

1-13-16

Lecture 3 January 13th

Finish Appendix section 7 if needed.

Appendix Section 8 word problems

1) Simple interest: (the interest is not compounding)

$$\underset{\substack{\uparrow \\ \text{interest}}}{I} = \underset{\substack{\uparrow \\ \text{principal}}}{P} \underset{\substack{\uparrow \\ \text{interest rate}}}{r} \underset{\substack{\leftarrow \\ \text{time}}}{t}$$

ex Deposit \$1000 (principal) = P

interest = 6% = r

time = 2 years = t

$$\begin{aligned} \rightarrow I &= \$1000 \cdot .06 \cdot 2 \\ &= 1000 \cdot .12 \\ &= 120 \end{aligned}$$

The interest is \$120

ex

Borrow \$500 for 6 Months, interest is 10% per year.

$$\begin{aligned} I &= 500 \cdot .10 \cdot \frac{1}{2} \\ &= 25 \text{ dollars} \end{aligned}$$

ex

Borrow \$500 for 6 Months interest is 10% per Month.

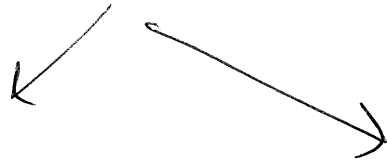
$$\begin{aligned} I &= 500 \cdot .10 \cdot 6 \\ &= 300 \text{ dollars} \end{aligned}$$

- Blending problem (omit for now)

- Uniform motion.

Moving at a constant speed, (rate)

$$\text{Distance} = \text{rate} \cdot \text{time}$$



$$500? = 50 \text{ mph} \cdot 10 \text{ minutes}$$

Wrong

$$500 \text{ miles} = 50 \text{ mph} \cdot 10 \text{ hours.}$$

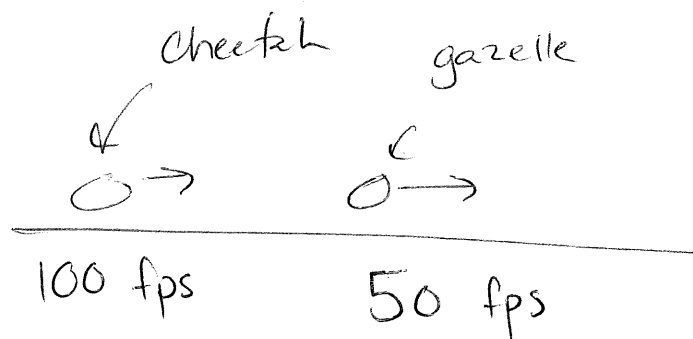
right ✓

easy: Orlando is 140 miles away.
How long does the drive take if
driving at 70 mph?

$$140 = 70 \cdot t \rightarrow t = 2 \text{ hours.}$$

~~hard:~~ Jack leaves Orlando driving 70 mph.
~~Jill leaves Jax driving 60 mph.~~
~~When and where do they meet?~~

harder:



the gazelle has a ~~100 foot~~ ^{100 foot} head start. How long & far does the cheetah run?

caught at time t .



$$d = rt$$

$$d = 100(t) \quad \text{cheetah}$$

$$(d - 100) = 50(t) \quad \text{gazelle}$$

$$d = 50t + 100$$

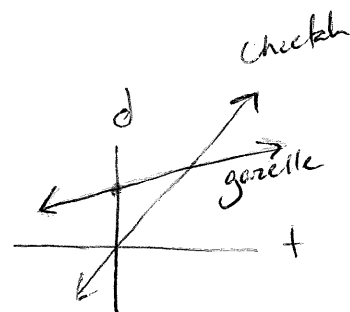
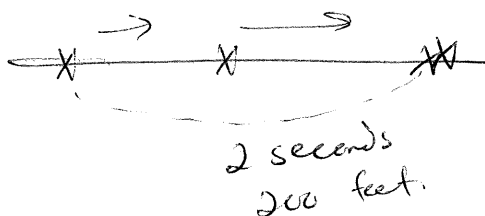
set equal to each other,

$$100(t) = 50(t) + 100$$

$$50(t) = 100$$

$$t = 2 \text{ seconds}$$

check answer,
Makes sense!



example. working together on a job.

- Jack takes 2 hours to paint a room and Jill takes 2 hours to paint a room. How about if they work together?
= 1 hour.

Jack takes 4 hours, Jill takes 2 hours, now what?

in one hour, Jack has painted $\frac{1}{4}$
Jill has painted $\frac{1}{2}$.
together, $\frac{3}{4}$ in one hour.

how many hours until done?

$$\frac{1}{\frac{3}{4}} = \frac{4}{3} \text{ hours } 1:20.$$

See 11.1



See 11.1

Systems of
linear equations.

ex)

Drinks are \$2

snacks are \$3 $\rightarrow 2x + 3y = 30$

made \$30

lets say ~~230~~¹² items sold total.

How many of each?

$$2x + 3y = 30$$

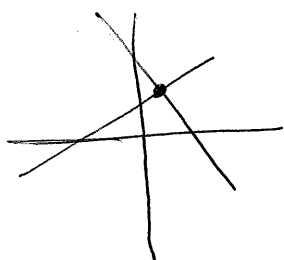
$$x + y = \del{30}^{12}$$

is there an x, y that makes
this work?

$$x=6, y=6$$

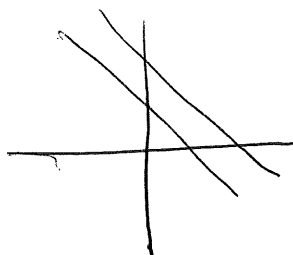
this is a system
of equations.

there are three scenarios:



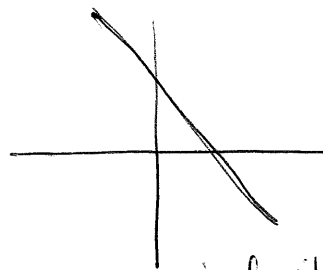
One answer
intersection

$$\begin{aligned} 2x + 3y &= 30 \\ x + y &= 12 \end{aligned}$$



No
answer
intersection

$$\begin{aligned} x + y &= 3 \\ x + y &= 5 \end{aligned}$$



infinite
answers
intersections.

$$\begin{aligned} x + y &= 6 \\ 2x + 2y &= 12 \end{aligned}$$

There are 2 ways to
solve a system:

Substitution

$$2x + 3y = 30$$

$$x + y = 12 \leftarrow \text{solve for } y.$$

$$y = -x + 12.$$

Substitute into the other.

$$2x + 3(-x + 12) = 30$$

$$2x - 3x + 36 = 30$$

$$-x = -6 \rightarrow x = 6.$$

$$6 + y = 12 \rightarrow y = 12.$$

Elimination

$$2x + 3y = 30$$

$$x + y = 12$$

$$\rightarrow \begin{array}{r} 2x + 3y = 30 \\ -2x - 2y = -24 \end{array}$$

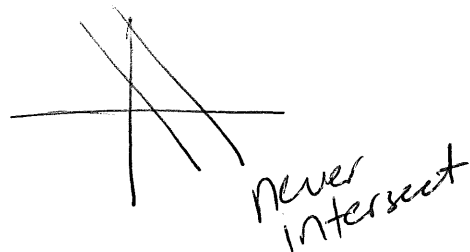
$$y = 6$$

$$\rightarrow x = 6$$

those were examples of 1 solution.

No solution example:

$$\begin{array}{l} 2x + y = 5 \\ 4x + 2y = 8 \end{array} \rightarrow \begin{array}{l} -4x - 2y = -10 \\ 4x + 2y = 8 \end{array}$$

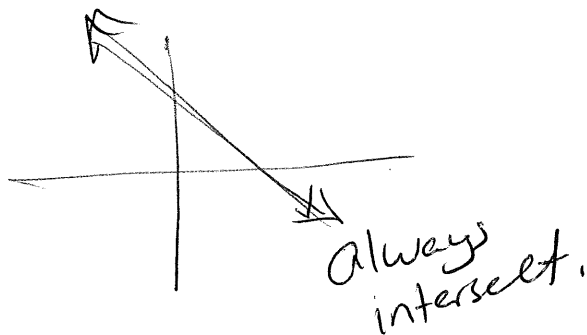


$$0 = -2 \quad ?$$

never true

infinite solution example:




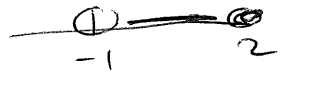

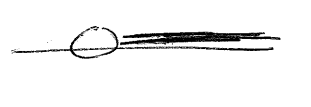

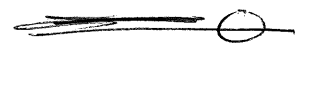

$$\begin{array}{l} 2x + y = 5 \\ 4x + 2y = 10 \end{array} \rightarrow \begin{array}{l} -4x - 2y = -10 \\ 4x + 2y = 10 \end{array}$$



$$0 = 0$$

always true.

A9) interval notation 2 inequalities.

a, b interval	inequality	graph/shading.
$(-1, 2)$	$-1 < x < 2$	
$[-1, 2]$	$-1 \leq x \leq 2$	
$[-1, 2)$	$-1 \leq x < 2$	
$(-1, 2]$	$-1 < x \leq 2$	
$[-1, \infty)$	$-1 \leq x \quad x \geq -1$	
$(-1, \infty)$	$-1 < x \quad x > -1$	
$(-\infty, 2]$	$x \leq 2$	
$(-\infty, 2)$	$x < 2$	
$(-\infty, \infty)$	$x = \text{anything}$	

infinity is a number?

$(2, -1)$ wrong or right?

Rules

- $a^2 \geq 0$
- $6 > 4$ divide by negative 2,
multiply by negative 1.
 $\swarrow \quad \searrow$
 $-3 < -2$ $-6 < -4$

* Always be careful about
dividing by a negative.

$$x^2 < x \rightarrow x < 1 \quad ? \quad \underline{\underline{\text{no.}}}$$

ex - $4x + 7 \geq 2x - 3$ same as equation.

$$\begin{aligned} 2x &\geq -10 \\ x &\geq -5 \end{aligned}$$

ex $-5 < 3x - 2 < 1$ means "and,"

$$-5 < 3x - 2 \quad \text{and} \quad 3x - 2 < 1$$

$$\begin{aligned} -3 &< 3x & \text{and} & & 3x &< +3 \\ -1 &< x & & & x &< 1 \end{aligned}$$

ex $\frac{1}{4x-1} > 0$

~~what~~ what does this
Mean about $4x-1$?

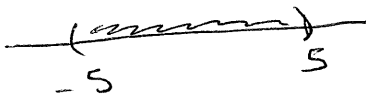
$$4x-1 > 0$$

$$x > 1/4$$

inequalities combined with absolute
values.

$$|x| < 5$$

↓



$$(-5, 5)$$

$$|x| > 5$$



$$(-\infty, -5) \cup (5, \infty)$$

rules

$$|x| < a \rightarrow -a < x < a$$

$$-a < x \text{ and } x < a$$

$$|x| > a \rightarrow x > a \text{ or } x < -a$$

Example

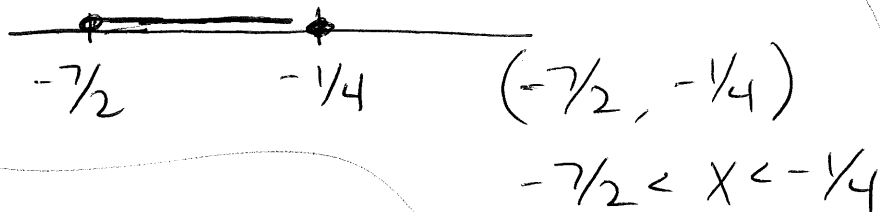
$$|2x + 4| \leq 3$$

$$-3 \leq 2x + 4 \leq 3$$

$$\downarrow \quad -3 \leq 2x + 4 \quad \text{and} \quad 2x + 4 \leq 3$$

$$x \leq -\frac{7}{2} \quad \text{and} \quad x \leq -\frac{1}{4}$$

3 ways
to write
answer.


$$(-\frac{7}{2}, -\frac{1}{4})$$
$$-\frac{7}{2} < x < -\frac{1}{4}$$

Example $|2x - 5| > 3$

$$2x - 5 > 3 \quad \text{or} \quad 2x - 5 < -3$$

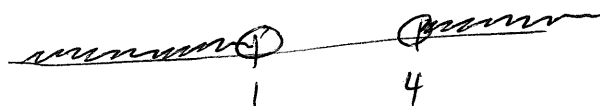
$$2x > 8$$

$$x > 4$$

$$\text{or} \quad x < 1$$

$$2x < 2$$

$$x < 1$$


$$(-\infty, 1) \cup (4, \infty)$$

$$\{x \mid x < 1 \text{ or } x > 4\}$$

$$\{x \mid x < 1 \text{ or } x > 4\}$$