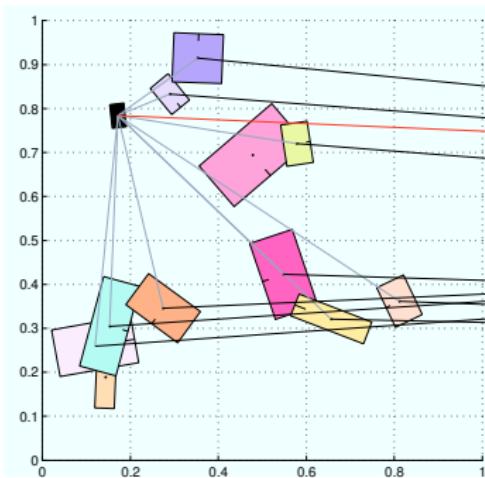
Feature map similarity

for all origins mapped to visual word v

$$S_F(P, Q) = \max_{v \in V(P, Q)} \max_{\substack{\hat{x} \in H_v(P) \\ \hat{y} \in H_v(Q)}} f_P^T(\hat{x}) f_Q(\hat{y})$$

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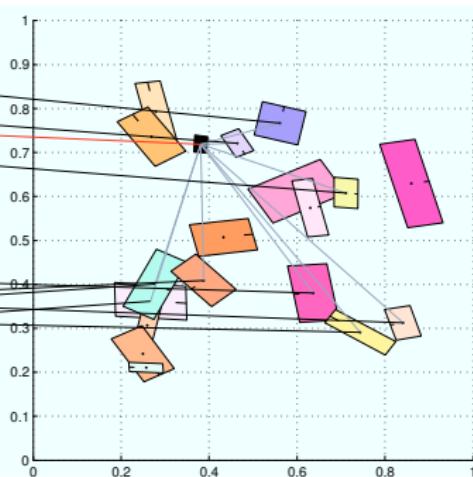
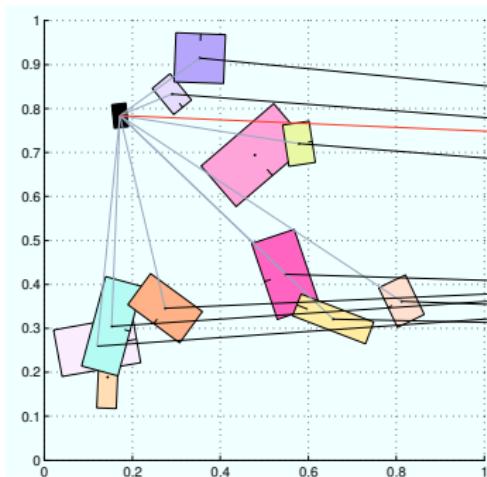
Feature map similarity

for all visual words that P, Q have in common

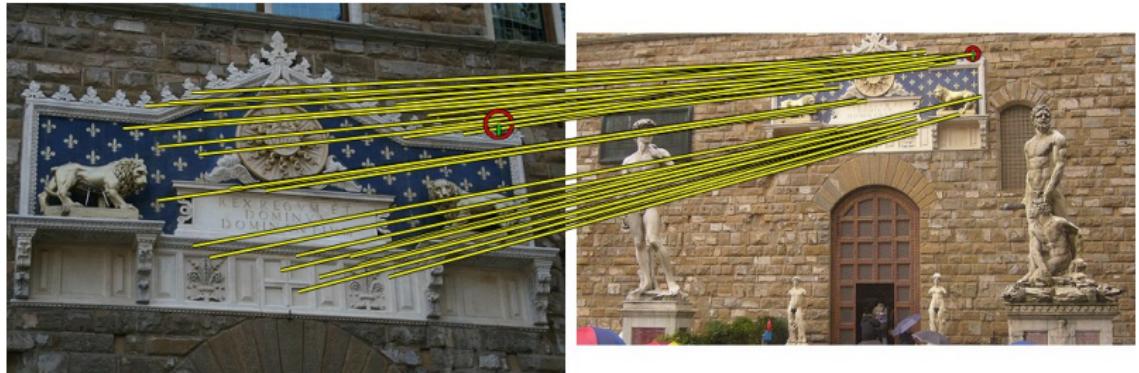
$$S_F(P, Q) = \max_{v \in V(P, Q)} \max_{\substack{\hat{x} \in H_v(P) \\ \hat{y} \in H_v(Q)}} f_P^T(\hat{x}) f_Q(\hat{y})$$

feature map of image P wrt origin \hat{x}

feature map of image Q wrt origin \hat{y}

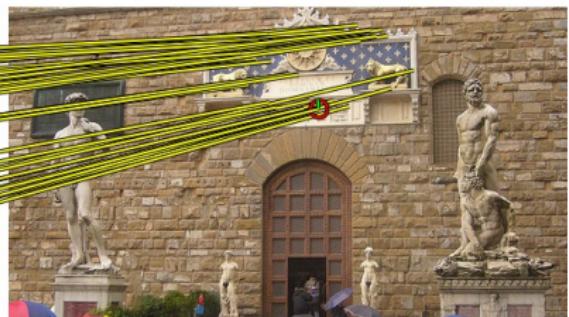
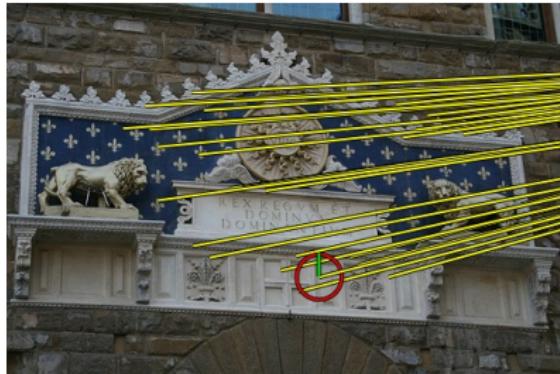


Feature map similarity—example



fast spatial matching [Philbin *et al.* 2007] (35 inliers)

Feature map similarity—example



feature map similarity (32 inliers)

Towards indexing

- FMS is a fast way of matching 2 images, but still not enough for indexing
- a feature map is an extremely sparse histogram; bin count typically takes values in $\{0, 1\}$
- each feature map f is represented by set $\bar{f} \subset \mathcal{W}$ of non-empty bins

Min-wise independent permutations

a.k.a. min-hashing [Broder 2000]

- feature space $\mathbb{F} = \mathcal{P}(\mathcal{W})$, the powerset of \mathcal{W}
- $h : \mathbb{F} \rightarrow \mathcal{W}$, hash function mapping objects back to \mathcal{W}
- $\pi : \mathbb{F} \rightarrow \mathbb{F}$, a random permutation
- given a feature map $\bar{f} \subset \mathcal{W}$, compute a hash value
$$h(\bar{f}) = \min\{\pi(\bar{f})\}$$
- two features maps are hashed to the same value with probability equal to their resemblance or Jaccard similarity coefficient

$$\Pr[h(\bar{f}) = h(\bar{g})] = \frac{|\bar{f} \cap \bar{g}|}{|\bar{f} \cup \bar{g}|} = J(\bar{f}, \bar{g})$$

An example

[Chum et al. 2007]

a	b	c	d	e	f	$\{a, b, c\}$	$\{b, c, d\}$	$\{a, e, f\}$
permutations						hash values		
3	6	2	5	4	1	2	2	1
1	2	6	3	5	4	1	2	1
3	2	1	6	4	5	1	1	3
4	3	5	6	1	2	3	3	1

An example

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Map sketch

- construct a set $\Pi = \{\pi_i : i = 1, \dots, m\}$ of m independent random permutations
- represent each feature map \bar{f} by **map sketch** $\mathbf{f} \in \mathcal{W}^m$,

$$\mathbf{f} = \mathbf{f}(\bar{f}) = [\min\{\pi_1(\bar{f})\}, \dots, \min\{\pi_m(\bar{f})\}]^T$$

- **sketch similarity**: count number of elements that sketches \mathbf{f} , \mathbf{g} have in common

$$s_K(\mathbf{f}, \mathbf{g}) = m - \|\mathbf{f} - \mathbf{g}\|_0$$

Feature map hashing (FMH)

- map sketch collection \mathbf{F} : set of all map sketches f of an image
- image similarity reduces to sketch similarity

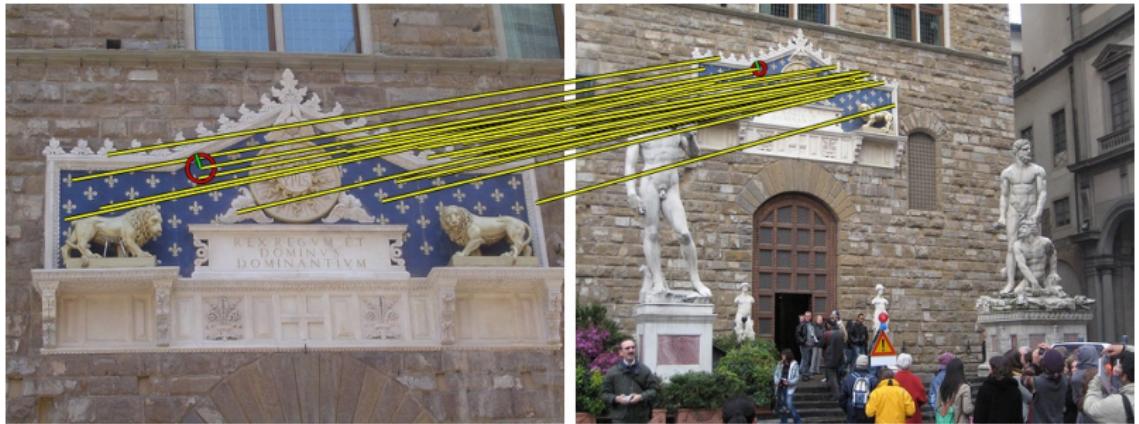
$$S_M(\mathbf{F}, \mathbf{G}) = \max_{\mathbf{f} \in \mathbf{F}} \max_{\mathbf{g} \in \mathbf{G}} s_K(\mathbf{f}, \mathbf{g})$$

- collisions may appear for several pairs of maps; sum all sketch similarities instead of keeping the best one

$$S_K(\mathbf{F}, \mathbf{G}) = \sum_{\mathbf{f} \in \mathbf{F}} \sum_{\mathbf{g} \in \mathbf{G}} s_K(\mathbf{f}, \mathbf{g})$$

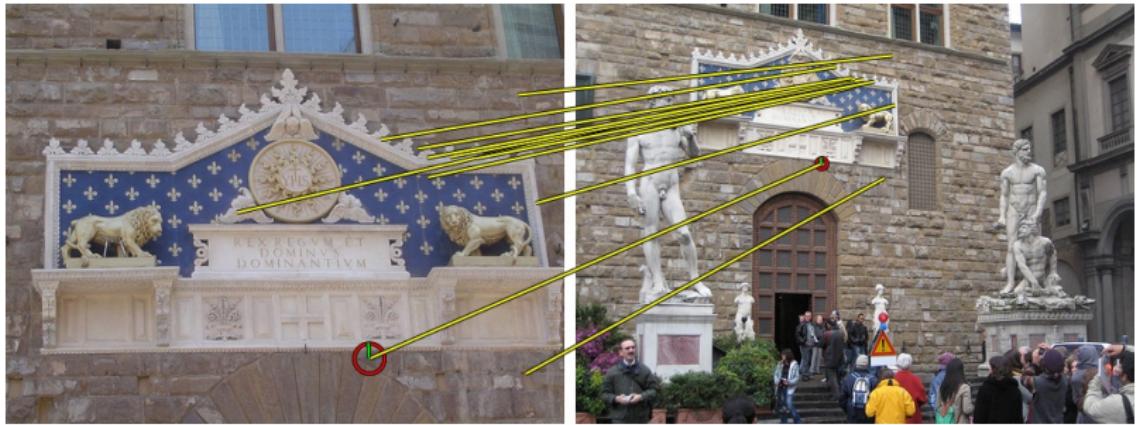
- constrain sketch origins to those mapping uniquely to the same visual words

Matching maps



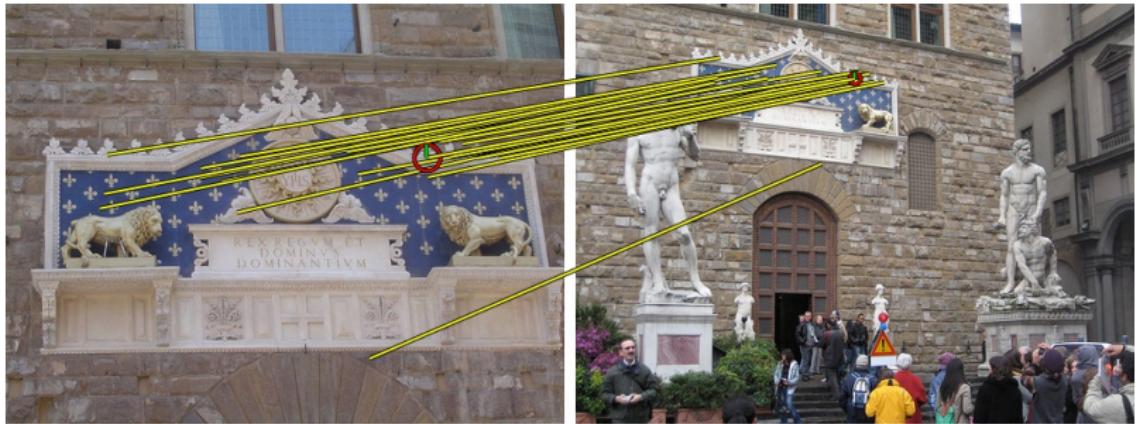
Multiple matching pairs of feature maps

Matching maps



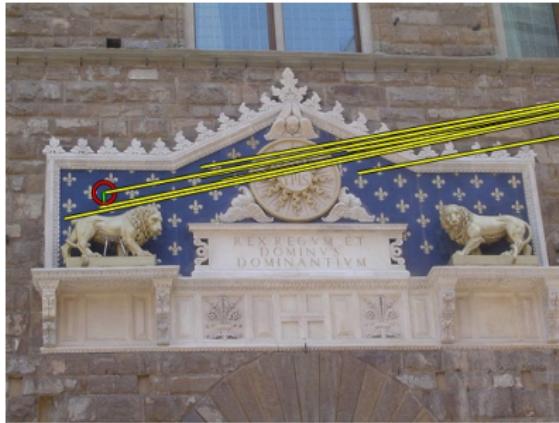
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Matching maps



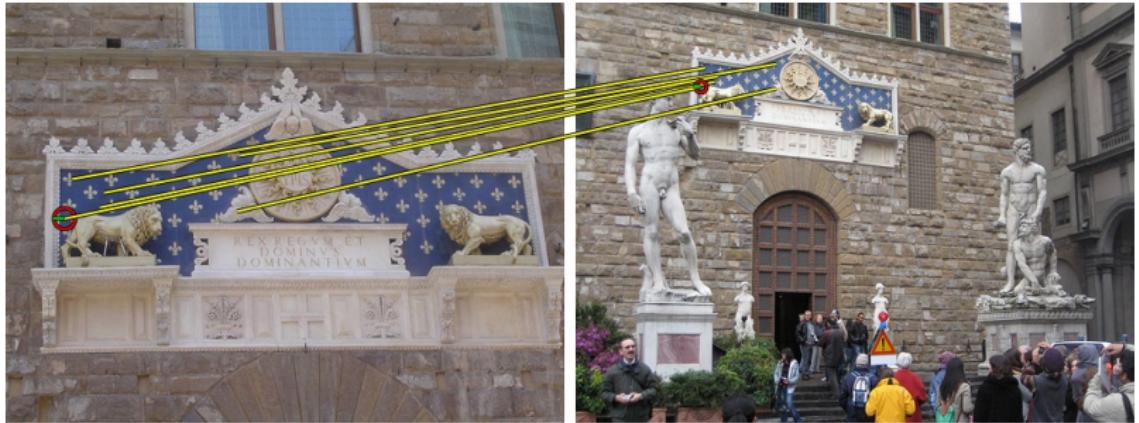
Multiple matching pairs of feature maps

Matching maps



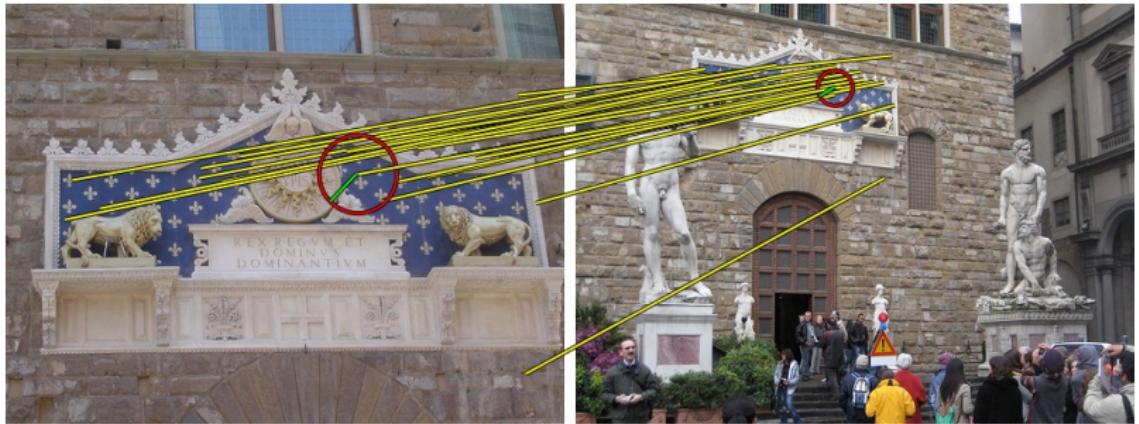
Multiple matching pairs of feature maps

Matching maps



Multiple matching pairs of feature maps

Matching maps



Multiple matching pairs of feature maps

Indexing

index construction

- construct inverted file of triplets (\hat{v}, w, π) (origin, hash value, permutation)
- memory requirements $5\times$ a typical baseline system

query

- retrieve images by triplets (\hat{v}, w, π) of query image
- re-estimate transformation parameters using LO-RANSAC
- **re-ranking** is an order of magnitude faster than FastSM, because an initial estimate is already available

European Cities dataset 50K (EC50K)

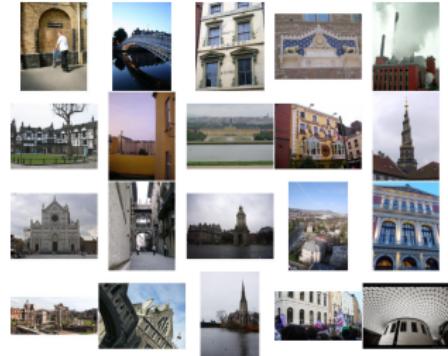
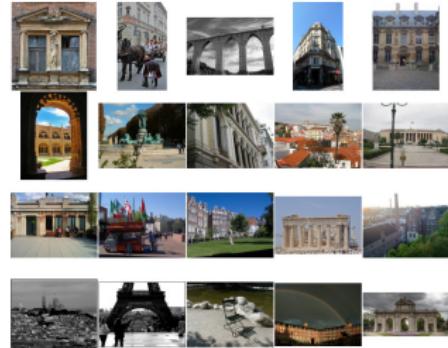
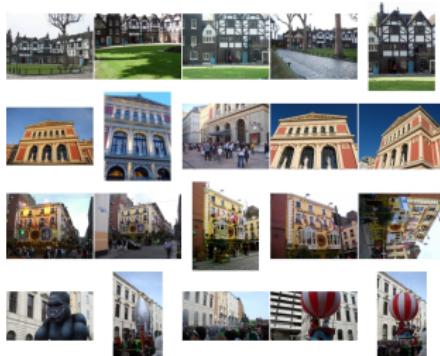
- 778 Annotated images
- 20 groups of photos
- 5 queries from each group



Publicly available: <http://image.ntua.gr/iva/datasets/ec50k>

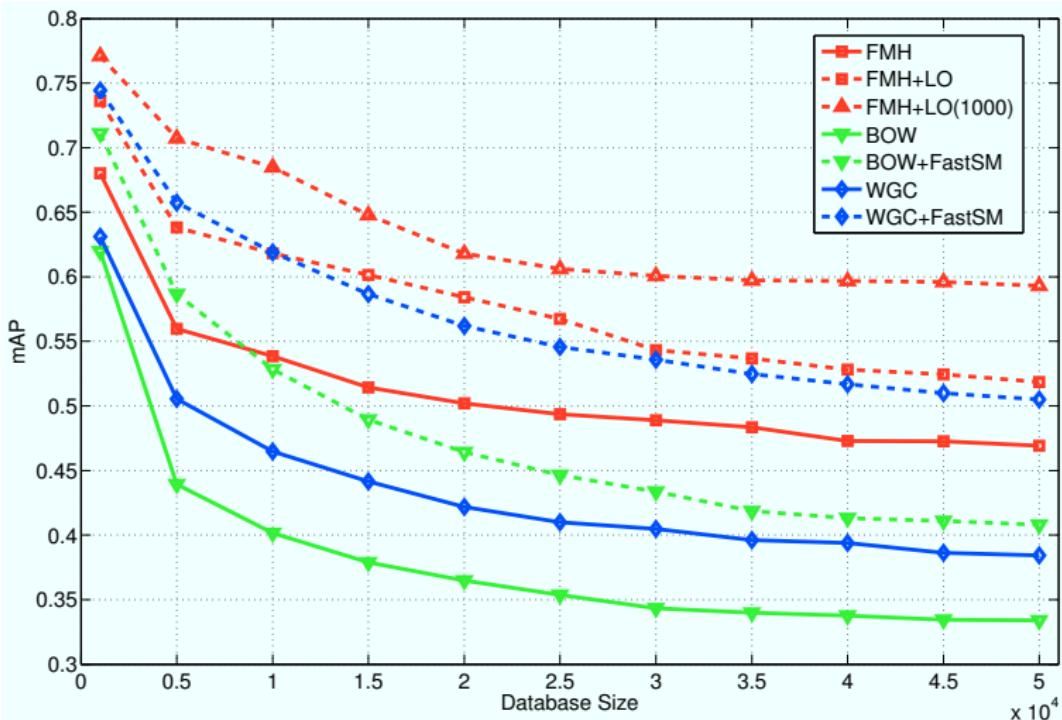
European Cities dataset 50K (EC50K)

- 778 Annotated images
- 20 groups of photos
- 5 queries from each group
- 50,000 distractor images



Publicly available: <http://image.ntua.gr/iva/datasets/ec50k>

Results EC50K



Outline

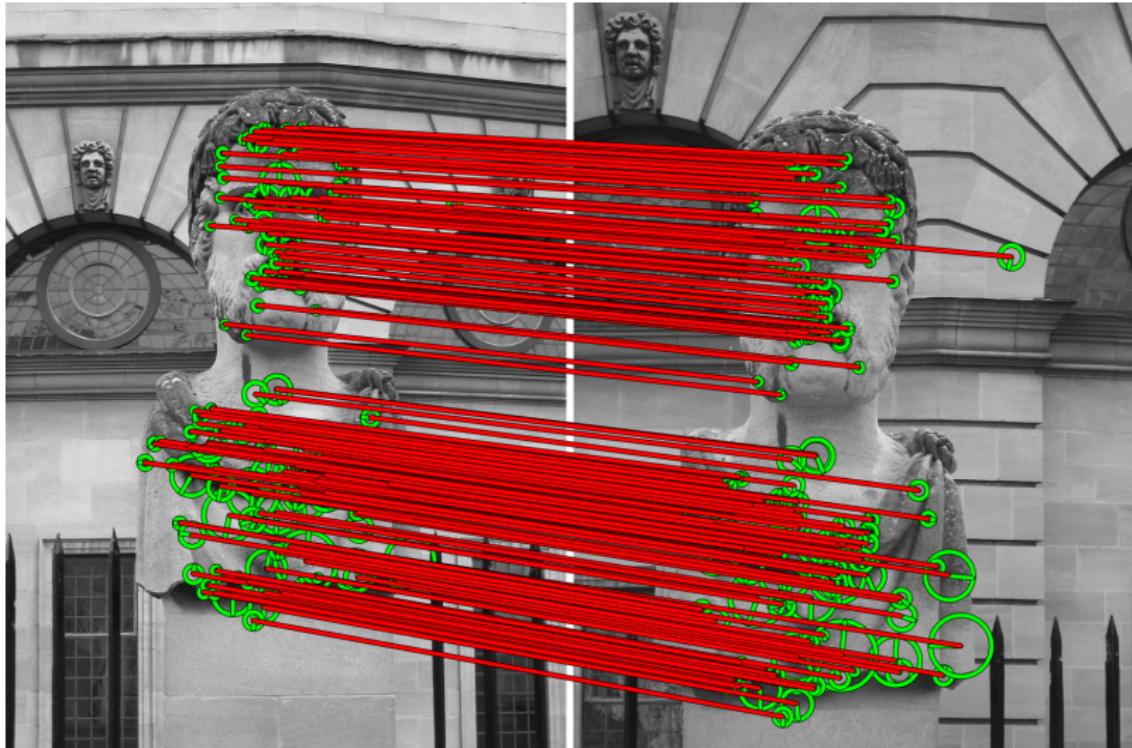
- 1 Visual search, local features and bag-of-words
- 2 Local features based on distance maps
- 3 Geometry indexing: feature map hashing
- 4 Relaxed spatial matching and re-ranking
- 5 Photo collections: view clustering and scene maps
- 6 Location and landmark recognition
- 7 Implementation: ivl library

Relaxed spatial matching

[Tolias and Avrithis 2011, unpublished]

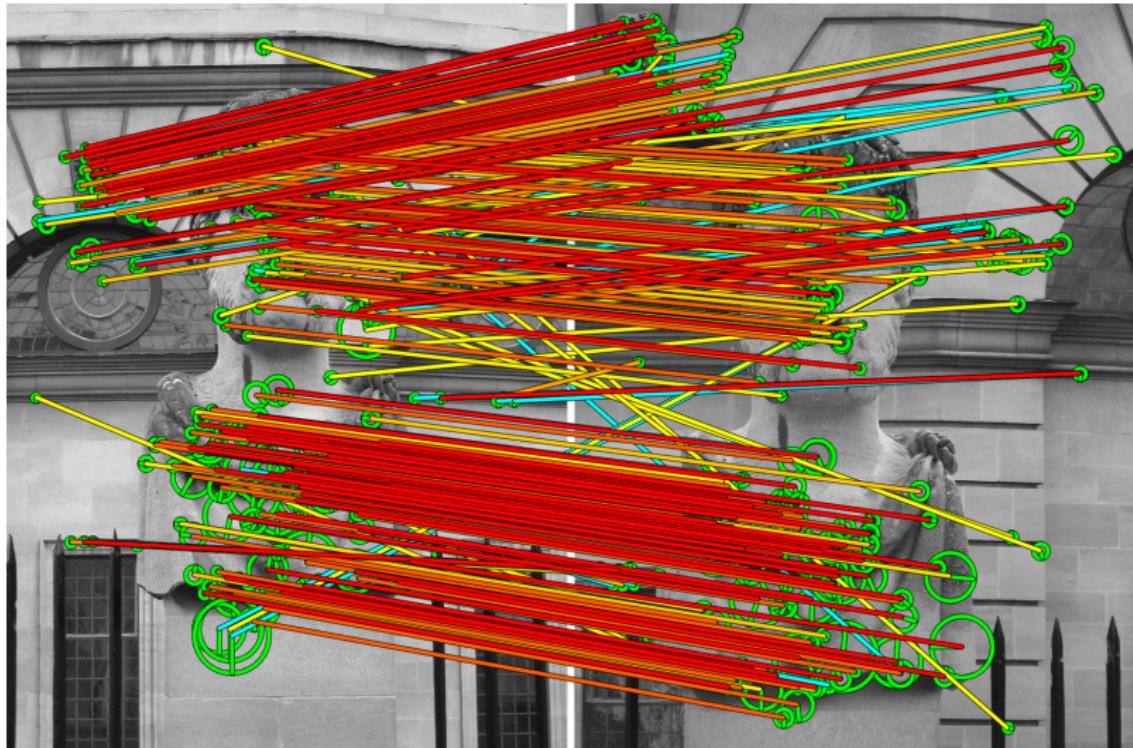
- invariant to similarity transformations
- flexible, allowing non-rigid motion and multiple matching surfaces or objects
- imposes one-to-one mapping
- non-iterative, and linear in the number of correspondences
- in a given query time, can re-rank one order of magnitude more images than the state of the art
- needs less than one millisecond to match a pair of images, on average

Relaxed matching—examples



fast spatial matching

Relaxed matching—examples



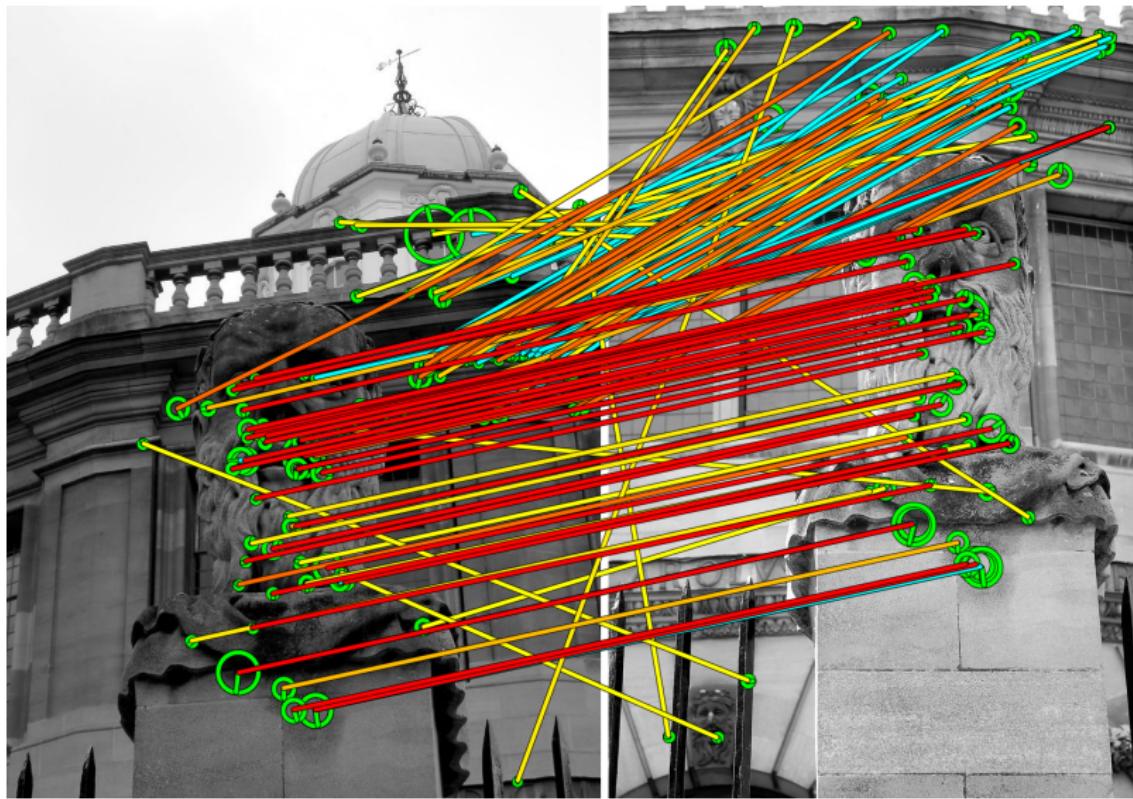
relaxed matching

Relaxed matching—examples



fast spatial matching

Relaxed matching—examples



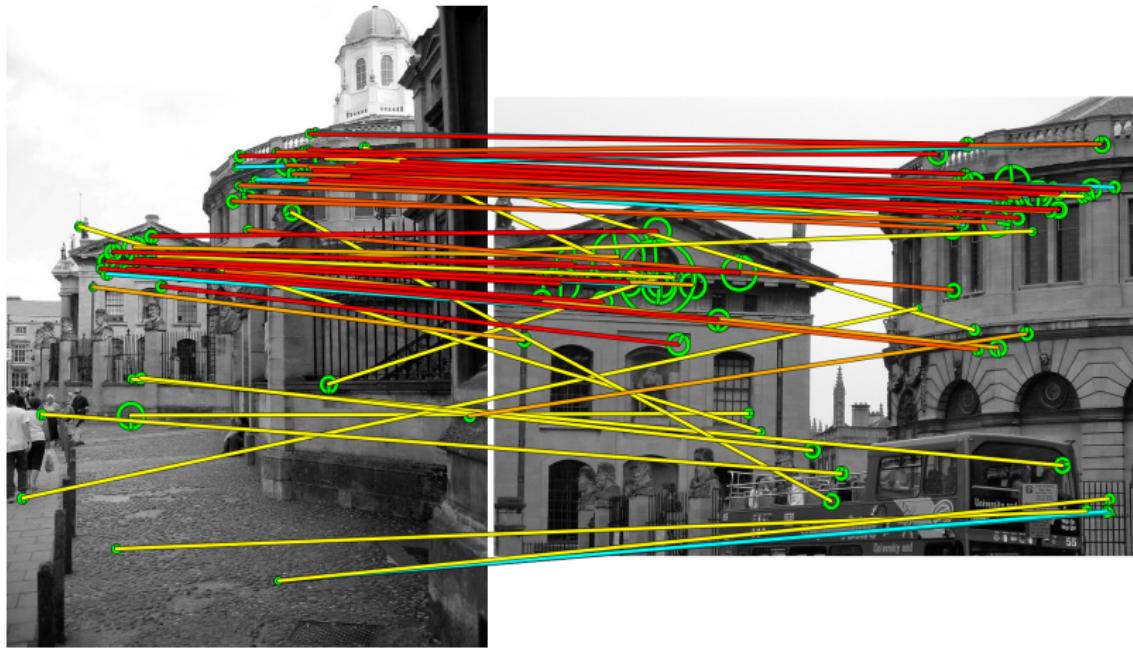
relaxed matching

Relaxed matching—examples



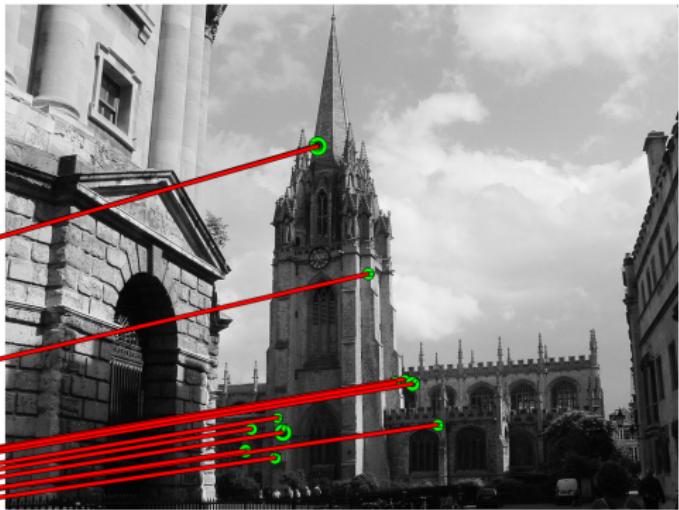
fast spatial matching

Relaxed matching—examples



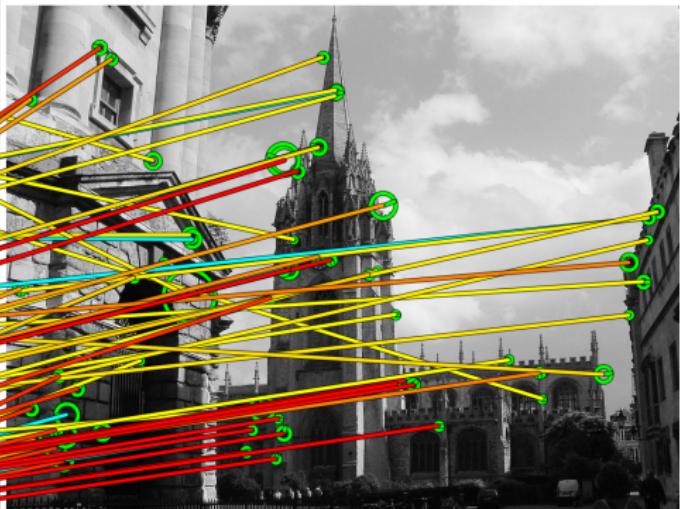
relaxed matching

Relaxed matching—examples



fast spatial matching

Relaxed matching—examples



relaxed matching

Relaxed matching—examples



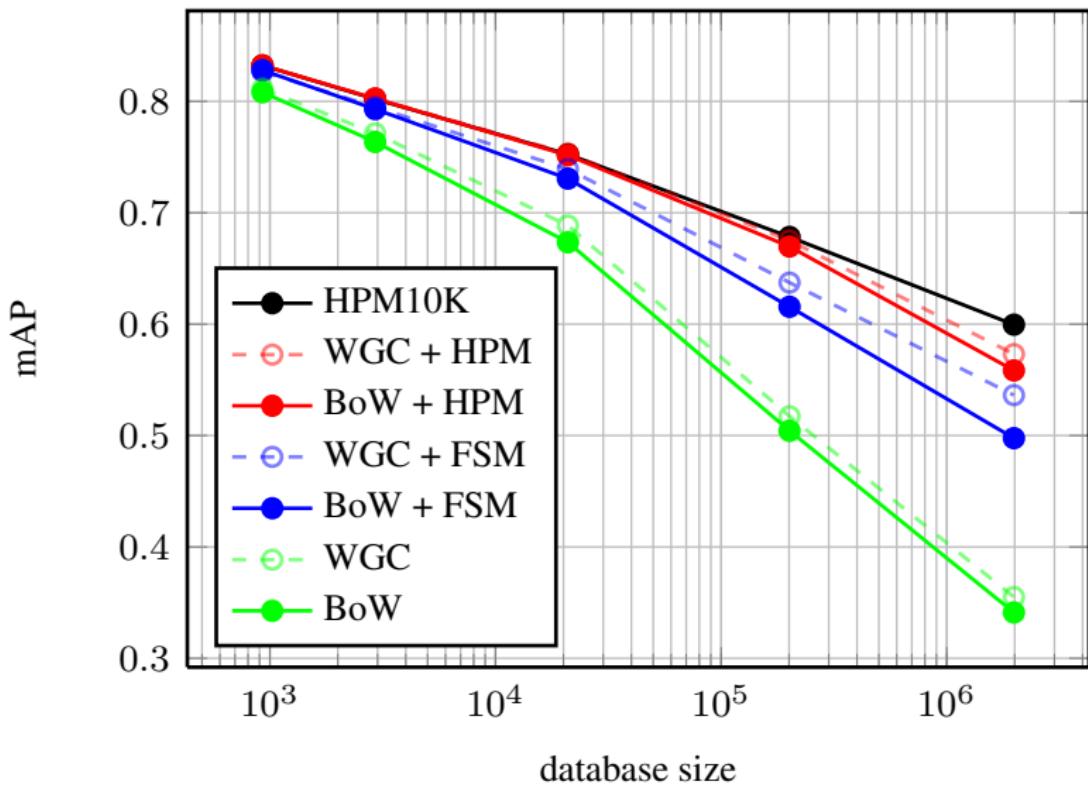
fast spatial matching

Relaxed matching—examples

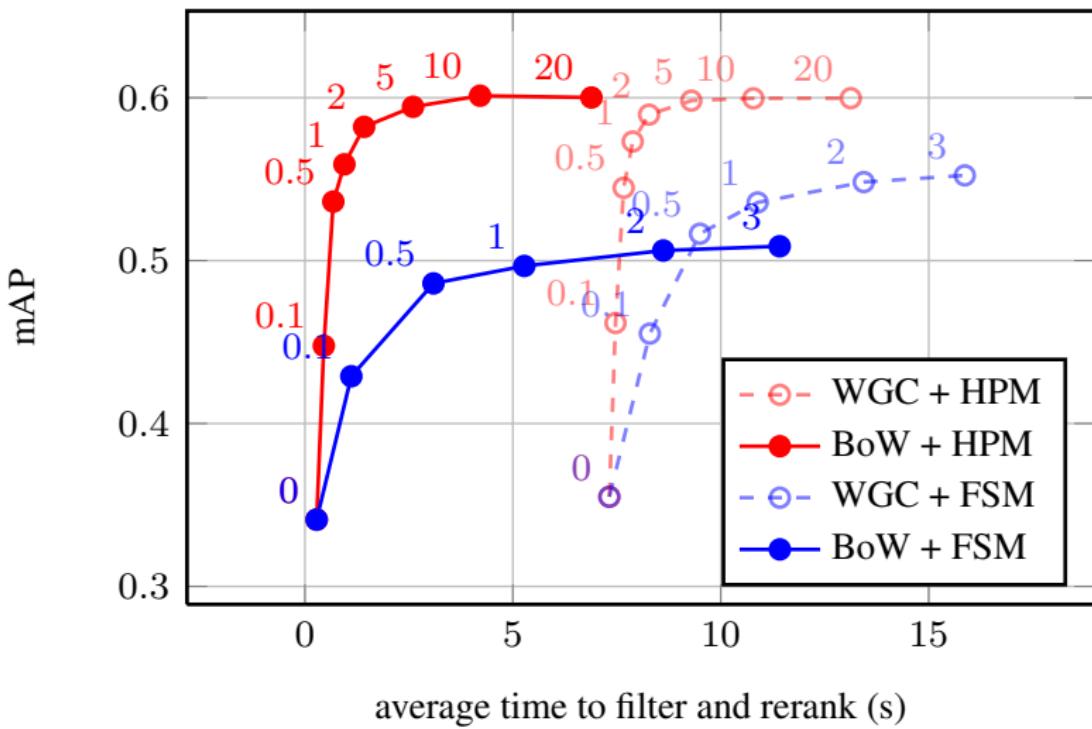


relaxed matching

Relaxed matching—statistics



Relaxed matching—timing



Outline

- 1 Visual search, local features and bag-of-words
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Community photo collections

clustering / landmark recognition

- focus on **popular** subsets
- applications: browsing, 3D reconstruction

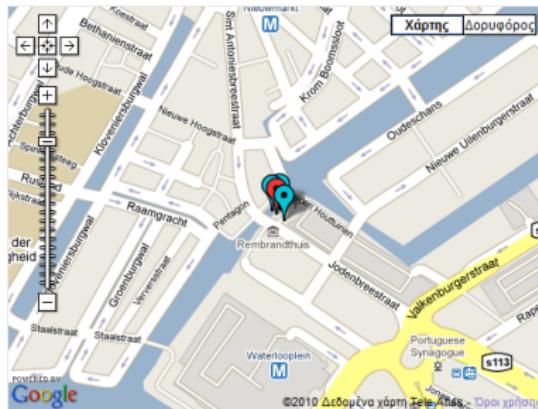


[Crandall et al. 2009]

Community photo collections

retrieval / location recognition

- include **all** images, has not yet scaled enough
- applications: automatic geo-tagging, camera pose estimation

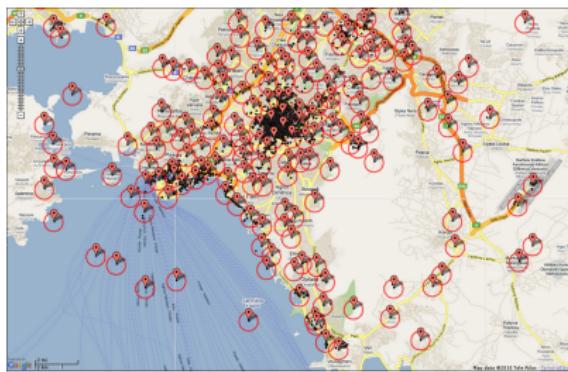


Suggested tags: Sint Antoniesbreestraat, Zwanenburgwal, Amsterdam
Frequent user tags: Anthoniesluis, sluijswacht, krom, stare, Skirt

View clustering

[Avrithis et al. 2010]

- identify images that potentially depict views of the **same scene**
- **geo clustering:** according to location
- **visual clustering:** according to visual similarity



- use **sub-linear indexing** in the clustering process

Kernel vector quantization (KVQ)

[Tipping and Schölkopf 2001]

- input dataset: $D \subseteq X$, where (X, d) is a metric space
- codebook: a small subset $Q(D)$ such that distortion is minimized
- for codebook vector $x \in Q(D)$, cluster $C(x)$ contains all points $y \in D$ within distance r :

$$C(x) = \{y \in D : d(x, y) < r\}$$

- sparse solution by solving a linear programming problem
- pairwise distance matrix: quadratic in the dataset size $|D|$

Kernel vector quantization

properties

- codebook vectors are points of the original dataset:
 $Q(D) \subseteq D$
- distortion upper bounded by r :
for all $x \in Q(D)$

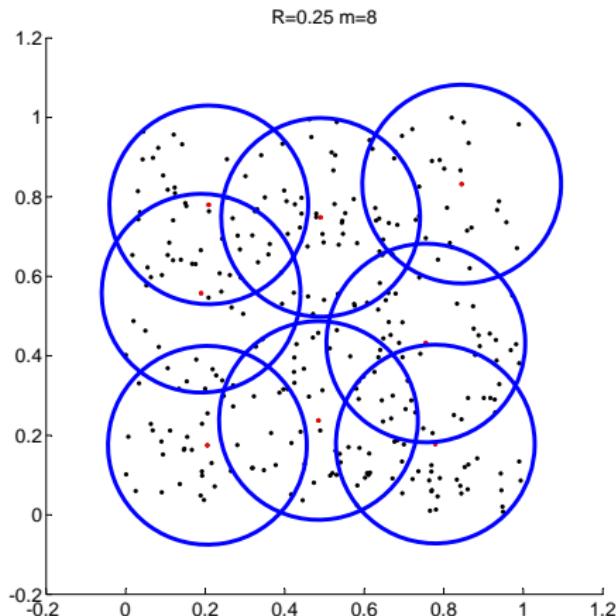
$$\max_{y \in C(x)} d(x, y) < r$$

- the cluster collection

$$\mathcal{C}(D) = \{C(x) : x \in Q(D)\}$$

is a cover for D

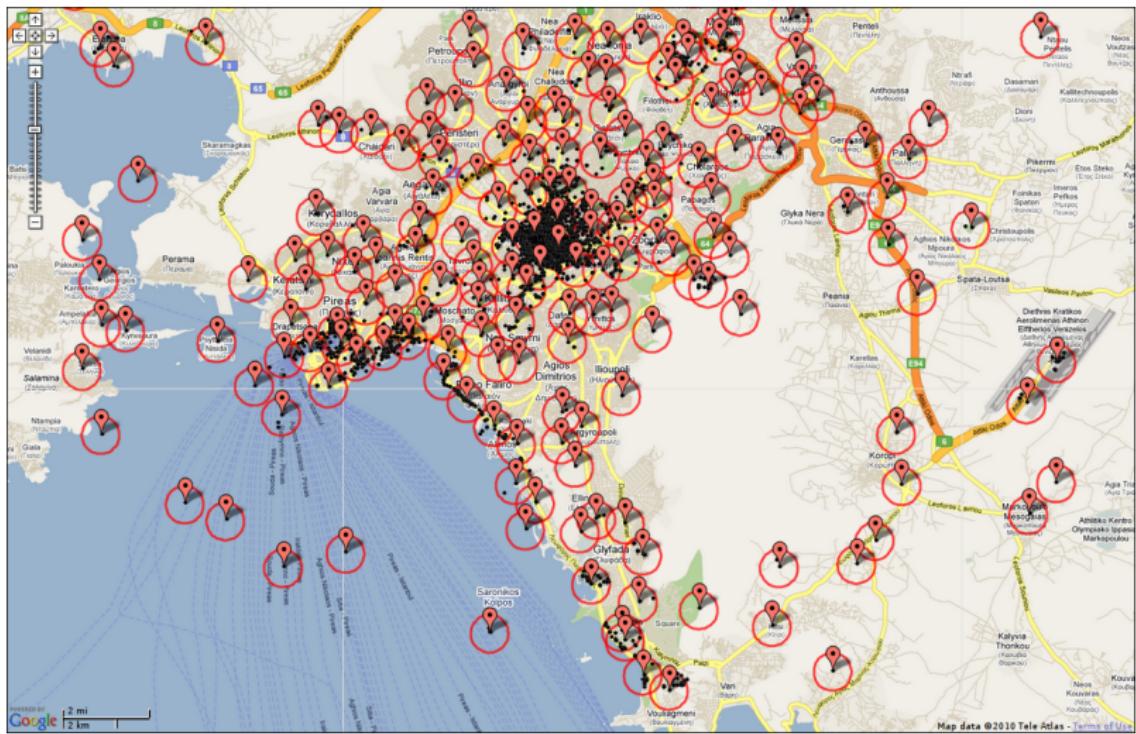
- clusters are overlapping



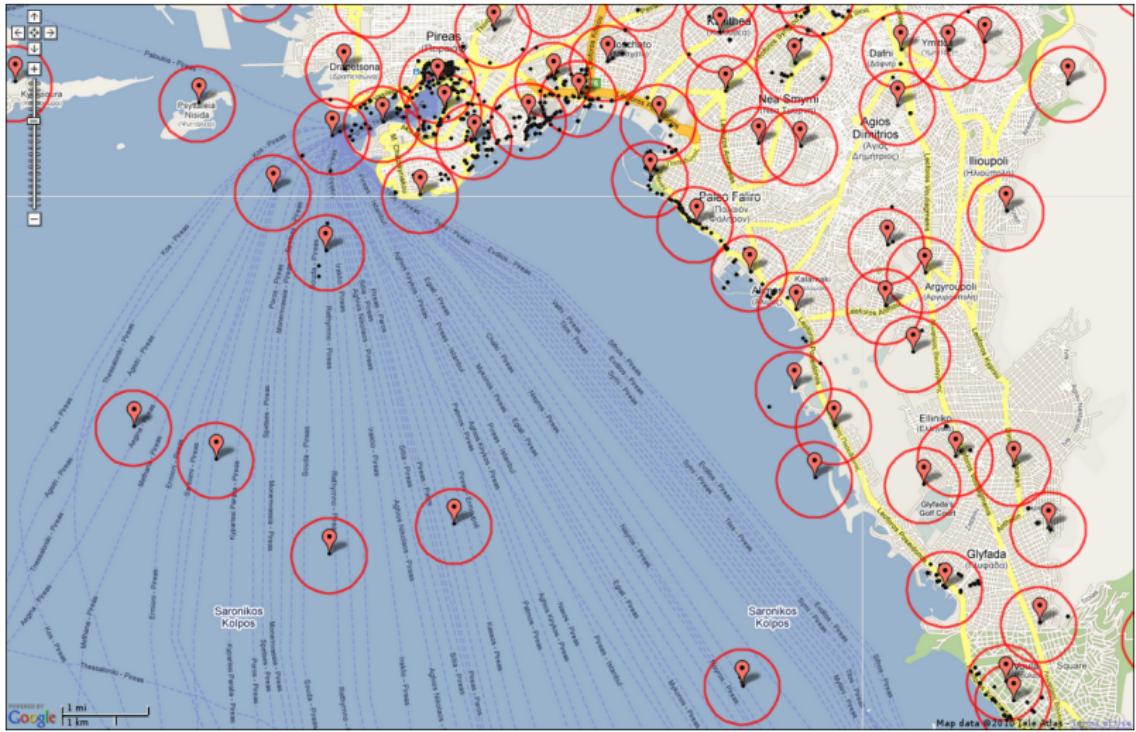
Geo clustering

- given set of photos $P \subseteq \mathcal{P}$ in metric space (\mathcal{P}, d_g)
- each photo $p \in P$ is represented by tuple (ℓ_p, F_p) (location, features)
- metric d_g : the great circle distance
- construct codebook $Q_g(P)$ by KVQ of P with scale parameter r_g
- maximum distortion: photos taken e.g. further than 2km apart are not likely to depict the same scene

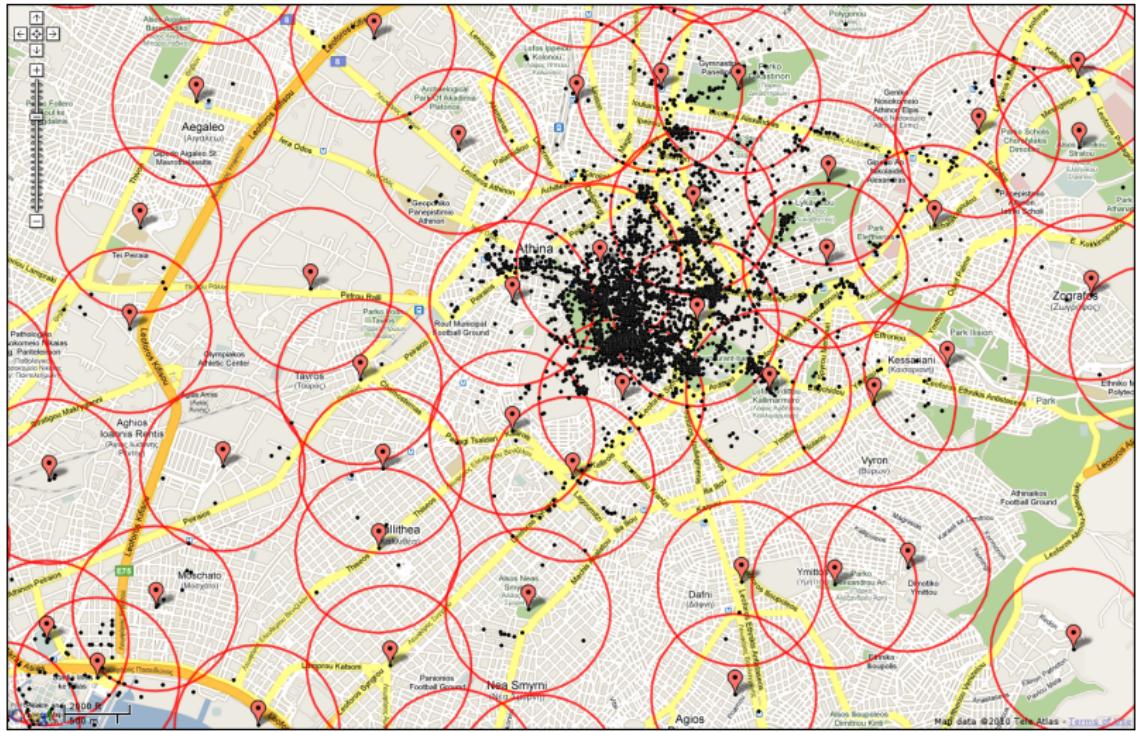
Geo clustering—example



Geo clustering—example



Geo clustering—example



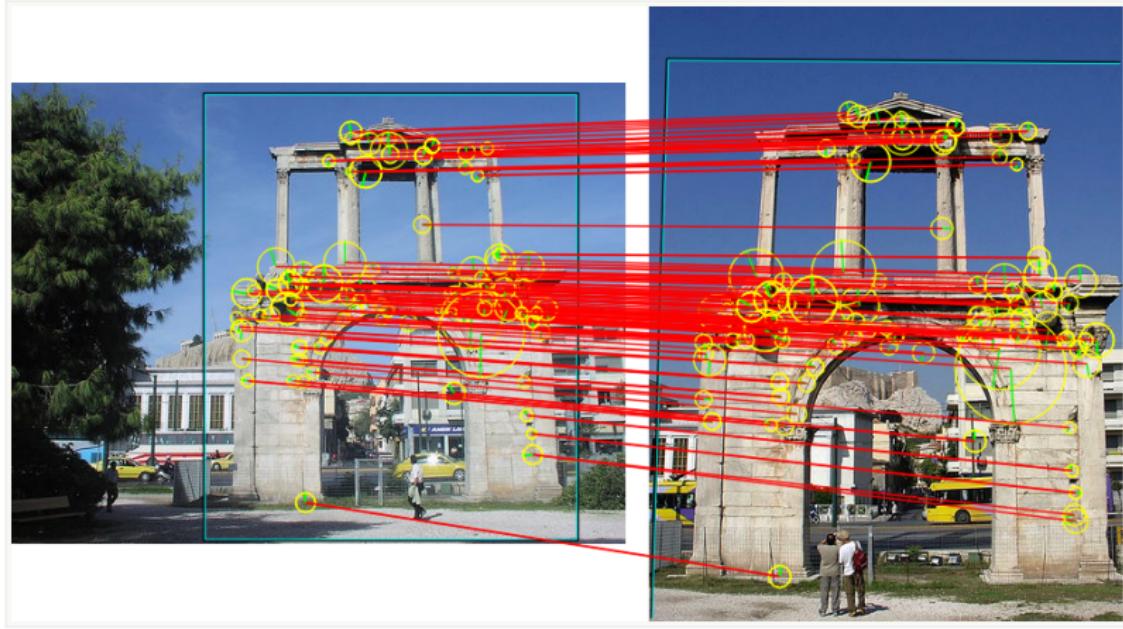
Geo clustering—example



Visual clustering

visual similarity measure

- $I(F_p, F_q)$: number of **inliers** between visual feature sets F_p, F_q of photos p, q respectively



Visual clustering

- for each geo-cluster G , construct codebook $Q_v(G)$ by KVQ in space (\mathcal{P}, d_v) with scale parameter r_v
- metric $d_v(p, q)$ and scale parameter r_v are expressed in terms of number of **inliers**
- **maximum distortion**: equivalent to minimum number of inliers
- **overlapping**: support gradual transitions of views

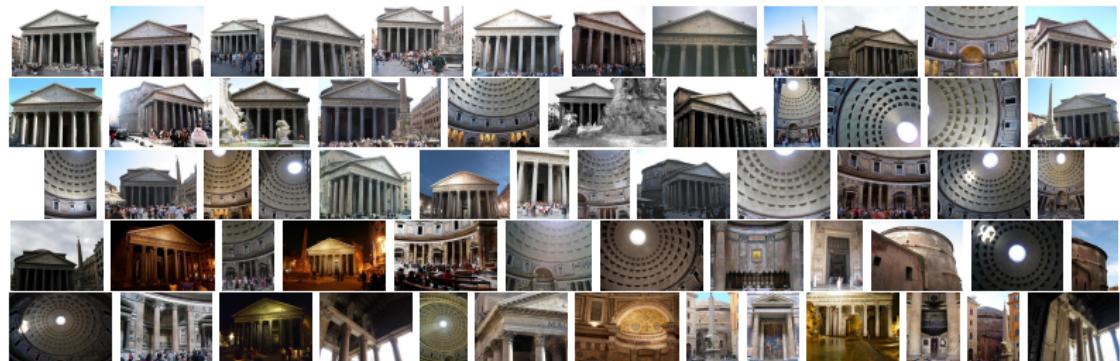
Visual clustering

- geo-cluster specific sub-linear indexing
- bottleneck: computation of pairwise distances, quadratic in $|G| \rightarrow$ inverted file indexed by both visual word and geo-cluster
- given a query image $q \in G$, find all matching images $p \in G$ with $I(F_p, F_q) > \tau$ in constant time, typically less than one second
- the entire computation is now linear in $|G|$

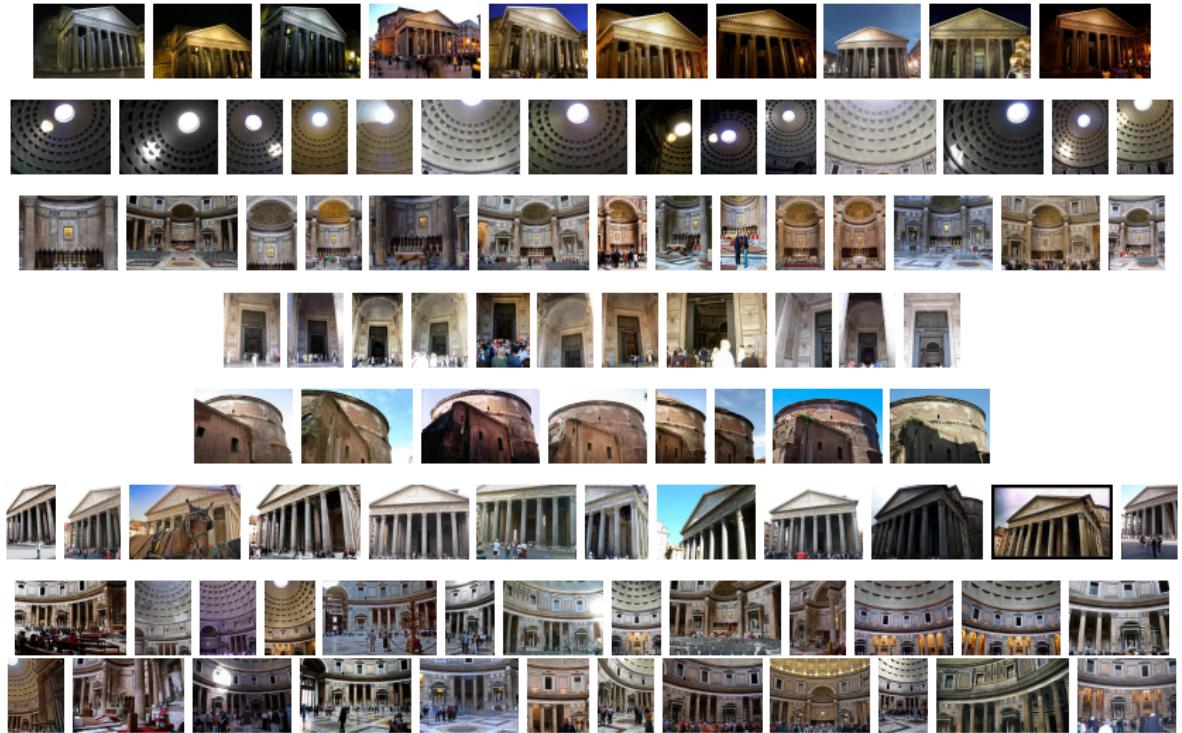
Visual clustering—example

1,146 geo-tagged Flickr images of Pantheon, Rome

- 258 resulting visual clusters
- 30 images at each visual cluster on average
- an image belongs to 4 visual clusters on average



Visual clustering—example



Scene maps

[Avrithis et al. 2010]

- the image associated to the center of a view cluster shares at least one **rigid object** with all other images in the cluster
- treat this image as a **reference** for the cluster and **align** all other images to it
- initial estimates available from the view clustering stage—only local optimization needed
- construct a 2D **scene map** by grouping similar local features
- extend index, retrieval, and spatial matching for scene maps

View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



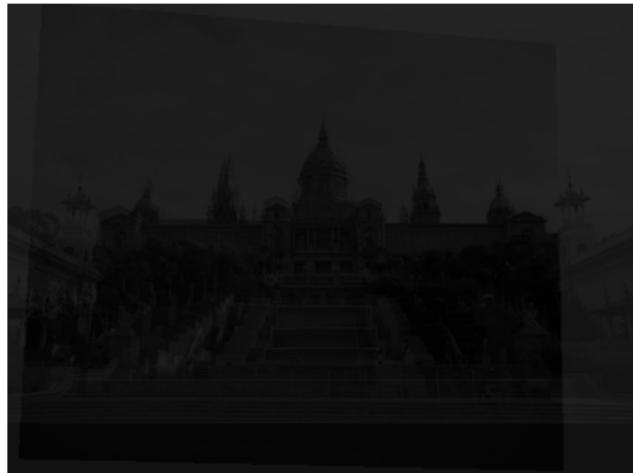
View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—input images



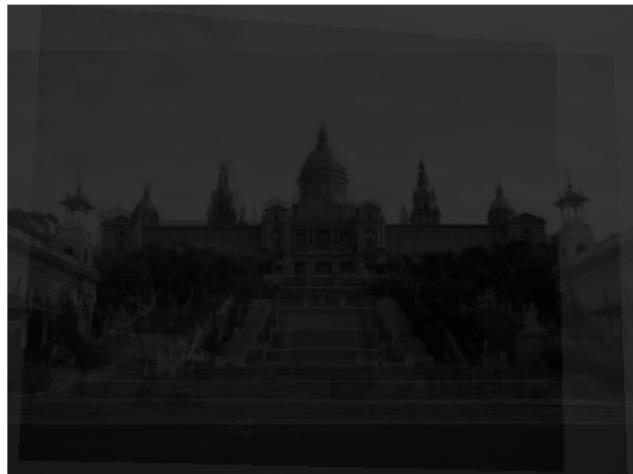
View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



View cluster alignment—example

Palau Nacional, Montjuic, Barcelona—aligned images



Scene map construction

- $F(p)$: the union of features over all images in visual cluster $C_v(p)$ after alignment

$$F(p) = \bigcup_{q \in C_v(p)} \{ (H_{qp}x, w) : (x, w) \in F_q \}$$

- apply **spatial** KVQ separately to features mapped to each visual word
- **join** the resulting codebooks into a single **scene map** $S(p)$

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feature set of photo q



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(position, visual word)

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position aligned to reference image p

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$$F(p) = \bigcup_{q \in C_v(p)} \{ (H_{qp}x, w) : (x, w) \in F_q \}$$

position aligned to reference image p

feature set of photo q

union over all photos q of $C_v(p)$

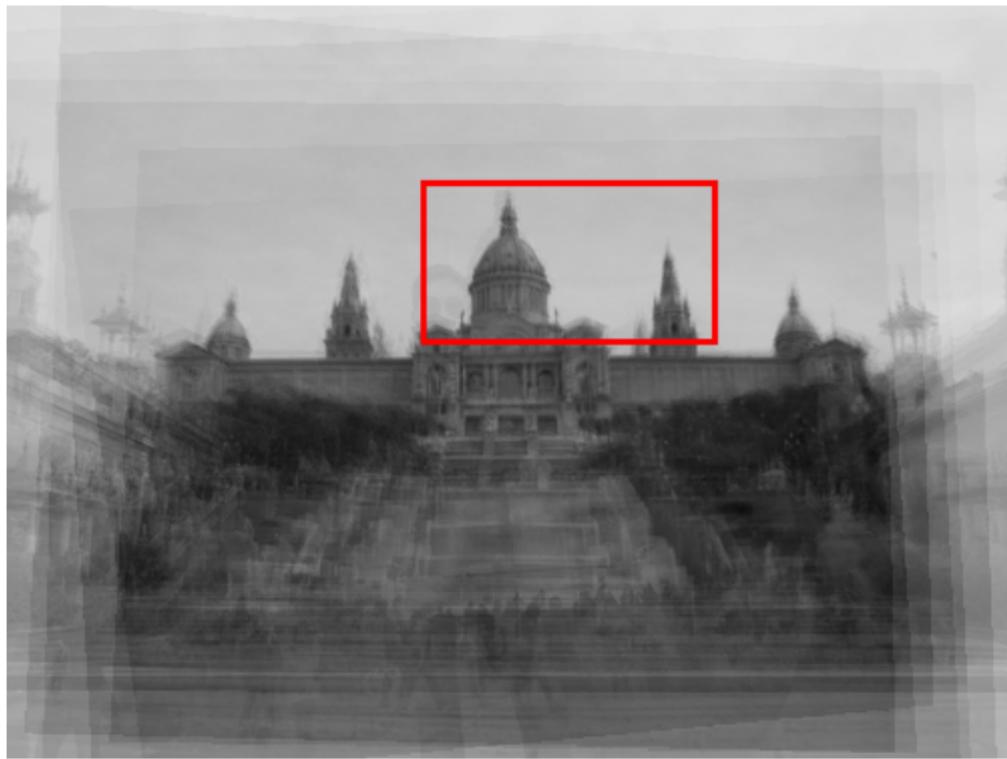
(position, visual word)

The diagram illustrates the mathematical expression for $F(p)$. It consists of three main components: a top row of labels in light blue boxes, a middle row of arrows pointing from these labels to specific terms in the equation, and a bottom row of labels also in light blue boxes. The top row contains 'position aligned to reference image p ' and 'feature set of photo q '. The middle row contains four red arrows: one from 'position aligned to reference image p ' to the term $H_{qp}x$, one from 'feature set of photo q ' to the term w , one from '(position, visual word)' to the term (x, w) , and one from 'union over all photos q of $C_v(p)$ ' to the union symbol. The bottom row contains 'union over all photos q of $C_v(p)$ ' and '(position, visual word)'. The equation itself is
$$F(p) = \bigcup_{q \in C_v(p)} \{ (H_{qp}x, w) : (x, w) \in F_q \}$$
.

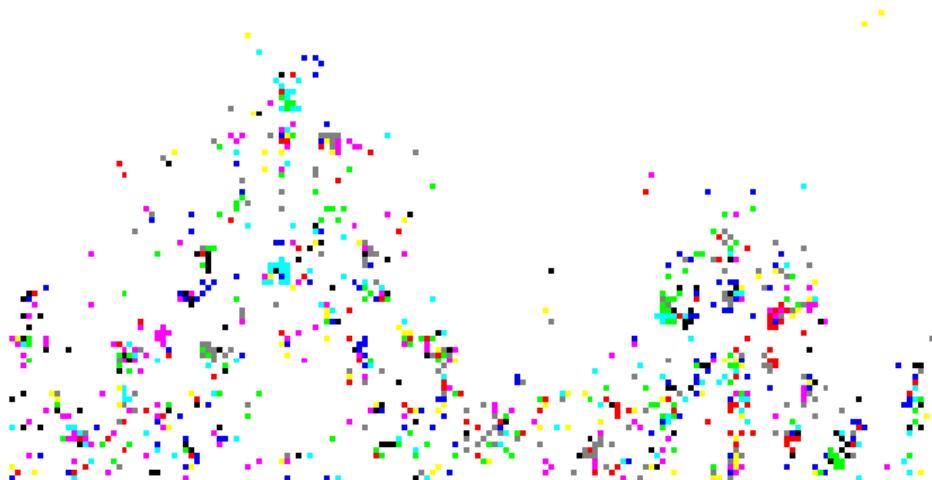
- apply **spatial KVQ** separately to features mapped to each visual word
- **join** the resulting codebooks into a single **scene map** $S(p)$

Scene map construction—example

visual cluster containing 30 images of Palau Nacional, Montjuic

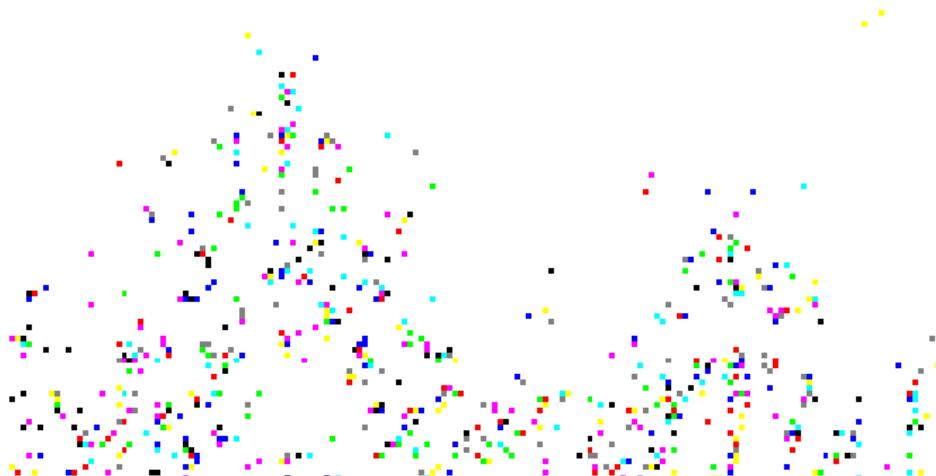


Scene map construction—example



before vector quantization

Scene map construction—example



after vector quantization

Scene map indexing

index construction

- scene maps and images have the same representation—sets of features
- index all scene maps by visual word in an inverted file

query

- re-rank using the single correspondence assumption [Philbin et al. 2007]
- whenever a scene map $S(p)$ is found relevant, all images $q \in C_v(p)$ are retrieved as well

European Cities 1M dataset (EC1M)

- 1,081 images from Barcelona annotated into 35 groups
- all geo-tagged Flickr images



17 landmark groups

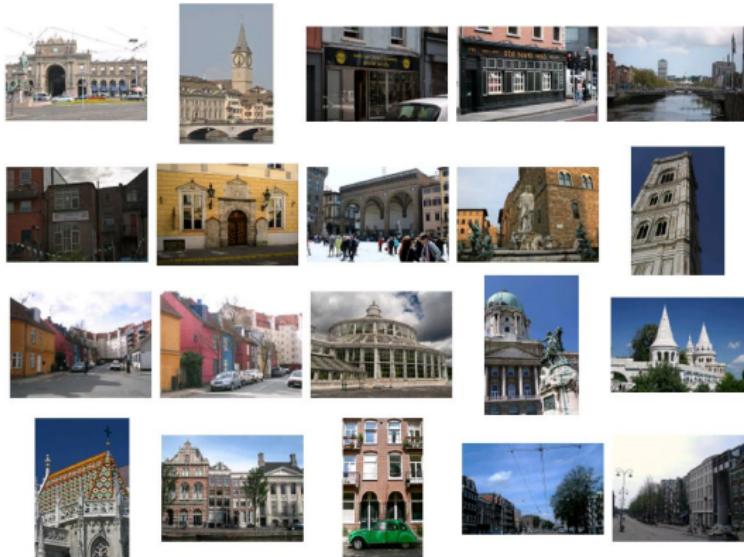


18 non-landmark groups

Publicly available: <http://image.ntua.gr/iva/datasets/ec1m/>

European Cities 1M dataset (EC1M)

- 908,859 **distractor** images from 21 European cities, excluding Barcelona
- most depict urban scenery like the ground-truth



Publicly available: <http://image.ntua.gr/iva/datasets/ec1m/>

Mining statistics—scene maps

- 1M images, 58 hours, single machine (8GB RAM), landmarks and non-landmarks



Mining statistics—related work

- [Chum et al. 2009] [web-scale clustering](#): 5M images, 28 hours, single machine (64GB RAM), [popular subsets only](#)
- [Agarwal et al. 2009] [Rome in a day](#): 150K images, 24 hours, 500 cores
- [Frahm et al. 2010] [Rome in a cloudless day](#): 3M images, 24 hours, GPU
- [Heath et al. 2010] [image webs](#): 200K images, 4,5 hours, 500 cores

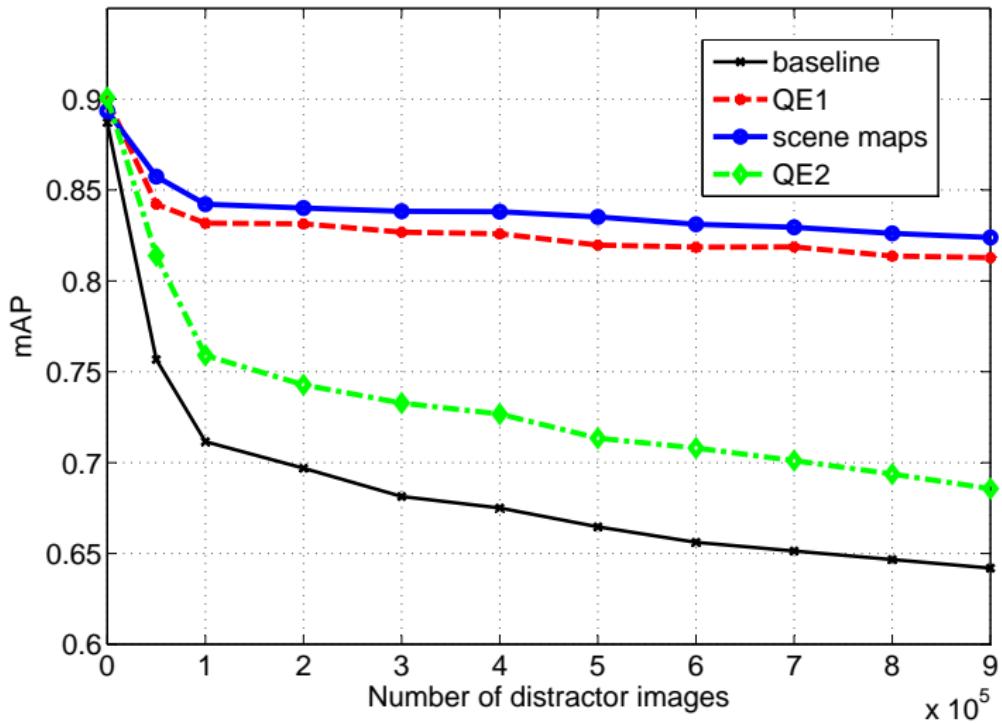
Retrieval comparisons

- **baseline:** bag-of-words with **fast spatial matching** [Philbin et al. 2007]
- **QE1:** iterative query expansion, re-query using the retrieved images and merge results, 3 times iteratively
- **QE2:** create a scene map using the initial query's result and re-query once
- both QE schemes similar to **total recall** [Chum et al. 2007]

query timing

Method	time	mAP
Baseline BoW	1.03s	0.642
QE1	20.30s	0.813
QE2	2.51s	0.686
Scene maps	1.29s	0.824

Retrieval statistics



Outline

- 1 Visual search, local features and bag-of-words
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- 7 Implementation: ivl library

Location and landmark recognition

[Y. Kalantidis et al. 2011]

- assume that a subset of similar photos are correctly geo-tagged, and not too far apart
- recognize the location where the query photo is taken, as the centroid of the most populated spatial (geo) cluster
- cross-validate locations and text (title, tags) of similar images with Geonames entries and geo-referenced Wikipedia articles
- link to known landmarks or points of interest

Location recognition—examples



Landmark recognition—examples



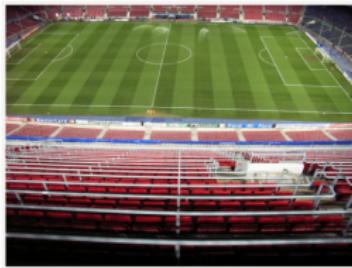
Suggested tags: Park Güell, Barcelona
Frequent user tags: Best of, me, Palau Güell



Suggested tags: La Barceloneta, Barcelona
Frequent user tags: honeymoon, wedding, straße



Suggested tags: Triumphal arch, Arc de Triomf, Barcelona
Frequent user tags: Sant Pere, Santa Caterina i La Ribera, macba, Passeig de Lluís Companys, Ilus companys, Sant Beltra



Suggested tags: FC Barcelona Museum, Camp Nou, Barcelona
Frequent user tags: champions league, vfb, vfb stuttgart, Zoo de Barcelona, Camp Nou



Suggested tags: Montjuïc circuit, Museu Nacional d'Art de Catalunya, Barcelona
Frequent user tags: Montjuic, castellers, Travelling Pooh, architecture, mnac



Suggested tags: Sagrada Familia, Sagrada Familia, Barcelona
Frequent user tags: gaudi, Sagrada Familia, sagrada, familia, expiatorio

<http://viral.image.ntua.gr>

Query



Results



 Estimated Location Similar Image, Incorrectly geo-tagged Unavailable



Suggested tags: Buxton Memorial Fountain, Victoria Tower Gardens, London

Frequent user tags: Victoria Tower Gardens, Buxton Memorial Fountain, Winchester Palace, Architecture, Victorian gothic

Similar Images



Similarity: 0.619



Similarity: 0.491



Similarity: 0.397



Similarity: 0.385

Similar or similar



Original ● ●



Original ● ●



Original ● ●



Original ••



Original ● ●



Original ••



Original ●



Original ••

Similar or similar



Original ●●



Original ●●



Original ●●



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Similar or similar



Original ●●



Original ●●



Original ●●



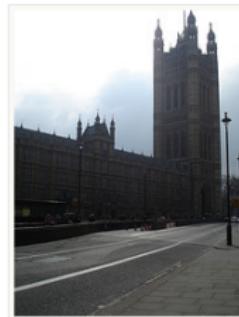
Original ●●



Original ●●



Original ●●



Original ●●



Original ●●

Suggested tags



Suggested tags: Buxton Memorial Fountain, Victoria Tower Gardens, London

Frequent user tags: Victoria Tower Gardens, Buxton Memorial Fountain, Winchester Palace, Architecture, Victorian gothic

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Article Discussion

Buxton Memorial Fountain

From Wikipedia, the free encyclopedia

The **Buxton Memorial Fountain** is a memorial and drinking fountain in London, the United Kingdom, that commemorates the emancipation of slaves in the British Empire in 1834.

It was commissioned by Charles Buxton MP, and was dedicated to his father Thomas Fowell Buxton along with William Wilberforce, Thomas Clarkson, Thomas Babington Macaulay, Henry Brougham and Stephen Lushington, all of whom were involved in the abolition. It was designed by Gothic architect Samuel Sanders Teulon (1812–1873) in 1865 coincidentally with the passing of the Thirteenth Amendment to the United States Constitution, which effectively ended the western slave-trade.^[1]

It was originally constructed in [Parliament Square](#), erected at a cost of £1,200. As part of the postwar redesign of the square it was removed in 1949 and reinstated in its present position in [Victoria Tower Gardens](#) until 1957.^[2] There were eight decorative figures of British rulers on it, but four were stolen in 1960 and four in 1971. They were replaced by fibreglass figures in 1980. By 2005 these were missing, and the fountain was no longer working. Between autumn 2006 and February 2007 restoration works were carried out. The restored fountain was unveiled on 27 March 2007 as part of the commemoration of the 200th anniversary of the act to abolish the slave trade.^[3]

A memorial plaque commemorating the 150th anniversary of the Anti-Slavery Society was added in 1989.

Description

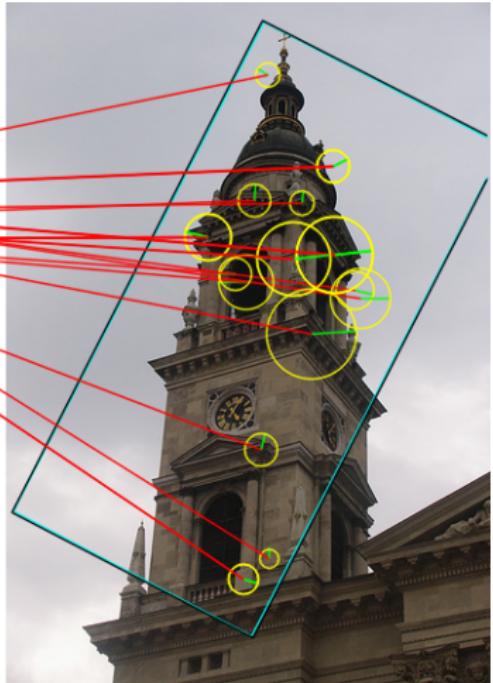
[edit]

The base is octagonal, about twelve feet in diameter, having open arches on the eight sides, supported on clustered shafts of polished Devonshire marble around a large central shaft, with four massive granite basins. Surmounting the pinnacles at the angles of the octagon are eight figures of bronze, representing the different rulers of England; the Britons represented by *Caractacus*, the Romans by *Constantine*, the Danes by *Canute*, the Saxons by *Alfred*, the Normans by *William the Conqueror*, and so on, ending with *Queen Victoria*. The fountain bears an inscription to the effect that it is "intended as a memorial of those members of Parliament who, with Mr. Wilberforce, advocated the abolition of the British slave-trade, achieved in 1807; and of those members of Parliament who, with Sir T.

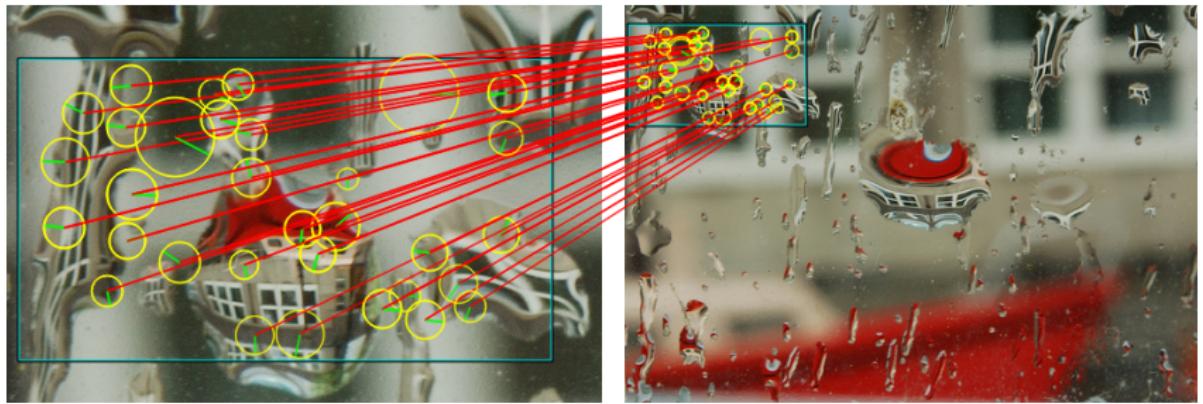


The Buxton Memorial Fountain, designed by Samuel Sanders Teulon, celebrating the emancipation of slaves in the British Empire in 1834, in Victoria Tower Gardens, Milbank, SW1.

Visual similarity



Visual similarity



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Recall feature point matching

- ① construct the $m \times n$ proximity matrix G with elements

$$g_{ij} = \exp(-d_{ij}^2/2\sigma^2)$$

- ② perform singular value decomposition of G

$$G = USV^T$$

where U, V are orthogonal matrices of dimension m, n and S is a non-negative diagonal $m \times n$ matrix

- ③ replace each diagonal element s_{ij} of S by 1 and reconstruct

$$P = UEV^T$$

- ④ finally, associate points a_i and b_j if element p_{ij} of P is the greatest element in its row and its column

Matlab code

```
function [m1, m2] =
match( x1, y1,
        x2, y2, F s)

[Ax1, Ax2] = meshgrid (x1, x2);
[Ay1, Ay2] = meshgrid (y1, y2);

D = sqrt((Ax1 - Ax2) .^ 2 + (Ay1 - Ay2) .^ 2);
G = exp(-D .^ 2 ./ (2 * s ^ 2));

[U, S, V] = svd (G);
E = S > 0;
P = U * E * V';

[tmp, c] = max (P, [], 2);
[tmp, r] = max (P, [], 1);

match = r(c) == (1 : length(c));
m1 = find(match);
m2 = c(match)';
```

ivl C++ code

```
template<class F>    ret<array<F>, array<F> >
match(const array<F>& x1, const array<F>& y1,
      const array<F>& x2, const array<F>& y2, F s)
{
    array_2d<F> Ax1, Ax2, Ay1, Ay2, U, S, V, tmp;
    _ (Ax1, Ax2) = meshgrid++(x1, x2);
    _ (Ay1, Ay2) = meshgrid++(y1, y2);

    array_2d<F> D = sqrt((Ax1 - Ax2) ->* 2 + (Ay1 - Ay2) ->* 2);
    array_2d<F> G = exp(-D ->* 2 / (2 * _ [s] ->* 2));

    _ (U, S, V) = svd++(G);
    array_2d<F> E = S > 0;
    array_2d<F> P = U ()* E ()* V(!_);

    array<int> c, r;
    _ (tmp, c) = max++(P, _, 2);
    _ (tmp, r) = max++(P, _, 1);

    array<bool> match = r[c] == rng(0, c.length() - 1);
    return _ (find(match),
              c[match]);
}
```

ivl library

(Kontosis and Avrithis, expected 2011)

- C++ **template** library, compatible to STL
- supports most types, syntax and built-in operations of **Matlab** language
- fully **optimized**: minimal overhead/temporaries/copying; all array expressions boil down to a single **for** loop
- uses multiple CPU cores
- integrated with basic image functionalities of **OpenCV**
- integrated with most common **LAPACK** routines

plans

- integration with **QT** to support visualization
- **CUDA** massively parallel implementation on GPU

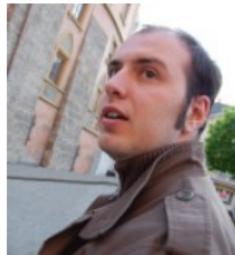
Credits



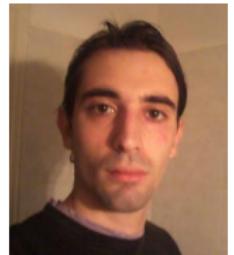
Yannis Kalantidis



Giorgos Tolias



Christos Varitimidis



Kimon Kontosis



Marios Phinikettos



Phivos Mylonas



Kostas Rapantzikos



Yannis Avrithis

project pages

<http://image.ntua.gr/iva/research>

VIRaL

<http://viral.image.ntua.gr>

datasets

<http://image.ntua.gr/iva/datasets>

thank you!