# Abundance and $\alpha$ -diversity

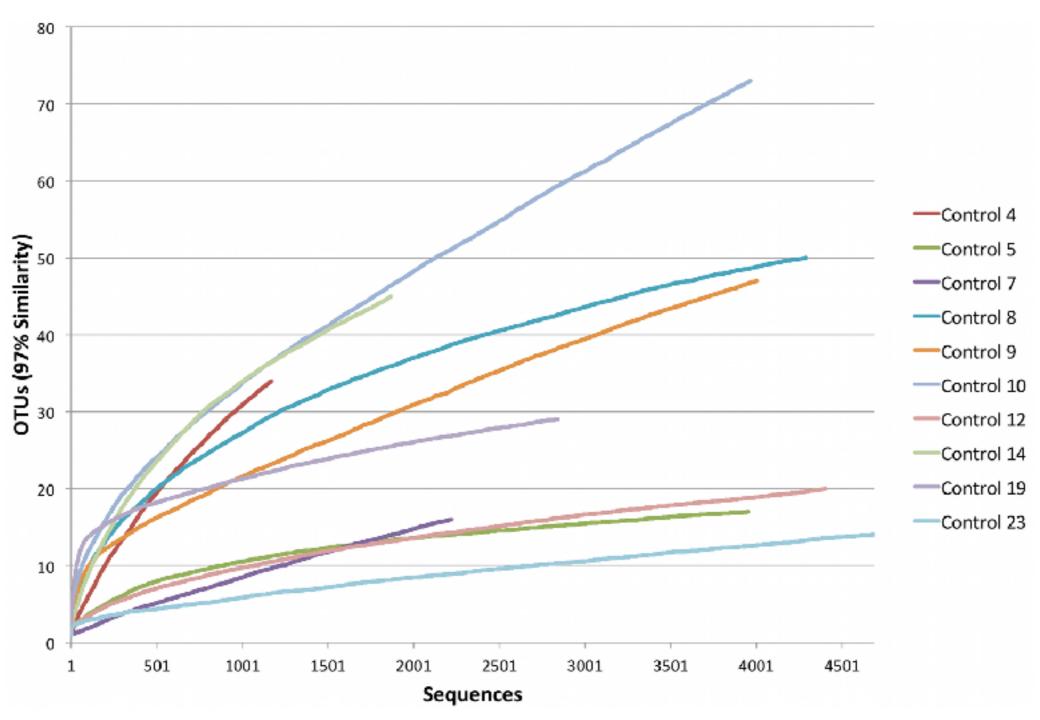
October 30, 2020

#### Count Data

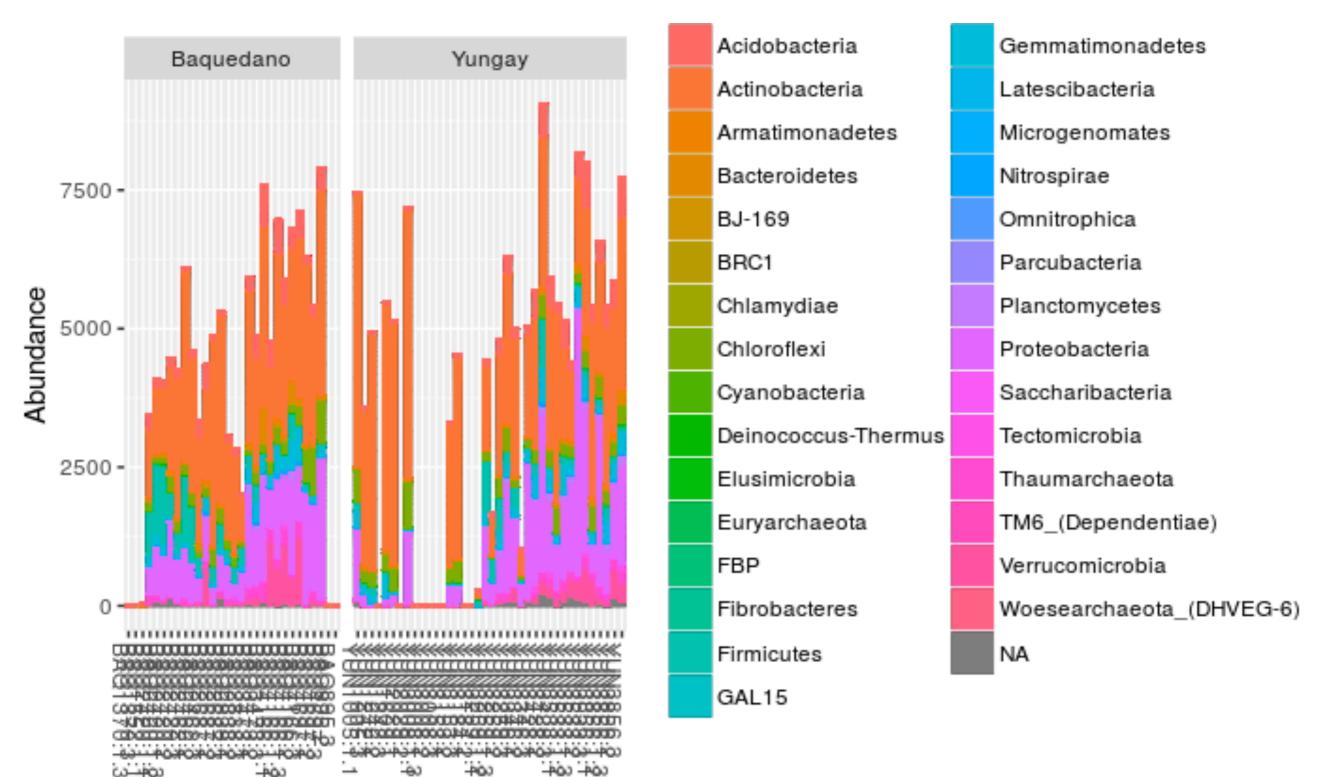
	OTU 1	OTU 2	 Meta 1	Meta 2	
Sample 1					
Sample 2					
Sample N					

## Exploratory Analysis and Quality Control

## Collector's Curves (aka rarefaction)



#### Absolute Abundance



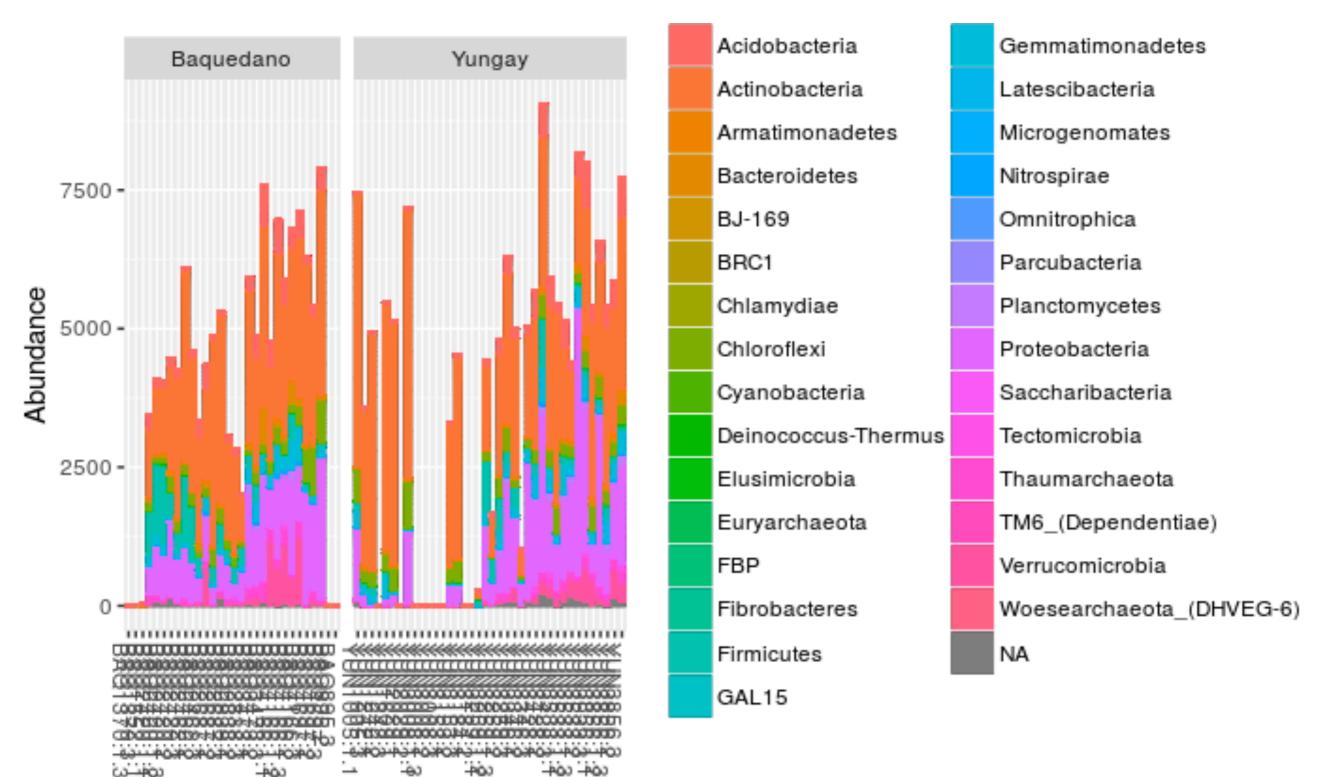
Sample

#### Caveat



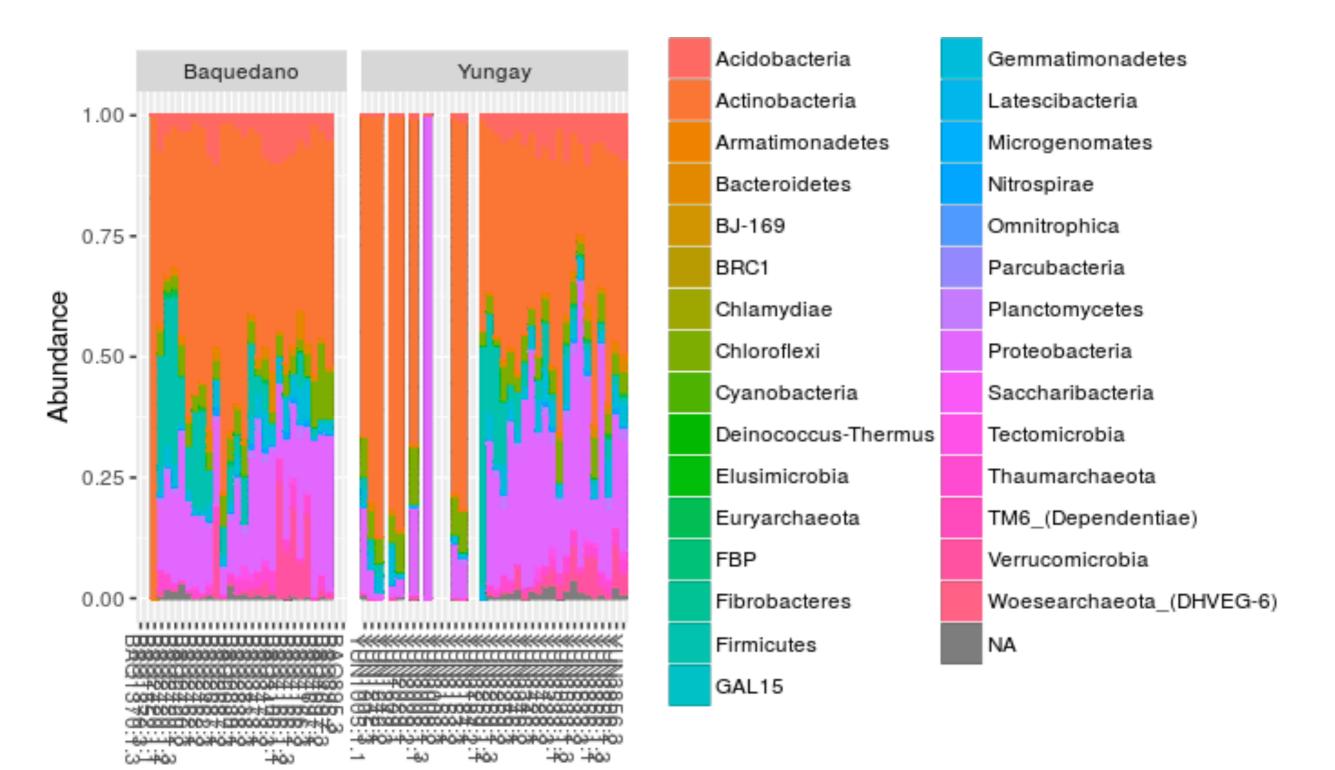


#### Absolute Abundance



Sample

#### Relative Abundance



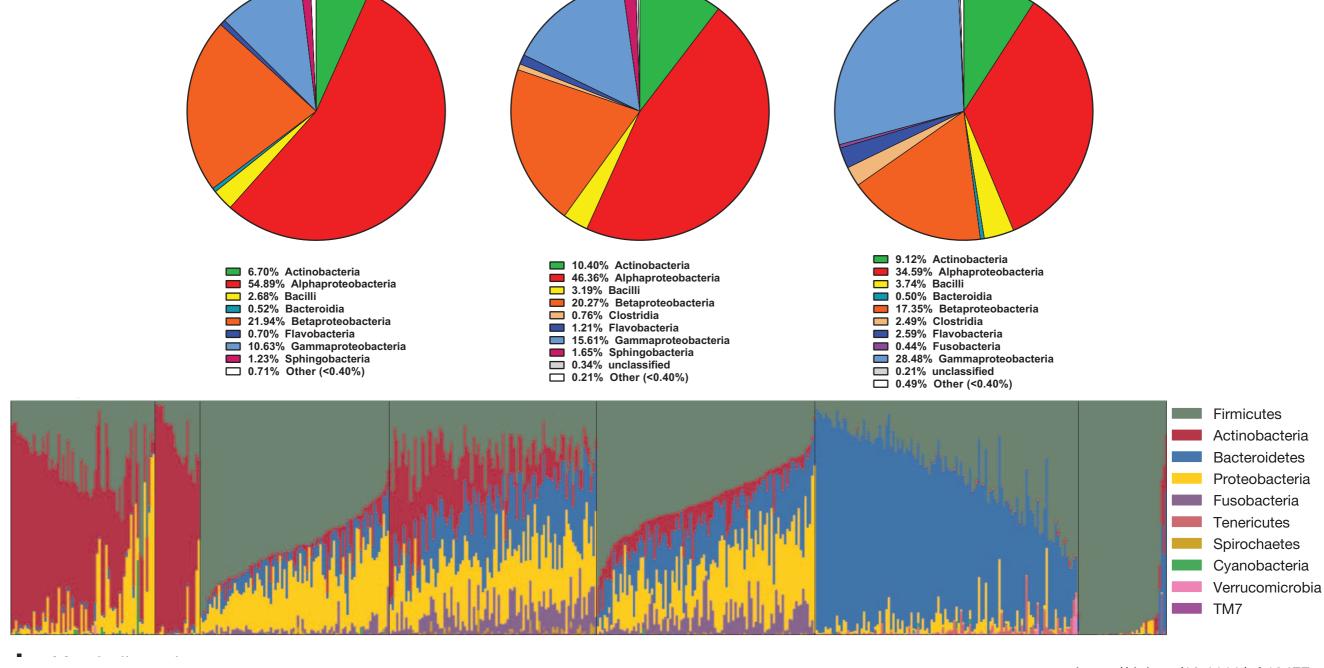
Sample

#### Bad Figures: Pie Charts

**Plasma** 

**Red Blood Cells** 

**Buffy Coat** 



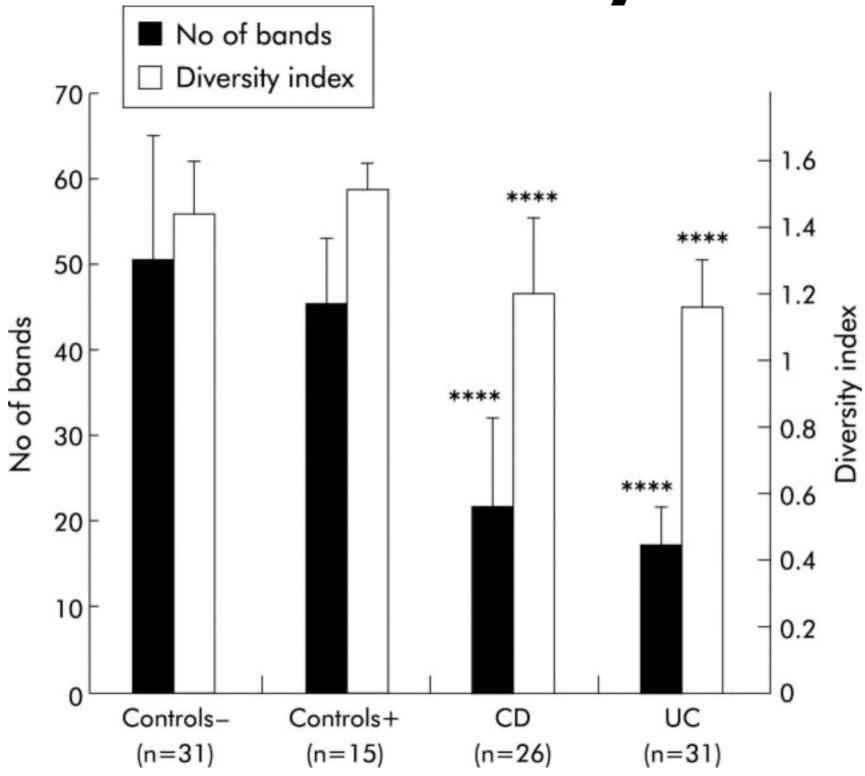
#### Diversity

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#### **Diversity**

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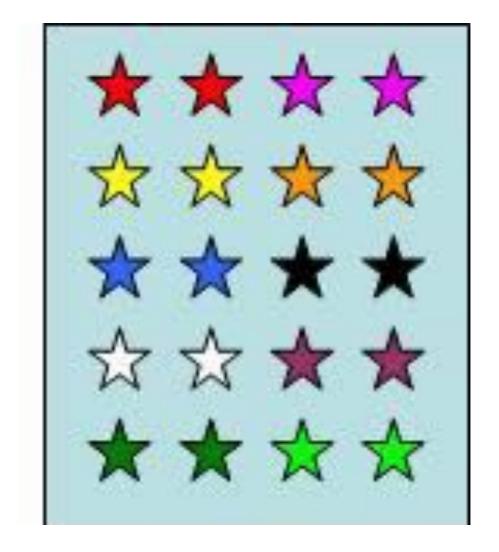


#### Alpha Diversity

- Diversity within a sample
  - Richness: number of different species
  - Evenness: distribution of species (i.e. relative abundance of species)

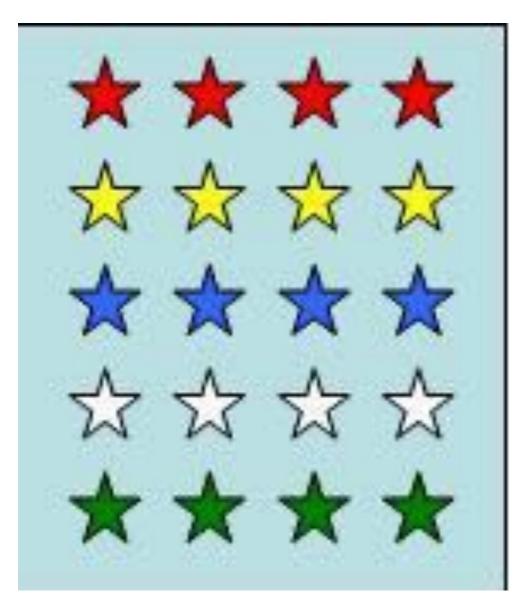
#### Richness





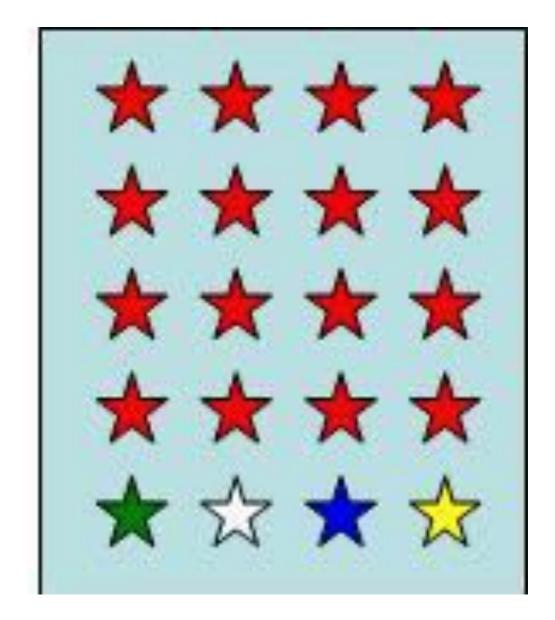
Richness: 5 Richness: 10

#### Evenness



Richness: 5

**Evenness: 1** 



Richness: 5

Evenness: 0.48

#### Alpha Diversity Metrics

Observed Richness

**Counting** 

Shannon (entropy)

**Gambling** 

- Simpson
- Chao1
- ACE (abundance-based coverage estimators)

Richness Estimators (Weirdos)

#### Gambling Metrics

- Jar with 8 balls
  - Shannon: How much would you bet that a randomly selected ball is red?

$$H' = -\sum_{i=1}^{R} p_i \ln p_i$$

 Simpson: How much would you bet that two randomly selected balls are the same color?

$$\lambda = \sum_{i=1}^{R} p_i^2$$

where  $p_i$  is the proportion of individuals belonging to the ith species

	Jar 1	Jar 2	Jar 3	Jar 4
Red	8	5	2	1
Yellow	0	1	2	2
Green	0	1	2	2
Blue	0	1	2	3
Total	8	8	8	8

shannon	0.00	1.07	1.39	1.32
simpson	0.00	0.56	0.75	0.72

## Richness Estimators (Weirdo Metrics)

 Chao1: How many species are present, and how many are observed only once or twice?

 ACE: How many species are present, and how many are observed less than 10 times?

## Richness Estimators (Weirdo Metrics)

 Chao1: How many species are present, and how many are observed only once or twice?

$$S_p = S_o + \frac{a_1(a_1 - 1)}{2(a_2 + 1)}$$

where So is the observed richness,  $a_1$  is the number of species observed once, and  $a_2$  is the number of species observed once

 ACE: How many species are present, and how many are observed less than 10 times?

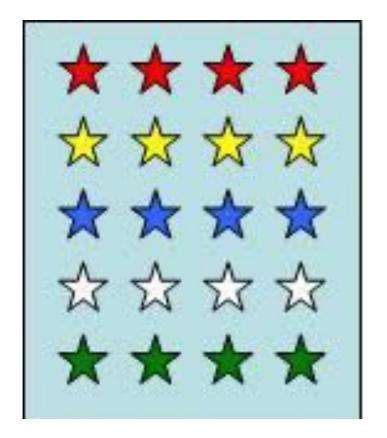
$$S_p = S_{\text{abund}} + \frac{S_{\text{rare}}}{C_{\text{ACE}}} + \frac{a_1}{C_{\text{ACE}}} \gamma^2, \text{ where}$$

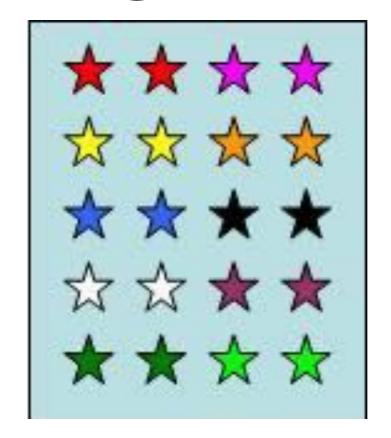
$$C_{\text{ACE}} = 1 - \frac{a_1}{N_{\text{rare}}}$$

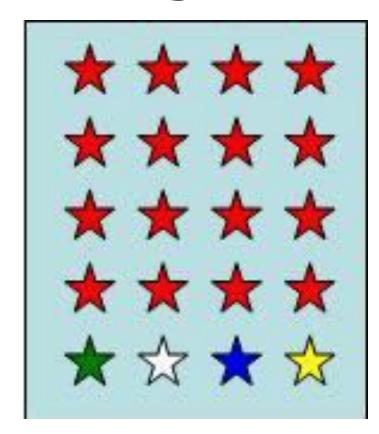
$$\gamma^2 = \frac{S_{\text{rare}}}{C_{\text{ACE}}} \sum_{i=1}^{10} i(i-1)a_1 \frac{N_{\text{rare}} - 1}{N_{\text{rare}}}.$$

 $S_{abund}$  and  $S_{rare}$  are the numbers of species of abundant and rare species, with an arbitrary upper limit of 10 individuals for a rare species, and  $N_{rare}$  is the total number of individuals in rare species

#### Calculating Diversity







Richness	5	10	5
Shannon	1.60	2.30	0.78
Simpson	0.8	0.9	0.35
Evenness	1	1	0.48
Chao1	5	10	11
ACE	5	10	NaN

#### Alpha Diversity Metrics

