

Electrical and Electronic Circuits

chapter 13. Operational Amplifier

Afarghadan@aut.ac.ir





Objectives of the Lecture

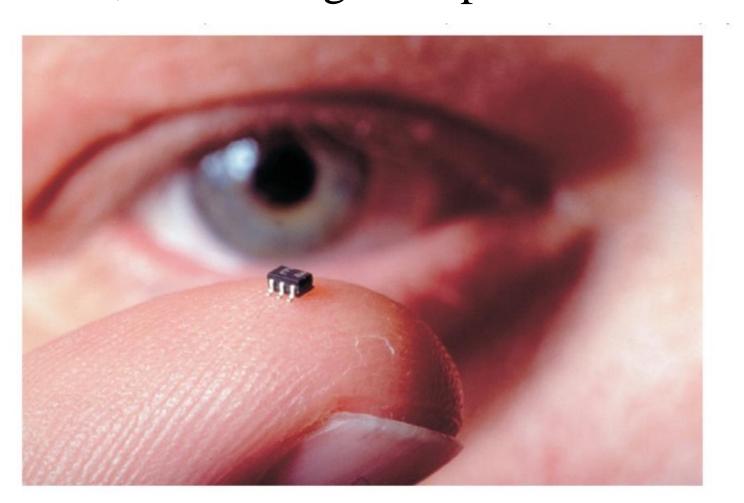
- > Introduction to Operational Amplifiers
 - Precise Model of Operational Amplifiers
 - > Ideal Model
 - > Applications of Operational Amplifiers
 - > Inverting Amplifier
 - Non-Inverting Amplifier
 - Voltage Follower (Buffer)
 - Multi-Stage Amplifier
 - ➤ Ideal Voltage and Current Sources
- Comparator Circuit
- > Several Examples

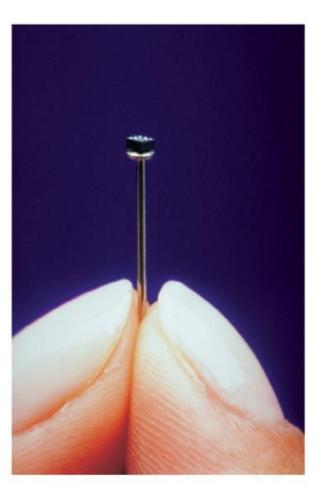


Operational Amplifier (Op-Amp)

- The **Operational Amplifier (Op-Amp)** is an integrated circuit (IC) widely utilized as an amplifier in various applications.
- ➤ Its origins date back to the 1940s when it was employed in analog computational circuits for constructing adders, sub tractors, and analog multipliers.

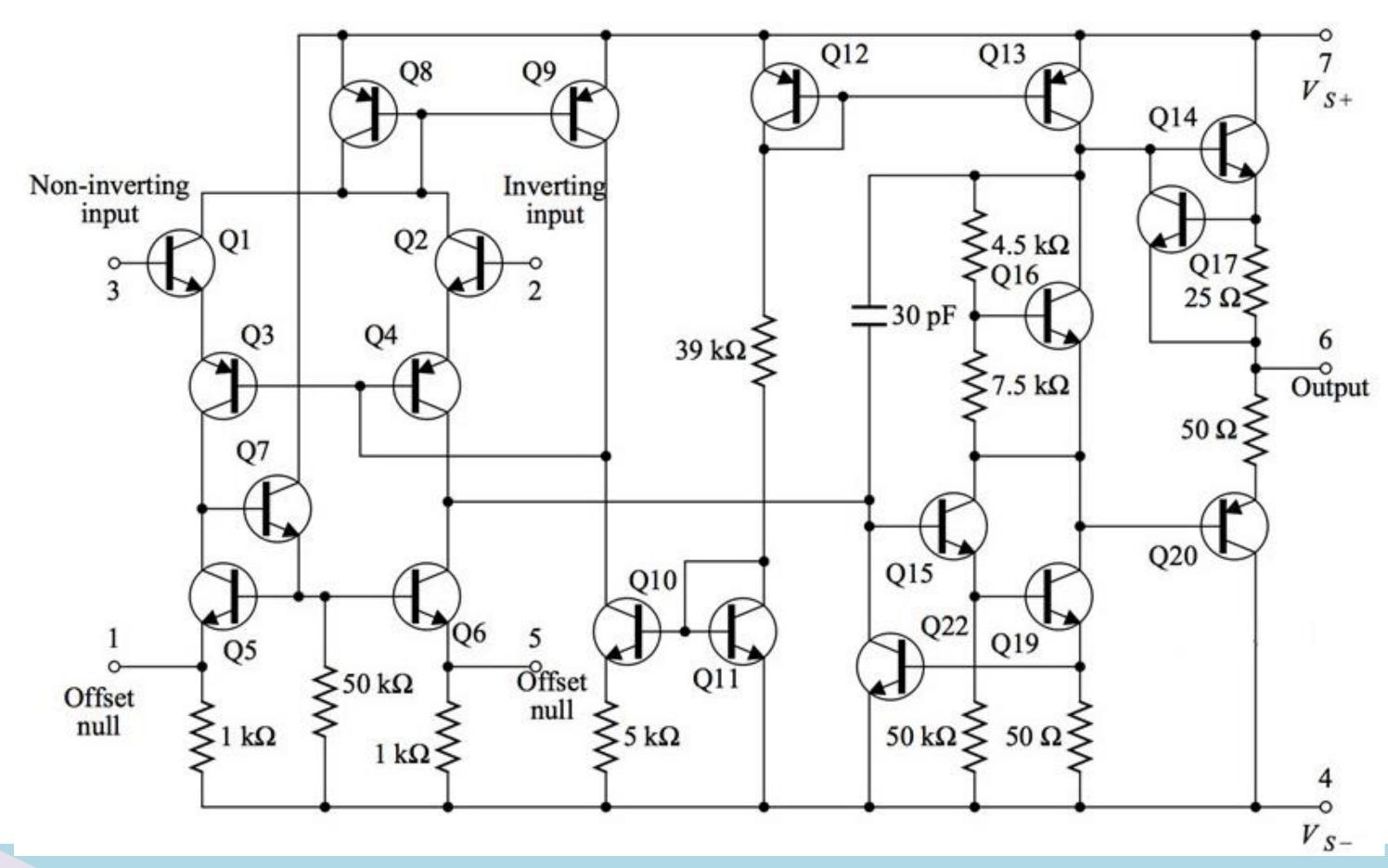








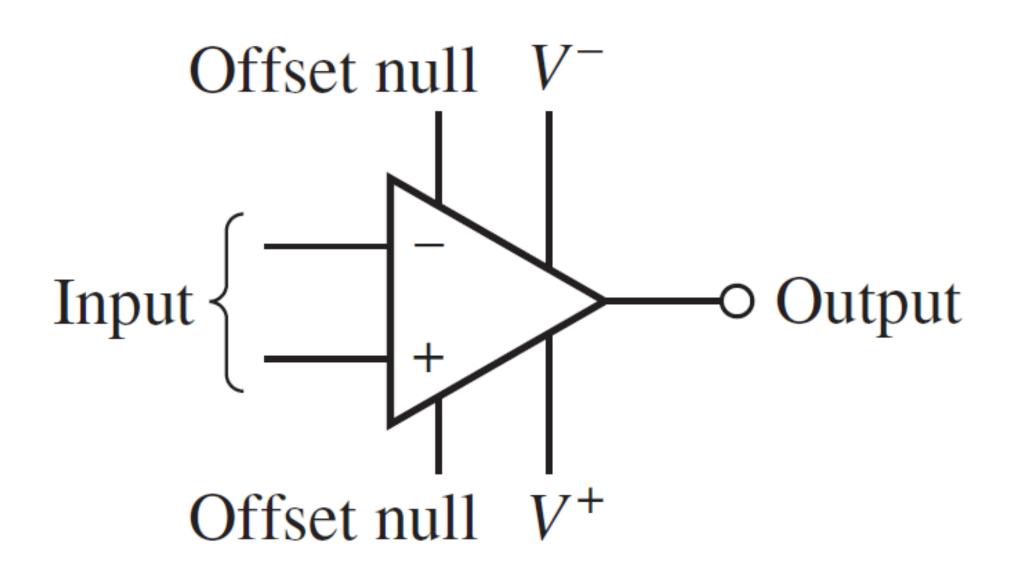
The Internal Circuit of a Typical Operational Amplifier



Nonlinear Behavior of the Diode

An operational amplifier (Op-Amp) is generally represented by the following symbol and includes the following pins:

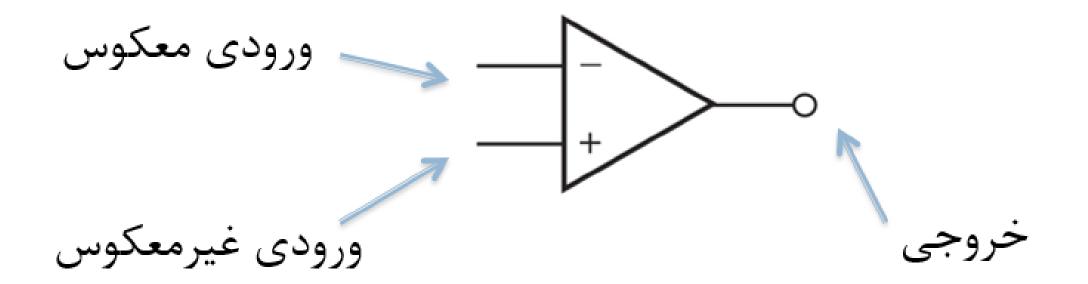
- > Input Pins: Input
- > Output Pin: Output
- \triangleright Power Supply Pins: V^+, V^-
- > Offset Adjustment Pins: Offset





Op-Amp Symbol

- ✓ Let us focus on the **input** and **output pins**, assuming the other pins are connected to appropriate voltage levels.
- ✓ An operational amplifier functions as a **differential amplifier**, meaning it amplifies the difference between its input signals.



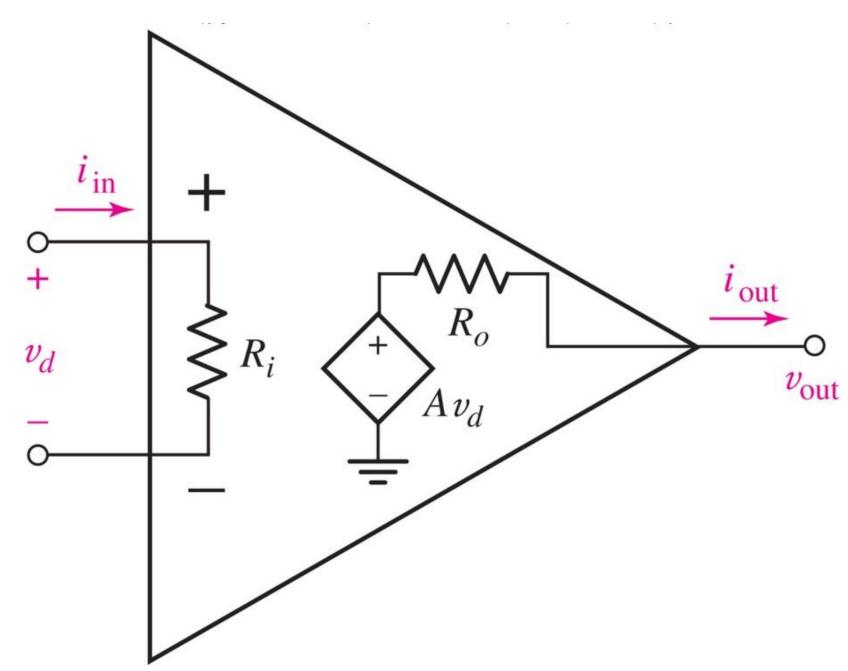


Precise Model of an Op-Amp

- A circuit that operates as a voltage amplifier can be modelled using the following
- This model includes:

equivalent circuit.

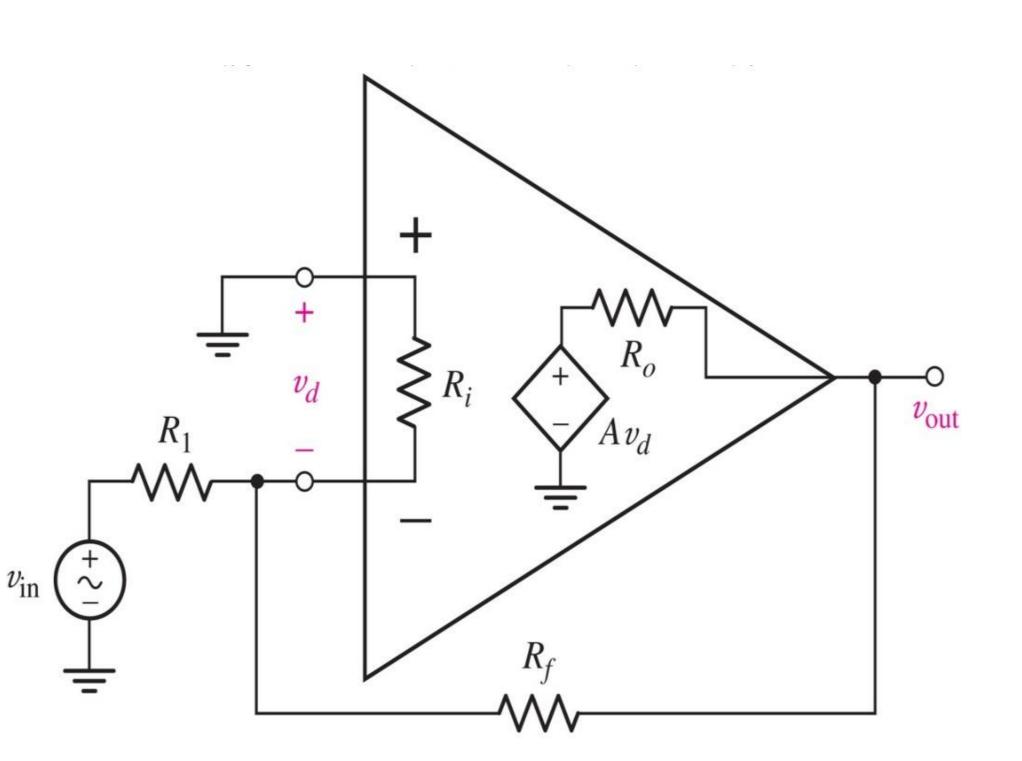
- \triangleright Input Resistance (R_i)
- \triangleright Output Resistance (R_o)
- > Open-Loop Gain (A)



Example: Using the Precise Model to Analyse an Inverting Amplifier

✓ In the circuit below, what is the gain of the amplifier?

>
$$KCL_1$$
: $\frac{-v_d - v_{in}}{R_1} + \frac{-v_d - v_{out}}{R_f} + \frac{-v_d}{R_i} = 0$



Example: Using the Precise Model to Analyse an Inverting Amplifier

✓ By solving the system of equations and eliminating v_d , we obtain:

Example Solution for the Inverting Amplifier Using LM741 Specifications

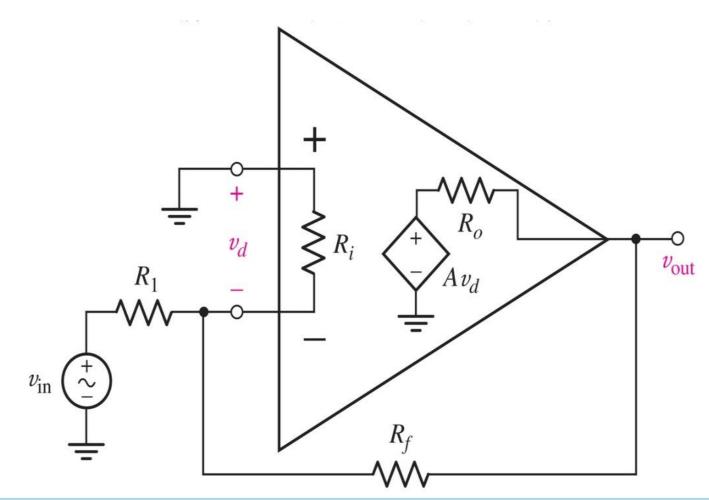
$$> A = 200000$$

$$> R_i = 2M\Omega$$

$$> R_o = 75\Omega$$

$$ightharpoonup$$
 If $R_f = 47$ and $R_1 = 4.7$

$$\triangleright$$
 Then: $A_v = -9.999$



Advantages of Using an Op-Amp as a Voltage Amplifier

- ✓ **High Input Resistance**:(in the range of mega-ohms to tera-ohms)
 - > To ensure that the maximum voltage of the source is applied across its input.
- ✓ Low Output Resistance:(in the range of a few ohms to a few tens of ohms)
 - > to ensure that the entire output voltage of the amplifier is delivered to the load.
- ✓ **Adjustable Gain**:(achieved by applying feedback resistance):
 - As observed in the circuit shown, provided that A is sufficiently large, the gain of the amplifier can be approximated with high accuracy as $Av \approx \frac{R_f}{R_s}$.



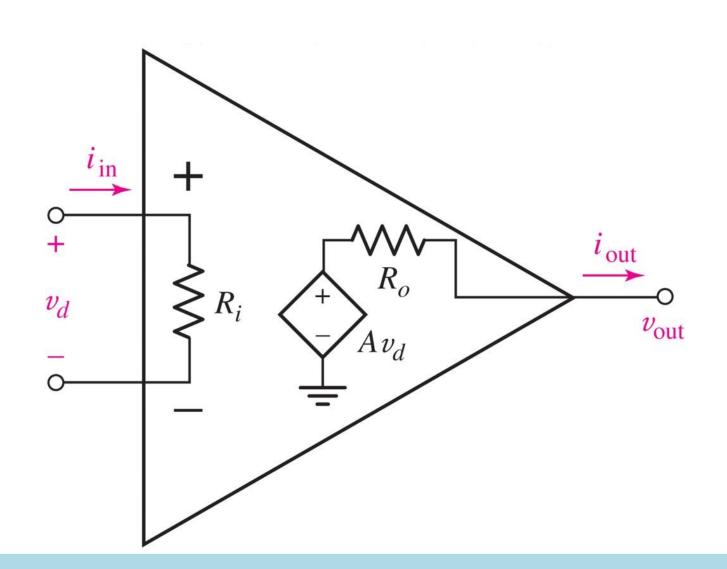
Ideal Model

In the ideal case, when $A=\infty$, $R_i=\infty$, and $R_o=0$, the behaviour of the operational amplifier can be described as follows:

 \triangleright Since v_{out} has a finite value (it cannot exceed the supply voltage),

$$v_d = \frac{v_{out}}{A} \approx 0$$
.

 \triangleright As a result, $i_{in} \approx 0$.



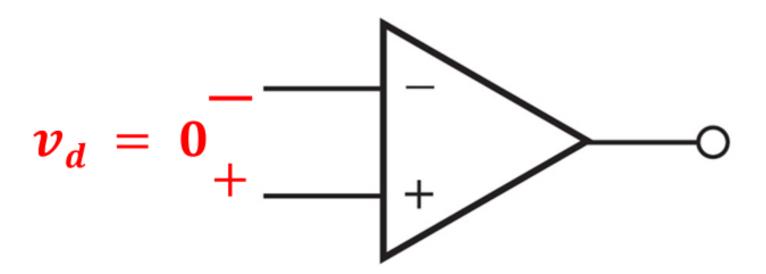
Ideal Model

Rules of the Ideal Model:

1. No current flows through the input terminals.

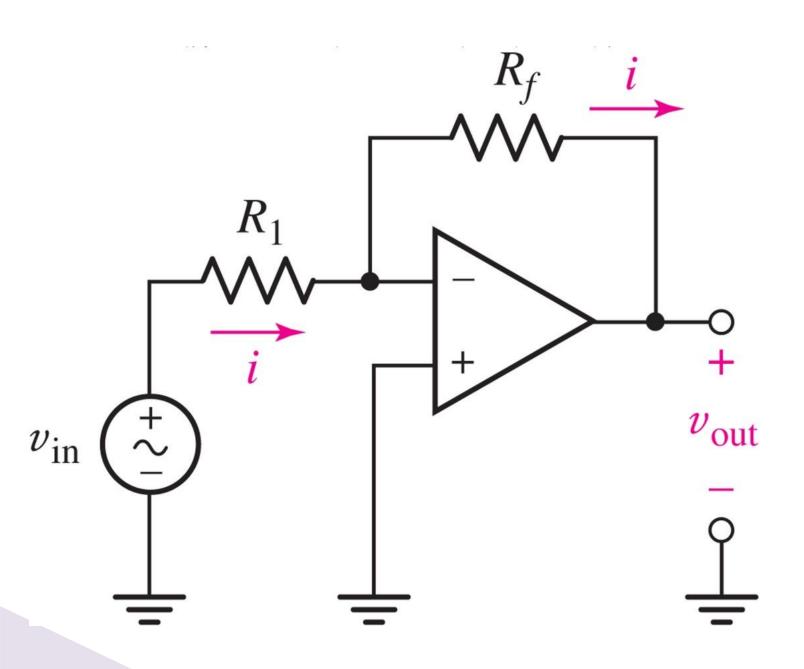
$$i = 0$$
 $i = 0$
 $+$

2. The voltage difference between the two input terminals is zero.



Inverting Amplifier

✓ By applying KVL and using the rules of the ideal operational amplifier, we have:

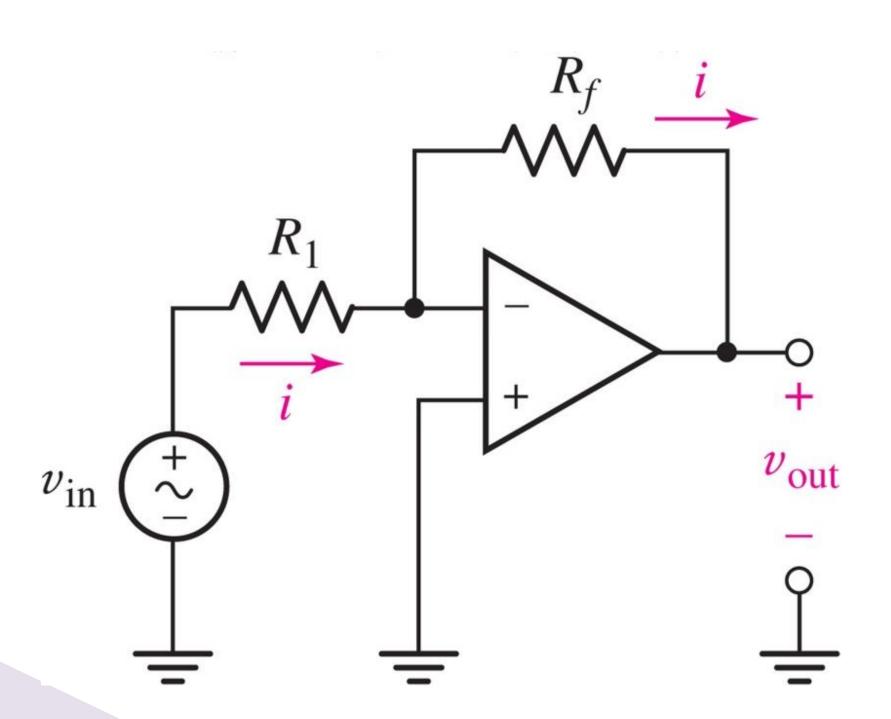


$$v_{out} = -\frac{R_f}{R_1}v_{in}$$

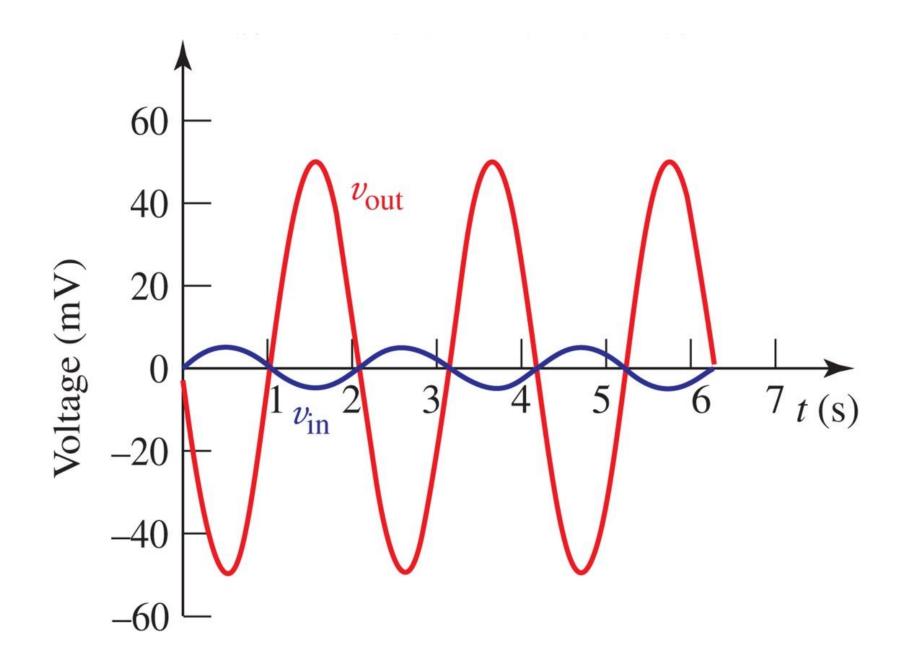


Example

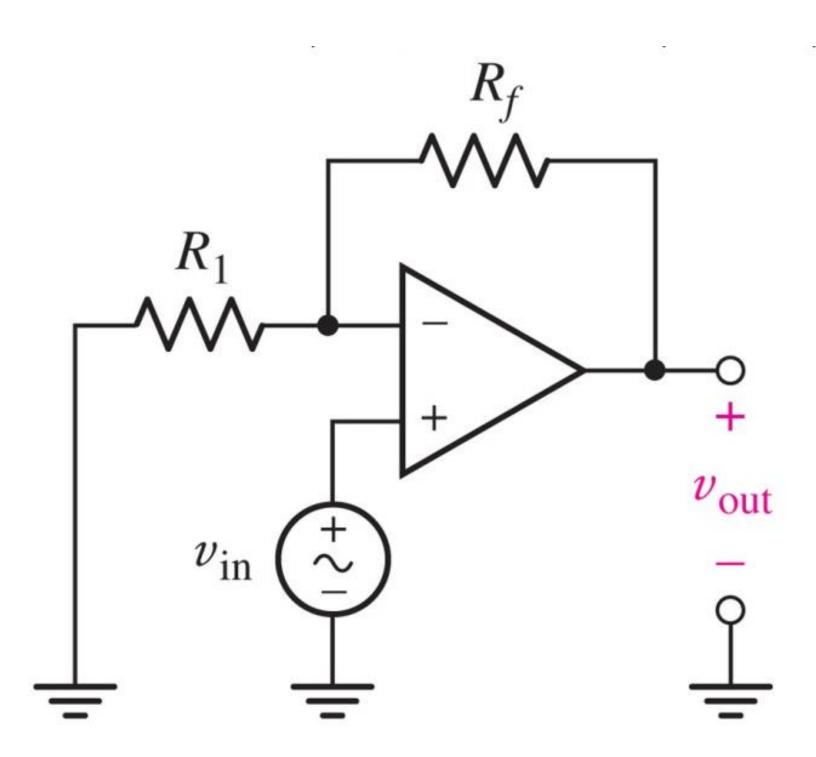
• $v_{in}(t) = 5\sin 3t \ mV$, $R_f = 47K\Omega$, $R_1 = 4.7K\Omega$



$$v_{out}(t) = -50 \sin 3t \, mV$$

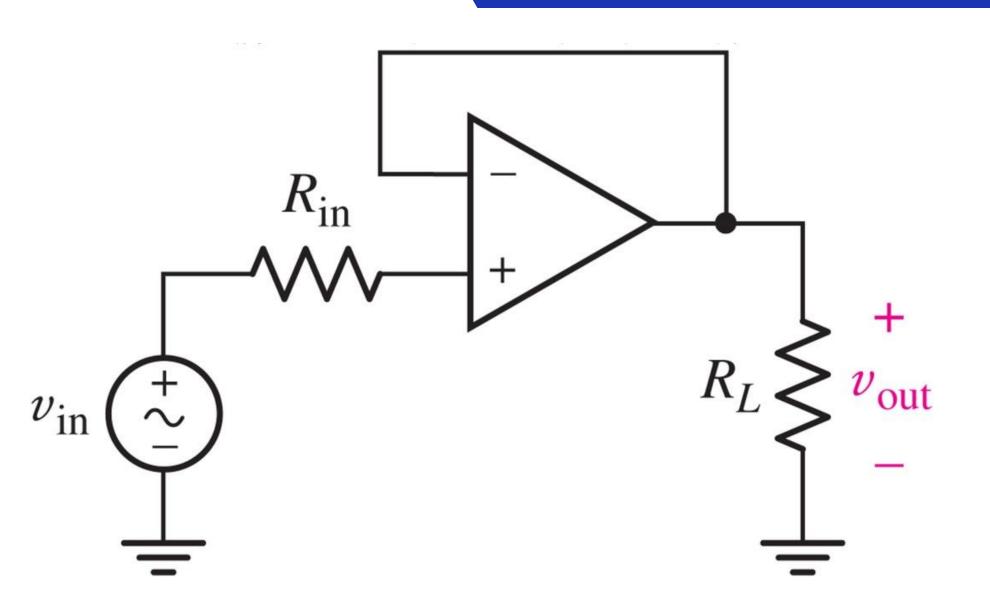


Non-Inverting Amplifier



$$v_{out} = \left(1 + \frac{R_f}{R_1}\right) v_{in}$$

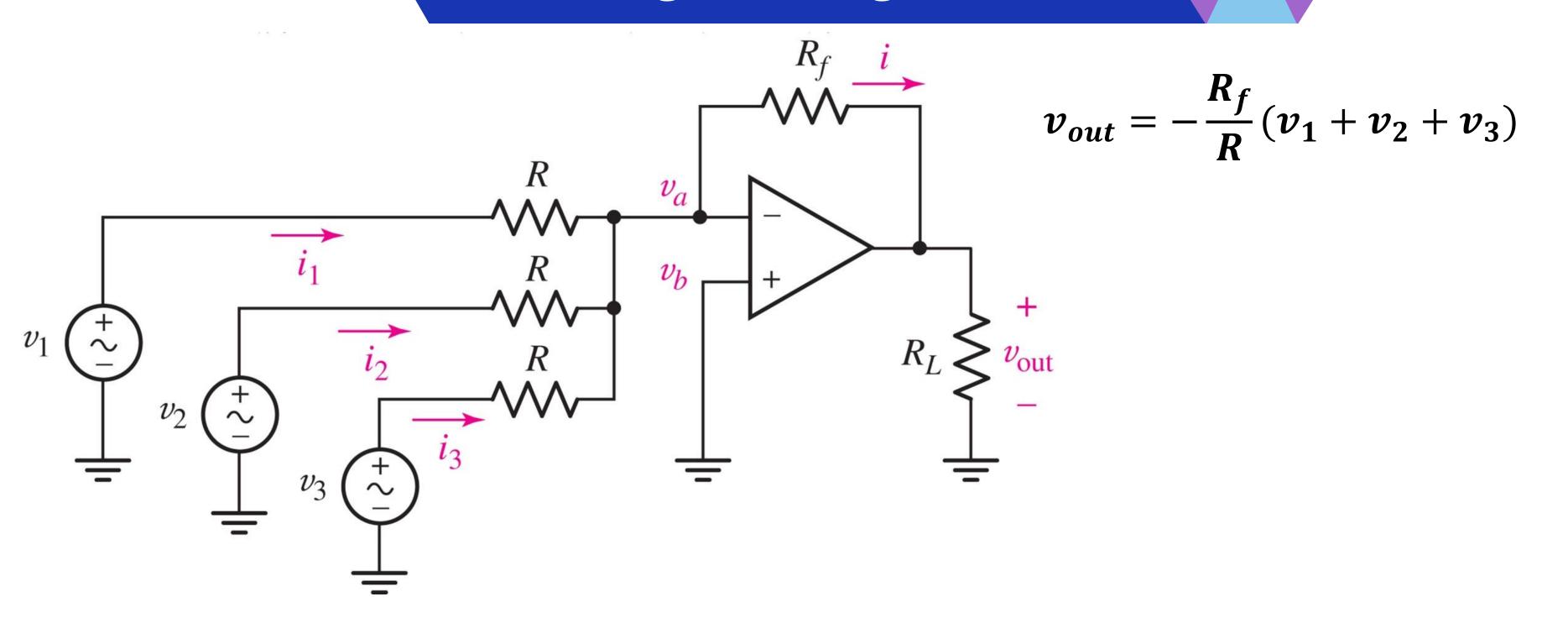
Voltage Follower (Buffer)



$$v_{out}(t) = vin(t)$$

- 1. The output voltage of the buffer is independent of the load resistance (R_L) . The buffer can supply the required current to maintain a constant output voltage, even if R_L changes.
- 2. This circuit eliminates the effect of the source's input resistance by presenting a very high input resistance to the source and a very low output resistance to the load.

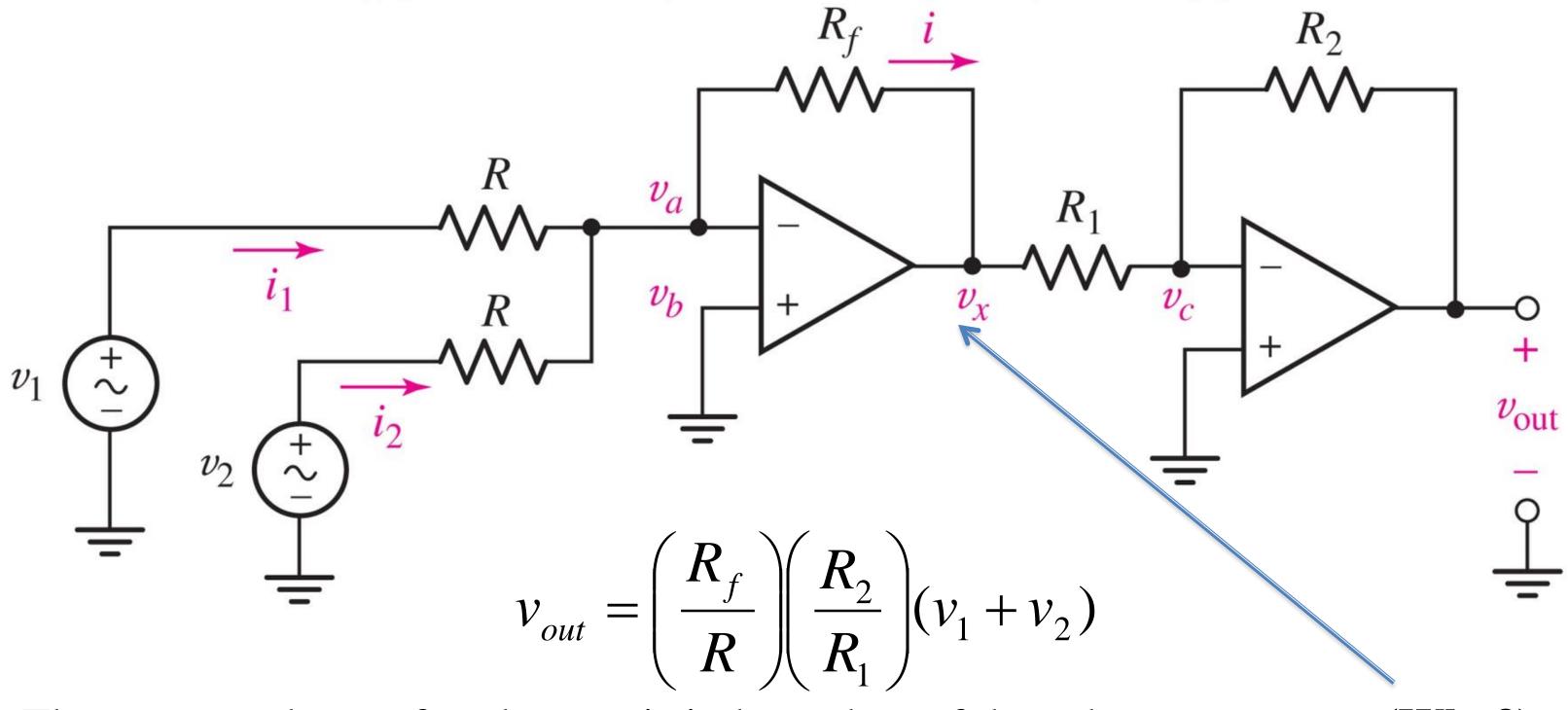
Analog Summing Circuit



 \checkmark This circuit performs the addition of input signals and amplifies the result by a factor of $-\frac{R_f}{R}$.



Cascading Multiple Operational Amplifiers

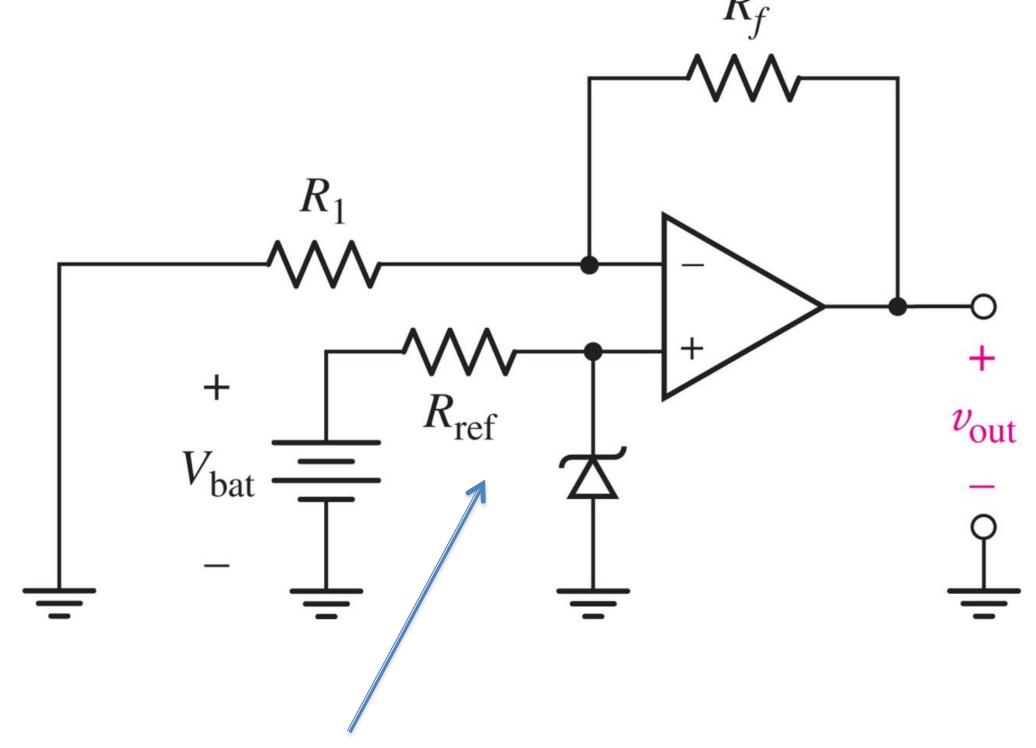


- ✓ The output voltage of each stage is independent of the subsequent stage. (Why?)
- ✓ As a result, **Op-Amp** can be cascaded without any alteration in their individual gains.



Op-Amp as an Ideal Voltage Source

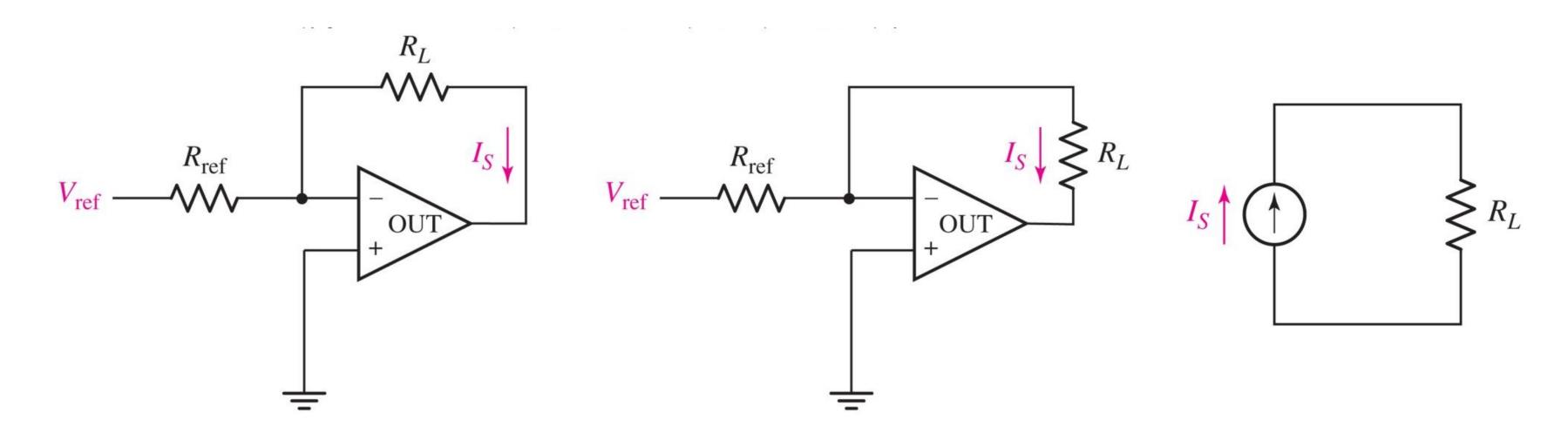
$$v_{out} = \left(1 + \frac{R_f}{R_1}\right) V_Z$$



This circuit resembles the voltage regulator using a Zener diode, which we have encountered before.



Op-Amp as an Ideal Current Source



 \triangleright Using a reference voltage V_{ref} and a resistor V_{ref} , an ideal current source can be constructed with a current:

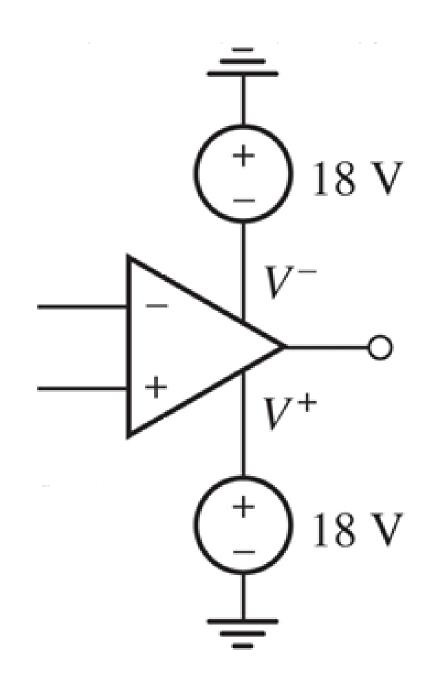
$$I_S = rac{V_{ref}}{R_{ref}}$$

 \triangleright This current is independent of the load resistance R_L ,



Power Supplies for Op-Amp

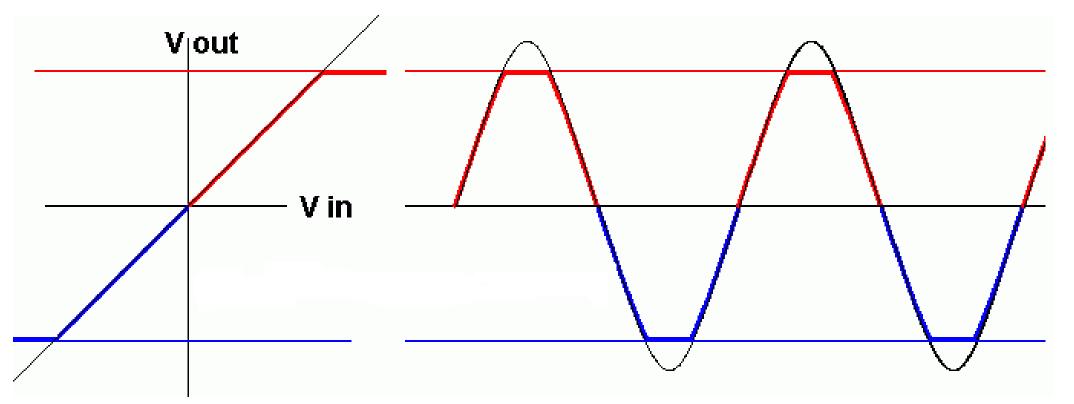
- An operational amplifier requires power to function and perform amplification. Therefore, it must be connected to a power supply.
- Typically, equal and opposite voltage values are applied to the V^+ and V^- terminals. These voltage levels usually range between $\pm 5 \text{V}$ and $\pm 24 \text{V}$.
- The ground of the power supplies must be connected to the input and output ground reference of the circuit to ensure proper operation and signal integrity.





Output Saturation

- ✓ If the input signal is such that the amplified output exceeds V^+ or falls below V^- , the output will saturate.
- ✓ In this state, the output voltage remains clamped at V^+ or V^- , depending on the direction of the input signal.



The output signal enters saturation and becomes clipped

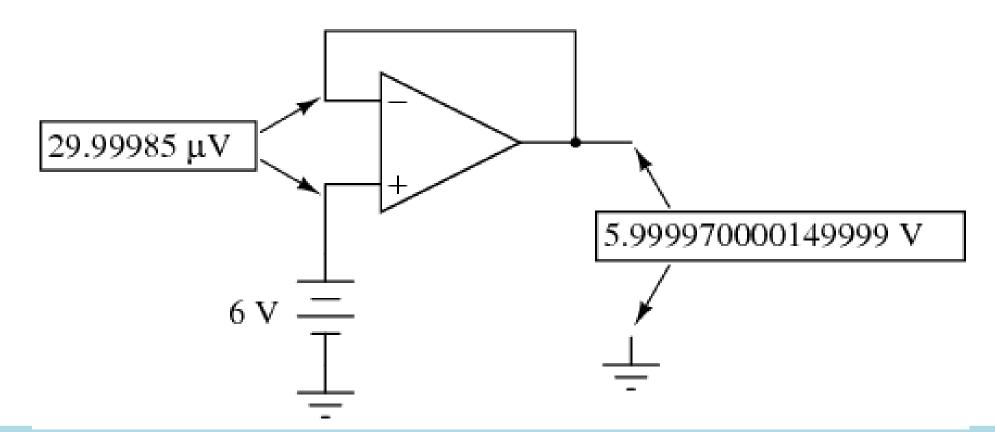


Role of Negative Feedback

- The role of negative feedback is to transform a large and undefined gain into a fixed, controlled gain.
- ➤ Why Don't We Apply Feedback to the Positive Terminal?

$$v_+ \uparrow \rightarrow v_d \uparrow v_{out} = Av_d \rightarrow v_{out} \uparrow \rightarrow v_- \uparrow \rightarrow v_d \downarrow \dots$$

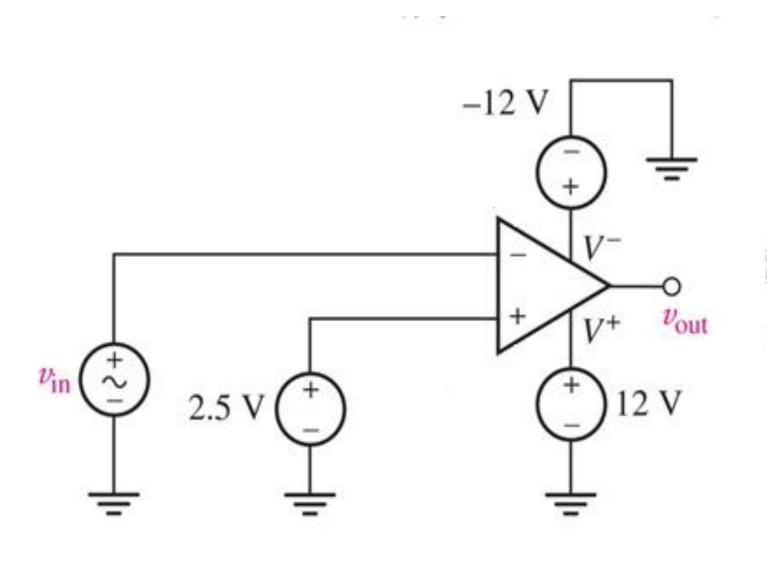
 \succ Thus, the negative feedback stabilizes the operation by keeping v_d close to zero



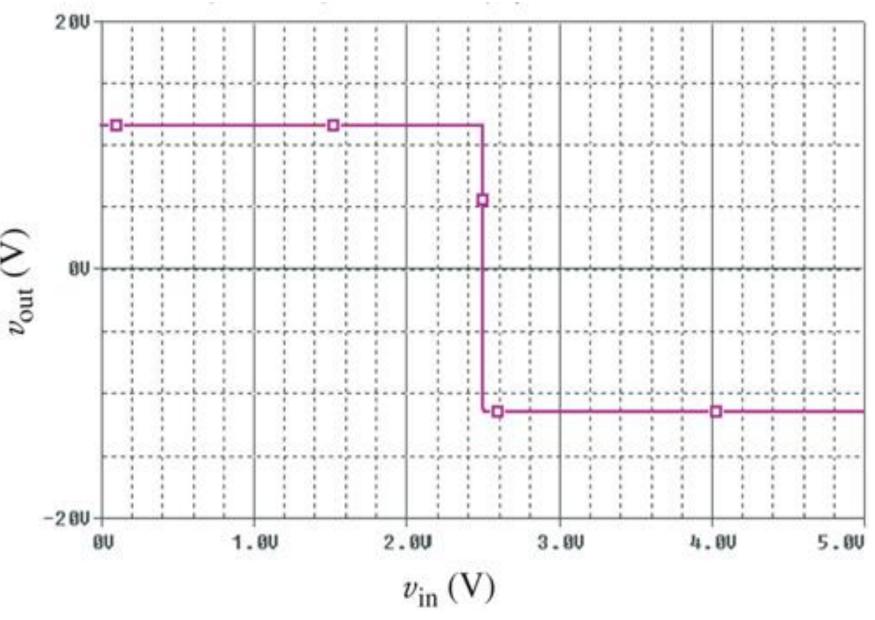


Voltage Comparator

An operational amplifier can be used as a voltage comparator when operated in open-loop configuration (without feedback). (12 $v_{in} < 2.5$)

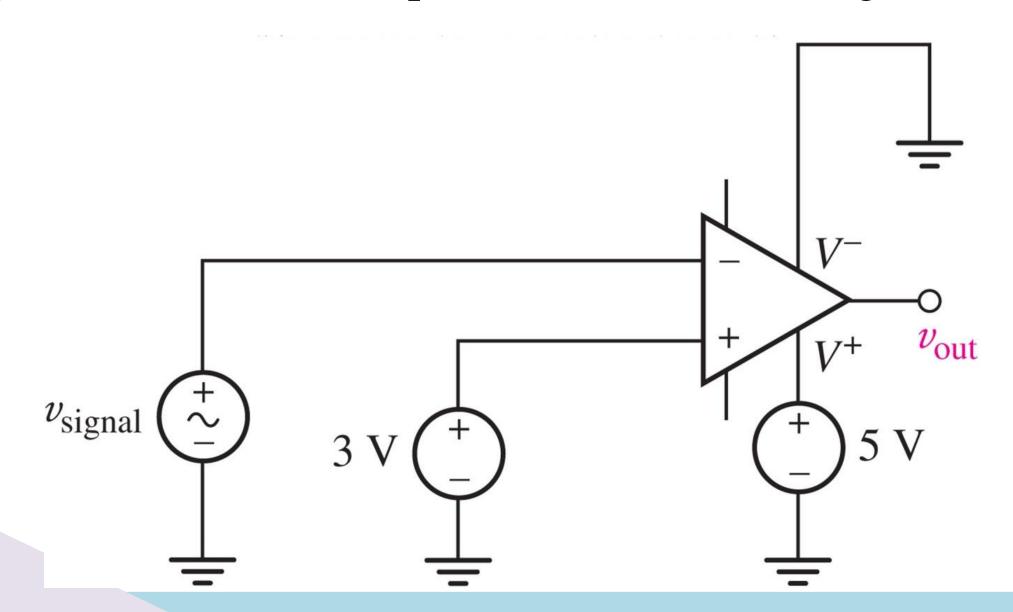


$$v_{out} = egin{cases} 12 & v_{in} < 2.5 \\ -12 & v_{in} > 2.5 \end{cases}$$



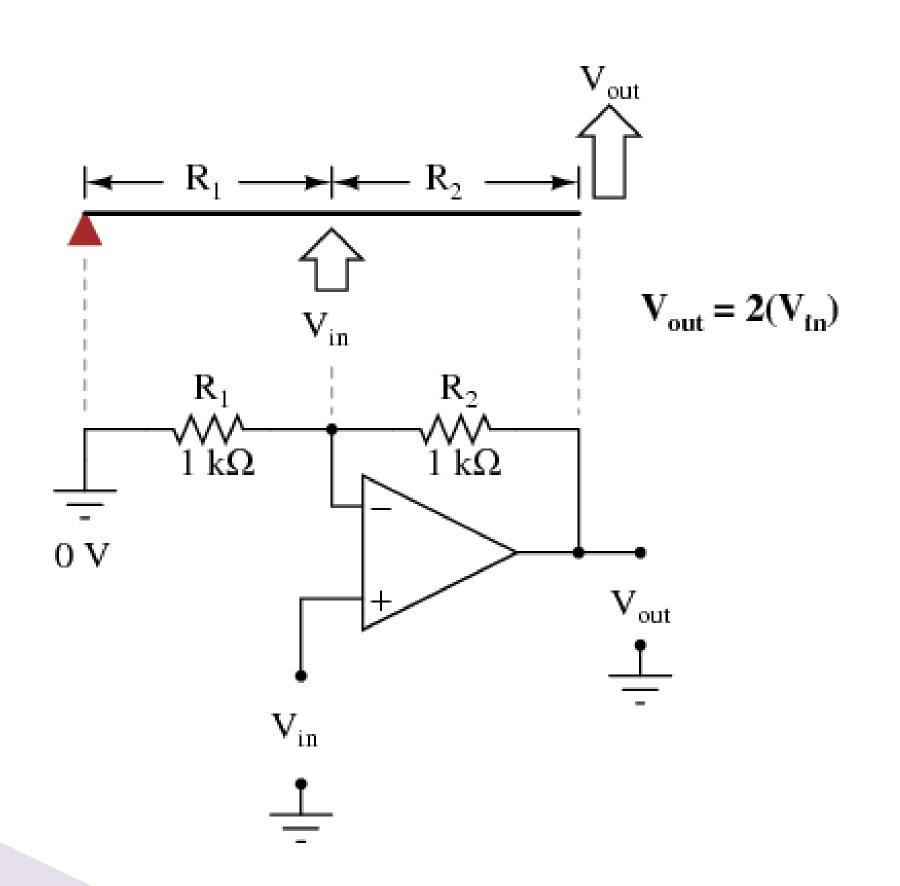
Example

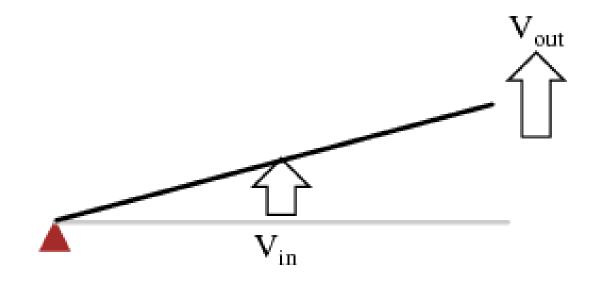
Assume we have a temperature sensor that generates a voltage ranging from 0 to 5 volts for temperatures between 0 and 100 degrees Celsius. Design a circuit that provides a logical output of 1 when the temperature is below 60 degrees.

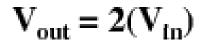


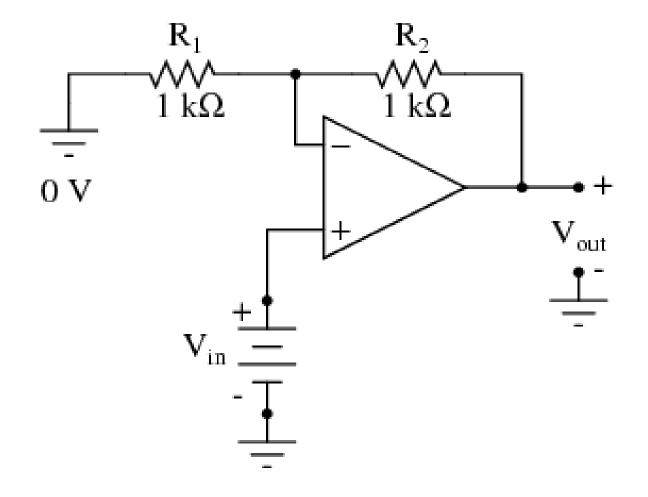


Similarity of Non-Inverting Amplifier to a Lever

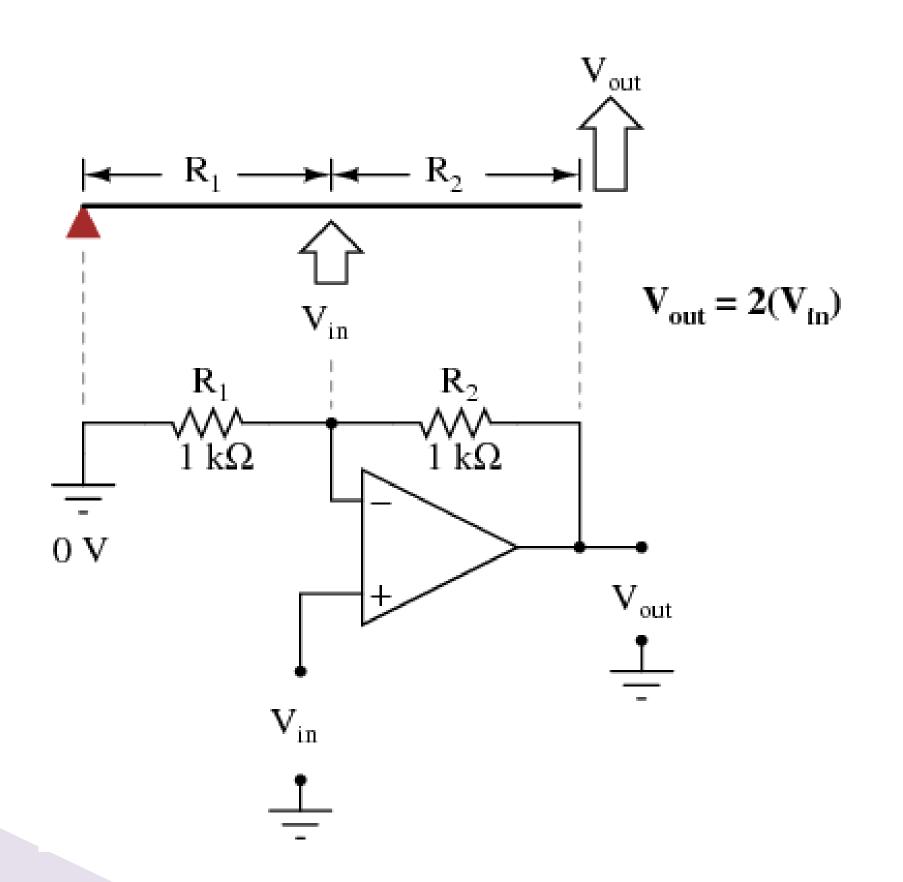


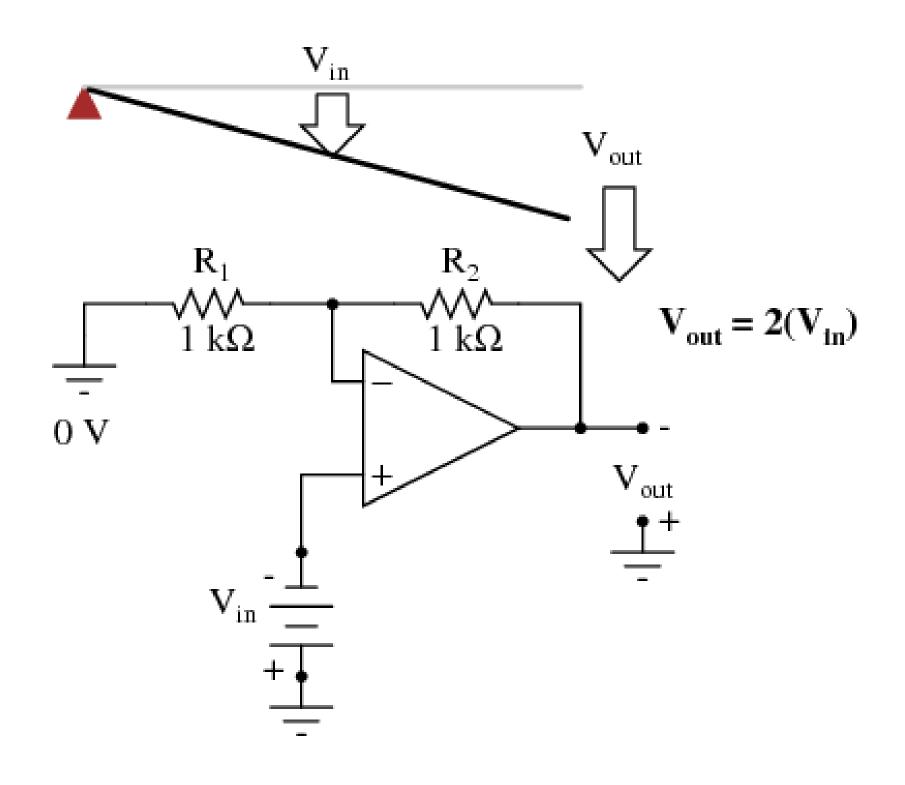




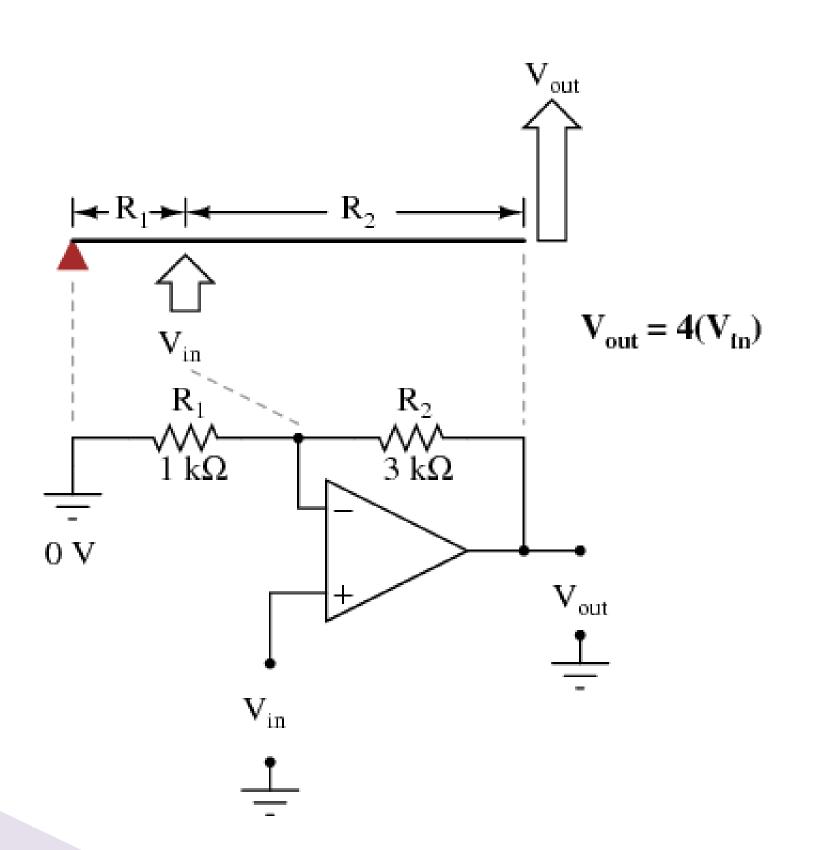


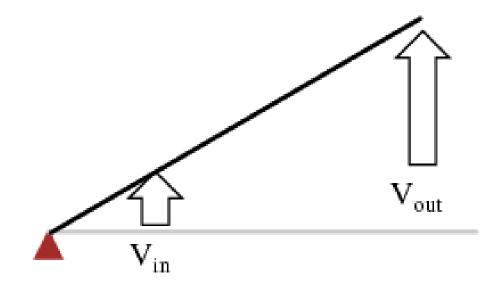
Similarity of Non-Inverting Amplifier to a Lever



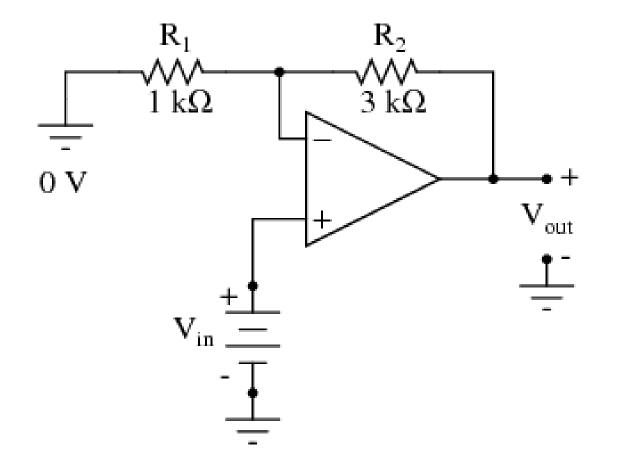


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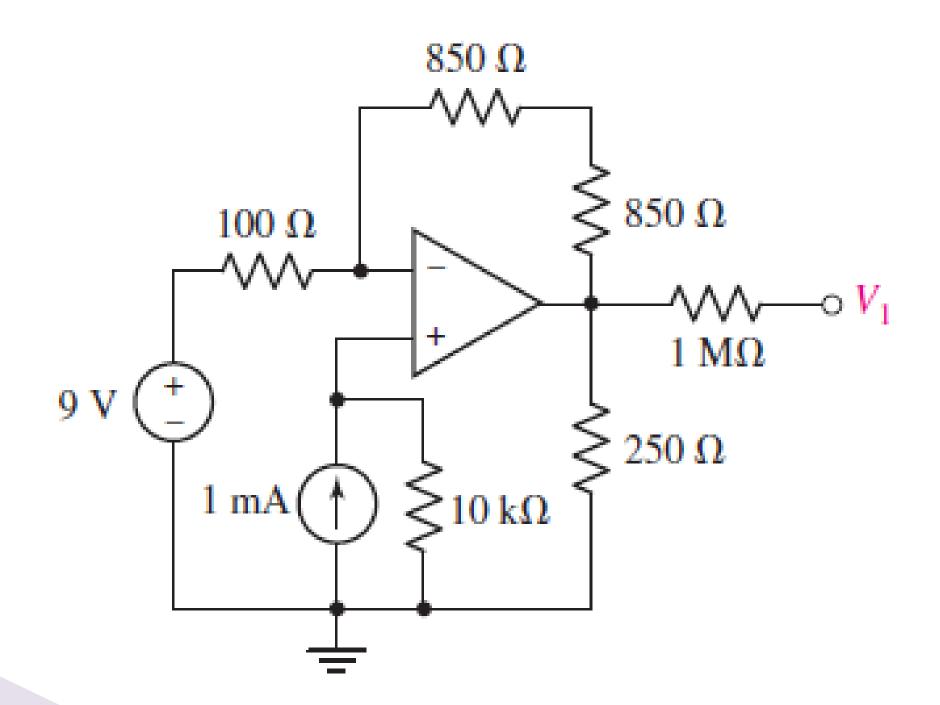




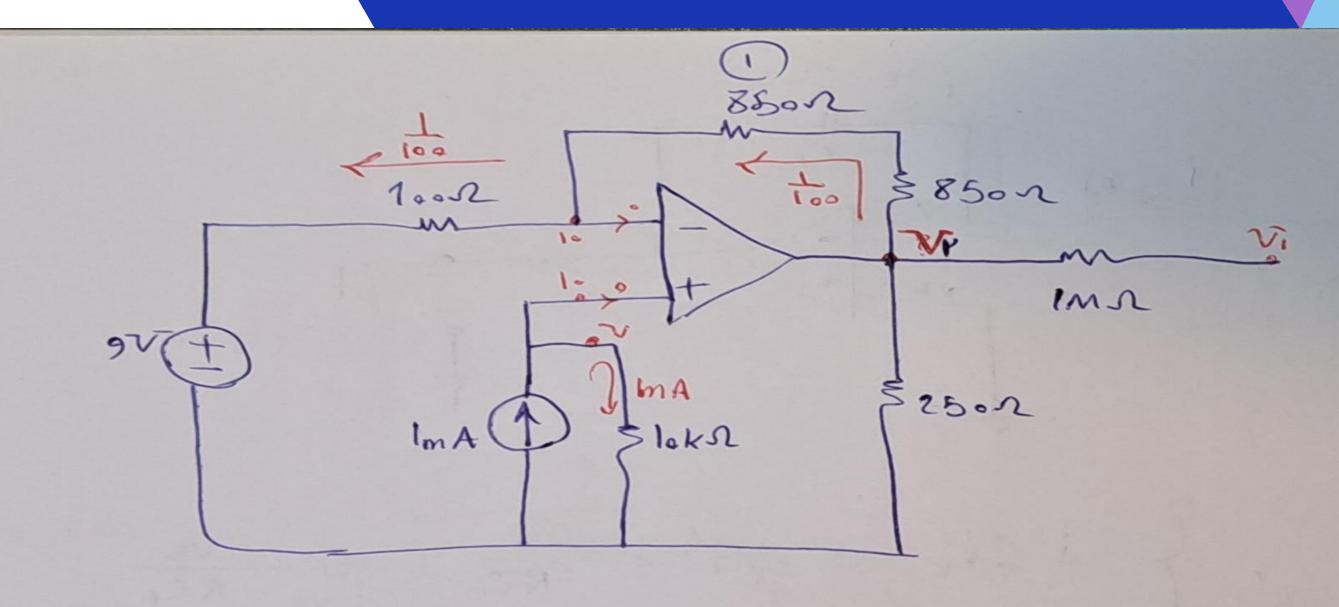
$$V_{out} = 4(V_{in})$$



$$V_1$$
=?



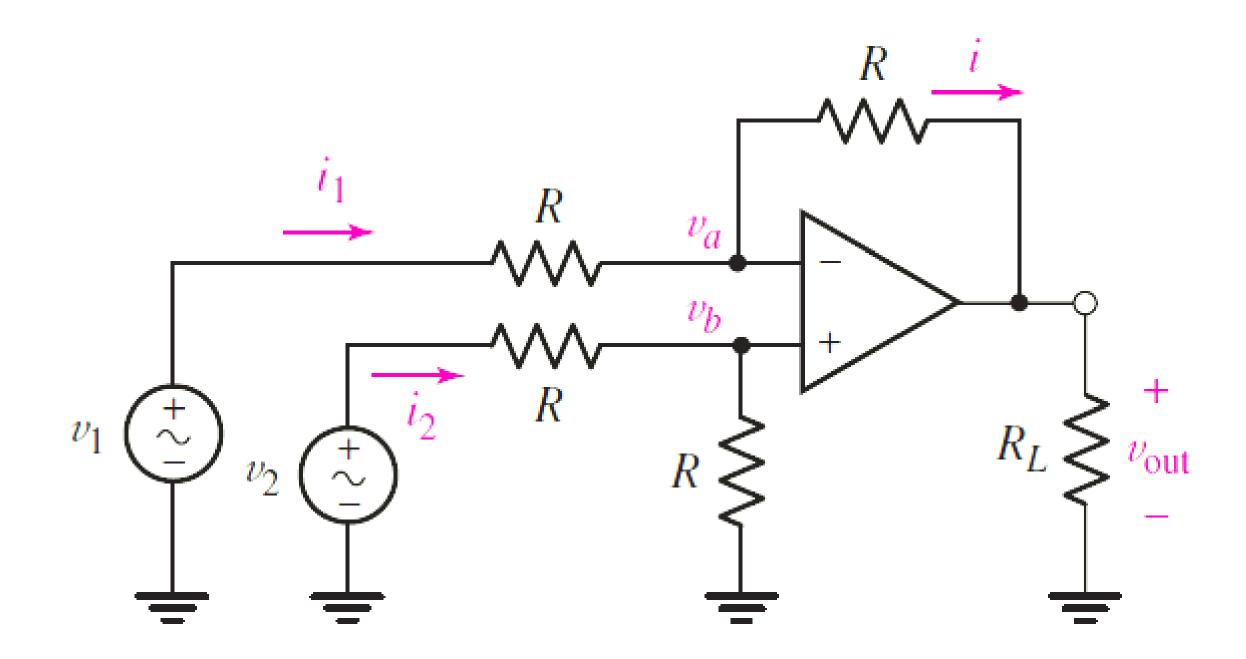




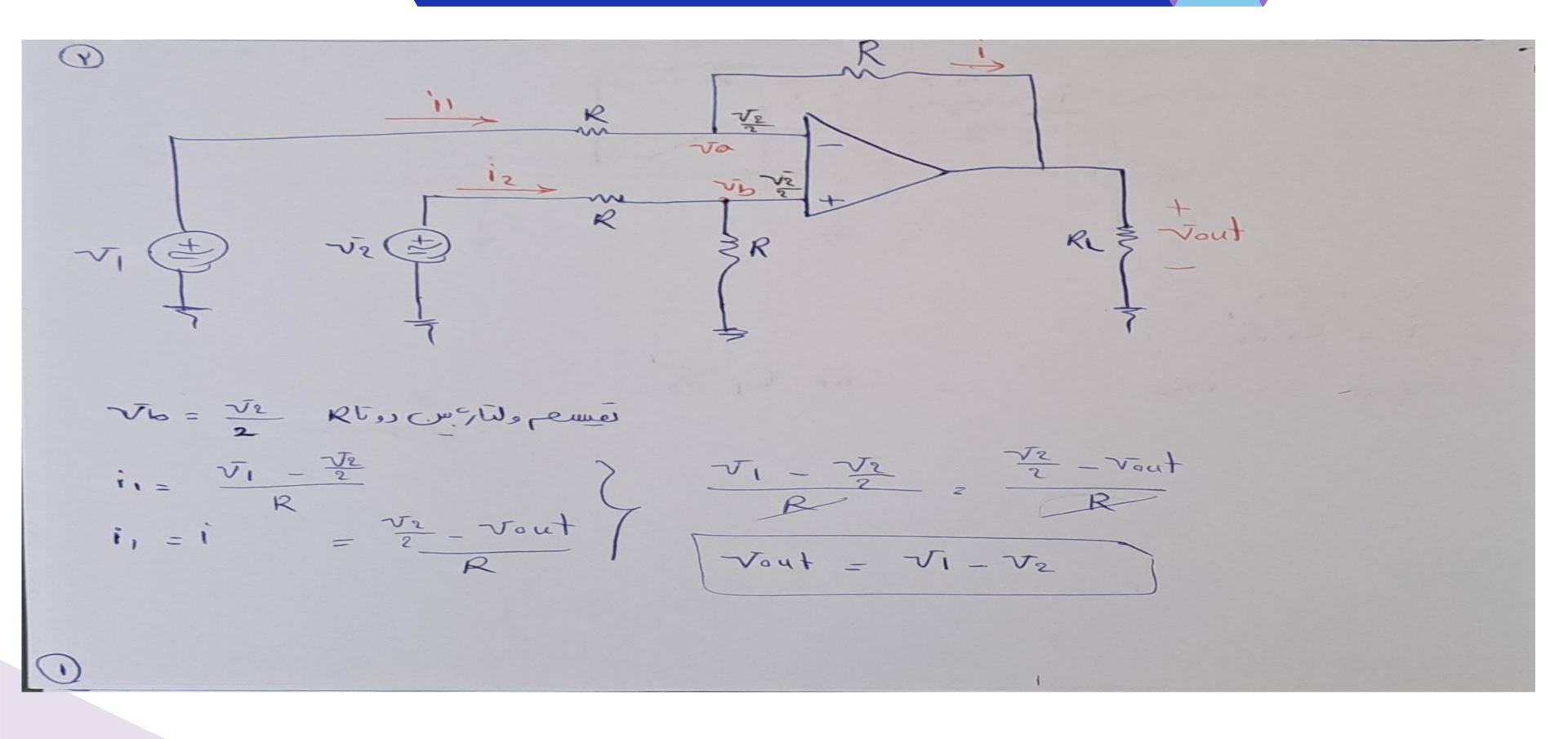
V = lok xlm = lov

 $\frac{\sqrt{2}-1^{\circ}}{1700} = \frac{1}{100} = \sqrt{2}-10=17 = \sqrt{2}=27-7$ $\frac{1700}{1700} = \frac{1}{100} = \sqrt{2}-10=17 = \sqrt{2} = 27-7$ $\frac{1}{1000} = \frac{1}{1000} = \sqrt{2}-10=17 = \sqrt{2} = 27-7$ $\frac{1}{1000} = \frac{1}{1000} = \sqrt{2}-10=17 = \sqrt{2} = 27-7$ $\frac{1}{1000} = \frac{1}{1000} = \sqrt{2}-10=17 = \sqrt{2} = 27-7$ $\frac{1}{1000} = \frac{1}{1000} = \sqrt{2}-10=17 = \sqrt{2}-10=17$ $\frac{1}{1000} = \frac{1}{1000} = \frac{1$

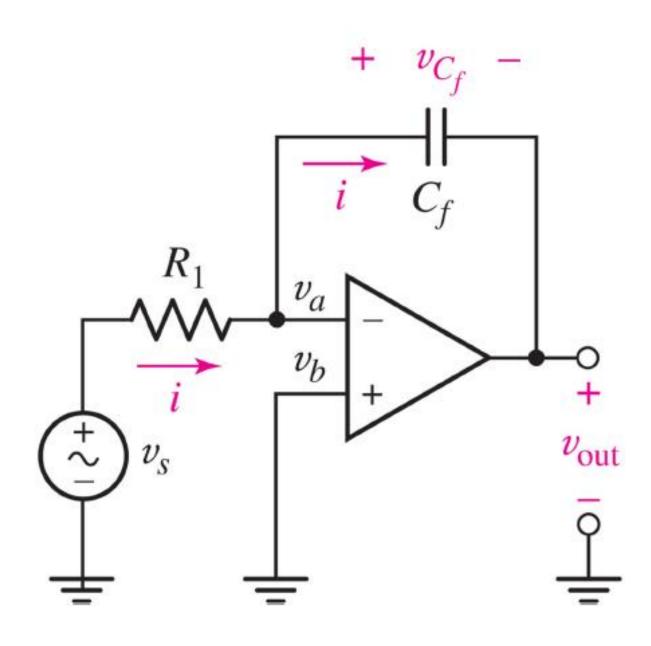
$$V_{out} = ?$$





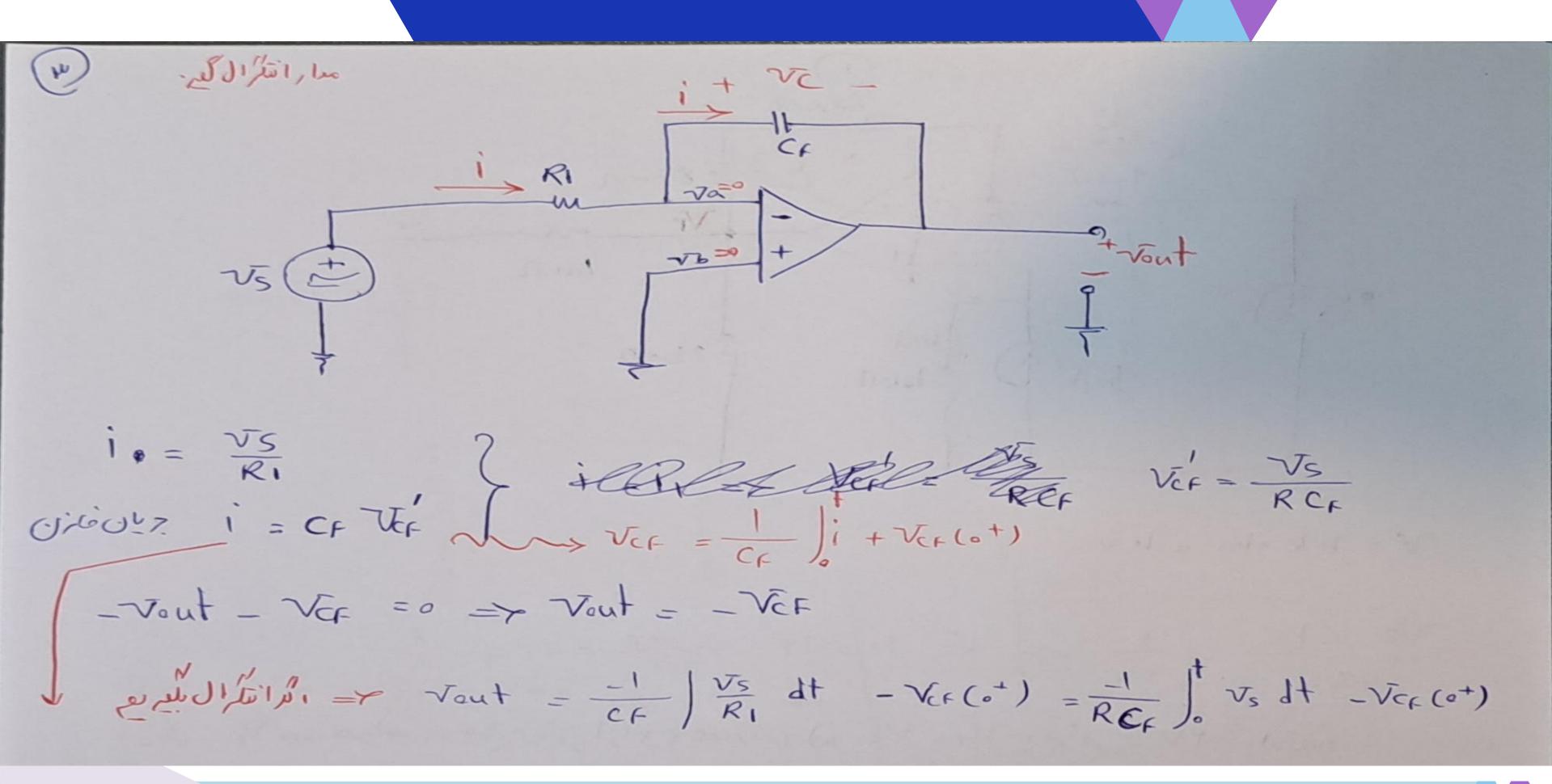


$$V_{out} = ?$$

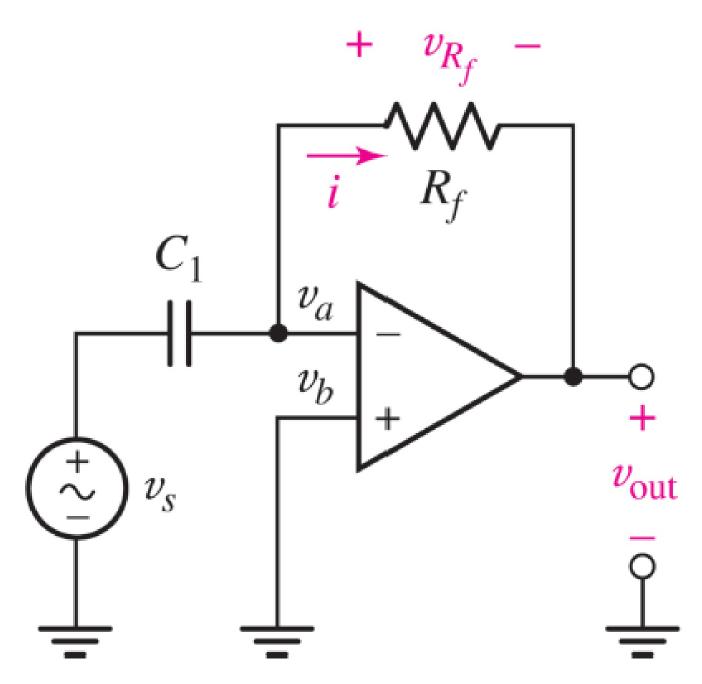


$$v_{\text{out}} = -\frac{1}{R_1 C_f} \int_0^t v_s \, dt' - v_{C_f}(0)$$

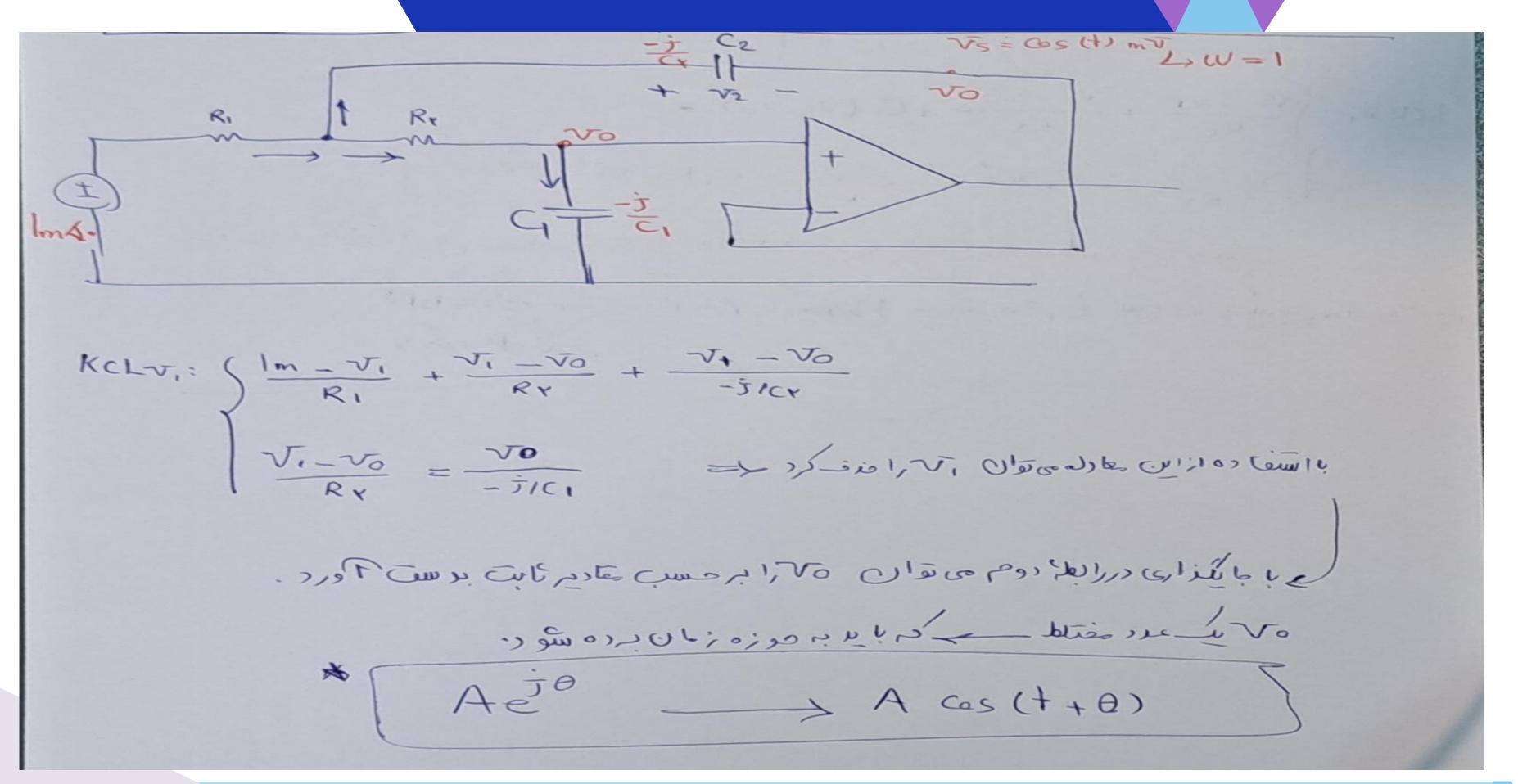




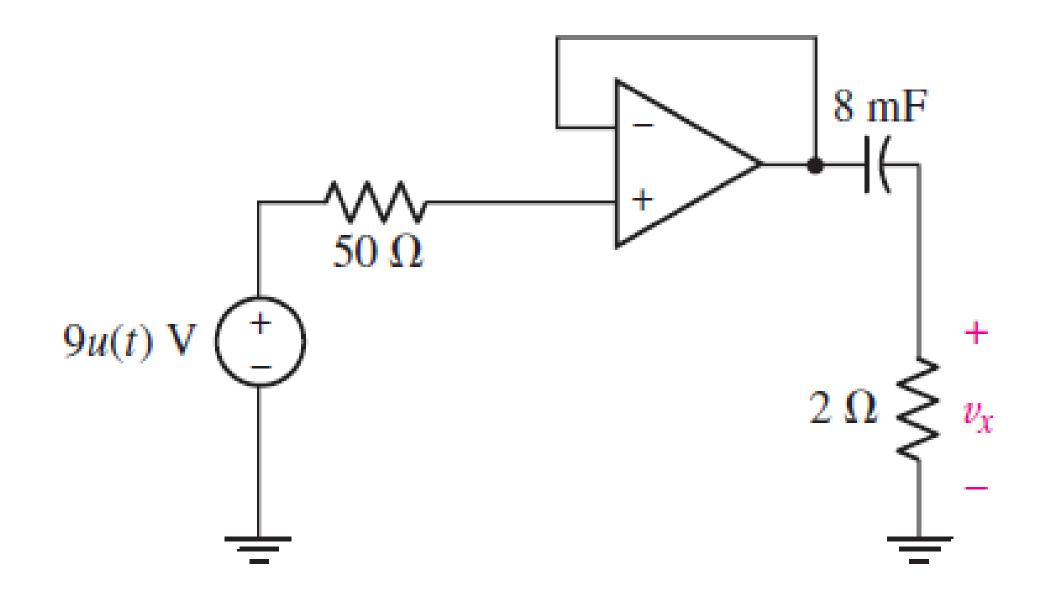
$$V_{out} = ?$$



$$v_{out} = -C_1 R_f \frac{dv_s}{dt}$$



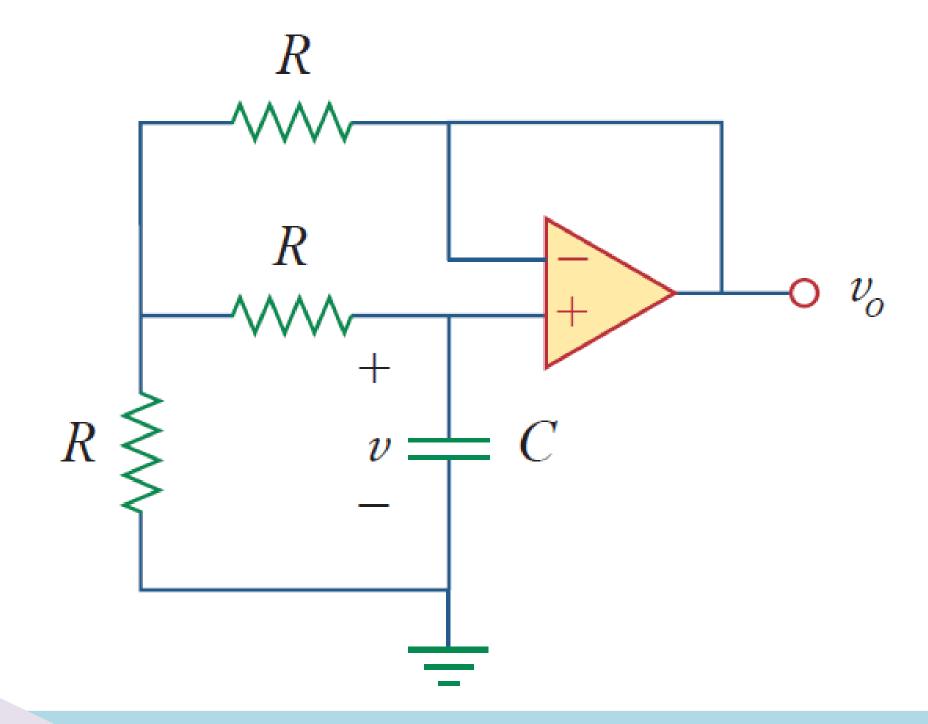
$$v_x=?$$



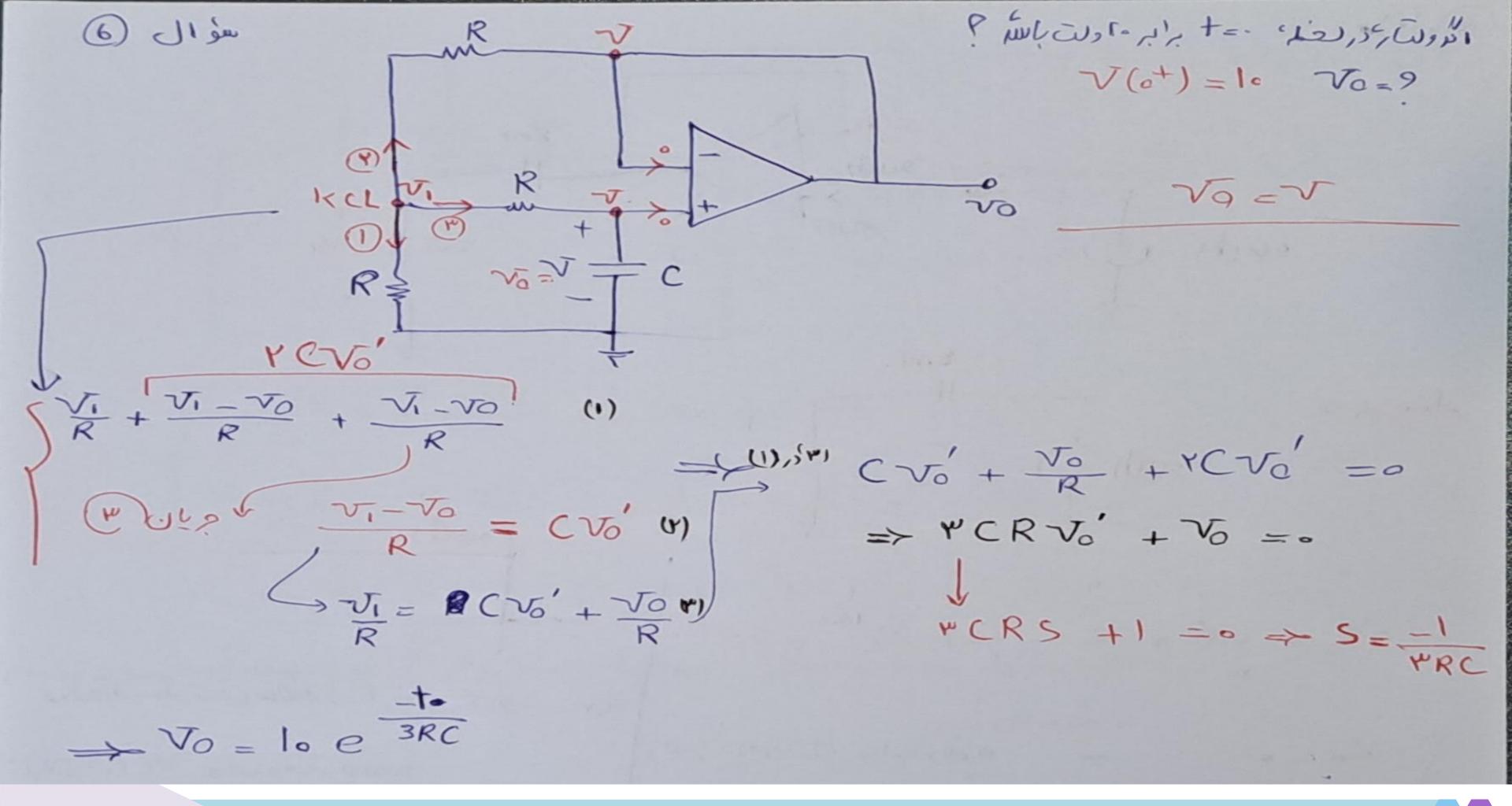


ou(t) 8mf , led , lea vu = V6 + (= - V6) e 16m = 9 e 16m و سرو دومرفان صدارباز سره (+) NC (=) = Vc(+) در نسجه ر رلفعلی صفرمس م که که و روی دوسم Viot = 9

If the initial voltage across the capacitor at time t = 0 is 10 volts, determine the output voltage v_o .

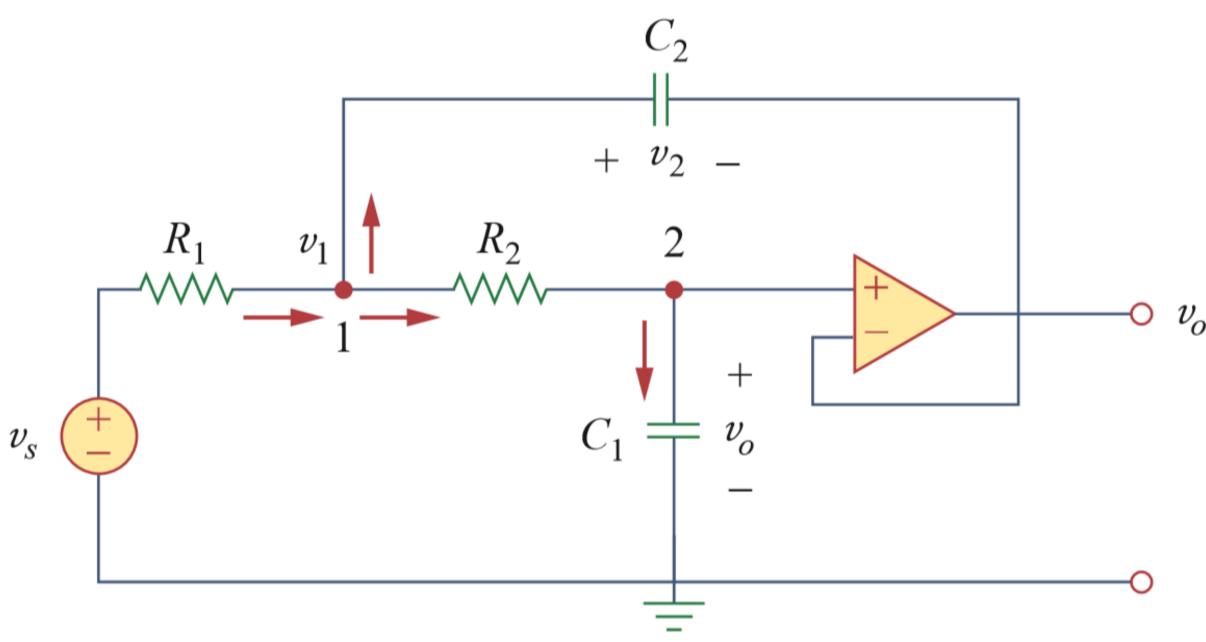






$$> v_S = 10u(t)mV, R_1 = R_2 = 10K\Omega, C_1 = 20\mu F, C_2 = 100\mu F$$

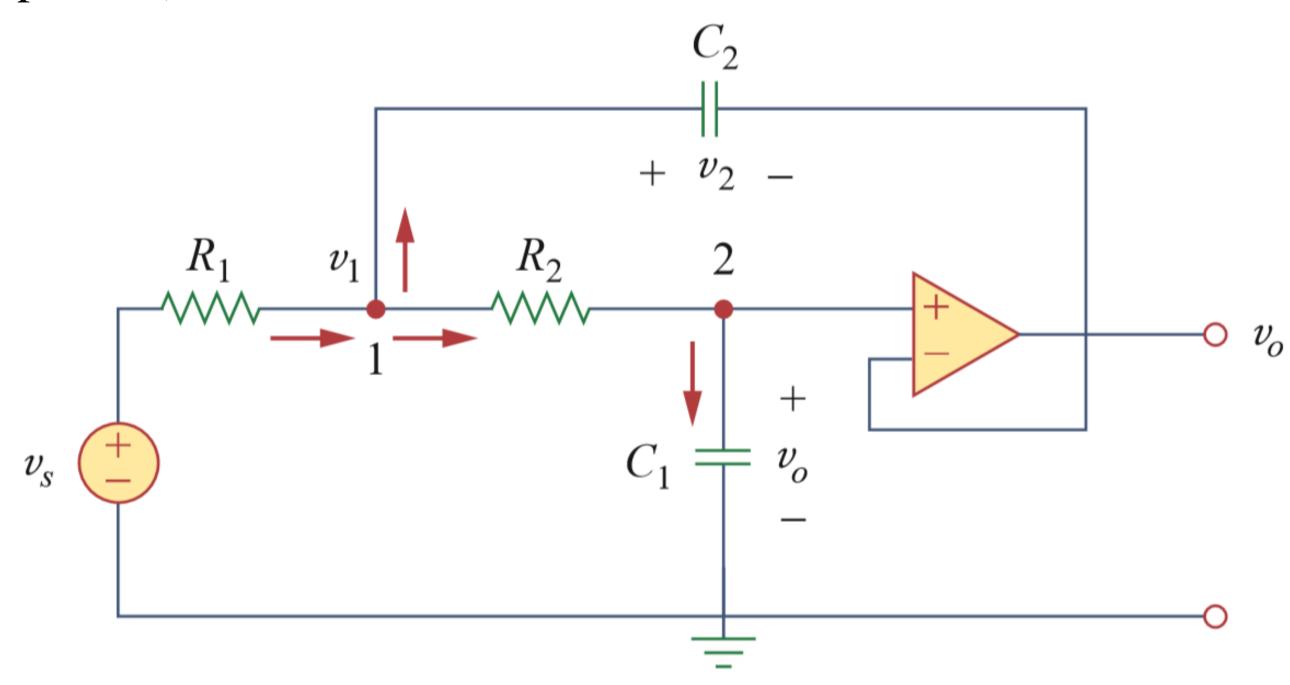
$$\triangleright v_o = ?$$

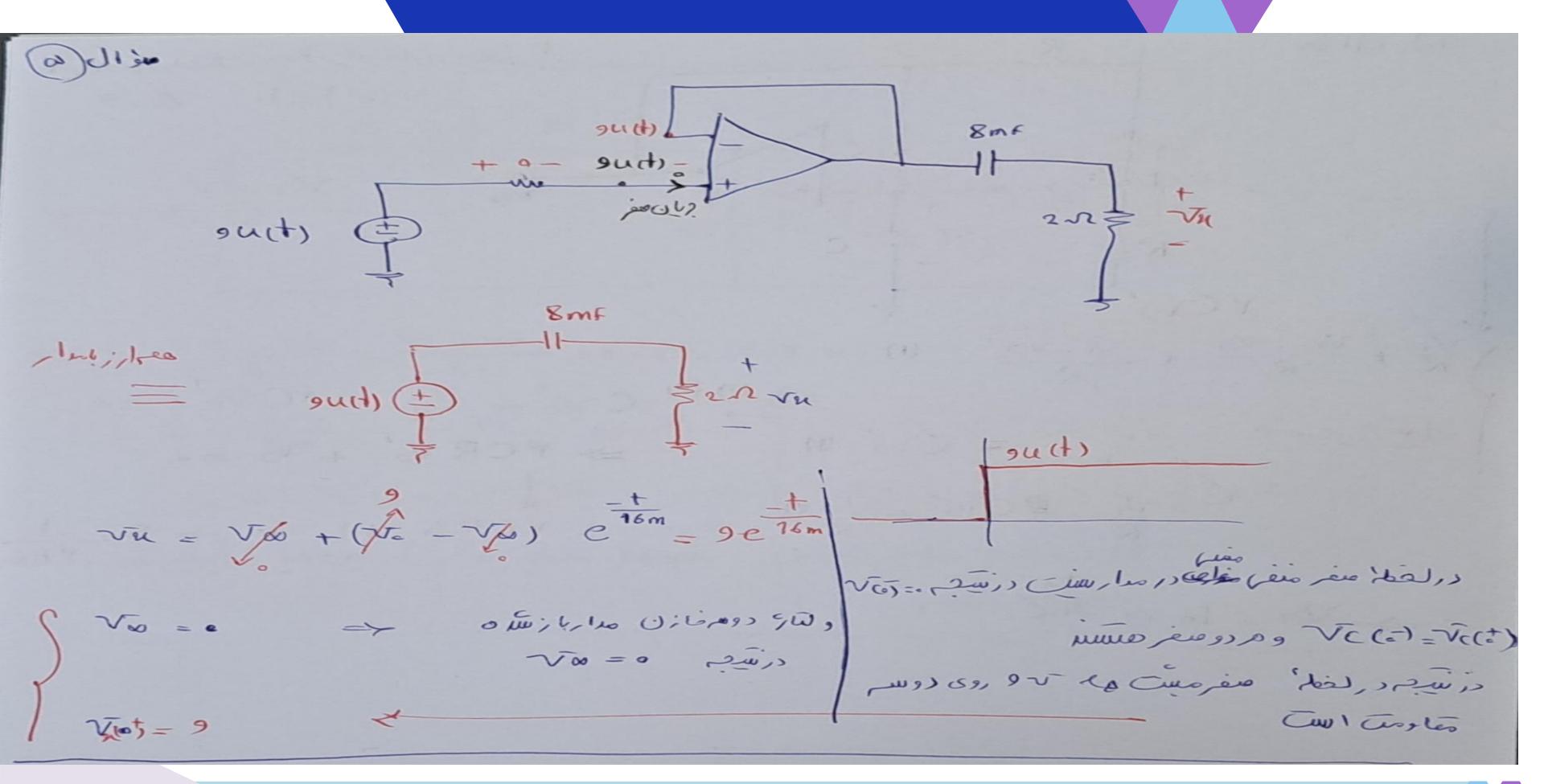




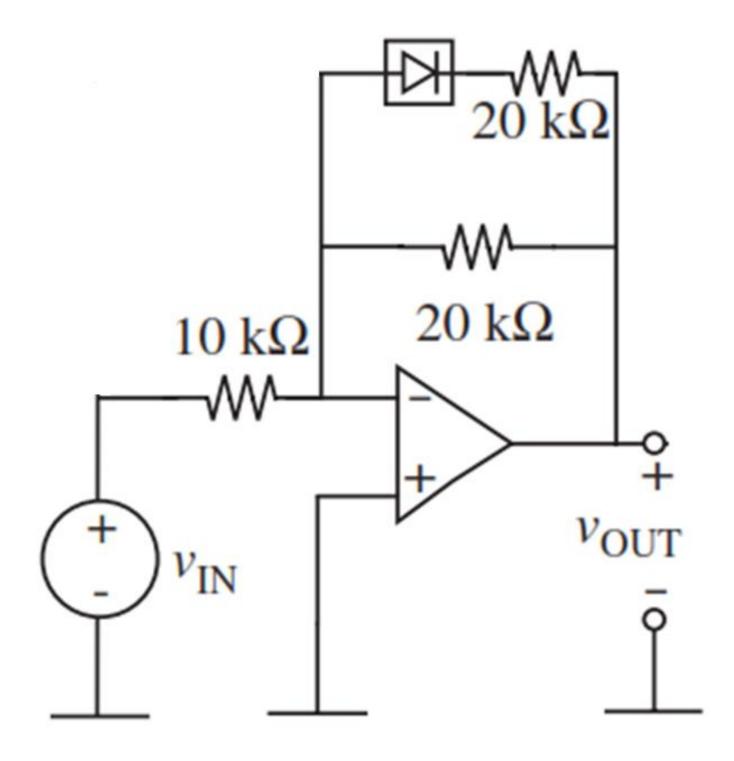
KCL VI: \\ \frac{\sqrt{\sin}\sint\sign{\sqrt{\sy}}}}}}}}}}}}}}} \end{\sqit{\sintitingset\sqrt{\sint{\sint{\sint{\sint{\sint{\sint{\sint{\s VI_VO = CIVO => [VI = CIRYVO' + VO یا دستاه مع دار مع ی توان آنرا فنوان آنرا و می را بر دسم کا نوسی . ان می نوسی کا نوسی . را فلونه دل لسعم.

- $v_s = \cos(t)mV, R_1 = R_2 = 10K\Omega, C_1 = 20\mu F, C_2 = 100\mu F$
- $\triangleright v_o = ?$ (Use phasors).

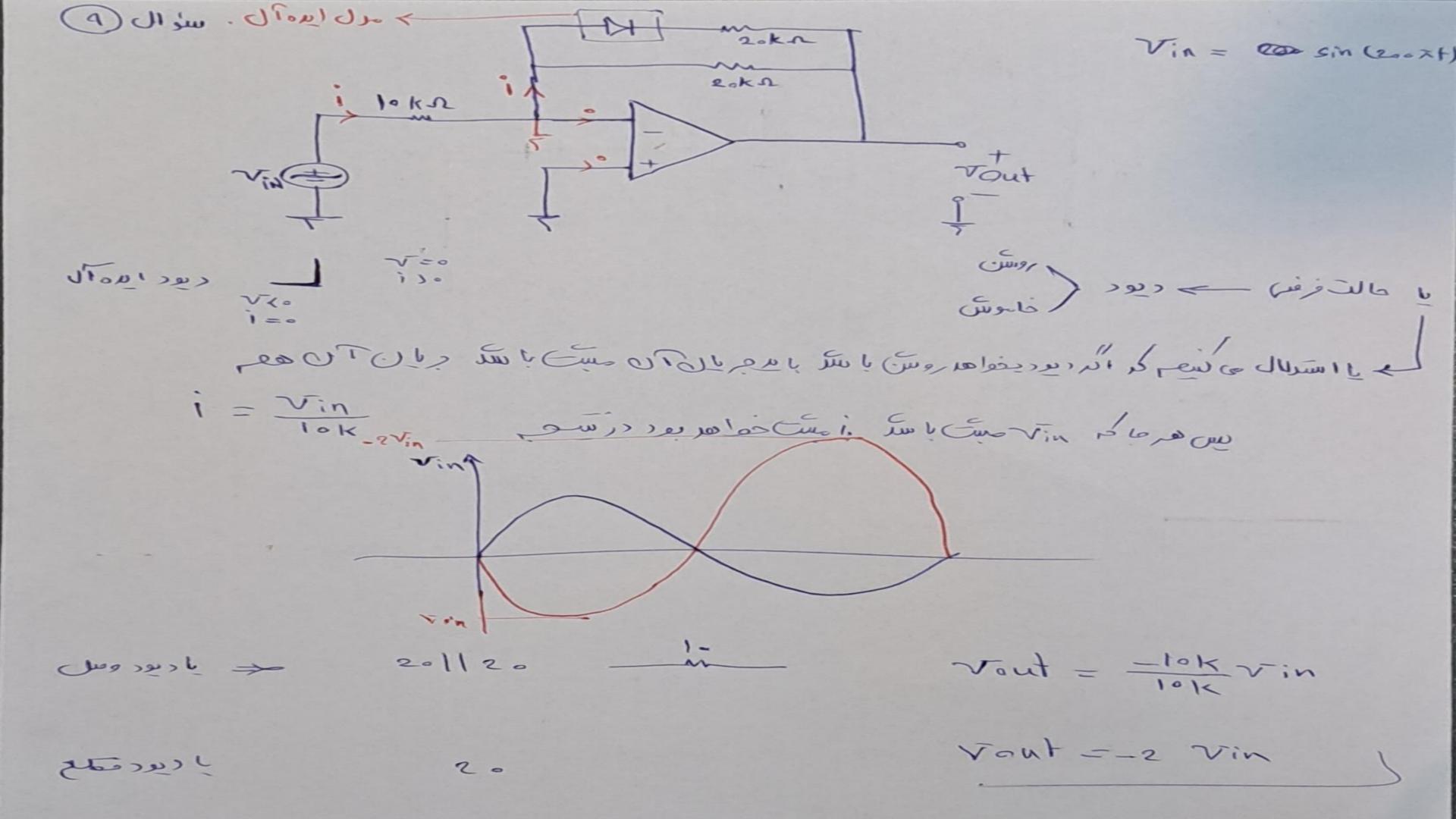




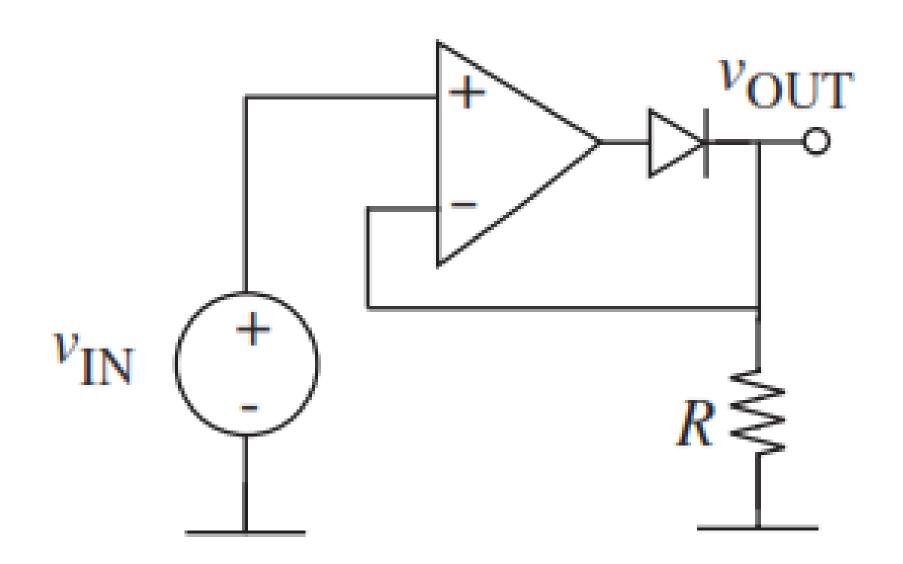
If $v_{in} = \sin(200\pi t)$, plot the output voltage v_{out} .







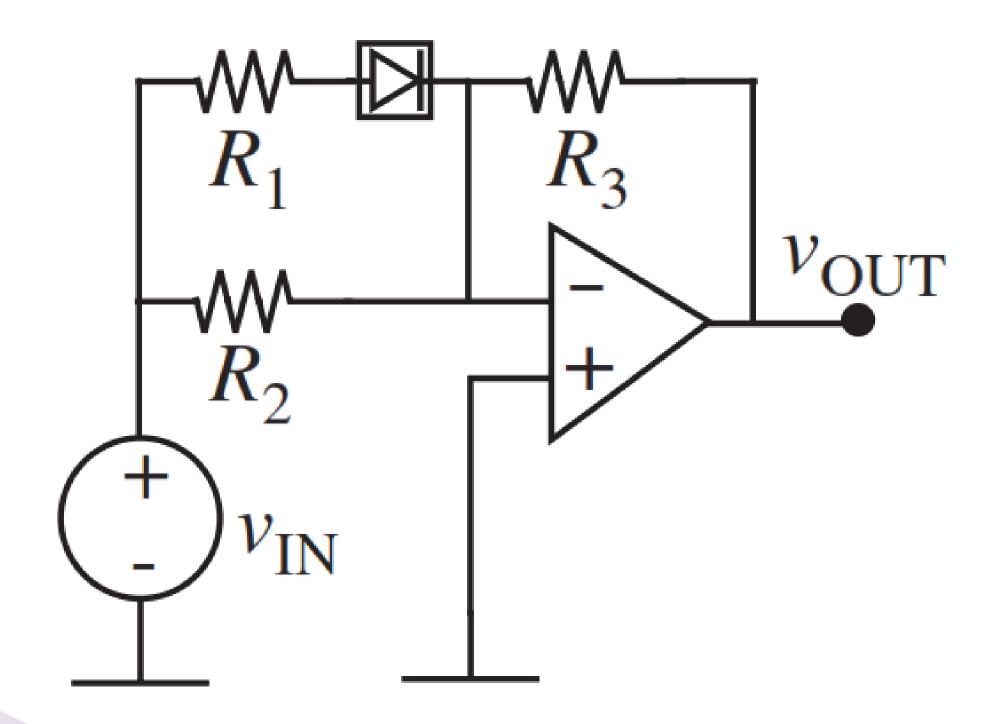
 \triangleright Plot the diagram of v_{out} as a function of v_{in} .



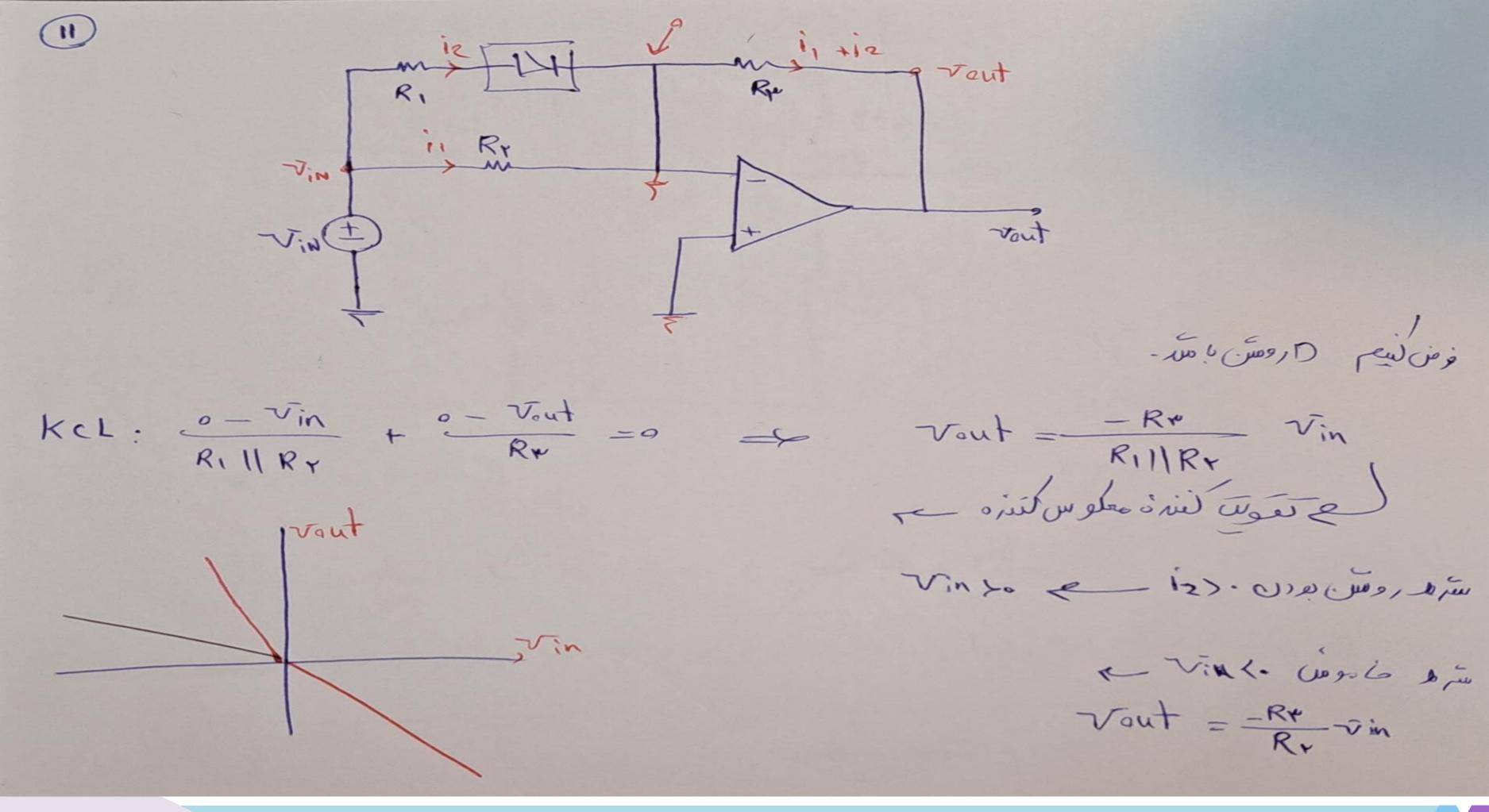


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 \triangleright Plot the diagram of v_{out} as a function of v_{in} .

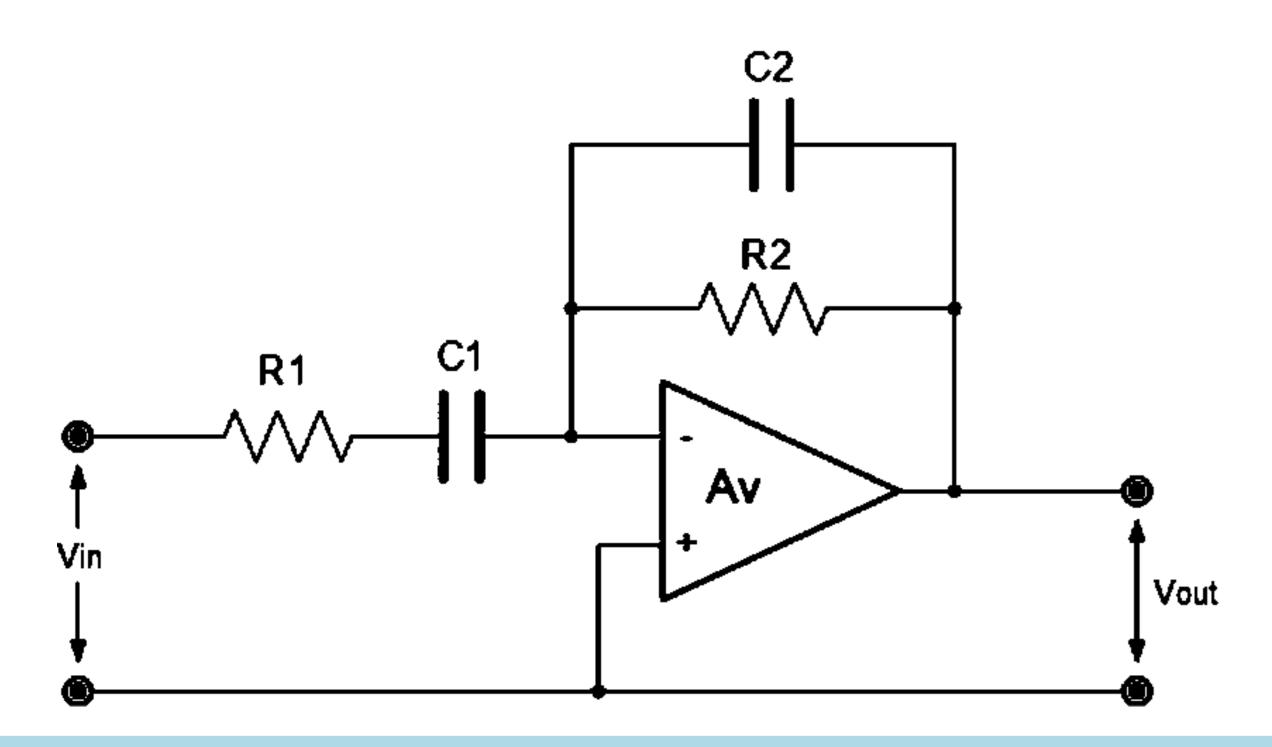




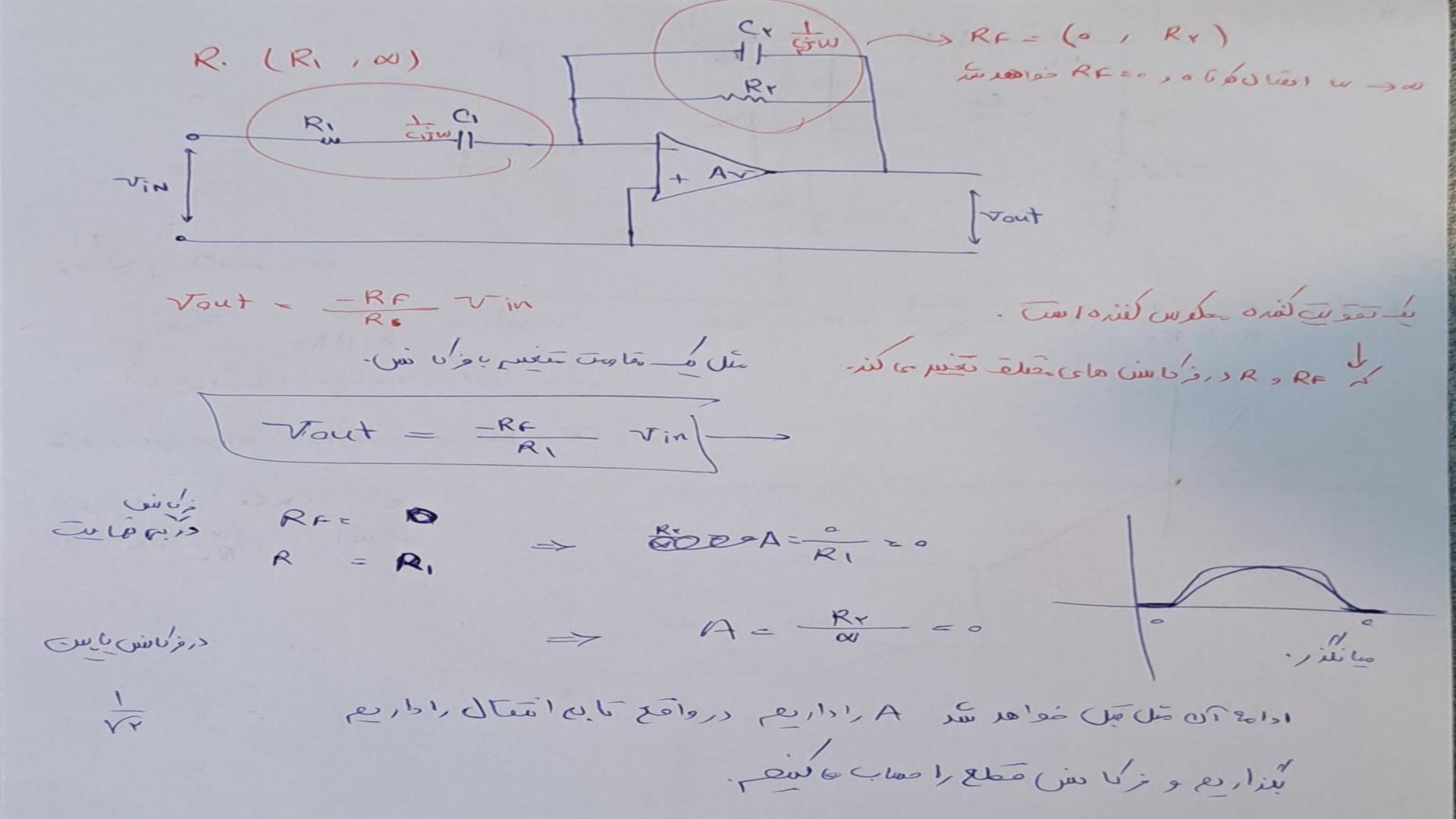


This is an active filter (using an op-amp in a frequency filter). Calculate:

- ✓ The type of filter
- ✓ The filter gain
- ✓ The cut-off frequency









Thanks