# **Calibration Certificate**

Invar rod (type, No.):

GPCL3 26909

No. of graduations measured:

5 - 345

Contract:

14-72-07

Date:

12.01.15

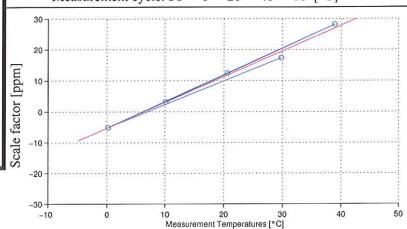


Coefficient of expansion:

$$\alpha_T = 0.83 \pm 0.05 \ ppm/^{\circ}C \ (k=1)$$

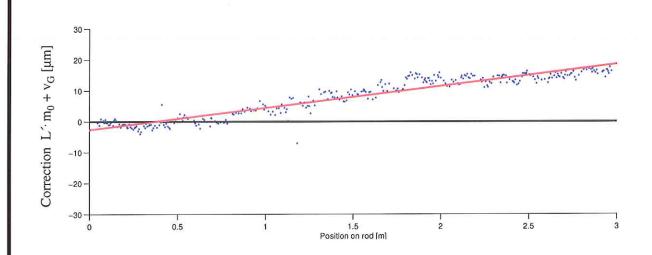
Determination of the coefficient of expansion Horizontal calibration position

Measurement cycle:  $30 \rightarrow 0 \rightarrow 20 \rightarrow 40 \rightarrow 10$  [°C]



**Determination of the scale factor** 

Vertical calibration position, middle 16 mm of scale



Scale factor:

$$m_0 = 7.06 \pm 1.15 \ ppm$$
 at  $T_0 = 19.8 \ ^{\circ}C$  (k=1)

Length adjustment from the vertical calibration (position of use)

$$L = l^0 + L'[1 + (m_0 + \alpha_T(T - T_0)) \cdot 10^{-6}] + v_G$$

 $l^0 = +0.019 \pm 0.007$  mm

$$v_G = -0.003 \text{ mm}$$
 (k=1)

$$l^0 = l_K^0 + v_K$$

L'[m] = observed rod length

 $v_{\rm G}$  [m] = graduation correction

 $l_{K}^{0} = +0.023 \pm 0.007 \text{ mm}$  $v_{K} = -0.004 \text{ mm}$ 

 $T[^{\circ}C] = temperature$ 

 $l^0[m]$  = index correction ( $l_K^0[m]$  = index correction of reference bar,  $v_K[m]$  = reference bar correction)

Technical specialist:

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13.01.2015

Laboratory director:

Institute director:

a. W =

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## **Calibration Certificate**

Number of Invar rod:

26909

Date: 12.01.15

Type of rod:

GPCL3

Contract:

14-72-07

Positions of graduations measured:

5 - 345 (counting bar number from bottom)

#### **Determination of the Scale Factor**

Measurement Direction up

Mean temp.:

19.8 °C

Mean press.:

959.3 hPa

Scale factor:  $6.77 \text{ ppm} \pm 1.15 \text{ ppm}$ 

Average deviation of measurements:

μm

Measurement Direction down

Mean temp.: 19.8 °C

Mean press.:

Scale factor: 7.29 ppm ± 1.16 ppm

Average deviation of measurements:

Both directions averaged

Mean temp.:

19.8 °C

Mean press .:

959.3 hPa

μm

Scale factor:  $7.06 \text{ ppm} \pm 1.15 \text{ ppm}$ 

Average deviation of measurements:

The scale factor is calculated using the middle 16 mm of the visible bar code. If the visible width is smaller than that amount, the whole visible width is used.

#### **Determination of the Index Correction**

Measurement Direction up

Correction: 0.024 mm ± 0.011 mm

Measurement Direction down

Correction:  $0.022 \text{ mm} \pm 0.010 \text{ mm}$ 

Both directions averaged

Correction: 0.023 mm ± 0.007 mm

Reference bar correction

Correction: -0.004 mm

The index correction is based on the lower edge of graduation bar No.66.825 [mm]Therfore this edge must theoretically have no scale factor correction. Because the scale factor is calculated using the graduation bar centers, a small correction for that reference bar will appear if its gauge is not exact.

# **Calibration Certificate**

Number of Invar rod: 26909

Date: 12.01.15

Type of rod: GPCL3

Contract: 14-72-07

Positions of graduations measured:

5 - 345 (counting bar number from bottom)

### **Correction of Graduations**

Correction of graduation bar centers is shown in [µm]

f	0	1	2	3	4	5	6	7	8	9
0 [						-0.8	-1.7	0.3	-0.5	-0.3
10	-1.0	-0.1	-1.0	-1.2	-0.8	-1.8	-1.9	-1.2	-2.3	-0.6
20	-0.2	-0.7	-2.9	-2.0	-3.2	-2.5	-2.3	-2.4	-2.4	-3.4
30	-3.6	-2.5	-3.5	-3.9	-4.3	-3.8	-3.6	-3.4	-5.1	-4.4
40	-6.1	-5.4	-3.6	-4.3	-2.9	-3.9	-2.6	-3.7	-3.5	-3.5
50	-5.3	-4.7	-3.9	-4.7	-3.9	-3.1	2.5	-4.1	-4.8	-3.8
60	-4.8	-5.2	-5.6	-2.9	-3.9	-2.9	-2.7	-2.5	-2.7	-1.2
70	-2.8	-3.5	-2.5	-1.7	-2.6	-3.1	-3.9	-4.9	-5.6	-5.3
80	-6.8	-2.8	-3.7	-4.1	-4.7	-4.9	-4.9	-6.4	-3.7	-3.9
90	-4.9	-5.5	-5.8	-5.6	-5.3	-5.5	-5.8	-5.6	-4.9	-6.2
100		-3.3	-3.5	-3.2	-3.4	-3.5	-2.2	-3.1	-1.9	-2.3
110	-3.1	-3.0	-2.9	-3.2	-2.5	-0.2	-2.8	-1.4	-3.2	-2.0
120	-2.6	-3.9	-5.1	-4.2	-5.4	-3.3	-3.3	-4.9	-2.2	-3.4
130	-4.9	-4.0	-7.9	-0.3	-0.8	-2.8	-0.6		-15.4	-2.4
140	-3.5	-2.6	-4.2	-2.6	-3.7	-0.8	-3.9	-6.3	-2.3	-3.9
150		1.1	-0.5		-0.0	0.1	-2.6	-2.4	0.2	-0.6
160	-0.4	-1.9	-2.1	-0.2	-2.3	-3.0	-2.1	-3.8	-3.9	-3.6
170	-1.0	-1.8	-0.2	-2.1	-0.9	-2.0	-2.1	-1.3	-1.2	-0.7
180	-1.2	-1.6	-3.9	-1.8	-1.7	-4.3	-3.8	0.2	1.0	1.6
190	-0.7	-2.0	0.1	-2.1	0.1	-1.6	-2.4	-1.8	-3.0	-2.5
200	-2.2	-1.0	1.5	1.0	1.8	1.9	2.9	2.0	0.7	2.4
210	2.1	1.0	1.9	0.8	-0.9	-0.1	0.4	-0.6	-1.0	0.4
220	0.3	-0.6	-1.8	-0.7	-1.6	1.1	-0.9	0.8	0.2	1.7
230	-0.1	-1.1	-2.1	-3.0	-3.3	-1.1	-1.9	-1.4	-2.6	-2.9
240	-2.9	-0.8	-0.2	-1.2	-0.2	-0.5	0.1	-1.1	-1.4	-0.1
250	-0.8	-0.8	-2.3	-3.0	-1.8	-4.9	-3.1	-4.4	-5.0	-3.4
260	-3.9	-1.8	-2.7	-1.6	-1.8	-4.0	-2.3	-1.8	-1.6	-1.8
270	-2.7	-2.0	-4.3	-3.4	-4.1	-4.3	-4.6	-3.7	-5.4	-5.1
280	-4.3	-3.0	-1.9	-2.0	-2.0	-2.3	-2.0	-1.3	-2.6	-2.9
290	-2.8	-3.4	-4.4	-5.7	-3.6	-4.2	-4.8	-4.8	-5.9	-4.7
300	-4.5	-3.4	-4.6	-4.0	-3.0	-4.7	-3.5	-4.3	-4.5	-3.5
310	-4.8	-5.3	-4.2	-3.0	-4.5	-4.5	-4.0	-3.9	-2.8	-3.3
320	-5.3	-6.3	-4.8	-2.6	-3.8	-3.2	-2.8	-3.4	-3.0	-3.4
330	-4.3	-3.2	-4.0	-4.6	-3.9	-5.1	-4.7	-4.5	-4.5	-6.5
340	-4.1	-4.1	-4.7	-5.5	-3.4	-4.7				

## Calibration of Invar Rods

Invar rods for precise levelling are examined on the comparators at the Geodetic Laboratory at the Chair of Geodesy of the Technical University in Munich. The distances between the single lines on the invar tape are tested with a laser interferometer. The lines are observed with an CCD-array camera. The observation process itself in these advanced comparators is therefore completely automated.

### Determination of the Index correction of the graduation

The distance between the reference edge of the graduation and the support area of the rod is measured in the axis of the invar tape and compared with the default value.

It become specified

- the index correction of the reference bar l<sub>K</sub><sup>0</sup>
  The reference edge of the reference bar is the only by the manufacturer used point which can be excerted to compare the graduation to the support area.
- the reference bar correction  $v_K$ In practice, not edges but bar centers are observed. The reference bar correction consists of any differences of the reference bar center from the reference edge, e.g. caused by a too wide/too narrow reference bar.
- the index correction of the rod  $l^0$  is the sum of index correction of the reference bar  $l_K^0$  and the reference bar correction  $v_K$ . This is the correction value which has to be added to each rod reading.

For rods with two line graduations, the offset between the graduations  $k^0$  is further determined.

### Determination of the scale factor in vertical position

The position of all graduation bars is observed in both measurement directions.

The nominal and real position are compared and the results are related to a straight line. The gradient of this regression is the scale factor  $m_0$  at the temperature of the measurement  $T_0$ .

Calibrating invar rods with line graduations the scale factor is determined for both scales separately. A tabulated certificate of the residuals of individual lines is supplied on paper or disc.

## Determination of the coefficient of expansion

For the evaluation of the coefficient of expansion the position of approx. 80 uniformly distributed lines (barcode rods) resp. all lines of the right graduation scale (line graduation rods) are observed at different temperatures on a horizontal comparator with an opto-electronic double-diode microscope. The respective scale factors depend on the temperatures, they are related to a regression line. Its gradient is the coefficient of expansion  $\alpha_T$ .

Observations are accomplished in a cycle of  $30 \rightarrow 0 \rightarrow 20 \rightarrow 40 \rightarrow 10$  [°C].

The ample differences of temperature between the single observations ensure, that malfunctions of the tension module and the influence of the friction between the invar tape and the housing of the rod can be detected.

