

Solve the following logarithmic equations.

$$(1) \quad 2\log(x-1) = \log(x+1)$$

$$\log_2(x-1) + \log_2(x+2) = 2$$

$$\log_2(x-1)(x+2) = 2$$

$$(x-1)(x+2) = 4$$

$$x^2 + x - 6 = 0$$

$$(x+3)(x-2) = 0$$

$$x = -3, 2$$

Since  $x > 0$ ,

$$x-1 > 0, \text{ or } x+2 > 0$$

which results to  $x > 1$

$$(2) \quad \log_5(x+1) + \log_5(x-3) = 1$$

$$(3) \quad \log_2(x+1) = \log_2(2-x) + 1$$

$$(4) \quad (1 + \log_2 x) \cdot \log_2 x = 2$$

$$(5) \quad (\log_3 x)^2 - 5\log_3 x + 6 = 0$$

$$(6) \quad (\log_2 x)^2 = \log_2 x^2 + 3$$

$$(7) \quad 2\log_2 x - 3\log_x 2 + 5 = 0$$