Asymmetric metric learning for knowledge transfer

Mateusz Budnik and Yannis Avrithis

Inria Rennes-Bretagne Atlantique

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asymmetric metric learning (AML)

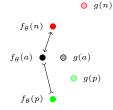
- instance-level image retrieval
- asymmetric testing: database represented by large network, queries by lightweight network on device, no re-indexing
- asymmetric metric learning: use asymmetric representations at training in teacher-student setup
- applies to both symmetric and asymmetric testing
- combines of knowledge transfer with supervised metric learning

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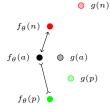
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symmetric

- labels used, teacher not used
- positive pairs of examples mutually attracted and negative pairs are repulsed in student space



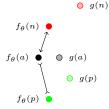
symmetric

• labels used, teacher not used $(f_{\theta}$: student, g: teacher)

Hadsell, Chopra, Lecun. CVPR 2006. Dimensionality reduction by learning an invariant mapping.

• contrastive $\ell_{\mathbf{C}}(a;\theta)$: independently, positive examples p close to anchor a, negative n farther from a by margin m in student space

$$\sum_{n \in N(a)} [s_{\theta}(a, n) - m]_{+} - \sum_{p \in P(a)} s_{\theta}(a, p)$$



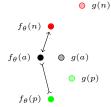
symmetric

- labels used, teacher not used $(f_{\theta}$: student, g: teacher)
- triplet $\ell_T(a; \theta)$: positive examples p closer to the anchor a than negative n by margin m in student space

$$\sum_{(p,n)\in L(a)} [s_{\theta}(a,n) - s_{\theta}(a,p) + m]_{+}$$

Wang, Song, Leung, Rosenberg, Wang, Philbin, Chen, Wu. CVPR 2014. Learning fine-grained image similarity with deep ranking. Budnik and Avrithis. CVPR 2021. Asymmetric Metric Learning for Knowledge Transfer.





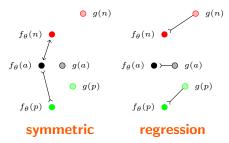
symmetric

- labels used, teacher not used $(f_{\theta}$: student, g: teacher)
- multi-similarity $\ell_{\mathrm{MS}}(a;\theta)$: positives p (negatives n) farthest from (nearest to) anchor a receive the greatest relative weight

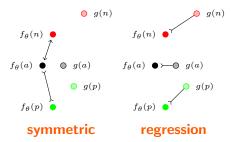
$$\frac{1}{\alpha} \log \left(1 + \sum_{p \in P(a)} e^{-\alpha(s_{\theta}(a,p)-m)} \right) + \frac{1}{\beta} \log \left(1 + \sum_{n \in N(a)} e^{\beta(s_{\theta}(a,n)-m)} \right)$$

Wang, Han, Huang, Dong, Scott. CVPR 2019. Multi-similarity loss with general pair weighting for deep metric learning. Budnik and Avrithis. CVPR 2021. Asymmetric Metric Learning for Knowledge Transfer.





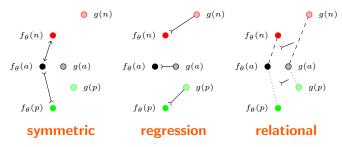
- labels not used, teacher used
- examples in student space attracted to corresponding examples in teacher space



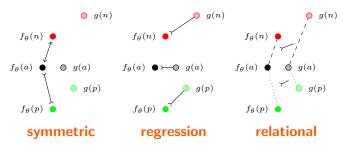
- labels not used, teacher used (f_{θ} : student, g: teacher)
- regression $\ell_R(a;\theta)$: representations of same example a by two models f_{θ}, q close to each other, where q is fixed

$$-s_{\theta}^{\text{asym}}(a, a) = -\sin(f_{\theta}(a), g(a))$$





- labels not used, teacher used
- pairwise / groupwise relations like distances, angles or ranks encouraged to be compatible in both spaces



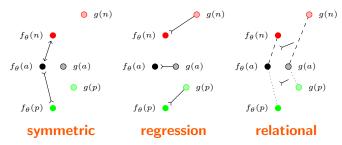
- labels not used, teacher used $(f_{\theta}$: student, g: teacher)
- relational distillation $\ell_{\text{RKD}}(a;\theta)$: measurements $\psi(\mathbf{a},\mathbf{x},\dots)$ of same examples (a,x,\dots) by two models f_{θ},g close to each other

$$\sum_{(x,\dots)\in U(a)^n} -\sin(\psi(f_{\theta}(a),f_{\theta}(x),\dots),\psi(g(a),g(x),\dots))$$

e.g. distance $\|\mathbf{a} - \mathbf{x}\|$, angle $\sin(\mathbf{a} - \mathbf{x}, \mathbf{a} - \mathbf{y})$; regression $\psi(\mathbf{a}) := \mathbf{a}$

Park, Kim, Lu, Cho. CVPR 2019. Relational knowledge distillation. Budnik and Avrithis. CVPR 2021. Asymmetric Metric Learning for Knowledge Transfer.



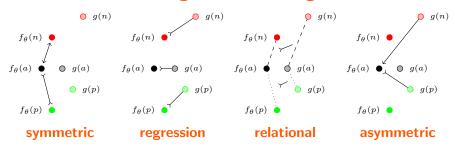


- labels not used, teacher used $(f_{\theta}$: student, g: teacher)
- DarkRank $\ell_{DR}(a;\theta)$: examples $y \in V(a,x)$ mapped farther from anchor a than x in teacher space do the same in student space:

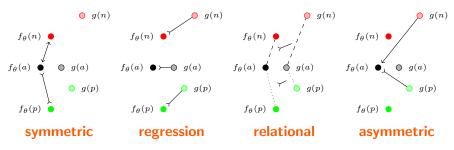
$$-\sum_{x \in U(a)} \left(s_{\theta}^{\text{sym}}(a, x) - \log \sum_{y \in V(a, x)} e^{s_{\theta}^{\text{sym}}(a, y)} \right)$$

Chen, Wang, Zhang. AAAI 2018. DarkRank: Accelerating deep metric learning via cross sample similarities transfer. Budnik and Avrithis. CVPR 2021. Asymmetric Metric Learning for Knowledge Transfer.





- both labels and teacher used
- anchors in student space attracted to positives and repulsed from negatives in teacher space



- both labels and teacher used $(f_{\theta}$: student, g: teacher)
- Asymmetric Metric Learning (AML): simply use

$$s_{\theta}^{\text{asym}}(a, x) := \sin(f_{\theta}(a), g(x))$$

with any supervised metric learning loss like $\ell_{\rm C}$, $\ell_{\rm T}$, $\ell_{\rm MS}$



best loss functions

• regression (Reg)

$$\ell_{\mathcal{R}}(a;\theta) := -s_{\theta}^{\text{asym}}(a,a) = -\sin(f_{\theta}(a), g(a))$$

asymmetric contrastive (Contr)

$$\ell_{\rm C}(a;\theta) := \sum_{n \in N(a)} [s_{\theta}(a,n) - m]_{+} - \sum_{p \in P(a)} s_{\theta}(a,p)$$

asymmetric contrastive + regression (Contr⁺)

$$\ell_{C^+}(a;\theta) := \sum_{n \in N(a)} [s_{\theta}(a,n) - m]_+ - \sum_{p \in P(a)} s_{\theta}(a,p) - s_{\theta}(a,a)$$

best loss functions

• regression (Reg)

$$\ell_{\mathbf{R}}(a;\theta) := -s_{\theta}^{\text{asym}}(a,a) = -\sin(f_{\theta}(a), g(a))$$

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$$\ell_{C^+}(a;\theta) := \sum_{n \in N(a)} [s_{\theta}(a,n) - m]_+ - \sum_{p \in P(a)} s_{\theta}(a,p) - s_{\theta}(a,a)$$

test set: revisited Oxford and Paris



- 11 + 11 landmarks, 70 + 70 queries, 5k + 6k images, easy/hard
- 1M distractor images
- performance measured by mAP: positive ranked first

Radenovic, Iscen, Tolias, Avrithis, Chum. CVPR 2018. Revisiting Oxford and Paris: Large-Scale Image Retrieval Benchmarking. Budnik and Avrithis. CVPR 2021. Asymmetric Metric Learning for Knowledge Transfer.



training set: SfM120k (positives)



- camera position (closest to query)
- number of inliers (co-observed 3D points with query)
- according to SIFT descriptors



training set: SfM120k (negatives)



- k-nearest neighbors from non-matching clusters
- at most one image per cluster
- according to learned descriptors



network models

Network	Teacher	d	GFLOPS	Param(M)
ResNet101		2048	42.85	42.50
EfficientNet-B3	ResNet101	1536 2048	5.36 6.26	10.70 13.84

• teacher: ResNet101 (RN101)

• student: EfficientNet-B3 (EN-B3), dimensions d adapted to teacher

• 7× less FLOPS

• 3× less parameters



Stu	d	ТЕА	Lab	MINING	Asym	Loss	Med ROxf		HA ROxf	
RN101 EN-B3	2048 512 2048		√ √ √	hard hard hard		Contr Contr Contr	65.4 53.8 59.6	76.7 70.9 75.1	40.1 26.2 33.3	55.2 46.0 51.9
EN-B3	2048	RN101	√ √ √	hard hard hard hard	√ √ √	Contr ⁺ Contr Triplet MS	66.8 66.3 39.5 39.9	77.1 77.4 69.4 69.7	42.5 41.3 11.6 11.7	55.5 55.5 45.8 46.2
				random random	√	Reg RKD DR	64.9 56.3 40.3	74.4 73.0 69.9	40.5 30.5 11.8	52.4 50.4 46.4

Contr, Contr⁺: student beats teacher



Reg: second best, slightly below teacher

everything else fails (worse than student alone)

Stu	d	Теа	LAD	Mining	Δgvm	Loss	Mei	OIUM	Hard	
510	a	IEA	LAD	MINING	лзім	LOSS	$\mathcal{R}Oxf$	$\mathcal{R}Par$	$\mathcal{R}Oxf$	$\mathcal{R}Par$
RN101	2048		\checkmark	hard		Contr	65.4	76.7	40.1	55.2
EN-B3	512		\checkmark	hard		Contr	53.8	70.9	26.2	46.0
EIN-D3	2048		\checkmark	hard		Contr	59.6	75.1	33.3	51.9
			✓	hard	✓	$Contr^+$	66.8	77.1	42.5	55.5
			\checkmark	hard	\checkmark	Contr	66.3	77.4	41.3	55.5
EN-B3	2048	RN101	\checkmark	hard	\checkmark	Triplet	39.5	69.4	11.6	45.8
			\checkmark	hard	\checkmark	MS	39.9	69.7	11.7	46.2
					√	Reg	64.9	74.4		52.4
				random		RKD	56.3	73.0	30.5	50.4
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Mateusz

Yannis

paper

https://arxiv.org/abs/2006.16331

code

https://github.com/budnikm/asymmetric_metric_learning

more

https://avrithis.net