

Solve the following logarithmic equations.

$$(1) \quad x^2 + 2x + 1 = 0$$

$$(2) \quad 2\log(x - 1) = \log(x + 1)$$

$$(3) \quad \log_5(x + 1) + \log_5(x - 3) = 1$$

$$(4) \quad \log_2(x + 1) = \log_2(2 - x) + 1$$

$$(5) \quad (1 + \log_2 x) \cdot \log_2 x = 2$$

$$(6) \quad (\log_3 x)^2 - 5\log_3 x + 6 = 0$$

$$(7) \quad (\log_2 x)^2 = \log_2 x^2 + 3$$

$$(8) \quad 2\log_2 x - 3\log_x 2 + 5 = 0$$