Solve the following logarithmic equations.

which results to x > 1

$$(1) \quad 2log(x-1) = log(x+1)$$

$$log_2(x-1) + log_2(x+2) = 2$$

$$log_2(x-1)(x+2) = 2$$

$$(x-1)(x+2) = 4$$

$$x^2 + x - 6 = 0$$

$$(x+3)(x-2) = 0$$

$$x = -3, 2$$
Since x > 0,
$$x-1 > 0, \text{ or } x+2 > 0$$

(2)
$$log_5(x+1) + log_5(x-3) = 1$$

(3) $log_2(x+1) = log_2(2-x) + 1$

(4)
$$(1 + log_2 x) \cdot log_2 x = 2$$

 (5) $(log_3 x)^2 - 5log_3 x + 6 = 0$

(6)
$$(log_2x)^2 = log_2x^2 + 3$$
 (7) $2log_2x - 3log_x2 + 5 = 0$