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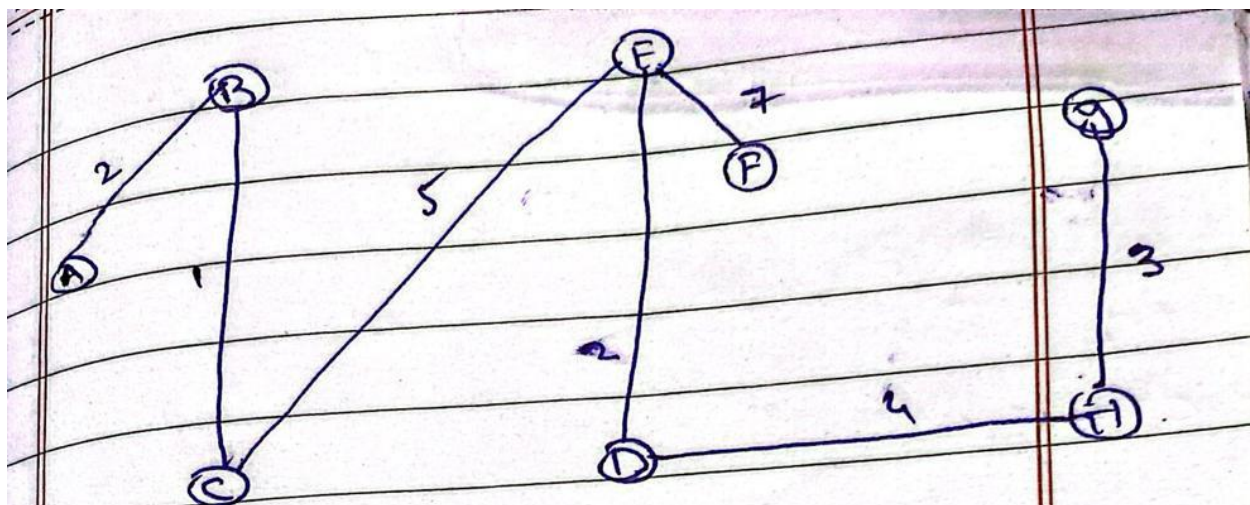
BSCS 5

### **Assignment 3**

#### **DAA**

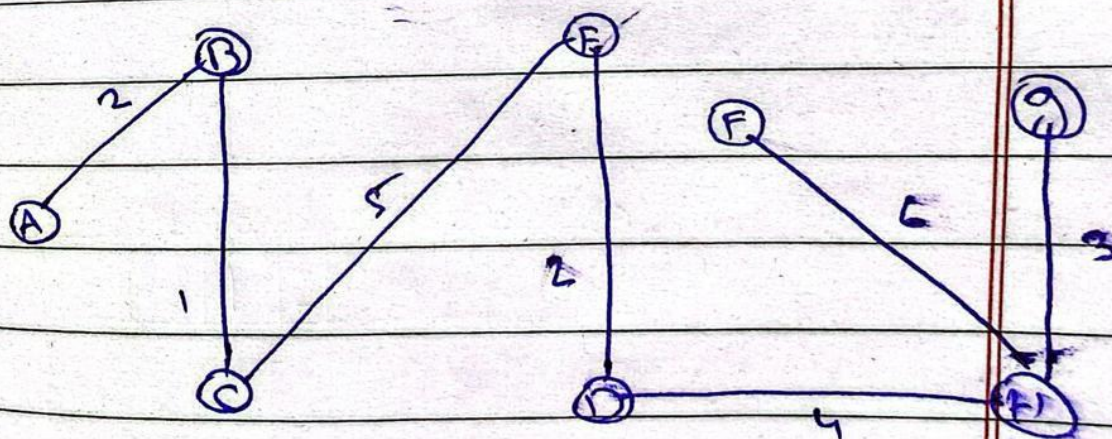
#### **Problem 1**

#### **Kruskal algorithm**



$$1 + 2 + 5 + 2 + 7 + 4 + 3 = 24$$

(b)  
Prims



$$1 + 2 + 5 + 2 + 4 + 3 + 6 = 23$$

## Problem 2

(a):

Steps of Dijkstra's Algorithm, Source = A

Graph Edges:

- $A \rightarrow B$  (5),  $A \rightarrow C$  (11)
- $B \rightarrow C$  (2),  $B \rightarrow E$  (3)
- $C \rightarrow E$  (4),  $C \rightarrow D$  (6)
- $E \rightarrow D$  (1),  $E \rightarrow F$  (7)
- $D \rightarrow F$  (8)

Part b :

Can Dijkstra's algorithm handle negative weights?

- **No.** Dijkstra's algorithm assumes that once a node's shortest distance is finalized, it won't change. Negative weights **violate** this.
- Example: If a shorter path with a negative weight is found **after** visiting a node, Dijkstra will **miss** it.

Which algorithm to use instead?

- Use Bellman-Ford Algorithm. It works correctly with negative weights (as long as there are no negative cycles).

## Problem 3 :

Given two strings A and B, find the **longest contiguous substring** that appears in both.

Example:

- $A = \text{"abcdefgyu"}$
- $B = \text{"bcdtyu"}$

Output: "bcd" (length = 3)

### **Dynamic Programming Approach :**

If  $A[i-1] == B[j-1]$ , then:

$$dp[i][j] = dp[i-1][j-1] + 1$$

Else:

$$dp[i][j] = 0$$

### **problem 4 :**

Given two sequences  $S$  and  $T$ , the **Longest Common Subsequence** (LCS) problem is to find the length of the longest subsequence present in **both** sequences.

- **Subsequence:** A sequence derived from another by deleting some or no elements, without changing the order of the remaining elements.
- For example, LCS of "abcdefg" and "bdf" is "bdf" (length = 3).

### **Dynamic Programming Solution :**

If  $S[i-1] == T[j-1]$ :

$$dp[i][j] = dp[i-1][j-1] + 1$$

Else:

$$dp[i][j] = \max(dp[i-1][j], dp[i][j-1])$$