

MEMORY MANAGEMENT

Chapter 7: Main Memory

CS220: OS -Spring 2021

Numericals

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Context Switch Time including Swapping

Problem:

100MB process swapping to hard disk with transfer rate of 50MB/sec from main memory.

- $\text{Swap Time (sec)} = \text{Size (mb)} / \text{transfer rate (mb/sec)}$
 - Swap Time = $100/50 = 2\text{sec} = 2000\text{ms}$
 - Swap[out] time of 2000 ms
 - Plus swap in of same sized process
 - Total context switch swapping component time = 4000ms (4 seconds)

Dynamic Storage-Allocation Problem

Given five memory partitions of 100Kb, 500Kb, 200Kb, 300Kb, 600Kb (in order), how would the first-fit, best-fit, and worst-fit algorithms place processes of 212 Kb, 417 Kb, 112 Kb, and 426 Kb (in order)? Which algorithm makes the most efficient use of memory?

First-fit:

212K is put in 500K partition

417K is put in 600K partition

112K is put in 288K partition (new partition 288K = 500K - 212K)

426K must wait

Best-fit:

212K is put in 300K partition

417K is put in 500K partition

112K is put in 200K partition

426K is put in 600K partition

Dynamic Storage-Allocation Problem

Worst-fit:

212K is put in 600K partition

417K is put in 500K partition

112K is put in 388K partition

426K must wait

In this example, best-fit turns out to be the best

Paging

- Calculating internal fragmentation

Given:

- Page size = 2,048 bytes
- Process size = 72,766 bytes
- 35 pages + 1,086 bytes

Calculate:

- Internal fragmentation of $2,048 - 1,086 = 962$ bytes
- Worst case fragmentation = 1 frame – 1 byte
- On average fragmentation = $1 / 2$ frame size
- Process view and physical memory now very different
- By implementation process can only access its own memory

Things to recall

- $2^{10} = 1 \text{ Thousand} = 1 \text{ KB}$
- $2^{20} = 1 \text{ million} = 1 \text{ MB}$
- $2^{30} = 1 \text{ Billion} = 1 \text{ GB}$
- $2^{40} = 1 \text{ Trillion} = 1 \text{ TB}$

$2^1 =$	2	$2^{11} =$	2,048	$2^{21} =$	2,097,152
$2^2 =$	4	$2^{12} =$	4,096	$2^{22} =$	4,194,304
$2^3 =$	8	$2^{13} =$	8,192	$2^{23} =$	8,388,608
$2^4 =$	16	$2^{14} =$	16,384	$2^{24} =$	16,777,216
$2^5 =$	32	$2^{15} =$	32,768	$2^{25} =$	33,554,432
$2^6 =$	64	$2^{16} =$	65,536	$2^{26} =$	67,108,864
$2^7 =$	128	$2^{17} =$	131,072	$2^{27} =$	134,217,728
$2^8 =$	256	$2^{18} =$	262,144	$2^{28} =$	268,435,456
$2^9 =$	512	$2^{19} =$	524,288	$2^{29} =$	536,870,912
$2^{10} =$	1,024	$2^{20} =$	1,048,576	$2^{30} =$	1,073,741,824

Paging Numerical-1

- Assuming a 1-KB page size, what are the page numbers and offsets for the following address references (provided as decimal numbers):
 - a. 3085
 - b. 42095
 - c. 215201
 - d. 650000
 - e. 2000001

Page Numerical-1 (Solution2)

$$3085/1024 = 3.0126953125$$

3 = pages

$$0.126953125 * 1024 = 13$$

Page size = 1 KB = 1024B

Page number	Offset
$3085/1024 = 3$	$3085 \bmod 1024 = 13$
$42095/1024 = 41$	$42095 \bmod 1024 = 111$
$215201/1024 = 210$	$215201 \bmod 1024 = 161$
$650000/1024 = 634$	$650000 \bmod 1024 = 784$
$2000001/1024 = 1953$	$2000001 \bmod 1024 = 129$

Paging Numerical-2

- Consider a logical address space (LAS) of 32 pages with 1024 words per page; mapped onto a physical memory of 16 frames.
1. How many bits are required in the logical address?
 2. How many bits are required in the physical address?

Answer:

1. $2^5 * 2^{10} = 2^{15} = 15$ bits.
2. $2^4 * 2^{10} = 2^{14} = 14$ bits.

Effective Access Time [Cont.]

- **Effective Access Time (EAT)**

$$\text{EAT} = \alpha \times \text{memory access time (hit)} + \text{fail} \times \text{memory access time (failed)}$$

Effective Access Time [Cont.]

- Consider $\alpha = 80\%$, 100ns for memory access
 - $EAT = 0.80 \times 100 + 0.20 \times (100+100) = 120\text{ns}$
- Consider more realistic hit ratio $\rightarrow \alpha = 99\%$, 100ns for memory access
 - $EAT = 0.99 \times 100 + 0.01 \times (100+100) = 101\text{ns}$

EAT Numerical

Consider a paging system with the page table stored in memory.

1. If a memory reference takes 200 nanoseconds, how long does a paged memory reference take?
2. If we add associative registers, and 75 percent of all page-table references are found in the associative registers, what is the effective memory reference time? (Assume that finding a page-table entry in the associative registers takes zero time if the entry is there.)

EAT Numerical (Sol)

Answer:

1. 400 nanoseconds: 200 nanoseconds to access the page table and 200 nanoseconds to access the word in memory.
2. Effective access time = $0.75 \times (200 \text{ nanoseconds}) + 0.25 \times (400 \text{ nanoseconds}) = 250 \text{ nanoseconds}$.

Thank you!