

Introduction to Data Science 2018

Assignment 4

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Your solution to Assignment 4 must be uploaded to Absalon no later than March 25th 2018, 12:00, (*i.e., by noon!*) .

Guidelines for the assignment:

- **The assignments in IDS must be completed and written individually.** This means that your code and report must be written completely by yourself.
- Upload your report as a single PDF file (no Word) named `firstname.lastname.pdf`.
- Upload your Python code. If the code is in several files, upload them in a `.zip` archive.

Data exploration with PCA

In the first part of the assignment we will work with the diatoms dataset, see the appendix below for details.

Exercise 1 (Plotting cell shapes, 10 points). Plot one of the cells by plotting the landmark points and interpolating between subsequent landmark points.

Next, plot all the cells on top of each other. Can you see any dataset tendencies from this plot?

When plotting, make sure to make the axes equal to get the right dimensions. If you use `matplotlib.pyplot` this can be done by typing `plt.axis('equal')`.

Deliverables. A plot of a cell, a plot of many cells, and a short description.

Exercise 2 (Visualizing variance in visual data, 10 points). Now, you will visualize the spatial variance of the cells by plotting some instances of the first three PCs. That is, if the mean of the data is given by m , you are going to plot the "cells"

$$\begin{array}{ccccc} m - 2\sigma_1 e_1 & m - \sigma_1 e_1 & m & m + \sigma_1 e_1 & m + 2\sigma_1 e_1 \\ m - 2\sigma_2 e_2 & m - \sigma_2 e_2 & m & m + \sigma_2 e_2 & m + 2\sigma_2 e_2 \\ m - 2\sigma_3 e_3 & m - \sigma_3 e_3 & m & m + \sigma_3 e_3 & m + 2\sigma_3 e_3 \end{array}$$

where the e_1, e_2 and e_3 are the eigenvectors defining the first three PCs, and σ_1, σ_2 and σ_3 denote the standard deviation of the data projected onto each of the first three PCs.

Plot the five cells corresponding to each PC in a single plot, and illustrate the temporal development with a changing color. This can, for instance, be done by importing a colormap with `blues = plt.get_cmap('Blues')`, where `blues(x)` returns a different shade of blue for every number x between 0 and 1.

Describe the variance captured by the three components.

Deliverables. Three plots with sequences of cells showing the variance. A description of the three components.

Exercise 3 (Critical thinking, 10 points).

- a) (5 points) Assume that you perform each of the following preprocessing steps *prior* to performing PCA. What is the effect on the PCA result? Is it a good idea?

- i) Centering
 - ii) Standardization
 - iii) Whitening
- b) (5 points) On the PCA toy dataset, run PCA and visualize the projection onto the first 2 PCs, as in the previous assignment. Repeat the procedure and leave out the last 2 datapoints. You should see a dramatic difference in result. Do you see the hidden structure? What happened? In this exercise, if you have not implemented PCA as part of Assignment 2, it is OK to use a pre-implemented version from e.g. `scikit-learn`.

Deliverables. a) Three short arguments, b) two dataset plots and an explanation.

Clustering II

This exercise continues Exercise 1 and Exercise 3 from the previous Assignment 3.

In Exercise 2 from Assignment 3, you were asked to perform PCA on `IDSWeedCropTrain.csv` and to visualize the data by projecting it on the first two principal components. In Exercise 3 from Assignment 3, you were asked to cluster the training data in `IDSWeedCropTrain.csv` using k -means clustering with $k = 2$ using the first two data points in `IDSWeedCropTrain.csv` as starting points. Now we bring these two exercises together. You are supposed to visualize the cluster centers.

Exercise 4 (Clustering II, 10 points). Visualize the data in `IDSWeedCropTrain.csv` by projecting it onto its first principal components (as in Exercise 2 from Assignment 3). Color the data points according to their class. Take the centers you found in Exercise 3 from Assignment 3 (2-means clustering of the input data in `IDSWeedCropTrain.csv`, the cluster centers initialized with the first two data points). Then project the centers onto the first two principal components found in the previous step and visualize them together with the data points (i.e., in the same plot). Briefly discuss whether you got meaningful clusters.

Deliverables. Description of software used; projection of the two cluster centers (i.e., two two-dimensional vectors), a 2D plot visualizing the data and the cluster centers, short discussion of results

Appendix: Data material

Diatoms

Diatoms are single celled algae, which can be classified into types (taxa) dependent on different features of e.g. their shape. We will perform principal component analysis on outlines of diatoms to explore their shape. The paper Jalba et al. [2006] (found on Absalon) contains more information about diatoms (the pages 338 and 339).

Figure 6 in the paper shows examples of diatoms and outlines of diatoms.

The dataset we will explore contains 780 outlines of diatoms represented by points sampled along the outline of each diatom. The dataset is a modified version of the data used in the paper. We have redistributed the points so that there is the same number of points along each outline, and the positions of the points on the outlines are approximately the same for all diatoms.

Each outline is represented by the coordinates of 90 points in the plane. The 90 x - and y -coordinates for each outline can be considered a vector in \mathbb{R}^n , $n = 180$. When we refer to the mean of the dataset and compute PCA below, we will consider the diatoms observations in \mathbb{R}^{180} . The mean will for example also be a vector in \mathbb{R}^{180} .

The file `diatoms.txt` contains the outlines. It can be opened using the command

```
data = np.loadtxt('diatoms.txt')
```

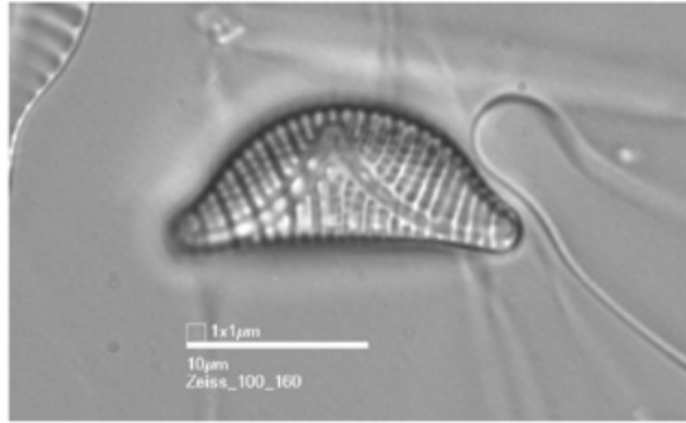


Figure 1: An example diatom.

The points are organized so that the x - and y -coordinates come in pairs, ie. each observation is on the form

$$x_1, y_1, \dots, x_{90}, y_{90}.$$

Please follow this convention when you work out your solution.

PCA toy dataset

This synthetic dataset can be opened with the command

```
data = np.loadtxt('pca_toydata.txt').
```

The dataset consists of 102 data points in the 2D plane. It contains hidden structure – can you find it?

References

A. Jalba, M. H. F. Wilkinson, and J. B. T. M. Roerdink. Shape representation and recognition through morphological curvature scale spaces. *IEEE Trans. Image Processing*, 15(2):331–341, 2006.