

Solve the following logarithmic equations.

$$(1) \log_2(x-1) + \log_2(x+2) = 2 \qquad (2) \quad 2\log(x-1) = \log(x+1)$$

$$(3) \log_5(x+1) + \log_5(x-3) = 1 \qquad (4) \log_2(x+1) = \log_2(2-x) + 1$$

$$(5) \quad (1 + \log_2 x) \cdot \log_2 x = 2$$

$$(6) \quad (\log_3 x)^2 - 5\log_3 x + 6 = 0$$

$$(7) \quad (\log_2 x)^2 = \log_2 x^2 + 3$$

$$(8) \quad 2\log_2 x - 3\log_x 2 + 5 = 0$$